







148m

MATHEMATICAL

AND Stampliments.

ASTRONOMICAL TABLES,

FOR THE USE OF

STUDENTS OF MATHEMATICS,

PRACTICAL ASTRONOMERS, SURVEYORS, ENGINEERS, AND NAVIGATORS:

WITH

AN INTRODUCTION,

CONTAINING

THE EXPLANATION AND USE OF THE TABLES,

ILLUSTRATED BY

NUMEROUS PROBLEMS AND EXAMPLES.

BY WILLIAM GALBRAITH, M. A.,

TEACHER OF MATHEMATICS IN EDINBURGH.

26355 193

EDINBURGH:

PUBLISHED BY

OLIVER & BOYD, TWEEDDALE-COURT; GEO. B. WHITTAKER, AND J. W. NORIE & CO., LONDON.

1827.

MATHEMATICAL

, अन्तरकारिकार है। इस वास

Security of the second security of the second secon

As dynamic riok.

SAME THE CALL STREET, STREET,

THE STRATEGICAL

ENTERED IN STATIONERS' HALL.

DECEMBER OF STREET OF SE

THE RESIDENCE OF THE PARTY OF T

DESCRIPTION

OLIVER & BOYD, PRINTERS.

SIR GEORGE CLERK, OF PENNYCUICK,

BART., M.P., F.R.S.,

ONE OF THE LORDS COMMISSIONERS OF THE ADMIRALTY, &c., &c., &c.

SIR,

THE following Work, which you have allowed me the honour of inscribing to you, is intended to promote the purposes of useful instruction, and the advancement of practical science; and it is therefore confined to subjects having a direct utility in the business of life.

THOUGH I am aware that no patronage can materially influence the success of a Work of this nature, which must depend upon its merits alone; yet I have been solicitous to inscribe it to you, in the hope, that practical men, in search of useful knowledge, may be induced to consult a Book sanctioned by a name intimately connected with many recent scientific improvements; and I confidently trust, that a reference to the volume itself will prove that your obliging permission has not been undeservedly bestowed.

I have the honour to be,

SIR,

With the utmost respect,

Your most obedient servant,

WILLIAM GALBRAITH.

EDINBURGH, Nov., 1826.

TO WITH SEE -

music of an arradulable manner of an

The Secretary of the control of the

Action 1 A feature and and and another art 1 and 1 and

Digitized by the Internet Archive in 2007 with funding from Microsoft Corporation

of a training to the part of the

PREFACE.

The application of the mathematical sciences to practical purposes has of late made great advances in accuracy and precision. The perfection also which astronomical and geodetical operations have reached, and the extreme delicacy of construction to which instruments have been carried, require correspondent improvements in the methods of computation and reduction; and, therefore, convenient tables of moderate expense must be of great value to those engaged either in the details of practice, or the business of instruction.

There are two classes of tables chiefly in use; one either large and expensive, or attached to expensive works, and which therefore can with difficulty be procured by the generality of purchasers; the other so limited and defective as to be totally unfit for constant reference. It has been my study to hold a middle course between these two extremes. By making such additions to the usual tables as to render their application more easy, without greatly increasing their bulk; by selecting the most useful from larger collections; by supplying some new tables, and simplifying the practical rules, several very laborious processes have been rendered more simple and precise, while the requisite accuracy for the nicest purposes has been strictly preserved.

In most of our initiatory works for popular instruction, the processes and examples are unfortunately conducted in such a manner as to be comparatively of little advantage in actual practice, and, consequently, what has been learned in youth, must, in a great degree, be forgotten in manhood, while new methods are then to be acquired.

To remedy this inconvenience, I have selected some of the most approved modes of treating the problems frequently required by Astronomers, Navigators, and Engineers, from the works of persons celebrated for their successful application of the exact sciences to the niceties of modern practice.

I have therefore taken many of the Astronomical Rules and Examples from the works of Maskelyne, Pond, and Brinkley; and such as relate to other topics from those of Captains Kater, Hall, Sabine, and Parry. To Captain Hall I am under great obligations, not only for access to his original papers, but also for his friendly advice relative to the application of these methods to practice.

To Mr Ivory I am indebted for his very accurate Table of Astronomical Refractions, which I have endeavoured to improve by expanding and adding proportional parts to the subsidiary tables, thereby facilitating its practical application.

Besides labouring to improve many of the ordinary Tables, I have added several which are new, chiefly for the purpose of simplifying some operations and rendering others more accurate.

The explanations will, it is hoped, be found full and explicit, especially towards the beginning. The explanation of some tables which follow others, analogous in structure or arguments, is sometimes less full, as it is presumed those previously given are well understood. For example, the note to Table XXV., at the bottom of page 91, can hardly be intelligible to a mere practical man who has little mathematical knowledge; but as the method of taking out the quantities from Table V., in whatever quadrant of the circle, or division of 24 hours, they are situated, is so fully explained before, it was thought unnecessary to repeat the same minutiæ a second time. Still, however, there may be some parts which require to be expanded, in order to be more readily understood, as well as others which might, perhaps with propriety, be abridged.

The Introduction is divided into three parts, followed by a copious explanation of the general tables, which may be called a fourth.

In the first I have shortly described the nature, and investigated the more simple series for the computation of Logarithms. I have generally, however, only given the more important rules in words at length, without investigation, so as to be readily com-

prehended by persons who have acquired a knowledge of the elementary principles of mathematics. In fact, the demonstrations can only be understood by those who have obtained a tolerable knowledge of the elements of geometry and algebra, and, since the generality of books containing these comprehend also the usual investigations in trigonometry, it was thought advisable to omit them. If, for example, a student should purchase Legendre's Elements of Geometry in order to study that science, he will find it to contain also very elegant investigations of almost all the useful properties in Plane and Spherical Trigonometry. On this account, I have only given the demonstrations of those propositions less commonly inserted in the usual treatises.

On the Barometric Measurement of Altitudes, I have given four different methods. The third is in a great degree new, and by the original subsidiary tables, calculated expressly for this purpose, it will be found easy and accurate.

The second part contains Spherical Trigonometry, with a great variety of its most useful applications. As the rules and examples are either new or selected from the best writers on the subject, it is hoped this section will prove interesting to students of Astronomy and Navigation, since it contains a number of the usual methods and examples practised by the most distinguished men of science of the day.

The third part contains a variety of Rules and Formulæ for the use of Surveyors, Engineers, Navigators, and practical Astronomers. Those for geodetical purposes are selected chiefly for their general utility, and comprehend a sufficient number for usual practice,—an idea which was suggested to me by some of my more advanced pupils who have been employed in government surveys. They were first collected in the form of notes and transcribed into their albums, to be used when they were engaged in geodetical, accurate military or marine surveying; and as they may prove generally useful to that class of Students, I have arranged them in as natural an order as possible.

The ingenuity and skill of Captain Kater having devised the most beautiful simplifications of the problem of determining the figure of the earth by means of the pendulum, and brought the experiment within the reach of our more active and intelligent military and naval officers, I have added the necessary rules and formulæ for that purpose, in order to initiate, as far as possible,

our Cadets and Midshipmen in these interesting researches; as such higher objects of pursuit, not only invigorate their faculties, but inspire them with enthusiasm for the attainment of professional renown.

The fourth part contains the necessary Explanation of the Tables.

I have thus endeavoured to collect, into as small a space as possible, the greatest quantity of useful matter naturally connected with the subjects treated in the work; but with what success I must allow the public to determine.

the state of the s

and the second second second

the last party and address to the state of the

WILLIAM GALBRAITH.

EDINBURGH, November, 1826.

CONTENTS

a most an exercise to the last transfer as

ILL ... The second second second second

INTRODUCTION.

| ADT | I. PROPERTIES of LOGARITHMS | Page. |
|-------|--|-------|
| | Construction of Logarithms | |
| , | Trigonometrical Lines, called Sines, &c | 8 |
| | Multiples and Powers of Arcs | |
| | and the second of the second o | |
| | PLANE TRIGONOMETRY | |
| | Its Application to Sailings in Navigation | |
| 10 | Its Application to the Mensuration of Heights and Distances | 25 |
| | To a be be be a second of the Barrey of the Lands and Lands of the | |
| | gular Fortresses, and a Table of their Measures4 | |
| 4-1 | Barometric Measurement of Altitudes | 44 |
| 15.11 | II. SPHERICAL TRIGONOMETRY, &c. | |
| | Definitions, Principles, and General Properties | 56 |
| | Solution of Spherical Triangles, with their Stereographic Projection | - |
| | Napier's Rule of the Circular Parts | 64 |
| | Maskelyne's Rules for determining the Latitude and Longitude, | 0.1 |
| | from the Right Ascension, Declination, and the Obliquity of | |
| | the Ecliptic, &c | 68 |
| | Solution of Oblique-Angled Spherical Triangles | 73 |
| | On finding the Latitude by Observation | 81 |
| | On Finding the Longitude by Observation. | 0. |
| | 1. By Lunars | 89 |
| | 2. By Chronometers | 104 |
| | Equation to Equal Altitudes | |
| 192 | 3. By Occultations | 114 |
| c | 4. By the Moon's Transit | 129 |
| î. | Of the Transit Instrument | 130 |
| | To take a Transit | 131 |
| | Method of Tabulating a Transit | 132 |
| 4 | To bring a Transit Instrument into the Meridian | 133 |
| | To determine the Error and Rate of a Clock or Chronometer by the | |
| | Transit Instrument | 136 |
| | | |
| 1 | III. MENSURATION, SURVEYING, AND FORMULÆ, &c. | |
| 34 | | |
| | Mensuration of Surfaces | 139 |
| Yr | Mensuration of Solids | 142 |

| 50.55 | Page. |
|--|--------|
| | 144 |
| Levelling | 146 |
| RULES and FORMULÆ | 147 |
| The best Form of Triangles | |
| To reduce Angles to the Centre of the Station | |
| To compute the Spherical Excess | |
| To reduce a Measured Base at any Height to the Level of the Se | |
| To determine the Horizontal Refraction by Rule or Formulæ | |
| To find the Angle made by a given Line with the Meridian | |
| To determine the Ellipticity of the Earth by the Measurement | |
| Arcs | |
| To determine a Degree of Latitude | |
| To determine a Degree of Longitude | |
| To determine an Oblique Degree | |
| Specific Gravity | |
| To determine the Specific Gravity of Air, Dry, saturated wi | |
| Moisture, and according to the actual State of the Atmosphere | |
| To determine the Specific Gravities in vacuo | |
| To determine the Effects of the Buoyancy of the Atmosphere | |
| the Pendulum | |
| Correction of Pendulums vibrating in Circular Arcs | 156 |
| Correction of Vibration for Buoyancy | 156 |
| for Expansion | 157 |
| for Height above the Sea | 157 |
| Determination of the Length of the Pendulum at different Poin | ts |
| on the Earth's Surface | 158 |
| Determination of the Figure of the Earth by the Pendulum | |
| Comparison of the English and French Pendulums | |
| Velocity of Sound16 | 0, 161 |
| Velocity of the Discharge of Water-pipes, Rivers, and Canals. 16 | 1, 162 |
| Fall in a River caused by Obstruction in the Stream | 162 |
| Tonnage of Ships | 162 |
| Strength of Timber166, 16 | 7, 168 |
| 10 American and the American Control of the Control | |
| The comment of the contract of | |
| and an analysis of the second | |
| white and the standard reason of the standard | |
| A major of the second of the s | |

CONTENTS

. OF

EXPLANATION OF THE TABLES, &c.

| | | Page. |
|--|----|-------|
| TABLE I. Miles of Longitude at any Latitude | 1 | 1 |
| II. Logarithms of Numbers | 1 | 1 |
| Logarithmic Arithmetic | 5 | |
| III. Angles which every Point and Quarter Point of the | | |
| Compass makes with the Meridian | 7 | 17 |
| IV. Logarithmic Sines, &c. to every Point and Quarter | | |
| Point of the Compasss | 7 | 17 |
| V. Logarithmic Sines, Tangents, &c. to Degrees | 7 | 18 |
| VI. Natural Sines, Tangents, Secants, and Versines, to | | |
| every Degree of the Quadrant | 11 | 63 |
| VII. Meridional Parts to every Degree of the Quadrant | 11 | 64 |
| VIII. Traverse Table | 11 | 64 |

| 100 | | Pa | ige. P | age. |
|--------|---------|---|---------|------|
| TABLE | XI S | Diurnal Logarithms | Exp. '. | 66 |
| LABLI | | Proportional Logarithms | 13 | 68 |
| | | Dip of the Horizon | 13 | 84 |
| | | Dip at different Distances | 13 | 84 |
| | XIII. | Correction of the Sun's Altitude at Sea | 14 | 84 |
| | XIV. | Correction of a Star's Altitude | 14 | 84 |
| | | Sun's Semidiameter, &c | 14 | 85 |
| | | Sun's Parallax in Altitude | 14 | 85 |
| 91 | XVII. | Mean Refractions by Mr Ivory | 14 | 86 |
| 24 | XVIII. | C. 1 1. WILL | 14 | 00 |
| 31 | XIX. | | 14 | 89 |
| | XX. | Augmentation of the Moon's Semidiameter in Alti- | | |
| | AAI. | tude, and Z.D | 16 | 90 |
| | XXII. | Reduction of the Moon's Parallax on the Spheroid | 16 | 90 |
| | | Logarithms of the Earth's Radii on the Spheroid | 16 | 91 |
| | | Reduction of the Latitude | 16 | 91 |
| | | For determining the Latitude by the Pole Star | 17 | 91 |
| | | Augmentation of the Moon's Semidiameter by the | | |
| 751 | 0.00 | Nonagesimal | 18 | 92 |
| 15 - 1 | | Equation of Second Differences for 12 and 24 hours | 19 | |
| Mary I | | Reduction to the Meridian | 21 | 94 |
| Mar- | | Reduction to either Solstice | 24 | 95 |
| | | To change Mean Solar into Sidereal Time | 28 | 96 |
| | | To change Sidereal into Mean Solar Time | 28 | 96 |
| 3 | | To convert Mean Time into Parts of the Equator | 29 | 97 |
| | | Lengths of Circular Arcs To XLVIII. For computing the Corrections of the | 29 | 97 |
| | AAAIV. | Fixed Stars | 29 | 98 |
| | XLIX. | Mean Obliquity of the Ecliptic | | 103 |
| | | And LI. Corrections of the Obliquity | | 103 |
| | | And LIII. Solar and Lunar Nutations of the Equi- | | |
| - 17 | | noxes in Time | 32 | 103 |
| | | Right Ascensions and Declinations of Stars for 1828 | | 104 |
| | | Decimal Numbers for each Day in the Year | | 104 |
| | | Sun's R.A. for 1828 | | 105 |
| | | Sun's Declination for 1828 | | 106 |
| | | Equation of Time for 1828 | | 107 |
| | | Correction of Longitude by Chronometers Latitudes and Longitudes of Places | | 107 |
| | | To convert Space into Time | | 108 |
| | | To convert Time into Space | | 109 |
| | | Useful Numbers in Calculation | | 110 |
| | | And LXV. To find the Time and Height of High Water | | 111 |
| | LXVI. | And LXVII. Tables of Equation of Third and | | |
| | LXVIII | Fourth Differences Table to find the Latitude by the Pole Star | 36 | 112 |
| 13 : | | The second by the a de butternesses | 01 | 114 |
| | MISCELL | ANEOUS TABLES IN THE INTRODUCTION | N | |
| 77.55 | . T | Simp of Thiranamatrical Times | | 10 |
| TABL | E I. | Signs of Trigonometrical Lines | 3 1 | 12 |
| | TIT. | Measures of Forts | 0, 14 | 44 |
| - | IV. | Depression of Mercury in Glass Tubes | | 48 |
| 1 10 | V. | Elastic Force of Aqueous Vapour (Dalton) | | 48 |
| | | Logarithms of the Bulk of Gas at different Tempera- | | |
| | | tures | | 49 |

7

•

| TABL: | | Page |
|-------|--|--------|
| | | 19, 50 |
| | VIII. Correction of the Oblique Semidiameter in Lunars by | |
| | Dr Young100 | , 101 |
| | IX. Equation of Second Difference for Three Hours or for | |
| | 60' and 100" | 102 |
| | X. Correction of Apparent Time depending upon the Equa- | |
| | tion of Second Difference and the Variation of the | |
| 57 | Distance between the Moon and the Sun, or a fixed | |
| | Star, in Three Hours | 102 |
| VI. | XI. Of the Decimal Fractions of a Day | 113 |
| | XII. Decimal Parts of an Hour | 113 |
| | XIII. To convert Decimals of Time into Degrees at the rate | |
| | of fifteen Degrees to an Hour | 113 |
| | XIV. Variation of the Sun's R.A. and D. in one Second for | |
| | each Month in the Year | 138 |
| | XV. Areas of Circular Segments | 141 |
| | XVIPolygons | 142 |
| | XVII. Regular Bodies | 143 |
| | XVIII. Table A. for Correcting the Number of Oscillations | |
| | for the Arc of Vibration | 156 |
| | XIX. Tables of Specific Gravity163, 164 | |
| | XX. Expansions of Solids and Liquids | 166 |
| | XXI. Table for computing the Strength of Timber | 166 |
| | XXII. Table for Correcting Lunars for Spheroidal Figure of | 40 |
| | the Earth. Explanation of Tables | 43 |
| | XXIII. Table for finding the Latitude by the Pole Star | 43 |
| | all and the second of the second of the second | |
| | 0.00-0-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1 | |
| | and the second s | |
| | name A sport of the least the second state of | |
| | | |
| J | | |
| | | |
| | | |

PRINCIPAL PROPERTY AND ADDRESS OF THE PARTY AN

Service and the service of

INTRODUCTION.

The property of the state of th

to the second se

PART I.

OF LOGARITHMIC AND TRIGONOMETRICAL TABLES.

SECTION I.

Of the Properties of Logarithms.

1. Logarithms are a series of numbers, originally invented by Baron Napier, for the purpose of facilitating arithmetical calculations. This end is attained by their enabling us to perform the operations of multiplication by addition, of division by subtraction, of involution by multiplication, and of the extraction of roots by division.*

2. It is evident that any two series of numbers, the one being in arithmetical and the other in geometrical progression, possess these

properties, thus, for example, let the

Ar. series be $\begin{pmatrix} 0 & 1 & 2 & 3 & 4 & 5 \\ Geo. series & 1 & 10 & 100 & 1000 & 10,000 & 100,000 \end{pmatrix} &c.$

Now, if we add any two numbers in the arithmetical series, such as 2 and 3, which are equal to 5, and multiply the corresponding numbers under them, 100 and 1000, we have 100,000, the number immediately under 5, which was obtained by the addition of 2 to 3. Hence, then, it is clear that, if tables of this kind, sufficiently extensive, were formed, by a reference to them, the operation of multiplication could be performed by means of addition.

In like manner, we perform division by subtraction, for, if from 5 we take 3, the remainder is 2, under which we get 100, that is 100,000, the number under 5, divided by 1000, that under 3, gives

100 as a quotient.

Roots are readily determined in a similar way; thus, 4, in the arithmetical series divided by 2 gives 2, under which, in the geometrical series, is 100, that is, the second, or square root of 10,000 the number under 4, is 100, the number under 2, and so on.

Napier called the first series the logarithms of the corresponding

numbers in the second.

3. Since the two series may be assumed at pleasure, we may have

as many different systems of logarithms as we choose.

4. The series in art. 2 being adapted to the common denary scale of arithmetic, is, on the whole, the most convenient for general purposes, though other systems have, in particular cases, their peculiar advantages.

On considering these series, it appears that the logarithm of 1 is

^{*} The identity of this process with that performed upon the exponents of quantities in the corresponding operations of algebra, will be obvious to those who have acquired the rudiments of that branch of mathematics.

0, and that of 10 is 1, and hence the logarithms of all numbers between 1 and 10 are greater than 0 and less than 1, that is, they are fractions. In the same manner, between 10 and 100 they are greater than I and less than 2, that is, they are I with some fraction annexed, and so on. The whole numbers or integers in the logarithmic series are hence easily obtained, being always a unit less than the number of figures in the integral part of the corresponding natural number. On this account it is customary, in the common printed tables, to put down only the fractional part in the form of a decimal, the computer supplying the whole number or integer under the name of index.

5. In order to generalize, let us assume the two following series:

 r^{x} , $r^{x'}$, $r^{x''}$, $r^{x''}$, &c. y, y'', y''', &c. (2)

in which r is some given number greater or less than unity, and x, x', x", &c. any variable quantities chosen in such a manner that $r^{x}=y$, $r^{x'}=y'$, $r^{x''}=y''$, $r^{x'''}=y'''$, &c., then the several exponents, x, x'. x", x"', &c. of the series (1) are called the logarithms of the corresponding terms in the series (2).

Thus if y, y', y'', y''', &c. be a series of numbers such that $r^x = y$, $r^{x'} = y'$, $r^{x''} = y'''$, &c., then $x = \log y$, $x' = \log y'$, $x''' = \log y''$, &c.

6. For the purpose of adapting the series (1) to the series of natural numbers 1, 2, 3, &c. the given number r must be greater than unity, the first index x must be equal to 0, and the several indices x', x'', x''', &c. must continually increase. For, since by the principles of algebra, $x^{\circ}=1$, whatever r may be, this series will increase from 1 to infinity; and by properly adjusting the values of x', x'', x''', &c. it is evident that the several quantities $r^{x'}$, $r^{x''}$, $r^{x'''}$, &c. may be made to coincide with the numbers 2, 3, 4, &c. For example, let r=10; then, since $10^{\circ}=1$, find $10^{\circ}=10$, the indices of 10, which would give 10^{x} , 10^{x} , 10^{x} , &c. equal to the numbers 2, 3, 4, &c., must be fractions between 0 and 1. If we take the number 3 we have $10^{\frac{1}{2}}$ =3.16 nearly, from which we infer that a fraction (x') somewhat less than $\frac{1}{2}$ or 0.5, being made the index of (r) 10, would give $10^{x'}=3$. This fraction is found by calculation to be 47712; hence $10^{47712} = 3$; therefore, when r=10, the logarithm of 3 is .47712.

In like manner, if we assume the number 5, whose logarithm is to be found in place of that of 3, we have $10^{\frac{1}{3}}$ =4.64 whence a fraction, $x^{(n)'}$ somewhat greater than $\frac{2}{3}$, or .666 being made the index or exponent of 10, would give $10^{x^{(n)}}=5$. This fraction more accurately computed is found to be .69897, that is, when r=10 the loga-

rithm of 5 is .69897.

7. From this it appears, that the value of the logarithm of any given number depends upon the value of the number r, and that by assuming it equal to different numbers, as many different systems of

logarithms may be formed as we please.

In every system, however, since $r^{\circ}=1$, the logarithm of 1 must be 0. This constant quantity r from the powers of which the natural numbers are formed, is called the radix or base of the system to which it belongs.

8. In the general equation $r^x = y$, (art. 5.), let us make x vary

and observe the correspondent variations of y.

If r is greater than 1, on making x=0, we have y=1; when x=1 then y=r or the logarithm of the base is=1; in proportion as x increases from 0 to infinity, y will increase from 1 towards r, and afterwards to infinity, so that if we suppose x to pass through all the intermediate values, in following the law of continuity, y will increase also in the same manner, though much more rapidly.

If we put for x, negative values, we shall have $y=r^{-x}$, or $y=\frac{1}{r^{-x}}$. Here we see, in like manner, that the more x increases the

more y or $\frac{1}{x^x}$ decreases, so that in proportion as x augments, negatively y takes all possible values less than 1 as far as 0, in which case x becomes infinite. This was the proposition which Napier made to Briggs on their celebrated meeting at Edinburgh, when conversing on the propriety of changing the logarithmic scale.

If r is less than 1 we shall make $r=\frac{1}{b}$, b being greater than 1 and

we have $y = \frac{1}{b^x}$ or $y = b^x$, according as x is positive or negative. We fall here upon the same case, with this difference, that x is positive when y is less than 1, and negative when y is greater than 1. This proposal Briggs made to Napier, but immediatly abandoned it on Napier suggesting that mentioned above, which was finally adopted.

If r=1, we have y=1 whatever x may be.

We may then say generally, that provided r is not unity, there can always be found a value for x, which renders r^x equal to any given number y. The constant use that is made of the properties of the equation $y = r^x$ requires the denominations of its parts to be fixed in order to avoid circumlocution. Hence as before remarked, x is called the logarithm of the number y, the invariable number r is called the base and, finally, the logarithm of a number, the power to which the base must be raised in order to produce that number.

With regard to the base r it is arbitrary, and when we write $x=\log y$ to show that x is the logarithm of the number y or that $y=r^x$, the base r is alway understood, because when once chosen it is supposed to remain fixed. If it should be changed the new base

ought to be indicated.

9. From these principles are derived several properties.

1°. In every system of logarithms, the logarithm of 1 is 0 and that

of the base r is 1.

 2° . If the base r is greater than 1, the logarithms of numbers greater than 1 are positive, the others are negative. The contrary takes place if r is less than 1.

 3° . The composition of a table of logarithms consists in determining all the values of x when y is made successively equal to 1, 2, 3,

&c. in the equation $y=r^x$.

The logarithms therefore increase in progression by differences, while the numbers increase in progression by the product or quotient, according as μ is an integer or a fraction.

The ratios are the arbitrary numbers e and μ . We may, therefore, regard the systems of values of x and y which satisfy the equation

 $y=r^{2}$, as classed in these two progressions, which coincides with what has been already said in art. (2.)

10. We shall now demonstrate algebraically the various properties

of logarithms.

Let N and n be any two numbers belonging to the series (1); and for example, let $N=r^x$ and $n=r^x$, then $N = r^x \times r^x = r^{x+x}$, but, by art. 5, the logarithm of $r^{x+x'}$ is $x+x'=\log r^x+\log r^{x'}=\log N+\log r$

In like manner, if n, n', n'' be any set of numbers in the series (1) it might be shown that the logarithm of $n \times n' \times n''$, &c.=log. $n + \log_{10} n' + \log_{10} n''$, &c., from which we infer that the logarithm of the product of any number of factors is equal to the sum of their logarithms.

11. Again $\frac{N}{n} = \frac{r^x}{r^{x'}}$; but the logarithm of $r^{x-x'} = x - x'$; therefore, the logarithm of $\frac{N}{r} = x - x' = \log r^x - \log r^x = \log N - \log n$; hence

it appears, that the logarithm of the quotient of any two numbers is equal to the difference of their logarithms; and that the logarithm of a fraction $\binom{N}{n}$ is equal to the logarithm of its numerator minus, the logarithm of its denominator.

If N be less than n, then log. N-log. n is negative; therefore,

the logarithms of all proper fractions are negative.

12. Let $N=r^x$ be raised to the m^{th} power, then $N^m=r^{mx}$; but the logarithm of r^{mx} is=mx, hence the logarithm of $N^m=mx=m$ log. r^x $=m \log N$; for the same reason, since $\sqrt{N=N_m^{\frac{1}{m}}=r_m^{\frac{1}{m}}}$, the logarithm of $\sqrt[m]{N=\frac{x}{m}=\frac{\log N}{m}}$; from which we infer, that the logarithm of the mth power of any number is found by multiplying its logarithm by m, and that of the m^{th} root of any number, by dividing its logarithm by m.

SECTION II.

Of the Construction of Tables of Logarithms.

13. Let r express generally any term of the series, (1), and let N be the corresponding number, then r=N. Hence to find the logarithm of N is merely to solve the equation $r^x = N$ where x is the unknown quantity. In order to accomplish this purpose let r=1+band N=1+n, then extract the y^{th} root of each side of this equation,

and we obtain $(1+b)\frac{x}{y} = (1+n)\frac{1}{y}$, which by expansion gives $1 + \frac{x}{y}(b) + \frac{x}{y}(\frac{x}{y}-1)(\frac{b^2}{2}) + \frac{x}{y}(\frac{x}{y}-1)(\frac{x}{y}-2)(\frac{b^3}{2\cdot 3}) + &c.=$ $1 + \frac{1}{y}(n) + \frac{1}{y}(\frac{1}{y} - 1)(\frac{n^2}{2}) + \frac{1}{y}(\frac{1}{y} - 1)(\frac{1}{y} - 2)(\frac{n^3}{2 \cdot 3}) + &c.$

Now suppose y to be indefinitely great with respect to x and 1, then will $\frac{x}{y}$ and $\frac{1}{y}$ vanish in reference to -1, -2, &c., so that $\frac{x}{y}$ 1 and $\frac{y}{y}$ 1 will each become equal to -1; $\frac{x}{y}$ -2, $\frac{1}{y}$ -2, each

equal to -2, &c. &c., hence rejecting 1 from each side of the equation we have

$$\frac{x}{y} \left(b - \frac{1}{2} b^2 + \frac{1}{3} b^3 - \frac{1}{4} b^4 + \&c. \right) = \frac{1}{y} \left(n - \frac{1}{2} n^2 + \frac{1}{3} n^3 - \frac{1}{4} n^4 + \&c. \right)$$
hence x the log $(1+n) = \frac{n-\frac{1}{2} n^2 + \frac{1}{3} n^3 - \frac{1}{4} n^4 + \&c.}{n-\frac{1}{2} n^2 + \frac{1}{3} n^3 - \frac{1}{4} n^4 + \&c.}$

hence x, the log. $(1+n) = \frac{n-\frac{1}{2} n^2 + \frac{1}{3} n^3 - \frac{1}{4} n^4 + \&c.}{b-\frac{1}{9} b^2 + \frac{1}{3} b^3 - \frac{1}{4} b^4 + \&c.}$

but n=N-1 and b=r-1, therefore, by substitution, the above expression becomes

14. Let
$$\frac{1}{(r-1)-\frac{1}{2}} (r-\frac{1}{2}(r-1)^2+\frac{1}{3}(r-1)^3-\frac{1}{4}(r-1)^4+&c.=\frac{1}{D}=M.$$

This quantity M, which evidently depends upon the base r, is called the modulus of the particular system of logarithms to which it belongs. As it is obvious the series $n - \frac{1}{6}n^2 + \frac{1}{3}n^3 - \frac{1}{6}n^4 + \frac{1}{6}n^5$ &c. will not converge when n is any whole number greater than unity, before proceeding to the calculation of the logarithms of any particular system, it will be proper to show the manner in which the value of x in the last article may be expressed in a converging series. This may be effected by means of the following process in which M is substituted for the quantity

 $(r-1) - \frac{1}{2} (r-1)^2 + \frac{1}{3} (r-1)^3 - \frac{1}{4} (r-1)^4 + \&c.;$ $Log. (1+n) = M (n-\frac{1}{2} n^2 + \frac{1}{3} n^3 - \frac{1}{4} n^4 + \frac{1}{5} - n^5 - \&c.)$ In the above for n put -n, and then Log. $(1-n) = M \left(-n - \frac{1}{2}r^2 - \frac{1}{3}n^3 - \frac{1}{4}n^4 - \frac{1}{5}n^5 - &c.\right)$. (4) Subtract (4) from (3), then log. $(1+n) - \log$. $(1-n) = \log$. $\frac{1+n}{1-n} = 2 \text{ M } (n+\frac{1}{3} n^3 + \frac{1}{5} n^5 + \frac{1}{7} n^7 + \&c.)$ Let $N = \frac{1+n}{1-n}$, then $n = \frac{N-1}{N+n}$, hence Log. N=2 M $\left\{ \left(\frac{N-1}{N+1} \right) + \frac{1}{3} \left(\frac{N-1}{N+1} \right)^3 + \frac{1}{5} \left(\frac{N-1}{N+1} \right)^5 + &c. \right\}$ (6) Again let $n = \frac{1}{2N-1}$, then $\frac{1+n}{1-n} = \frac{N}{2N-1}$, hence by substitution in formula Log. $\frac{N}{N-1} = 2 M \left(\frac{1}{2N-1} + \frac{1}{3(2N-1)} + \frac{1}{5(2N-1)^5} + &c. \right)$ Log. N—log. (N—1) =2 M $\left(\frac{1}{2N-1} + \frac{1}{3(2N-1)^5} + \frac{1}{5(2N-1)^5} + &c.\right)$; and log. N=2 M $\left(\frac{1}{N-1} + \frac{1}{3(N-1)^5} + \frac{1}{5(N-1)^5} + &c.\right)$ +log. (N-1)

^{*} By means of this formula the logarithm of a quantity exceeding unity by a very small fraction may be readily found.

Since the log. of 1=0, this last series which converges very rapidly, will give the logarithms of all the natural numbers, with facility in succession. To these theorms might have been added others still more convenient, but they are sufficient for ordinary cases.

15. Before proceeding to compute a table of logarithms, some value must be assigned to M. Since the value of r is arbitrary, let it be so assumed that $(r-1)^{-1} (r-1)^{2} + (r-1)^{3} + 8rc$ or M shall

it be so assumed that $(r-1)-\frac{1}{2}(n-1)^2+\frac{1}{3}(r-1)^3-&c.$ or M shall be equal to 1, that adopted by Napier. Taking series (8) we have since

Log.
$$1 = 0$$
 (art. 6.)
 $2 = 2\left(\frac{1}{3} + \frac{1}{3^4} + \frac{1}{5 \cdot 3^5} + &c.$ to 8 terms $\right)$ = 0.6931472
 $3 = 2\left(\frac{1}{5} + \frac{1}{3 \cdot 5^3} + \frac{1}{5^6} + &c.\right) + \log. 2$ = 1.0986123
 $4 = 2 \log. 2$ (art. 12) = 1.3862944
 $5 = 2\left(\frac{1}{9} + \frac{1}{3 \cdot 9^3} + \frac{1}{5 \cdot 9^5} + &c.\right) + \log 4$ = 1.6094379
 $6 = \log. 2 + \log. 3$ (art. 10) = 1.7917595
 $7 = 2\left(\frac{1}{13} + \frac{1}{3 \cdot (13)^5} + \frac{1}{5 \cdot (13)^5} + &c. + \log. 6$ = 1.9459101
 $8 = 3 \log. 2$ (art. 12) = 2.0794415
 $9 = 2 \log. 3$ (art. 12) = 2.0794415
 $9 = 2 \log. 3$ (art. 12) = 2.1972246
 $\frac{1}{3} = \frac{1}{3} + \frac{1}{3} = \frac{1}$

In this manner the Napierean logarithms of all the natural numbers may be found. As their accuracy, however, depends upon those immediately preceding, being derived successively from each other, it would be necessary to check the computations in the actual construction of a table of logarithms by some independent formula, such as (6), though this in large numbers would be rather inconvenient from its slow convergency.

16. To find the value of r, the base, in this system recourse must be had to the series (3) art. (14). If \log . (1-n) or \log . N be put =l and M=1, we have $l=n-\frac{1}{2}n+\frac{1}{3}n^3-\frac{1}{4}n^4+$, &c.; reverting this series, and 1+n, or $N=1+l+\frac{1}{2}l^2+\frac{1}{2\cdot 3}l^3+\frac{1}{2\cdot 3\cdot 4}l^4$, &c. Now let l=1, then the number whose logarithm is 1, that is, the base $r=1+1+\frac{1}{2}+\frac{1}{2\cdot 3}+\frac{1}{2\cdot 3\cdot 4}+$, &c. =2.7182818. To prevent confusion, however, we shall always designate the base or radix of this system by R, retaining r for that of the common logarithms. Hence R=2.718,281,32846.

These are also called hyperbolic logarithms from their application to the quadrature of the hyperbola; but this designation is improper, as any system may be similarly employed.

as any system may be similarly employed.

17. When we have the logarithm of a number N for any particular value of r, the base, we can readily obtain the logarithm of the same number in every other system. Since, art. (5), when the base is r we have $r^x = N$, we shall likewise have $R^X = N$ when the base is R, in which x is different from X, therefore, $R^X = r^x$.

=0.9542425

Now taking the logarithms relatively to the system whose base is r, then

but $l.r_x = x$ by hypothesis, and $l.R_x = X l.R$, art. (12), whence X l.R = x, or $X = \frac{x}{l.R}$. But if R is the base, X will be the logarithm of N in the system having that base, and designating this by L.N to distinguish it from the other, we shall have $L.N = \frac{l.N}{l.R}$. (12)

consequently we obtain the logarithm of N in the second system, by dividing its logarithm taken in the first system by the logarithm of the base of the second system. Again from formula (12) we get

L.N $\times l.R = l$, N (13) Hence in every system the logarithm of any number is the product of its Napierean logarithm by the logarithm of R, called the modulus.

Also since $\frac{l. N}{L.N} = l. R$, there exists between l. N and L.N a constant ratio represented by l.R

Since we have by formula (12) L.N= $\frac{l.N}{l.R}$, as N=10, then art (15)

 $2.3025851 = \frac{1}{M}$, or $M = \frac{1}{2.3025851} = 0.4342944819$, and 2M = 0.8685889638

18. It is now easy to construct a table of common logarithms whose base r=10, for by formula (13) we have $l.N=l.R\times L.N$, but l.R=M=0.4342944849; consequently $l.N=0.4342974819\times L.N$. It therefore only is necessary to substitute this value for M in any of the series formerly give for the computation of the Napierean logarithms to obtain the common; thus, if in series (8) for 2 M we substitute its value 0.86858896 we shall have

log. (N+1)=0.86858896 $\left(\frac{1}{2N+1} + \frac{1}{3(2N+1)^3} + \frac{1}{5(2N+1)^5} + &c.\right)$ + log. N, and making N successively 1, 2, 3, &c. Log. 1 = 0.0000000

 $2 = 86858896 \left(\frac{1}{3} + \frac{1}{3^4} + \frac{1}{5.3^5} + , &c.\right)$ $3 = 86858896 \left(\frac{1}{5} + \frac{1}{3 \cdot 5^5} + \frac{1}{5^6} + , &c.\right) + \log. 2$ $4 = 2 \log. 2.$ $5 = 86858896 \left(\frac{1}{9} + \frac{1}{3.9^5} + \frac{1}{5.9^5} + , &c.\right) + \log. 4$ $6 = \log. 2 + \log. 3$ $7 = 86858896 \left(\frac{1}{13} + \frac{1}{3(13)^5} + \frac{1}{5(13)^5} + , &c.\right) + \log. 6. = 0.8450980$ $8 = 3 \log. 2$ = 0.90309900

10=
19. After Lord Napier had computed his first tables of logarithms it occurred to him that it would be proper to change the radix R=2.7182818 to r=10, at the same time making the logarithms of integers positive, and those of fractions negative, (art. 8.), as more conformable to the denary scale notation, and more convenient in practice.

It appears that Mr Henry Briggs had also conceived the idea of

 $9 = 2 \log_{10} 3$

changing the radix, and had computed logarithms on a plan somewhat less commodious, by making the logarithms of integers negative, and those of fractions positive, which, upon a personal communication with Lord Napier, he rejected, and finally adopted his lordship's views. He soon afterwards published the first thousand logarithms of this kind under the title of Logarithmorum Chilias Prima.

SECTION III.

Of the Trigonometrical Lines, called Sines, Tangents, &c.

20. THE Egyptians and Chaldeans began to study astronomy at a very early period. As the determination of the relations and distances of the heavenly bodies involve the mensuration of lines and angles, it was necessary to invent some method of ascertaining the value of these quantities, at least in an approximate manner, before any useful results could be obtained. Some of the more elementary propositions in geometry must have been discovered in the most remote antiquity, and the inventive genius of the Greeks filled up the general outline. The properties of geometrical figures thus acquired, would, without doubt, be applied to the mensuration of several magnitudes, and the distances of various points in space. About six hundred years before the Christian era, Thales measured the heights of the pyramids in Egypt by means of their shadows; a method which depends upon the proportionality of the sides of similar triangles. This simple property forms the basis of modern trigonometry. If, for example, a pole or gnomon be set perpendicular to the horizontal plane, it will, in a clear day, when the sun is not vertical, cast a shadow to a given distance, while any other high object, such as a steeple near, it will do the same. If straight lines be conceived to be drawn from the top of these objects to the extremity of each of their shadows, it is evident that, unless they are very distant, by this means triangles nearly similar will be formed, whose sides are proportional; that is, as the shadow of the gnomon is to its height so is the shadow of the object to its height. Now, suppose the length of the shadow of the gnomon to be made the radius with which an arc of a circle is described commencing at the bottom of the gnomon, and, as will be afterwards explained, measuring the angle between the horizontal line and the line from the extremity of the shadow to the top of the gnomon, that gnomon will, by the principles of geometry be a tangent to the circle. Whence the former proportion becomes as the radius is to the tangent of the angle of elevation, so is the length of the shadow of the object to its height. It would thus require the length of the shadow of the pole or gnomon to be measured each time any height was determined. This, however, might be avoided by having the measure of a set of triangles whose sides, to an assumed radius, and a corresponding series of angles, are previously determined by computation. By this means, in such cases, it is only necessary to measure the angle of elevation of the object, at a given point, and its distance from it, and comparing it with one of those computed triangles equiangular to it, to determine, in a manner similar to the former, the height of the object. It is obvious that the same principles may be applied to objects situated in any plane, whether vertical, horizontal, or oblique.

Several series of triangles of the kind now mentioned have been

actually computed and arranged in tables under the designation of

trigonometrical tables.

These were not accomplished at once, but were the improvements of successive ages. Hipparchus, about 150 years before the Christian era, supposed similar triangles to be inscribed in circles, and employed in his computation the chords subtending the arcs measuring them in sexagesimal parts of the radius. Nearly 300 years afterwards, Ptolomy, in his Μεγαλη Συνταξε, recomputed the chords, but in his Analemma employs the half chords instead of the chords approaching very nearly to the use of sines, afterwards introduced by the Arabians.

Some notions of the tangents, secants, and versed sines, were, towards the beginning of the tenth century, entertained by the more learned Arabians. About the beginning of the fifteenth century the sciences began to be cultivated in Europe, where the greatest progress has been made. At that period Müller invented the tangents, and shortly after Maurolycus produced his table of secants. These were all in natural numbers to a given radius now generally taken at unity, and, therefore, their application was in many cases troublesome. To remove this inconvenience as far as possible, Napier invented his logarithms, which have brought them perhaps to the last degree of perfection.

Hipparchus, who has been followed by most of the moderns, employed the circle to measure angles. He supposed the whole circumference to be divided into 360 equal parts each called a degree. The degree was divided into 60 equal parts called minutes, and the minute into 60 equal parts called seconds, and the sexagesimal division was continued, though now the fractions of seconds are more commonly expressed in decimals, which are more convenient for calcula-

tion.*

Whence the semicircle contains 180 degrees and the quadrant 90. As four right angles can be constituted about a point, 90 degrees must be the measure of a right angle. For the purposes of abbreviation a degree is marked with a small circle, a minute with one accent, a second with two accents, &c. Thus 57° 17′ 44″.806, denotes 57 degrees, 17 minutes, 44 seconds, and .806 the decimal, whose value is 806 thousandths of a second. This, being an arc whose length is equal to the radius as will be afterwards explained, is also expressed in degrees and decimal parts of a degree, thus 57°.2957795, a mode of using it, which in some cases has its advantages.

The number of these parts, in either case, contained in the arc between the lines constituting the angle, of which are the angular point is the centre, indicates the measure of that angle accordingly.

Hence, if to any number expressed in sexagesimal degrees oneninth of itself be added, the sum will be the same number expressed in the centesimal degrees; and if from any number expressed in centesimal degrees one-tenth of itself be subtracted, the remainders will be the same number expressed in sexagesimal degrees.

The French have lately adopted the centesimal division, which, in many cases, is preferable to the sexagesimal. The whole circle is divided into 400 degrees, each degree into 100 minutes, and the centesimal division is continued. Hence the semicircle contains 200 degrees, the quadrant 100, and the ratio of the centesimal to the sexagesimal is as 9 to 10.

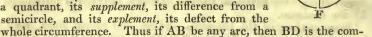
To convert sexagesimal degrees into centesimal add $\frac{1}{3}$ of the arc to itself. The converse is effected by subtracting $\frac{1}{10}$ of the arc from itself.

DEFINITIONS.

21. If two straight lines intersect one another in the centre of a circle, the arc of the circumference intercepted between them is called

the measure of the contained angle, whatever be the radius of the circle, since the arcs are proportional to their radii. Thus, the arc AB or A'B', is the measure of the angle ACB, and is expressed in degrees, &c.

22. The *complement* of an arc is its difference from a quadrant, its supplement, its difference from a semicircle, and its explement, its defect from the



plement, BE the supplement, and BDEFA the explement. The same thing holds with regard to the angles of which the arcs are the measures, that is, if ACB be any angle, BCD its difference from a right angle is called the complement, BCE the supplement to two right angles, and BCA, measured by the arc BDEFA, the explement or difference from four right angles.

23. The sine of an arc, or of an angle of which the arc is the measure, is a perpendicular let fall from one of its extremities upon a radius or diameter passing through the other.

24. The versed sine or versine of an arc is that part of the diameter

intercepted between its sine and the circumference.

25. The tangent of an arc is a perpendicular to the extremity of the radius at one end of the arc, and limited by a straight line drawn from the centre passing through the other.

26. The secant of an arc is the straight line drawn from the cen-

tre to the extremity of the tangent.

27. It is usual to express the sine, tangent, and secant of the complement of an arc by the abbreviated terms cosine, cotangent, and cosecant.

28. Let ACDE be a circle of which the diameters AD and CE are at right angles to one another.

Take any arc AB, produce the radius OB, and draw BG, AK perpendicular to AO or AD, and HB, CI perpendicular to CE; then BG is the D sine, BH or GO the cosine, AG the versine, CH the coversine, DG the suversine, and HE the sucoversine of the arc AB. Also of that arc AK is the tangent, CI the cotangent, OK the secant, and OI the cosecant.



29. Since the diameter which bisects an arc, also bisects the chord of that arc at right angles, therefore, the sine of an arc is equal to half the chord of twice the arc. Thus $BG=\frac{1}{2}BF=$ half the chord of the arc BAF, the double of the arc AB.

30. In the right-angled triangle OGB, $BG^2 + OG^2 = OB^2$, that is, the squares of the sine and cosine are together equal to the square

of the radius.

31. The triangle OGB being similar to OAK, OG: GB:: OA: AK, or the cosine of an arc is to the sine as radius is to the tangent.

Also the triangles OGB, OAK being similar, as before, OG: OB:: OA: OK, the radius is a mean proportional between the cosine and the secant.

33. Since DG: GB:: GB: GA, it follows that the sine is a mean

proportional between the versine and suversine.

34. Again, AD: AB:: AB: AG, or the chord of an arc is a mean proportional between the diameter and versine.

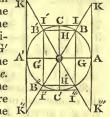
Cor.—Since $AB^g = AD \cdot AG$, then, because AD is constant, AB^g varies as AG, or $(\frac{1}{2}AB)^g \propto AG$, that is, the square of the sine varies directly as the versine, or inversely as the cosine, of twice the arc.

35. The triangles OAK and ICO are similar, therefore AK: AO:: OC: CI; consequently the radius is a mean proportional between

the tangent and cotangent of an arc.

36. In the application of algebra to geometry, where the trigonometrical lines are employed, it is necessary to trace their changes in the several quadrants of the circle, since it is obvious that the same

lines treated of above, may be applied to each. In the first quadrant AC, if the sine BG and cosine GO be supposed positive, then the sine B'G' on the same side of the diameter AA', and in the same direction, still remains positive; but the cosine OG' having changed its position with respect to the centre O, or diameter CC', becomes negative. In the third quadrant, the cosine AG' and sine G'B'', having both changed their positions, are both negative. In the fourth quadrant, the cosine K'



 $R \times \sin$.

having resumed its original position, OG is now positive, while the sine GB", remaining as in the third quadrant, is negative. The tangents and secants depending upon the sines and cosines have their signs determined accordingly.

From article 30, to 35 and inclusive, R being radius, &c. we obtain

^{*} In the above wood-cut, B" has been omitted near I", which may easily be supplied by the pen.

37. Now, since (7) $\tan = \frac{\sin}{\cos}$, then it follows from the principles of algebra, that when the signs of the sine and cosine are *like*, the sign of the tangent is *positive*, and when *unlike*, the sign of the tangent is *negative*. In like manner, the signs of the cotangent, secant, and cosecant may be determined from formulas (8), (9), and 10).

Table of the Signs of Trignometrical Lines.

| Quadrants. | | Sine. | Cosine. | Tangent. | Cotangent. | Secant. | Cosecant. |
|------------|-----------|-------|---------|---------------|-------------|---------|-----------|
| 1 | 5 9 | + | 1 1 1 | 1 - 1 - 1 NO. | + | dit- | |
| 2 | 6 10 | 1 + | 1 | - | of the con- | | + > |
| 3 | 7 11 | | y()() | + 4 | + | | 100 |
| 4 | 8 12, &c. | (| 101 | | - | 4 | |

Of the Multiples and Powers of Arcs.

38. In most treatises on geometry, such as Leslie's, Legendre's, &c. the elementary propositions containing the principles of trigonometry are also given. It is therefore unnecessary to repeat them here, as it only puts the student to the expense of purchasing the same things in two or three different works. We shall only give a few of the results most generally useful, referring to those works on geometry and trigonometry where the requisite information may be obtained.*

If a and b are two given arcs of a circle of which the radius is

unity, then

$$\sin (a+b) = \sin a \cos b + \sin b \cos a$$
 (1)
 $\cos (a+b) = \cos a \cos b = \sin a \sin b$ (2)

$$sin. (a-b) = sin. a cos. b = sin. b cos. a$$

$$cos. (a-b) = cos. a cos. a + sin. b sin. a$$
(3)

 $\cos (a-b)=\cos a \cos a + \sin b \sin a$ (4) If we divide these equations, the one by the other in succession, that is, (1) by (2), and (3) by (4), then

$$\tan (a+b) = \frac{\sin a \cos b + \sin b \cos a}{\cos a \cos b - \sin a \sin b}$$
 (5)

$$\tan (a-b) = \frac{\sin a \cos b - \sin b \sin a}{\cos a \cos b + \sin b \sin a}$$
 (6)

Dividing the two terms of the second numbers by $\cos a \cos b$, and substituting $\tan a$ and $\tan b$ for their values in terms of the sine and \cos

$$\tan (a+b) = \frac{\tan a + \tan b}{1 - \tan a \tan b} \qquad (7)$$

$$\tan (a-b) = \frac{\tan a - \tan b}{1 + \tan a \tan b} \qquad (8)$$

expressions which give the tangent of the sum and of the difference of two arcs in terms of the tangents of these arcs.

If we make a=b in the preceding formulæ, they give

$$\tan 2 a = \frac{2 \tan a}{1 - \tan^2 a}$$
 . (11)

^{*} Those we would more particularly recommend are the treatises of Gregory, Woodhouse, Lardner, and Cagnoli. Dr Kelly's Spherics is a very good treatise for teaching the practice of the stereographic projection of spherical triangles.

expressions which give the sine, cosine, and tangent of twice the arc in terms of the sine, cosine, and tangent of the simple arc.

39. Returning to equations (1), (2), &c. we have by addition and

subtraction

$$\sin (a+b) + \sin (a-b) = 2 \sin a \cos b$$
 (12)

$$\cos (a+b+\cos (a-b)) = 2 \cos a \cos b$$
 (13)

$$\sin (a+b) - \sin (a-b) = 2 \sin b \cos a$$
 (14)

 $\cos (a-b) = \cos (a+b) = 2 \sin a \sin b$ (15)Let (a+b)=u, and (a-b)=v, then by addition and subtraction

 $a=\frac{1}{2}(u+v)$, $b=\frac{1}{2}(u-v)$, consequently the preceding formulæ become

$$\begin{array}{lll} \sin u + \sin v &= 2 \sin \frac{1}{2} \left(u + v \right) \cos \frac{1}{2} \left(u - v \right) & . & . & . & . & . \\ \sin u - \sin v &= 2 \cos \frac{1}{2} \left(u - v \right) \cos \frac{1}{2} \left(u + v \right) & . & . & . & . \\ \cos u + \cos v &= 2 \cos \frac{1}{2} \left(u + v \right) \cos \frac{1}{2} \left(u - v \right) & . & . & . & . \\ \end{array}$$

$$\sin u - \sin v = 2 \cos \frac{7}{2} (u - v) \cos \frac{7}{2} (u + v) .$$
(17)
$$\cos u + \cos v = 2 \cos \frac{7}{2} (u + v) \cos \frac{7}{2} (u - v) .$$
(18)

$$\begin{array}{l}
\cos u + \cos v = 2 \cos \frac{1}{2} (u+v) \cos \frac{1}{2} (u-v) \\
\cos v - \cos u = 2 \sin \frac{1}{2} (u+v) \sin \frac{1}{2} (u-v)
\end{array} \tag{19}$$

expressions which serve to transform the sum or the difference of the sine or cosine into the product, and thus to unite the two terms into one.

If we divide formula (16) by formula (17) they give

$$\frac{\sin u + \sin v}{\sin u - \sin v} = \frac{\tan \frac{1}{2}(u + v)}{\tan \frac{1}{2}(u - v)}$$
 (20)

If we multiply these equations member by member, observing to substitute sin. $2a=2\sin a\cos a$, formula (9), then

$$\sin^2 u - \sin^2 v = \sin (u+v) \cos (u+v)$$
 (21)

(21) $\cos^2 v - \cos^2 u = \sin(u+v) \cos(u+v)$ Since sin. 2 $a=2 \sin a \cos a$, and $\cos 2 a=\cos^2 a=\sin^2 a$.

The second of these equations may be put under the two following forms:

cos.
$$2 a = 1 - 2 \sin^2 a$$
, and cos. $2 a = 2 \cos^2 a - 1$
whence $\sin^2 a = \frac{1 - \cos 2 a}{2}$, and $\cos^2 a = \frac{1 + \cos 2 a}{2}$. (22)

These expressions are used when, for the squares of the sine and cosine, the first power of the cosine of the double arc is substituted.

40. Let 2a = u, then $a = \frac{1}{2}u$ formula (22), these formulæ become

$$\sin^{2}\frac{1}{2}u = \frac{1-\cos u}{2}, \cos^{2}\frac{1}{2}u = \frac{1+\cos u}{2}$$
 (23)

and dividing each corresponding number successively, they give

$$\tan^{2}\frac{1-\cos u}{1+\cos u}$$
 (24)

and cos.
$$u = \frac{1 - \tan^{\frac{2}{2}} \frac{1}{2} u}{1 + \tan^{\frac{2}{2}} \frac{1}{2} u}$$
 (25)

If b in formulæ (1), (2) be made 2a, 3a, &c. we may obtain multiple arcs thus:

sin.
$$3 a$$
=sin. $a \cos 2 a$ + sin. $2 a \cos a \cos 3 a$ =cos. $a \cos 2 a$ —sin. $a \sin 2 a$

Substituting for sin. 2 a and cos. 2 a, their values, they become $\sin 3 a = 3 \sin a \cos^2 a - \sin^3 a$

$$\sin 3 a = 3 \sin a \cos^2 a - \sin^3 a$$
 (26)
 $\cos 3 a = -3 \cos a \sin a + \cos^3 a$ (27)

These may be put under the form

$$\sin 3 a = \cos^3 a (3 \tan a - \tan^3 a)$$

 $\cos 3 a = \cos^3 a (1 - 3 \tan^2 a)$

the transfer of the second state of the second

In general n being any integer,

$$\sin n \, a = \cos^{n} \, a \, \left\{ n \, \tan. \, a - \frac{n \, (n-1) \cdot (n-2)}{1 \cdot 2 \cdot 3} \tan.^{3} \, a + \frac{n \cdot (n-1) \cdot (n-2) \cdot (n-3) \cdot (n-4)}{1 \cdot 2 \cdot 3 \cdot 4 \cdot 5} \tan.^{5} \, a \dots &c. \right\}$$
(29)

$$\cos na = \cos na \left\{ 1 - \frac{n(n-1)}{1 \cdot 2} \tan^2 a + \frac{n(n-1)(n-2)(n-3)}{1 \cdot 2 \cdot 3 \cdot 4} \tan^4 a, \&c. \right\} (29)$$
The coefficients of the different terms and the first of the different terms and the different terms and the different terms are the different terms and the different terms are the different terms and the different terms are t

The coefficients of the different terms are those of the nth power of the binomial, whence these series may be collected under the following form:

$$\sin n \, a = \frac{1}{2\sqrt{-1}} \left\{ \cos a + \sqrt{-1} \sin a \right\}^n \frac{1}{2\sqrt{-1}} \left\{ \cos a - \sqrt{-1} \sin a \right\}^n (30)$$

cos. $n = \frac{1}{2} \left\{ \cos a + \sqrt{-1} \sin a \right\}^n + \frac{1}{2} \left\{ \cos a - \sqrt{-1} \sin a \right\}^n (31)$ These formulæ, by development, will give the two foregoing series, and are thus easily verified.

41. It may be shown* that if
$$x$$
 represent any arc $\sin x = x - \frac{x^3}{1.2.3} + \frac{x^5}{1.2.3.4.5} - \frac{x^7}{1.2.3.4.5.6.7} +$, &c. (32) $\cos x = 1 - \frac{x^2}{1.2} + \frac{x^4}{1.2.3.4} - \frac{x^6}{1.2.3.4.5.6} +$, &c.

In these expressions the arc x is supposed to be divided by the radius, which is here taken for the unit of length, and consequently if we wish to restore it we must write $\frac{x}{r}$ in place of x and

instead of sin. x in the two members of these equations.

These formulæ might be carried much farther than can be introduced into this place. Most of them may be seen by consulting the books already referred to, but above all the analysis infinitorum of Euler.

Tables of Multiples and Powers of Arcs.

1. 2.
$$\sin a = s, s \begin{cases} \text{being the sine of the force } \\ \text{arc } a. \end{cases} \cos a = (1-s^2)$$

$$\sin 2 a = 2s (1-\sin^2) \frac{1}{2} \cos 2 a = 1-2s^2$$

$$\sin 3 a = 3s-4s^5 \cos 3 a = (1-4s^2) (1-s^2) \frac{1}{2}$$

$$\sin 4 a = (4s-8s^5) (1-s^2) \frac{1}{2} \cos 4 a = 1-8s^2+8s^4$$

$$\sin 5 a = 16s^5-20s^5+5s, &c. \cos 5 a = (1-12s^2+16s^4) (1-s^2 \frac{1}{2}) &c. \end{cases}$$

$$\tan a = t, t \begin{cases} \text{being the tangent } a. \end{cases} \cot a = \cot.$$

$$\tan 2 a = \frac{2t}{1-t^2} \cot 2 a = \frac{\cot^2 - 1}{2 \cot}$$

$$\tan 3 a = \frac{3t-t^5}{1-3t^2} \cot 3 a = \frac{\cot^2 - 1}{3 \cot^2 - 1}$$

$$\tan 4 a = \frac{4t-4t^5}{1-6t^2+t^4} \cot 4 a = \frac{\cot^4 - 6 \cot^2 + 1}{4 \cot^5 - 4 \cot^4 - 1}$$

$$\tan 5 a = \frac{5t-10t^5+t^5}{1-10t^2+5t^4}, &c. \cot 5 a = \frac{\cot^5 - 10\cot^5 + 5\cot^4 - 1}{5\cot^4 - 10\cot^5 + 1}, &c.$$

^{*} Woodhouse's Trigonometry, third edition, page 245-Gregory, page 42 and 50.

 $2 \sin^2 a = 1 - \cos 2a$ $2 \cos^2 a = 1 + \cos 2a$

 $4 \sin^{5} a = 3 \sin^{2} a - \sin^{3} a$ $4 \cos^{5} a = 3 \cos^{2} a + \cos^{3} a$

 $8 \sin^4 a = 3 - 4 \cos^2 2a + \cos^4 4a = 3 + 4 \cos^2 2a + \cos^4 4a$

42. Having given a short abstract of the more useful formulæ relative to multiples and powers of arcs, we shall now proceed to shew the method of constructing the tables of sines, tangents, &c.

When the radius of a circle is unity, the semicircumference is 3.1415926536 nearly. Now there are 180° or 10800′ in a semicircle, consequently, if the former be divided by the latter, the result will be 0.0002908382, the measure of an arc of one minute, which, as the arc is so small, may be considered its sine.

Now, art. 35. 2, $\cos = (1 - \sin^2 2)$ consequently $\cos 1' = 0.9999999577$. If these values are substituted in formulæ, (32), and (33), art. 41 the sines and cosines may be obtained through the

whole quadrant.

Thus let the arc a=1', and, therefore, sin. x=0.0002908882. Let $a=5^{\circ}$, then $\frac{5 \times 3.1415926536}{180} = 0.08726646$ the length of a or x, and

$$x = +0.08726646$$

$$-\frac{x^5}{1.2.3} = -0.00011076$$

$$+\frac{x^5}{1.2.3.4.5} = +0.00000004$$

therefore, $x = \frac{x^5}{1.2.3} + \frac{x^5}{1.2.3.4.5}$, &c.=0.08715574= the natural sine of 5°, the logarithm of which is 8.740206, the log. sine the same arc. This method is easy when the arc is small, as the series then converges very rapidly, but it is rather laborious when the arc is large, in which case recourse must be had to other methods depending upon the properties of multiple arcs, as may be seen in most of our treatises on trigonometry.

As the sines are computed, the cosines of the same arcs may be found from art. 41, formula (33), or from art. 35, formula (2), the tangents and cotangents, from formula (7) and (8), and the secants and

cosecants from (9) and 10).

SECTION IV.

Of the application of Tables of Sines, Tangents, Secants, &c. to plane Trigonometry.

CASE I.

43. In any plane triangle it is shewn in our usual treatises, that the sides are proportional to the sines of their opposite angles, or

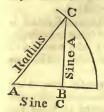
The sine of any one angle,
Is to the sine of another angle;
As the side opposite to the first,
Is to the side opposite to the second.

These terms may be taken alternately, inversely, &c.

44. When one of the angles is a *right* angle, then the preceding rule may either be applied, or a modification of it derived from the properties which are peculiar to right-angled triangles.

In right-angled triangles, it is usual to call that side subtending the right angle the *hypotenuse*, and the other sides which contain the right angle the *legs*, or the one the *base* and the other the *perpendi*cular.

Then if one of the sides of any triangle ABC, be assumed equal to the radius, the names of the other sides must be determined by art. 28, as follows:—







The names of the sides being thus known when three of the parts of a triangle including a side are given, the rest may be found by the following rules:—

I.—To find a side.

As the name of the given side,

Is to the name of the required side;

So is the given side,

To the required side.

II.—To find an angle.

As the side made radius,
Is to the other given side,
So is radius,

To the name of this side.

Any side may be made radius to find a side, but one of the given sides must be made radius to find an angle.

In the solution of plane triangles, it must be recollected that all the angles in any triangle are together equal to two right angles, or 180°. Whence if two of the angles are given, the other may be found by subtracting their sum from 180°; when one angle is given the sum of the other two may be found by subtracting it from 180°; and if one be right or 90°, the sum of the other two is also 90°, and the one is the complement of the other.

CASE II.

45. In a plane triangle when the two sides and contained angle are given.

I. As the sum of the given sides,

Is to their difference;

So is the tangent of half the sum of the opposite angles,

To the tangent of half their difference.

Half the difference added to half the sum of those angles gives the greater, and subtracted from half the sum gives the less.

All the angles being now known, the third side may be found by

the rules in case I.

Or, after having found half the sum and half the difference of the angles, the remaining side may be found without determining the actual angles, as proposed by Thacker in 1743, and recommended by Professor Wallace, in the Edinburgh Philosophical Transactions, in the following manner:

II. As the sine of half the difference of the opposite angles,Is to the sine of half their sum,

So is the difference of the containing sides;

To the remaining side; or,

III. As the cosine of half the difference of the opposite angles, Is to the cosine of half their sum; So is the sum of the containing sides

To the remaining side.

These two methods may be used as a verification to each other, and will be found somewhat more easy in practice than the first method, as several of the quantities may be taken out from the tri-

gonometrical tables at the same time.

Should the sides come out in logarithms from some previous operation, then Gauss' table for finding the logarithm of the sum and difference of numbers from their logarithms, without first determining the natural numbers themselves, would be some advantage, though it was not thought sufficient to warrant an insertion of it among the tables.

The following method of resolving this problem is convenient, par-

ticularly when the logarithms of the sides are given.

IV. From the logarithm of the greater of the two given sides, having its index increased by 10, subtract the logarithm of the less side, the remainder will be the logarithm tangent of an arc, from which, 45° being subtracted, there will be obtained a remainder. To the logarithm tangent of this remainder add the log. tangent of half the sum of the opposite angles, the sum, rejecting 10 in the index, will be the log. tangent of half their difference, from which the angles themselves may be found.

CASE III.

46. In any plane triangle, when the three sides are given, . I. As the base

Is to the sum of the sides; So is the difference of the sides

To the difference of the segments of the base made by a perpendicular upon it, or upon it produced from the opposite angle.

It may perhaps be convenient to call the longest side the base,

in order that the perpendicular may fall within the triangle.

When the three sides of a triangle are given, the difference of the segments of the base may thus be found. Then half the difference added to half the sum, that is, to half the base, will give the greater segment adjacent to the greater side; and half the difference taken from half the sum will give the less. From these the angles may be found by Rule II. § (44).

II. In a plane triangle, as the rectangle under any two sides, is to the rectangle under the excesses of the semiperimeter above those sides; so is the square of the radius to the square of the sine of half their contained angle, as shown in Leslie's Geometry. In practice, this rule, when logarithms are employed, may be stated as follows:

To the arithmetical complements of the logarithms of the two sides containing the required angle, add the logarithms of the differences between those sides and half the sum of the three sides, then half the sum of these four logarithms will be the log. sine of half the required angle.

III. To the arithmetical complements of the sides containing the required angle, add the logarithm of half the sum of the three sides.

and the logarithm of the difference between this half sum and the side opposite the required angle; half the sum of these four logarithms will be the log. cosine of half the required angle.

IV. To the arithmetical complement of the logarithm of half the sum of the three sides, add the arithmetical complement of the difference between half the sum of the three sides and the side opposite the required angle, and the logarithms of the differences between that half sum and the sides containing the required angle; half the sum of those four logarithms will be the log. tangent of half the required angle.

It may be remarked that these three last rules will, in general, be the most commodious in practice, though, in particular cases, each may have its peculiar advantage when great accuracy is required.

When the required angle does not exceed 90°, Rule II. may be used, when it does, Rule III. may be employed; and in either case Rule IV. will give correct solutions. These observations depend upon the variation of the trigonometrical lines in certain parts of the circle, as, for example, near 90°, the sines vary very slowly, so that the true value of an arc cannot be obtained by our ordinary tables, while the tangents always vary by such perceptible quantities as to leave no doubt of the real value of the required arc. These remarks may be easily verified by examining any of our tables extended to six or seven places of decimals.

Of the Construction of Triangles.

47. Previous to the numerical solution of any triangle, it is generally first constructed geometrically. This is accomplished by means of what are termed mathematical instruments, consisting of scales, compasses, &c. contained in a case, at various prices, to suit the convenience of purchasers. Printed descriptions of these, as well as of many others, are to be found in Jones' edition of Adams' Geometrical and Graphical Essays.

In the construction of plane triangles the sides are taken from a scale of equal parts, and the angles are laid down by a scale of chords,

or more conveniently by a protractor.

EXAMPLES.

CASE I.

48. 1. Given the angles and hypotenuse of a right-angled triangle, to find the base and perpendicular.

Let the hypotenuse AC of the right-angled triangle ABC be 288,

and the angle A 39° 22'; it is required to find the sides AB and BC.

Construction.—In the indefinite straight line AB take any point A, and by a protractor or scale of chords, make the angle A equal to 39° 22'; from any convenient scale of equal parts take AC equal to 288, and from C draw CB, perpendicular to AB;

a

then ABC will be the triangle required. In order to simplify and preserve uniformity, the angles may, in general, be denoted by the capital letters A, B, C, and the opposite sides by the small letters a, b, c. The sides a and c being measured by the same scale from which b was taken, will be found to be 182.7 and 222.7.

Calculation

1. By natural numbers, § (43).

To find a.

As sin. B: sin. A:: b: a, or $a = \frac{\sin A \times b}{\sin B}$

 $1:0.634281::288:\frac{0.634281\times288}{1}=182.673=a$

To find c.

And sin. B: sin. C, or cos. A:: b:c

 $1:0.773103::288:\frac{0.773103\times288}{1}=222.654=c$

2. By logarithms.

To find a.

| As sin. B, or radius Is to sin. A 39° 22′ So is b 288 | . 10.000000 9.802282 . 2.459392 |
|---|---------------------------------------|
| To a 182.673 . To find c. | 2.261674 |
| As radius | 10.000000 9.888237 2.459392 |
| То с 222.653 | 2.347629 |

The solutions may be varied by assuming any of the sides for radius, according to art. (44), and verified by Gunter's scales.

2. Given the angles and one side, to find the hypotenuse and the

other side.

Let the side AB be 758, and the angle C 39° 26'; to find the angle A, and the sides BC and AC.

Ans.—BC is 921.7, and AC 1193.36, and the angle A 50° 34'.

Construction.—From a scale of equal parts make AB equal to 758, the angle A 50° 34′, the complement of C, and draw BC at right angles to AB; produce AC and BC till they meet in C; then ABC is the triangle required, and a and b measured on the same scale from which c was taken will be found to be about 922 and 1193 respectively.

3. Given the hypotenuse and one side, to find the angles and other

side

Let the hypotenuse AC be 544, and the base 464; to find the angles A, a and c, and the side BC.

Ans.—The angle A is 31° 28′, though C is 58° 32′ and BC 284.

Construction.—Make AB equal to 464 from a scale of equal parts, and from B draw BC perpendicular to AB, then from the centre A at the distance AC equal to 544 describe an arc intersecting BC in C, join AC, and the triangle is constructed. The angle A being measured by a protractor or scale of chords, will be found to be 31° 28′, consequently C is 58° 32′, and the side BC 284 from the same scale by which the other sides were laid down.

4. Given the base and perpendicular, to find the angles and hypo-

tenuse.

Let the base AB be 558, and the perpendicular BC 456; required the angles A and C and the hypotenuse AC.

Ans.—A 39° 15′ 21″, and 50° 44′ 39″, and AC 720.622.

Construction.—Make AB equal to 558, and draw BC perpendicular to AB and equal to 456, join AC, and the triangle is constructed. The angle A will measure 39½°, and the hypotenuse will be about 721 nearly on the scale of equal parts. The other side may be found by Euclid I. and 47, or Leslie's Geometry II. 10, and 13.

5. Given the angles and one side of an oblique-angled plane trian-

gle, to find the other sides.

In the triangle ABC, are given the side AC, 532, the angle A 38° 40′, C 92° 46′, and consequently the angle B 48° 34′; to find the sides AB and BC.

Ans.—AB 708.76, BC 443.34.

Construction.—Draw the indefinite AB, at A make the angle BAC equal to 38° 40′, and from a scale of equal parts make AC 532, at C draw CB making the angle ACB equal to 92° 46′, it will cut AB in B forming the triangle ABC which was required.



6. Given two sides, and an angle opposite one of them, to find the

other angles and the third side.

In the triangle ABC are given the side AB 274, AC 306, and the angle B 78° 13'; required the angles A and C, and the third side BC.

Ans.—The angle C is 61° 14′, the angle A 48° 33′, and the side BC 203.22.

Construction.—Make AB equal to 274, the angle B equal to 78° 13′, and with an extent equal to AC, 306, intersect the line BC in

C; ABC is the triangle required.

If in this triangle the side B be greater than C, there may be two triangles formed, constituting what is called the ambiguous case, that is, it admits of two solutions, either of which answers the conditions required, unless from some known circumstances one of them must be adopted in preference to the other.

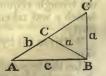
Thus in the oblique-angled triangle ABC there are given AB318,

BC 195, and the angle A 32° 40′.

Ans.—The angle B is 61° 50′ or 118° 20′, the angle C is 85° 40′

or 29°, and the side AB is 360.246 or 175.15.

Construction.—Make AB equal to 318 from any convenient scale of equal parts, the angle A equal to 32° 40′, and with the centre B and distance equal to BC 195 describe an arc cutting AC in C or C′; ABC or ABC′ will be the triangle required.



CASE II.

49. Given two sides and the contained angle, to find the other angles and the third side.

In the triangle ABC let the side AB be 920 and AC 500, and the contained angle A 36° 52′; required the angles B and C, and the third side BC.

Ans.—B is 20° 58′ 50′, C 113° 0′ 10′′, and BC is 600.31.

Construction.—Make AB equal to 920, at the point A make the angle BAC equal 36° 52′, and AC equal to 500; join BC; ABC is the triangle required.

b C B

| uired. | | 3101 3010 100 | |
|---|------------|-------------------------|-----------|
| By Calculation, as | rt. 45, I. | A 38 | c B |
| As AB+BC 1420 | | | 3.152288 |
| Is to AB—BC 420 | ٠, | 139.71 | 2.623249 |
| So is $\tan \frac{1}{2} (B+C) 71^{\circ} 3$ | 34' 10' | 100 % | 10.477162 |
| 70.000 | | and the same | |
| To tan. $\frac{1}{2}$ (B—C) 41 3 | 35 10 | - MA - 100 | 0.948123 |
| . 110 | 0.30 | | |
| | 9 10 | | |
| B 29 5 | 08 50 | | 0.000#14 |
| As sin. B 29° 58′ 50″ | | STATE I LEVEL OF | 9.698714 |
| Is to sin. A 36 52 0 | • | • | 9.778119 |
| So is AB 500 . | | • | 2.698970 |
| To BC 600.31 . | | | 2.788375 |
| Or by art. 45, II. and II | II . | Contractor Contractor | 2.700070 |
| As sin. $\frac{1}{2}$ (B—C) 41° | 35′ 10″ | ITA DESIT | 9.822001 |
| Is to sin. $\frac{1}{2}$ (B+C) 71 | 34 0 | 1 1 1 1 1 1 1 1 1 1 1 1 | 9.977125 |
| So is AB—BC 420 | | 11 12 100 110 | 2.623249 |
| 20 10 1120 20 120 | | | |
| To BC 600 | .31 | | 2.778373 |
| As cos. ½ (B—C) 41° | 35' 10" | 1000 | 9.873877 |
| Is to cos. $\frac{1}{2}$ (B+C) 71 | | Dec 2 | 9.499963 |
| So is AB+BC | 1420 | | 3.152388 |
| I wanted and a second | | | |
| To BC | 600.30 | | 2.778374 |

The advantage of these two last methods consists in its being unnecessary to find the values of the angles C and B to determine BC, and that several of the quantities are found among the tables at the same opening of the book, and if computed both ways they are a check upon each other.

CASE III.

50. Given the three sides of a triangle, to find the angles.

In the triangle ABC, there are given AB 800, AC 320, and BC 562; to find the angles.

Construction.—Draw the line AB equal to 800 from a scale of equal

parts, then from the same scale take an extent equal to AC 320, and with the centre A and distance 320 describe an arc, in like manner, with the centre B and distance BC 162, intersect the former arc in C; ABC is the triangle required.

In the solution of this question, if the angles A or B are first to be determined, then rules II. or IV. § 46, will be found most convenient and accurate; but if C be wanted first, then if great accuracy is required it would be improper to use rule II., but rule III. or IV. should be employed, so as to give the angle with all the requisite accuracy in nice operations.

If they said after while the coord and that the order of the

-- 10.01 hmpyld merce (

(map a

or or or

By Calculation.

| Rule II. | |
|--|----------------------|
| AB 800 AC 320 ar. co. | 7.494850 |
| BC 562 art. co. | 7.250264 |
| Sum 1682 | 11-14-1 |
| Half 841 | PIG (=0 W |
| 1st diff. 521 log. 2d diff. 279 log. | 2.716838 2.445604 |
| Sum | 19.907556 |
| Half 64° 1′ 54″.4 sin. | 9.953778 |
| C 128 3 48 .8 | |
| AB 800 | |
| AC 320 ar. co | 7 494850 7 250264 |
| Sum 1682 | |
| Half 841 log | 2.924797 1.612784 |
| Sum | 19.282694 |
| Half 64° 1′ 54″.9 cos. | 9.641347 |
| 2 | |
| C 128 3 49 .8 | prist in white |
| AB //.800 | ndi ali ami |
| AC 320 BC 562 | gain outs hour o |
| | safe from the |
| of all are, le blue manager - 2 | Marie Alleria |
| Half 841 ar. co. | 8.387216 |
| 2d diff. 521 log | 2.716883 2.445604 |
| Sum in the state of the state o | · |
| Half 64° 1′ 54″.7 tan. | 10.312431 |
| G 100 0 40 4 | |

1 104

do 3/1

From these solutions it appears that the first and second differ about 1" from each other, while the second and last only differ 0".4.

C 128 3 49.4

Had the angle C been nearer 180°, the first and second solutions might perhaps have differed more considerably, while the second and third would have agreed more nearly. Hence it is clear that the proper rules, when great nicety is required, must be chosen according to the nature of the angle.

EXAMPLES FOR EXERCISE.

51. 1. What angle will one foot subtend at the distance of fifty

miles? Ans.— $0^{\prime\prime}.78$.

2. The hypotenuse of a right-angled triangle being 5472 feet, and the acute angle adjacent to the base, 29° 50′ 58″, what are the base and perpendicular?

Ans.—The base 4746.064, and the perpendicular, 2723.538.

3. If the base of a plane triangle be 384, and the other two sides 288 and 192, what is the length of the perpendicular upon the base, and the length of the segments of the base made by a line bisecting the vertical angle?

Ans.—Perp. 139.4274, segments 230.4 and 153.6.

4. There are three towns, A, B, C, so situated that the bearing of B and C from A forms an angle double that of A and C from B, and that of A and B from C double that of A and C from B, or the angle opposite b is double of that opposite c, and the circuit round all the three is just one hundred miles; what are their relalative distances from each other in succession?

Ans.—19.8073, 35.6861, and 44.5066 miles.

5. In the right-angled triangle right-angled at B, given the base AB 70, and the sum of the hypotenuse and perpendicular AC and BC 200, to find the hypotenuse and perpendicular, and the remaining angles?

Ans.—The angle ACB is 37° 16′, AAC 51° 24′, and AC 112.52,

and BC 87.68.

6. In an oblique-angled triangle ABC let the side BC be 532, the angle BAC 110° 30′, and the sum of the sides AB, AC 637; required the angles C and B, and the sides AB and AC?

Ans.—The angle C is 45° 5′, B 24° 25′, and the side AB 402.3 and

AC 234.7.

7. In the oblique-angled triangle ABC, let the side BC be 250, the angle BAC 96° 50′, also the difference between the sides AB and AC 106; required the angles ACB and ABC, together with the sides AB and AC′?

Ans.—ACB is 57° 55′, ABC 25° 15′, and AB 213.4, and AC 107.4.

8. Given the base 214, the vertical angle 49° 16′, and the sum of the other two sides 459; to find the sides and remaining angles?

Ans.—The acute angle is 33° 44′ 48″, the obtuse angle is 91° 59′ 12″, the side opposite the acute angle is 176.75, and the side opposite the obtuse angle is 282.245.

9. Given one of the sides 252, the opposite angle 20° 46′, and the excess of the base above the remaining side 86; to find the remaining

angles and sides.

Ans.—The vertical angle is 94° 22′ 28″, the remaining angle is

55° 51′ 32″, the base is 507.08, and the other side 421.08.

10. Given the base 1514, the vertical angle 75° 24′ 50″, and the perpendicular 972.41; required the remaining sides and angles.

Ans.—The sides are 1298 and 1172, and the angles are 56° 4' 5"

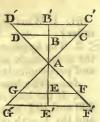
and 48° 31′ 5" respectively.

52. The various sailings in navigation are only the applications of

trigonometry in particular circumstances.

The course is the angle formed between the meridian and the point on which the ship sails, the distance is the hypotenuse, and the difference of latitude and departure, the legs of a right-angled triangle.

Thus let AB represent the meridian; then if a ship sails north-easterly, the line AC is drawn to the right-hand, making an angle BAC equal to the course, and AC represents the distance, AB, the difference of latitude, and BC the departure. If she sails north-westerly, then BAD is supposed to be the angle of course shown by the compass, and is generally in points and quarter points, AD the distance,—AB the difference of latitude and BD the departure. Again, if the ship sail south easter-



ly, AF is the distance, AE the different latitude, EF the departure, and FAE the course. If, however, AE' be the meridian difference of latitude, E'F' is the difference of longitude, E'AF' is the course, and AF is still the distance. Hence the course and distance between two places can be found, by this method, when their latitudes and longitudes are known. This is commonly called Mercator's sailing.

Parallel, middle latitude, and oblique sailings, may readily be explained on similar principles, though these can only be completely

discussed in regular treatises on navigation.

See Mackay's, Norie's, Riddle's, Inman's, or Robertson's Navigation.

EXAMPLES.

1. A ship from latitude 47° 30′ N, sails S. W. by S. 98 miles; what latitude is she in, and what departure has she made?

Ans.—Difference of latitude 81.48, departure 54.45 miles, and the

latitude come to 46° 9' N.

2. A ship from latitude 48° 32′ N. sails between north and west till her departure is 54 miles, and then finds herself in latitude 49° 54′ N.; what course did she steer, and what distance did she run?

Ans.—Course 32° 22′ N. W., and distance 98.18 miles.

3. Coasting along shore I saw a cape bearing N. E. by N. After standing N. W. 20 miles the same cape bore E. N. E. Required the distance of the ship at each station.

Ans.—From the first station 33.26, and from the second 35.31

miles.

4. Required the course and distance from Caithness point in Scotland, in latitude 58° 46′ N. longitude 3° 17′ W., to New York in North America, in latitude 41° 5′ N. and longitude 74° 15′ W.

Ans.—Course 68° 32' or W. S. W. nearly, and distance 2899.2

miles

5. A ship from latitude 60° 24′ N. and longitude 43° W. sails between South and West till she is in latitude 56° 30′ N., and has made 226 miles of departure; required her course, distance, and longitude?

Ans.—Course S. E. nearly, distance 325.4 miles, and the longitude

of the ship 35° 47′ W.

6. Required the course and distance between the Isle of May, in lati-

tude 56° 12′ N. longitude 2° 33′ W., and Heligoland in latitude 54° 12′ N. longitude 7° 53′ E?

Ans.—Course S. 71° 27' E. and Dist. 377 miles.

7. A ship from the Isle of May sailed on the following true courses; required her situation?

| Courses. | Dist. | Diff. Lat. | | Depar | ture. |
|--|---|----------------------|-------------------------------------|---|-------------|
| - mag (Fo) 1 | 0.5 1.0 | N. | S. | E. | W. |
| S. E. S. S. E. N. E. S. E. b. S. E. S. E. W. b. S. N. N. W. N. E. b. N. E. S. E. \(^3\) E. | 40 50 20 60 200 15 20 76 60 | 14.1 18.5 63.2 | 28.3 46.2 49.9 76.5 2.9 | 28.3 19.1 14.1 33.3 184.8 42.2 58.2 | 14.7 7.7 |
| S. 71½ E. | 378 | 95.8 | 218.4 95.8 | 380.0 22.4 | 22.4 |
| و ماران برو ر | | 1000 | 122.6 | 357.6 | ma o |
| Diff. of Lat. Lat. left | To the | Acres - Acres | 2° 3′S. 5 12 N. | | i i |
| Lat. in | | 54 | 9 N. | | |

Hence the ship is about 3 miles south of Heligoland light.

SECTION V.

Application of Plane Trigonometry to the Mensuration of Heights and Distances.

53. One of the most important applications of plane trigonometry is the mensuration of heights and distances. The data are some of the sides and angles of a triangle. The sides are measured by rods, lines, tapes, or chains, constructed according to the degree of accuracy required; and the angles are measured by some angular instrument, such as the quadrant, sextant, reflecting circle, repeating circle, or theodolite. The repeating theodolite is perhaps, in general, the most convenient of all for taking the necessary angles, and the chain, properly constructed, the best for measuring the side called the base, though, to military engineers, the small pocket circular box-sextant, or semicircle, as improved by Sir Howard Douglas, will be found highly useful, when accompanied by the box-measuring tape. One of Schmalcalder's surveying compasses will also be found very commodious in military and nautical surveying. A complete description* of these instruments would far exceed our limits; and their use is best

Those who wish for written descriptions may consult Jones' edition of Adam's Geometrical and Graphical Essays, already mentioned, Biot's Traité d'Astronomie Physique, Delambre's Astronomie, Base du Systeme Metrique, Woodhouse's, Vince's, and Pearson's Treatises of Astronomy.

learnt under the superintendence of a master. In general, it may be remarked, that an allowance must be made for the height of the eye above the horizontal plane; and when the base above-mentioned is inclined to the horizon, it must be reduced to it according to the given inclination, though in nice operations the base is selected so as to be, if not exactly, at least nearly level. Then, from a little attention, by driving in stakes at moderate distances, and levelling their tops, on which deals properly prepared are laid, an exact horizontal line may be obtained. This truly level line is to be most carefully measured, allowance being made for the contraction or expansion of the materials of which the chain is composed according to the state of the thermometer; in nice operations reduced to the level of the sea; and such other precautions as the nature of the case may require must be observed, in order to insure the greatest possible accuracy; many examples of which may be seen in the Trigonometrical Survey of the British islands under the direction of the Board of Ordnance.* A number of the more useful problems connected with trigonometrical surveying may be seen in the third volume of Hutton's Course of Mathematics by Dr O. Gregory, in Baron Zach's Work on the Attraction of Mountains, in the Base du Systeme de Metrique Decimal, and in Piussant's Geodesie.

EXAMPLE I.

To determine the distance of a tower, inaccessible by reason of an intervening river, I measured, on a horizontal plane, the base AB, 500 yards, and at each end took the angle included between the

other end and the tower, which were 50° 56′ and 75° 10′ respectively: What is the distance of the tower from each end of the base?

In the annexed figure,

AB = 500 $CAB = 50^{\circ} 56'$

 $CBA = 75^{\circ} 10'$, and consequently Angle $C = 180^{\circ}$ — $(A+B)=53^{\circ} 54'$

Hence, sin. C 53° 54′ 9.907406 Is to AB 500′ 2.698970 So is sin. A 50° 56′ 9.890093

To BC 480.46 2.681657 So is sin. B 75° 10′

To AC 590.2

The perpendicular or nearest distance Cd may, if required, be easily found thus:

9.907406

2.698970

9.985280

As radius . 10.000000
Is to AC 598 2 . 2.776844
So is sin. A 50° 56′ 9.890093

To C d 464.45 2.666937

Remarks.—These distances might have been determined without an instrument to measure the angles. Thus, suppose that, in the

^{*} There are several methods of approximating to the heights of objects by means of mirrors, shadows, staffs, geometrical squares, and Gunter's quadrants; but as they are seldom used where much accuracy is required, they are omitted here.

continuation of the base AB, and the lines CA, CB, the four distances, AD, AE, BF, BG, were taken all equal to 100 feet, and DE measured 86, and FG 122 feet, the respective chords, to a radius of 100 feet, of the exterior angles DAE, FBG, which are equal to their vertical interior angles CAB, CBA. Now, since half the chord is the sine of half the angle, we have $\frac{43}{100} = 43 = \sin \frac{1}{2} A = 25^{\circ} 28'$, and $A = 50^{\circ} 56'$. In like manner, $\sin \frac{1}{2}B = 61 = 37^{\circ} 35'$, and $B = 75^{\circ} 10'$, which results agree with the former.

Note 1.—The number 100 was chosen for the sake of simplicity; but any other convenient number may be adopted, taking care to divide

half the measure of the chord by it.

Note 2.—The same thing may be accomplished when the sides of the triangles bear any proportion to each other, by finding from them the angles DAE, FBG. Also the supplements EAB, ABG of the original angles may be found in the same manner, or otherwise by joining AG and BE.

EXAMPLE II.

Wanting to know the breadth of a river, I measured 100 yards in a straight line by the side of it; and at each end of this line I found the angles subtended by the other end, and a tree close by the opposite side, to be 53° and 79° 12′; what is its perpendicular breadth?

Ans.—105.89.

EXAMPLE III.

In order to find the distance between two trees A and B, which could not be directly measured on account of a pool of water which occupied the intermediate space, I measured the distance of each from a third object C, which were 588 and 672 yards respectively, and then at C took the angle ACB between the two trees 55° 40′. Required their distance.

180° 0′
Angle C 55 40

A+B 124 20

1/2 (A+B 62 10

As BC+AC 1260 3.100371

Is to BC—AC 84 1.924273

So is tan. 1/2 (A+B)62° 10′ 0″ 10.277379



| To tan. $\frac{1}{2}$ (A—B) | 7 | 11 53 |
|-----------------------------|-------------|-----------------|
| Angle A | 54 ' 53" | 21 53 58 - 7 |

9.971203 2.827369 9.916859

2.773025 *

To AB 592.96

EXAMPLE IV.

In the trigonometrical survey of Britain, Colonel Mudge found, from computations depending on former operations, that the logarithm of the number expressing the distance between Cheviot and Cross Fell in feet was 5.4654017, and between Cheviot and Wisp Hill 5.2672278, and the angle contained by these, corrected for

In some of the examples the computations in proportion are performed by comparing the sines of the angles with the sides, a method sometimes more easy to beginners.

spherical excess, was 53° 30′ 18″. Required the other angles, and the distance between Wisp Hill and Cross Fell, without first finding the value of the given sides in natural numbers.

Ans.—The angle at Wisp Hill is 87° 14′ 4″.
Cross Fell 39 15 46

The distance of Wisp Hill from Cross Fell 235018.6 feet.

EXAMPLE V.

In order to determine the height of a tower, I measured in a direct line AB 366 feet on a horizontal plane. I then took the angle Cab 37° 30′, the height Aa of my instrument being 5 feet. Required BC the height of the tower.

 $\begin{array}{rcl}
 Ans. & bC \\
 Add & Aa
 \end{array}
 = 280.84.$

Height BC =285.84.



Walking along the side of a river, I observed an obelisk on the opposite side, which on account of the river was inaccessible, but

whose height I wanted to ascertain. For this purpose I took at B the angle CBD 50° 39′ at A the angle CAB 33° 30′, which was distant from B 368 feet. Required the height of the obelisk and the distance of the station D from its base.

Solution.—Because the angle CBD=CAB+ACB, CBD—CAB=ACB=50° 39′—33° 30′=17° 9′, hence sin. C: AB:: sin. A: BC; and in the right-angled triangle DBC are now given BC and the angle CBD, to find DC and BD, 521 and

427.2 feet respectively.

EXAMPLE VII.

A solution of this problem, more easy and commodious in practice,

may be obtained thus:-

Let CD represent any object whose height is to be determined; at the points A and B observe the angles of elevation, and measure the distance AB, the points A,B,C, and D being in the same plane. See preceding figure.

For in the triangles ABC, CBD,

sin. ACB: AB:: sin. A: BC,

and R: BC:: sin. CBD: CD, from which we have sin. ACB: AB \times BC:: sin. A \times sin. CBD: BC \times CD or sin. ACB \times BC \times CD= sin. A \times sin. CBD \times AB \times BC; radius being unity.

Hence $CD = \frac{\sin A \times \sin CBD \times AB}{\sin ACB}$; or, making the terms homo-

geneous, and substituting cosec. for $\frac{1}{\sin}$,

 $R^5 \times CD = \sin A \times \sin CBD \times \csc ACB \times AB$.

That is, to the sines of the observed angles of elevation, add the cosecant of the difference of these angles, and the logarithm of the measured distance; the sum, rejecting 30 from the index, will be the height of the object.

Let the angles of elevation be 55° 54', and 33° 20' respectively, and the distance between the stations 100 feet. Required the

height of the object.

A THE REAL PROPERTY.

| Angles of elevation | $\left\{\begin{array}{cc} 55^{\circ} \ 54' \ \text{sine} \\ 33 \ 20 \ \text{sine} \end{array}\right.$ | 9.918062 9.739975 |
|-------------------------------|---|-----------------------|
| Difference . Distance . | 22 34 cosec. 100 feet | 10.415942 2.000000 |
| Height . Height of the eye | 118.5 5.5 | 2.073979 |
| Height of object. | 124.0 feet. | arii. |

EXAMPLE VIII.

In order to determine the distance of two inaccessible objects lying in a direct line from the bottom of a tower 90 feet high, on the top of which I took the angles of depression of the two objects; that of the most remote being 24° 48′, and that of the nearest 58° 36′. Required their distance from the tower, and from each other.

Ans.—139.842 feet.

EXAMPLE IX.

Wanting to know the distance between two boats lying at anchor in a straight line from a light-house, which is 110 feet high, on the top of which I took the angle of depression of the farthest, and found it to be 18° 26′, and that of the nearest 56° 44′. What was their distance?

Ans.—129.5286 feet.

EXAMPLE X.

From the top of a hill I observed two mile-stones on a horizontal road, which ran straight from its bottom, and took their respective angles of depression below the horizontal plane passing through the place of my eye; that of the nearer mile-stone was 36° 12′, and that of the more distant 15° 26′. Required the height of the hill.

Ans.—780.17 yards.

EXAMPLE XI.

In order to find the height of an obelisk standing on the top of a regularly sloping hill, I measured from its bottom a distance of 40 feet, and then found the angle formed by the inclined plane, and a line from the top of the obelisk to centre of the instrument, to be 41°; and, after measuring downward in the same direction 60 feet farther, the angle formed as before was only 23° 45′. What was the height of the obelisk and the angle of the inclined plane with the horizon?

Ans.—Height 57.623 feet. Inclination 21° 54½.

EXAMPLE XII.

Wishing to know the height of a tower standing on the top of a regularly sloping hill, to the bottom of which I could not approach on account of a ditch around it, at the outside of which I took the angle formed by the inclined plane, and a line from the centre of the instrument to the top of the obelisk, and found it 41; but after measuring downward in the same sloping direction 54 feet farther, I found the angle formed in like manner to be 23° 45′. What was the height of the obelisk itself, and that of its top above the last place of observation, supposing the angle formed by the inclined plane and the horizon to be 21° 54′ ½?

Ans.—51.86 feet the height of the obelisk, and 83.51 above the last

place of observation.

EXAMPLE XIII.

Being on a horizontal plane, and wanting to know the height of a tower on the top of an inaccessible hill, I took the angle of elevation of the top of the hill 40°, and of the top of the tower 51°; then measuring in a direct line 100 feet farther from the hill, I took in the same vertical plane the angle of elevation of the tower 33° 45. Required the height of the tower?

Ans.-46.666 feet.

EXAMPLE XIV.

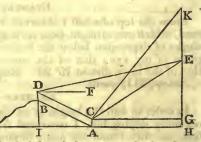
In order to know the height of a castle standing on a hill, I took the angle of elevation of the top of the castle above the horizontal plane 58°, and of the top of the hill 25°; but could not, as in last example, measure a sufficient distance directly from the castle. I therefore measured in an oblique direction 52 yards, making with the castle an angle of 72° 10′, at the farther end of which the angle, in the same manner, was 64° 30′. What was the height of the castle?

Ans.-34.464 feet.

EXAMPLE XV.

Wanting to ascertain the height of a tower standing upon a hill, the height of the hill, and the horizontal distance from the nearest place of observation, on account of the nature of the ground I proceeded as follows:—

At A I took the angle GCK 3° 38′, and GCE 2° 44′; then having set up a staff AC equal in height to the centre of the theodolite, I measured 1810 feet up the sloping ground AB in a direct line with the tower, keeping the points K, E, C, B, in the same vertical plane. At B I took the angle FDC=BAI=1° 54′,



and EDF=1° 32' Required the height of the tower, the height of the hill, and the horizontal distance from the first place of observation.

1. In the triangle DCE, are given the side DC=1810 feet, the angle ECD 175°22′, EDC 3°26′, and DEC 1°12′; to find CE=5175.89 feet.*

2. In the triangle CKE, the angle K=86° 22′, CEK=92° 44′, KCE=0° 54′ and CE=5175.89; hence EK=81.463 feet.

3. In the triangle CGE, the angle GCE=2° 44′, and CE=5175.89; hence CG=AH=5170 feet; and GE=246.826.

4. In the triangle ABI, AB=1810, the angle BAI=1° 54′; hence AI=1809 feet, and BI=60.011 feet.

If EK, the height of the tower, were only wanted, it may be found thus:

In calculations where the same number is used which has been found from previous computation, its log. should be reserved from the first to be used in the next, &c.

Sin. DEC: DC:: sin. CDE: CE=DC sin. CDE. cosec. DEC, sin. K: CE (=DC. sin. CDE. cosec. DEC):: sin. KCE: KE, and R⁴KE=DC. sin. CDE. sin. KCE, sec. GCK. cosec. DEC.

By logarithms. CDE 3° 26' 8.777333 sin. 8.196102 KCE 0° 54' sin. GCK 3° 38' 10.000874 sec. cosec. DEC 1° 12' 14.678923 DC 1810 3.257679 log. 1.910961 EK 81.463

EXAMPLE XVI.

At the top of a castle which stood a hill near the sea-shore, the angle of depression of a ship's hull at anchor was 4° 52′; at the bottom of the castle the angle of depression was 4° 2′. Required the horizontal distance of the vessel, and the height of the hill on which the castle stands above the level of the sea, the castle itself being 64 feet high.

Ans.—4373.75, and 308.4 feet respectively.

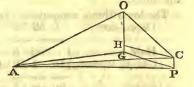
EXAMPLE XVII.

From a window in the lower part of a house, nearly on a level with the bottom of a steeple, I took the angle of elevation of the top of the steeple 40°; and from another window 18 feet directly above the former, the same angle of elevation was 37° 30′. Required the height and distance of the steeple.

Ans.—210.44, and 250.79 feet respectively.

EXAMPLE XVIII.

Suppose A and C to be two stations on sloping ground, O an object on the top of a hill, and the angles OCA, OAC, measured with a sextant, to be 79° 29′ and 63° 11′ respectively; also let the angle of elevation of AO above the horizon-



tal plane be 6° 36', and that of CO 5° 22'; what are the horizontal

distances and height of the object, AC being 410 yards?

In the triangle AOC are given all the angles, and the side AC; to find AO and CO. Again, in the triangle AGO right-angled at G, are given the angle OAG and the side AO; to find AG=660.3 and OG=76.4. Lastly, in the triangle COB, right-angled at B, are known CO and the angle OCB; to find CB 600.7, and OB 56.4, and OG—OH=76.4—56.4=20 yards nearly =HG=CP, the difference of the heights of the stations, supposing AP to be horizontal. Now in the right-angled triangle APC are given AC and CP, to find AP= $\{(AC+CP) (AC-CP)\}^{\frac{1}{2}} = \sqrt{430 \times 390} = \sqrt{167700} = 409.5$ yards. Hence the sides of the horizontal triangle APG are given, to find the angles, which may be determined by Case III, Plane Trigonometry, to be AGP=37° 31′ 29″, GAP=63° 19′ and GPA=79° 9′ 31″

The present may serve as an example of reducing hypotenusal lines to their horizontal measure, and of determining the height of an object above each place of observation in most common cases.

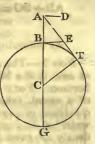
EXAMPLE XIX.

The height of the mountain called the Peak of Teneriffe was found,

barometrically, by the methods described in Gregory's Mechanics, Vol. I. book 5, to be 12,356 feet, or 2.34 English miles, and the angle of depression of the horizon, from the mean of a great number of observations, 1° 58′ 12″; it is required to determine the diameter of the earth, supposing it to be a perfect sphere.

Ans.—7913.6 miles.

Let C be the centre of the earth, the circle BTG a vertical section passing through the centre, AB the height of the Peak, AT the tangential line drawn from its top to the visible horizon, and AD a line perpendicular to a plumb-line hanging freely: also, let BE, a tangent to the earth's surface at B, meet the other tangent AT in E. Then, in the triangle ABE, right-angled at B, there are given BAE the complement of DAT, the angle of depression=88° 1' 48", and AB=2.34, hence R: AB:: tan. A: BE:: sec. A: AE. But since the triangles



CBE, CTE, are right-angled at B and T, have the side CB=CT, and CE common, they are (Leslie's Geom. I, 22, or Hutton's Geom. theo. 34, cor. 2) equal, and therefore BE=ET; hence, AE+BE=AE+ET=AT. In the triangle ATC, right-angled at T, we have R: AT:: tan. A: TC, the radius of the earth. The operation thus performed occupies but small compass, which may still be farther shortened. For since tan. A+sec. A=tan. $(A+\frac{1}{2}$ comp. A) we shall, by incorporating the proportions from which AE, BE, and CT are deduced, have

R² CT=AB tan. $(A + \frac{1}{2}comp. A)$ tan. A; or, log. CT=log. AB+log. tan. $(A + \frac{1}{2}comp. A)$ +log. tan. A—20, in the index.

The logarithmic computation is as follows:— Depression 1° 58′ 12″

| Half Comp. depress. | 59 6 88 1 48 | tan. | 11.4634852 |
|------------------------|------------------------|----------|-------------------------|
| Sum Height of Peak | 89 0 54 2.34 miles, | tan log. | 11.7646436 0.3692159 |
| Earth's semid. | 3956.8 | | 3.5973447 |

Diameter 7913.6 Distance 136.1

2.1338595

If AT were required, we have only to take radius (10) from the sum of the two last lines, and the remainder, 2.1338595, is the log. of 136.1, the distance sought.*

Note 1.—This method of determining the earth's radius, though elegant in theory, is useless in practice, at least where any thing more than an approximation is wanted, by the great irregularity of

the horizontal refractions.

Note 2.—When the diameter of the earth is known, and height of the object given, the distance of the visible horizon may be easily found; for, Euc. III. 36. AB. AG—AT².

By logarithms.

AB 2.34 log. 0.369216

7913.6

AB+BG=AG 7915.94 log. 3.898503

4.267719

As before 136.1 miles, log. 2.133859*

Note 3.—The depression of the horizon, or the dip, as it is called at sea, is the angle DAT contained between the true and visible horizon. For if an observer, whose eye is situated at A on the deck of a vessel, takes the altitude of a celestial object with Hadley's quadrant or sextant, by bringing that object to the surface of the water at T, instead of the true horizon AD, the altitude is evidently too great by the angle DAT=TCA. This may be calculated by the usual formulæ of trigonometry for that purpose; but as it will, at any probable altitude, be a small quantity, those which give the cosine or secant of its value are not sufficiently correct; for which reason we shall give the following method:—

 $(BG+AB)\times AB=AT^2$, (Euc. III. 36.), hence $BG\times AB+AB^2=AT^2$, or $2BC\times AB+AB^2=AT^2$, and AT^2 being, at any probable elevation, but a small quantity in comparison of AC, it may be safely neglected; therefore $\sqrt{(2BC\times AB)}=AT$. But CT(=BC):R:AT [$\sqrt{(2BC\times AB)}$]: tan. $C=\tan$. DAT = $\frac{R\sqrt{(2BC\cdot AB)}}{BC}=\sqrt{\frac{2R^2\cdot AB}{BC}}$.

Now since $\frac{2 R^2}{BC}$ is a constant quantity, and BC being taken in gene-

ral at 3956 miles =20887680 feet, hence the log. of $\frac{2R^s}{BC}$ is 12.98114,

and tan. DAT=\frac{1}{2}(12.98114+\log. AB). Since, in the present case, the arc may be substituted for its tangent, the radius, therefore, becomes 57° 17′ 44″.8=206264″.8; and we have log. DAT in seconds

 $=\frac{1}{9}(3.60999 + \log \cdot AB \text{ in feet}).$

The dip is affected by terrestrial refraction, which is very variable, and by different authors it is estimated at different quantities. Dr Maskelyne estimated it at one-tenth of the whole; M. Delambre, one-eleventh, and Col. Mudge, one-twelfth. See Dr Hutton's Course, vol. III. page 138.

Ex.—Required the dip, the height of the eye being 40 feet, and estimating the terrestrial refraction at $\frac{1}{1}$.

Constant log. 3.60999 Height of eye 40 feet 1.60206

5.21205

Refrac. sub. 1/3 33 .6 2.60602

Dipt . 370=6' 10".

[•] See also the method by Leslie in his Geometry.

+ The dip in minutes is equal to the square root of the height in feet nearly.

Note 4.—Since $AB \times BG + AB^2 = AT^2$, therefore

 $AB(AG + AB) = AT^2$, and $AB = \overline{BG + AB}$ (1.)

Now, if AB is the unknown quantity, and being small in comparison of BG, it may be found approximately by making, first, AB'= BG nearly, substituting this value of AB' for AB in formula (1.), and

$$AB = \frac{AT^2}{BG + AB'} \qquad (2.)$$

which will be sufficiently correct for most purposes. If not, the operation may be repeated till it is so.

This is useful in determining the height of an object considerably

distant.

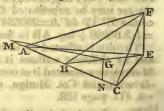
Now, the mean diameter of the earth is about 7912 miles, or 1775360 feet =GB, of which the logarithm is 7.620920, and its arithmetical complement is 2.379080; therefore to twice the log of AT, in feet add the constant log. 2.379080, the sum, rejecting tens in the index, will give AB', which will be sufficiently correct if AT does not exceed 1000 feet. If more distant, the operation must be repeated. This correction must always be added to heights determined geometrically as the usual instruments give their elevation only above the tangent AT.

EXAMPLE XX.

Given the angles of elevation of any distant object, taken at three places in a horizontal straight line, which does not pass through the point directly below the object; and the respective distances between the stations: to find the height of the object, and its distance from either station.

Let AEC be the horizontal plane; FE the perpendicular height of the object F above that plane; A, B, C, the three places of observa-

tion; FAE, FBE, FCE, the respective angles of elevation, and AB, BC, the given distances. Then, since the triangles AEF, BEF, CEF, are all right- M angled at F, the distances AE, BE, CE, will manifestly be as the cotangents of the angles of elevation at A, B, and C; and we must determine the point E, so that these lines may have that ratio.



Construction.

To effect this geometrically, we must take BM, or AC produced, equal to BC, BN equal to AB; and make

MG : BM (=BC) :: cot. A : cot. B, and

BN (=AB): NG:: cot. B: cot. C.
With the lines MN, MG, NG, construct the triangle MNG; and join BG. Draw AE so, that the angle EAB may be equal to MGB; this line will meet BG produced in E, the point in the horizontal plane falling perpendicularly under F.

Demonstration.

By the similar triangles AEB, GMB, we have

AE : BE :: MG : MB :: cot. A : cot. B, and

BE : BA (=BN) :: BM : BG.

Therefore the triangles BEC, BGN are similar; consequently

BE: EC:: BN: NG:: cot. B: cot. C. Whence it is obvious that AE, BE, CE, are respectively as cot. A, cot. B, cot. C.

Calculation.

In the triangle MGN are given all the sides, to find the GMN, equal to the angle AEB. Then, in the triangle MGB, are given two sides, and the contained angle; to find the angle MGB, equal to the angle EAB. Hence, in the triangle AEB are known the side AB, and all the angles; to find AE and BE. And then EF=AE . tan. A=BE . tan. B.

Analytically.

Let AB=r, BC=s; also let the cotangents of the angles FAE,

FBE, FCE, be denoted by the letters a, b, c, respectively.

Then, putting EF=x, we have, to radius 1, 1: a::x:ax=AE, 1: b::x:bx=BE, 1: c::x:cx=CE; and on AC from E, letting fall the perpendicular ED, we have (Euc. II. 12) $a^2 x^2=b^2 x^2+$

 $r^2 + 2r$. BD; hence BD= $\frac{a^2 x^2 - b^2 x^2 - r^2}{2s}$. In like manner CD=

 $\frac{b^2 x^2 - c^2 x^2 - s^2}{2 s} = BD - BC = BD - s: \text{ whence } BD = \frac{b^2 x^2 - c^2 x^2 + s^2}{2 s}.$

Therefore $\frac{b^2 x^2 - c^2 x^2 + s^2}{2 s} = \frac{a^2 x^2 - b^2 x^2 - r^2}{2 r}$. Hence $x^2 = \frac{r s^2 + r s^2}{s(a^2 - b^2) - r(b^2 - c^2)}$, and $x = \sqrt{\frac{r s(r+s)}{s(a^2 - b^2) - r(b^2 - c^2)}}$.

Otherwise thus;

If AB and CB be conceived to be bisected in M' and N', and ED a perpendicular upon AC, which are however omitted to avoid complexity in the figure; then, (Leslie's Geometry, II, 21.) AE²—BE² =AB × 2M'D, and CE²—BE²=BC × 2N'D; therefore, AE² × BC —BE² × BC=AB × BC+2M'D, and CE² × AB—BE² × AB=AB × BC × 2N'D. Adding equals to equals, and AE² × BC+CE² × AB—AC × BE²=AB × BC × AC; consequently AE² × BC+CE² × AB =AC × BE² × AC × AB × BC.

If AB=BC, then $AE^2+CE^2=2AB^2+2BE^2$, the line EB being drawn from the vertex E of the triangle ACE, to any point B in the base. Put AB=D, BC=d, EF=x, and then expressing algebraically

the foregoing theorem.

The equation thence resulting is,

 $d x^2 \cot^2 A + D x^2 \cot^2 C = (D+d) x^2 \cot^2 B + (D+d) D d$. Hence, transposing all the unknown terms to one side of the equation, dividing by the sum of the coefficients, and extracting the

square root, we shall have $x = \sqrt{\frac{(D+d)D d}{d \cot^2 A + D \cot^2 C - (D+d)\cot^2 B}}$ Thus EF becoming known, the distances AE, BE, CE, are found by multiplying the cotangents of A, B, and C, respectively, by EF. Cor.—When D=d, or D+d=2D=2d, the expression becomes

 $x=d \div \sqrt{(\frac{1}{2}\cot^2 A + \frac{1}{2}\cot^2 C - \cot^2 B)}$, which is pretty well suited to logarithmic computation. The rule may, in that case, be thus expressed.—Double the logarithm cotangents of the angles of elevation of the extreme stations, find the natural numbers answering thereto, and take half their sum; from which subtract the natural number answering to twice the logarithm contangent of the middle angle of elevation: then half the log. of this remainder subtracted

from the log. of the measured distance between the first and second, or the second and third station, will be the log. of the height of the

object.

1. Let AB=60 feet, BC 72 feet; angle FCE=50° 23′, the angle FBE=40° 33′, and the angle FAE=30° 48′; required the distances AE, BE, CE, and EF, the height of the object.

Ans.—AE=159.09 feet, BE=110.84 feet, CE=78.51 feet, and

EF=94.84 feet.

2. Let the three angles of elevation be 36° 50′, 21° 24′, 'and 14°, and the two equal measured distances 84 feet; required the height of the object.

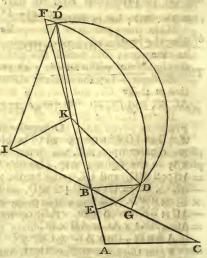
Ans.—53.964 feet.

EXAMPLE XXI.

Given the angles of elevation at which an object is seen from three given points in a horizontal plane; to find its position and altitude.

Let A, B, and C be the three points of observation, and D the bottom of the perpendicular from the given object to the horizontal plane. It is evident that the horizontal distances AD, BD, and CD are proportional to the cotangents of the vertical angles at the stations A, B, C,; let these cotangents be respectively denoted by the L, M, and N.

Divide AB internally and I externally at the points E and F in the ratio of L to M; and the lines DE and DF joining in the vertex D must bisect internally and externally the angle, whence EDF is a right angle, and contained in a semicircle; wherefore on EF de-



scribe a semicircle. In the same manner, divide CB internally and externally at G and H* in the ratio of M to N, and on GH describe a semicircle. The point D common to both semicircles must occur in their intersection.

From this construction the trigonometrical calculation is readily deduced. For L+M: M:AB:BE and L-M: M:AB:BF; whence $DE = \frac{BE+BF}{2} = \frac{EF}{2}$, or radius KE is found. In like manner N+M: M:CB:BG, and N-M: M:CB:BH, consequently $DI = \frac{BG+BH}{2}$. In the triangle IBK, the sides BI and BK, with their included angle, = ABC, are given; and, therefore,

^{*} See Leslie's Geometry, fourth edition, page 275. To avoid extending the figure too much, the point H, which should be in continuation of BI, in the same way as BF is in continuation of BK, as well as the lines joining DE and DF, is omitted.

the angle BKI and the base IK are found. Again, all the sides of the triangle IDK being given, the angle IKD is found. Hence, in the triangle BDK the whole angle BKD and its containing sides are given; and, therefore, the base BD, or the horizontal distance from the station B, and consequently its altitude, is determined.

It is obvious, that the opposite semicircles will likewise, by their intersection, give, on the other side, a second position D' for that point. In practice, however, this ambiguity could be easily removed. It may be remarked too, that the point D may fall either with-

in or without the triangle.

If the object be seen at the same elevation from all the three points, the arcs of the circles will evidently become tangents, which bisect at right angles the sides of the triangle ABC. The projection D of the object on the horizontal plane, will then be the centre of the circle circumscribing that triangle; and, therefore, the radius or distance AD may be found by prop. 18, book VI. Leslie's Geometry, as shown in the notes, page 347.

If the three points of observation should lie in the same straight line, the centres of the determining circles will occur in that line or its extension; and hence the process of calculation will be greatly

abridged, and will coincide with the foregoing proposition.

Example.—Let the angle of elevation of the object at A, be 50° 45′, that at B 58° 15′, and that at C 46° 45′; also the side AB 24′ yards,

AC 38, and BC 50. Required its height?

Hence L = cot. 50° 45′, M = cot. 58° 15′, and N = cot. 46° 45′. From the given sides the angle ACB = 27° 35′ 10″, ABC = 47° 9′ 22″, and BAC 105° 15′ 28″. Also L = 0.8170343, M = 0.6188188, N=0.9407061; therefore, BE = 10.343, and BF = 74.928, whence KE = 42.6355, and BK = 32.2925. In like manner, BG = 19.846, BH = 96.123, hence DI = 57.9845, and IB = 38.1385. From these the angle IKB = 77° 11′ 24″, and KIB 55° 39′ 14″; and the side IK = 23.677. Now from the three sides ID, IK, and KD, the angle IKD = 107° 10′ 26″. To this, by applying the angle IKB by addition and subtraction we obtain the angle BKD′ = 184° 21′ 50″, and BKD = AKD = 29° 59′ 2″.

From the sides BK and KD, and the contained angle BKD, are found the angle KBD = 102° 16′ 39″, and KDB = 47° 44′ 19″, from which BD = 21.8065, and the height of the object 35.24 yards.

Should the point D' be the foot of the perpendicular, the angle $KBD' = 2^{\circ} 29'$ and $KD'B = 1^{\circ} 52' 50''$, and BD' = 74.876; whence the height above D' will be 121 yards.

EXAMPLE XXII.

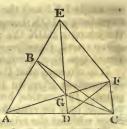
Otherwise thus:

Given the angles of elevation of the object from three points in the same plane forming a triangle, of which the sides are known, to find the position of the object referred perpendicularly to that plane and its altitude above it.

AND THE RESERVE THE PARTY OF TH

Construction .- The perpendicular from the object to the plane

may fall either within or without the triangle. In both cases, let A, B, and C be the points of observation; and α , β , and γ the angles of elevation at these points respectively. Join A, B, and C, and on AB produced, if necessary, make AE equal to AC, and AD to AB, join ED, and upon it construct the triangle EDF so that cotangent β : contangent β :: AE: EF, and cotangent β : cotangent γ :: AD: DF. Join AF, and from



B draw BG, making the angle ABG equal to the angle ATE, and join CG. The point G in which the straight lines BG and AF intersect each other will be the point at which a perpendicular let fall from the object would meet the plane, thus ascertaining the position of the object, from which, and the given angles, its alti-

tude may be found.

Demonstration.—It is obvious that the straight lines drawn from each of the points of observation to the point at which a perpendicular let fall from the object meets the plane, ought to be in proportion to the cotangents of the angles of elevation at these points respectively. The proposition therefore resolves itself into this. To find a point in a plane from which straight lines drawn to three given points in the same plane shall have to each other a given ratio which follows from the construction just given.

Solution.—In the triangles ABG, AFE, the angles at B and F are equal by construction, and the angles BAG is common to both; these two triangles are therefore similar. And AG: BG:: AE: EF

:: cot. α : cot. β . Hence $EF = \frac{AC \times \cot \beta}{\cot \alpha}$. Again AG : AE::

AB: AF or AG: AC:: AD: AF; and as the angle at A is common to the two triangles AGC, and ADF; these triangles similar, consequently AG: CG:: AD: FD:: cot. α : cat γ , whence FD=AB×cot. γ .

cot. a

The triangles ADE, ABC having the sides AD, AE of the one equal to the sides AB, AC of the other, and the angle at A, common to both, are equal, and the side ED is equal to the side BC. Therefore in the triangle ADE, the three sides are given, and those of the triangle FDE are already found; whence the angles AED and FED, and consequently the angle AEF may be obtained; and from the angle AEF, with the sides AE and EF, the angle AFE or ABG, which is equal to it, may be determined. Then in the triangle ABG, having the two angles at A and B, and the side AB the distance, BG may be found, consequently, with it and the angle \$\beta\$, the height of the object becomes known.

Example.—Let the side AB be 80 feet, BC=119, and AC=140, also the angle at A or $\alpha = 50^{\circ}$, that at B or $\beta = 60^{\circ}$, at C or $\gamma = 55^{\circ}$;

required the height of the object.

From these EF=96.329, DF=66.758; the angle AED=34° 48′, EDA=87° 6′ 23″, EAD=87° 6′ 23″, EAD=58° 5′ 37″, GEF=34° 6′ 57″, AFE, or ABG=70° 37′ 8″, FAE or AGB=40° 28′ 16″, BG=55.673; and the height 96.392 feet.

THE STATE OF THE STATE OF

EXAMPLE XXIII.

From a convenient station P, there could be seen three objects A, B, and C, whose distance from each other were AB=8 miles, AC=6 miles, BC=4 miles; I took the horizontal angles APC=33° 45′, BPC=22° 30′. It is hence required to determine the respective distances of my station from each object. Here it will be necessary, as illustrative and preparatory to the computation, to describe the manner of

Construction.

Draw the given triangle ABC from any convenient scale. From

the point A draw a line AD to make with AB an angle equal to 22° 30′, and from B a line BD to make an angle BDA equal to 33° 45′. Let a circle be described to pass through their intersection D, and through the points A and B. Through C and D draw a straight line to meet the circle again in P, which is the point required. For drawing PA, PB, the angle APD is evidently equal to ABD, since it stands on the same are AD; and for a like reason BPD.



the same arc AD; and, for a like reason, BPD=BAD. So that P is the point where the angles have the assigned value.

· Computation.

In the triangle ABC, all the sides are given; to find the angles. In the triangle ABD, all the angles are known, and the side AB; to find one of the other sides AD. Take BAD from BAC, the remainder, DAC is the angle included between two known sides AD, AC; from which the angles ADC and ACD may be found. The angle CAP = 180°—(APC + ACD). Also, BCP = BCA—ACD; and PBC=ABC+PBA=ABC+ sup. ADC. Hence, the three required distances are found by these proportions.

As sin. APC: AC:: PAC: PC, and :: sin. PCA: PA; and, lastly, as sin. BPC: BC:: sin. BCP: BP. The operation at length

is as under:

By Rule II., Case III., we have

Sin.
$$\frac{1}{2}$$
 BAC = $\sqrt{\frac{1 \times 3}{8 \times 6}} = \sqrt{\frac{1}{16}} = \frac{1}{4} = 25 = \sin . 14^{\circ} 28' 39''$, and

BAC = $28^{\circ} 57' 18''$.

Sin. $\frac{1}{2}$ ABC = $\sqrt{\frac{1 \times 5}{18}} = \frac{1}{4} \sqrt{10} = 3952847 = \sin . 23^{\circ} 17' 1'' = \frac{1}{4}$, and

Sin. $\frac{1}{2}$ ABC = $\sqrt{\frac{1 \times 5}{8 \times 4}} = \frac{1}{8} \sqrt{10} = 3952847 = \sin 23^{\circ} 17' 1'' \frac{1}{2}$, and ABC = $46^{\circ} 34' 3''$.

Sin.
$$\frac{1}{2}$$
 ACB = $\sqrt{\frac{3 \times 5}{6 \times 4}} = \sqrt{\frac{6}{6}} = \frac{1}{4} \sqrt{10} = 7905694 = \sin. 52^{\circ} 14' 19''\frac{1}{2}$, and

ADB 123 45

| As sin. ADB 123° 45′ ar. co. Is to AB 8 miles So is sin. ABD 33° 45′ | 0.0801536 0.9030900 9.7447390 |
|--|-------------------------------------|
| To AD log | 0.7279826 10.7781513 |
| Arc . 48° 18′ 7″ tan. Subtract 45 0 0 | 10.0501687 |
| Remainder 3 18 7 tan. ½(ADC+ACD)=86 46 21 tan. | 8.7611283 11.2487967 |
| ½(ADB—ACD) 45 39 17 tan. | 10.0099250 |
| | 0.2552610 |
| Sum 74 52 4 180 0 0 | |
| PAC 105 7 56 sin | 9.9846740 0.7781513 |
| PA 7.10199 miles 0.8513801 | |
| PC 10.42525 miles | 1.0180863 180° 0′ 0″ 85 51 35 |
| BCP= 63 21 35 PBC= As sin. BPC 22° 30′ 0″ ar. co. 0.4171600 Is to BC 4 miles 0.6020600 So is sin. BCP 63° 21′ 35″ 9.951259 | 0 |
| To PB 9.34285 miles . 0.670479. The computation of problems of this kind, however, m | |

The computation of problems of this kind, however, may be a little shortened by means of the following

General Investigation.*

Put AC=a, BC=b, APC=P, BPC=P', ACD=C, and let there be taken for unknown quantities PAC=x, PBC=y. The triangles PAC and PBC give

Sin. APC: sin. CAP:: AC: CP, and Sin. BPC: sin. CBP:: BC: CP; that is, Sin. P: sin. $x: a: \frac{a \sin x}{\sin P}$ = CP, and $b \sin y$ OP

Sin. P': $\sin y :: b : \frac{b \sin y}{\sin P'} = CP$.

Hence, $\frac{a \sin x}{\sin P} = \frac{b \sin y}{\sin P}$; which may be reduced to $a \sin P$ sin. $x-b \sin P \sin y = 0$.

^{*} See Lacroix Trigonometrie, and Gregory's Trigonometry.

In the quadrilateral ACBP, we have CBP=360°-APC-BPC

-ACB-CAP, or y=360-P-P'-C-x.

Make 360° —P—P'—C=R, then we shall have y=R-x; and consequently, $a \sin P' \sin x - b \sin P (\sin R \cos x - \cos R \sin x) = 0$.

Dividing by sin. x, there results, $a \sin P' - b \sin P$ (sin. R $\frac{\cos x}{a}$ $-\cos R = 0.$

Whence we have $\frac{\cos x}{\sin x} = \cot x = \frac{a \sin P' + b \sin P \cos R}{b \sin P \sin R}$

This expression separated into two parts, we have
$$\cot x = \frac{a \sin P'}{b \sin P \sin R} + \frac{\cos R}{\sin R}; \text{ or,}$$

$$\cot x = \frac{\cos R}{\sin R} \left(\frac{a \sin P'}{b \sin P \cos R} + 1 \right); \text{ or,}$$

$$\cot x = \cot R \left(\frac{a \sin P'}{b \sin P \cos R} + 1 \right); \text{ or, lastly,}$$

cot. $x = \frac{a}{h} \sin P'$ cosec. P cosec. R cot. R + cot. R.

Hence, x being thus determined, we get y from the equation y=R-x; and CP from either of the expressions given above.

We shall now apply the foregoing formula to the solution of the

question last proposed.

EXAMPLE XXIV.

Here
$$a = 6$$
 $P = 33^{\circ} 45'$ $0''$ $PAC = x$
 $b = 4$ $P' = 22$ 30 0 $PBC = y$

$$ACB = 104$$
 28 39 found by computation
$$160 43 39$$

$$360 0 0$$

$$R = 199 16 21$$

cot. $x = \frac{a}{h} \sin P'$ cosec. P, cosec. R cot. R+cot. R; or,

cot.
$$x = \text{cot. R} \left(\frac{a \sin. P'}{b \sin. P \cos. R} + 1 \right)$$
 and using logarithms we have $a' = 3 \log. 0.4771212$ $b' = 2 \text{ ar. co. } 9.6989700$ $P' = 22^{\circ} 30' 0'' \sin. 9.5828397$ $P = 33^{\circ} 45' 0'' \text{ ar. co. S. } 0.2552610$ R whose cos. is neg. 199 16 21 ar. co. C. 0.0250452

| S S | |
|--|--|
| — 1.09458 log. + 1.00000 | 0.0392371 |
| cot. R — 0.09458 log. $199^{\circ} 16' 21''$ | 8.9757993 10.4563594 |
| cot. x — 105 8 10 | 9.4321587 |
| As sin. 33° 45′ 0′′ ar. co. Is to sin. x 105 8 10 So is 6 | 0.2552610 9.9846660 0.7781513 |
| many or arrange and the control of the party | particular management and an arrangement |

To PC 10.4251 Whence the rest may be found. 1.0180783

In using these formulæ great attention must be paid to the signs of the quantities.

EXAMPLE XXV.

Suppose the objects A,B,C, are seen from D, and have their distances AB 7½ miles, BC 12 miles, and AC 8 miles, the angle BDA 25°, and CDA 19°; it is required to determine the distances DA, DB, DC.

Ans.—DA 10.0286, DC 16.7857, DB 14.9095 miles.

EXAMPLE XXVI.

Suppose the objects A, B, C, are seen from D, and have their distances AB 8 miles, BC 12, and AC 7½; the angle BDC being 17° 47′ 19″. Required the distances DA, DC, and DB.

Ans.—DB 12, DC 22.85, and DA 20 miles.

EXAMPLE XXVII.

If, AB be 8, AC 7.2, and BC 12 miles, and the angle ADB 107° 56′ 13″. Required the distances DA, DC, and DB.

Ans.—DB 5, DA 4.892, and DC 7 miles.

EXAMPLE XXVIII.

Let the objects A, B, C, be in a straight line; and their distances AC 3.626, AB 12, and BC 8.374, the angle ADC being 19°, and BDC 25°. Required the distances DA, DC, and DB.

Ans.—DA 9.4711, DC 10.861, and DB 16.8485.

EXAMPLE XXIX.

Let the objects A, B, C, as seen from D, be within the triangle; and let the distance AB be 6 miles, BC 12, and AC 9, the angle BDC being 123° 45′, and ADC 132° 22′. Required the distances DA, DC, and DB.

Ans.—DA 1.372, DB 5.523, DC 8.018.

EXAMPLE XXX.

A ship from Bombay in latitude 18° 57′ N, sailed S. W. by S. 224 miles. Required the latitude come to, and the departure.

Ans.—The difference of latitude is 186.2, and the departure 124.4

Latitude of Bombay . . . 18° 57′ N. Diff. of lat. 186 miles = . . 3 6 S.

Latitude come to . 15 51 N.

EXAMPLE XXXI.

Having occasion to travel through the counties of Kent and Surrey, I perceived the fort built by Lady James, on Shooter's hill, which bore from me N. N. E.; and after going 20 miles in a W. N. W. direction, I perceived the fort again, which now bore N. E. by E. Required my distance from it at each station.

Ans.—29.93 miles, and 36 miles.

EXAMPLE XXXII.

From a ship at sea, I observed a point of land to bear E. by S., and after sailing 12 miles N. E., it bore S. E. by E. Required the distance of the last place of observation from the point of land. Ans.—26 miles.

in heart of the rest-mary land of the

EXAMPLE XXXIII.

Sailing N. N. W. at the rate of 6 knots an hour, at 8h. P. M. I discovered two light-houses, the northernmost of which bore N. N. E. and the other E. by N., and at 10h. 30m. the northernmost light bore E. N. E., and the other E. S. E. The bearing and distance of

the lights from each other are required.

Calculation.—In the triangle ACD are given the side AC equal to 15 miles, the angle ADC 3 points, the interval between E by N. and E. S. E. and the angle CAD 4 points, the distance between S. S. E. the opposite point to N. N. W., and E. S. E.; to find CD = 19.09. Again, in the triangle ABC are given AC as before equal to 15 miles, the angle ABC equal to 4 points, the interval between N.N.E. and E.N.E. and the angle ACB also 4 points, the interval between the N. N. W. and N. N. E. points; hence the angle CAB is a right angle; consequently, we get BC = 21.21.

Lastly, in the triangle BCD are given the sides CB, CD, equal to 21.21 and 19.09 respectively, and the included angle BCD 5 points, the interval between N. N. E. and E. by N.; to find the angles CDB $=67^{\circ}$ 30', CBD $=56^{\circ}$ 15' =5 points, CBE = BCN =2 points, and

the distance BD = 19.09.

EXAMPLE XXXIV.

The side AB of a pentagon being 180 toises, the face of the bastion AC 50, the normal or perpendicular KL 30; it is required to find, by trigonometrical calculation, all the other lines and angles of the fortification, supposing the line of defence AH to be equal to a line drawn from A to D.

Solution.—Here $\frac{AB}{2} = \frac{180}{2} = 90 = AK$.

Hence, in the right-angled triangle AKL, AK (90): R:: KL (30): tan. of a regular pentagon, we have $\frac{360^{\circ}}{5}$ =

LAK=18°26'. Because AB is the side P $72^{\circ} = AOB$, and $\frac{72^{\circ}}{2} = 36^{\circ} = AOK$,

whence 90° — 36° = 54° = EAK, and 54° — 18° 26' = 35° 34' = EAC, which being doubled is 71° 8′, the sallent angle PAC or DBR. Join BC, then will ABC be a triangle in which are given AB, AC, and their contained angle BAC; to find ABC=6° 48'. Now sin. ABC (6° 48'): AC (50):: sin. BAC (18° 26'): BC = 133.52, equal to the line of defence AH or BG. In the triangle BCG, ABG-ABC=18° $26'-6^{\circ}$ $48'=11^{\circ}$ 38'=CBG. Because BC=BG, we have 180°—11° 38′ 168° 22′ $= 84^{\circ} 11' = CGB.$

Again, because AB and EF are parallel, and AH, BG equal; we have the angles BAH, ABG, AHE, and BGF all equal, that is, each equal to 18° 26'.

In the triangle CGH, we have the angle $CGB + BGH = 84^{\circ} 11'$ $+18^{\circ} 26' = 102^{\circ} 37' = CGH$; $180^{\circ} - (CGH + CHG) = 180^{\circ} - (102^{\circ})$ $37' + 18^{\circ} 26'$ = $58^{\circ} 57'$ = the angle HCG; and the side CH = AH -AC = 133.52 - 50 = 83.52 = CH. Then sin. CGH (102° 37'): CH (83.52):: sin. CHG (18° 26'): the flank CG or DH = 27.062:: sin. HCG (58° 57'): the curtain GH = 73.323.

TABLE OF THE MEASURES OF THE PRINCIPAL LINES AND ANGLES IN REGULAR FORTRESSES, FROM FOUR TO TWELVE SIDES INCLUSIVE.

| Names of Polygons. | | | | | | | | | |
|--|---|--|--|--|--|---|--|------------------------|--|
| Names of Sides and Angles. | Square | Pentag | Hexag | Hepta. | Octag. | Nonag. | Decag. | Undec. | Dodec |
| Exterior side, in toises Radius of exterior side Interior side Radius of interior side Capital Normal Curtin Flank Face Line of defence Demigorge | 180. 127.3 115.5 81.7 45.6 22.5 78.0 20.3 50.0 133.0 18.7 | 180. 153.1 123.9 105.4 47.7 27.0 77.1 24.5 50.0 134.2 23.4 | 130.6 49.3 30.0 76.4 27.3 30.0 135.1 | 157.0 50.5 32.0 75.9 29.2 50.0 135.8 | 180. 235.2 140.0 183.0 52.2 34.0 75.3 31.1 50.0 136.4 32.4 | 142.9 208-9 54.2 36.0 74.7 33.0 50.0 137.2 | 180. 291.2 144.3 233.4 57.8 39.0 73.7 35.8 50.0 138.2 35.3 | 146.3 259.7 59.7 | 180. 347.7 148.1 286.1 61.7 43.0 69.3 38.1 52.0 138.2 39.4 |
| Angle of the Centre Angle of the Polygon Angle of the Curtin Angle of the Shoulder Angle of Bast, or Flank. Angle Diminished Angle Exterior Flanking Angle | 90°0′ 90°0′ 97°1 111°3 61°56 14°2 151°56 | 7290' 108 0 98 21 115 3 74 36 16 42 146 36 | 117 39 83 8 18 26 | 128 34 99 47 119 21 89 26 19 34 | 135 0 100 21 121 3 93 36 | 140 0 100 54 122 42 96 24 21 48 | 101 43 125 9 97 8 23 26 | 147 16 102 15 | 30° 0 150 0 102 46 128 18 98 56 25 32 128 56 |
| Breadth of Foss, in Toises | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 |

APPENDIX.

= 1942000 = 27,70% D

BAROMETRIC MEASUREMENT OF ALTITUDES.

Having given a pretty full view of the method of measuring the heights of objects geometrically, we shall here subjoin that of determining them by the barometer, thermometer, and hygrometer.

That the observations may be carefully and properly made, the persons who undertake them should be provided with two portable barometers of the best construction, filled with mercury of the same specific gravity, on which, by means of a vernier properly adapted to the scale, the height of the mercurial columns may be read off to the 500th part of an inch; each barometer being fitted up with an attached thermometer, set in the wooden frame in the same manner as the barometer tube is. The ball of each thermometer would be best if nearly of the same diameter as the barometer tube. Besides these, they must also be provided with two other thermometers detached from the barometers. Of these barometers, one, with its attached and detached thermometers, is to be placed in the shade at the top of the eminence, while the other remains below. Let them continue in their places at least a sufficient time for the detached thermometer to acquire the temperature of the air, that is to say, till the contained fluid is stationary. Then the observer on the eminence must note down the height of the mercurial column in the barometer, as well as the temperatures exhibited by the attached and detached thermometers; and, at the same time, the other observer must make like observations upon the instruments below. If, in

this manner, three or four sets of observations be taken, at each station, after short intervals of time, and the mean of the results furnished by these sets respectively be taken, the probability of error in the [true altitude deduced by the following rules will be much diminished. When our third method of computation is adopted, two of Daniell's hygrometers must be employed to determine the dew points at each station. If the observations be repeated on several successive days, the position of the instruments ought to be changed at each station alternately, at the same time comparing each pair of instruments to determine their index error should there be any. It is also advisable to make the observations in serene weather, between 11 and 12 o'clock. For it has been found that the computed heights are too small, when the observations have been made near sunrise or sunset, or when the wind blows fresh from the south; and that, on the contrary, the computed results are too great, when the observations are made about three o'clock in a hot summer day, or during a brisk wind from the north or east.*

I. Dr Robison's Method.

In this method no tables are required; it will be sufficiently exact for most purposes, and is not difficult to remember. It was deduced from the following considerations:

1. The height through which we must rise in order to produce any fall of the mercury in the barometer is inversely proportional to the density of the air, that is, to the height of the mercury in the

barometer.

2. When the barometer stands at 30 inches, and the air and quick-silver are at the temperature of 32° of Fahrenheit's thermometer, we must rise through 87 feet to produce a depression $\frac{1}{10}$ of an inch.

3. But if the air be of a different temperature, this 87 feet must be increased or diminished by about 0.21 of a foot for every degree of

difference of the temperature from 32°.

4. Every degree of difference of the temperatures of the mercury at the two stations makes a change of 2.833 feet in the elevation.

Hence the following rules:

I. Take the difference of the barometric heights in tenths of an

inch; call this D.

II. Multiply the difference d between 32° and the mean temperature of the air by 21, and take the sum or difference of this product and 87 feet. This is the height through which we must rise to cause the barometer to fall from 30 inches to 29.9; and may be called h.

Thus $\frac{30Dh}{m}$ is the approximated elevation very nearly.

IV. Multiply the difference & of the mercurial temperatures by 2.833 feet, and add this product to the approximated elevation if the upper barometer has been the warmest; otherwise subtract it; then will the resulting sum or difference be the corrected elevation.

Or, this rule may be expressed by the following formula, where d is the difference between 32° and the mean temperature of the air, D is the difference of barometric heights in tenths of an inch, m is the

^{*} One person may perform the whole operation with one set of instruments, by making the observations two or three times alternately at the top and bottom, and taking a mean of the results at each station.

mean barometric height, I the difference between the mercurial temperature, and E is the correct elevation.

 $E = \frac{30(87 \pm 0.21 d)}{m} \pm \delta \times 2.833.$

For an example, suppose that the mercury in the barometer at the lower station was 29.4 inches, its temperature 50° of Fahrenheit's thermometer, and the temperature of the air 45°; the height of the mercury at the upper station 25.19 inches, its temperature 46, and the temperature of the air 39°.

II. Dr Hutton's Method.

1. Observe the height of the barometer at the bottom of any height or depth intended to be measured, with the temperature of the quick-silver by means of a thermometer attached to the barometer, and also the temperature of the air in the shade by a detached thermometer.

2. Let the same thing be done also at the top of the said height or depth, and, at the same time, or as near the same time as may be. And let those altitudes of the barometer be reduced to the same temperature, if it be thought necessary, by correcting either the one or other; that is, augment the height of the mercury in the colder temperature, or diminish that in the warmer, by its $\sqrt[3]{600}$ th part for every degree of difference of the two. The altitudes so corrected being denoted by M and m.

3. Take the difference of the common logarithms of the two heights of the barometer, corrected as above, if necessary, cutting off 3 figures next the right hand for decimals, when the log. tables go to 7 figures, or only 2, when they go to 6, and so on; or, in general, remove the decimal point 4 places more towards the right hand, those on the left

are fathoms in whole numbers.

4. Correct the number last found for the difference of temperature of the air as follows: Take half the sum of the two temperatures for the mean one; and for every degree which this differs from the temperature 31° , take so many times the $\frac{1}{435}$ th part of the fathoms above found, and add them if the mean temperature be above 31° , but subtract them if the mean temperature be below 31° ; and the sum or difference will be the true altitude in fathoms; or, being multiplied by 6 it will be the altitude in feet.

| | Same example. | |
|----------|---------------|--|
| Thermo | meters. | Barometers. |
| Detached | Attached | The state of the s |
| 45 | 50 | 29.4 lower |
| 39 | 46 | 25.19 upper |
| - | | |
| Mean 42 | Diff. 4 | |

435 : 11 :: 669.374 : 16.924 Corr. 16.924

The altitude sought 686.298 fathoms.

Let the state of the barometers and thermometers be as follows to find the altitude.

| Thermon | neters. | \parallel B | arometer | s. |
|-----------|-----------|-----------------|----------|----------|
| Detached. | Attached. | Lower | 29.68 | |
| 57 | 57 | Upper | 25.28 | |
| 42 | 43 | Altitude | 719.897 | fathoms. |
| | Method I | II. | 0 | |

The foregoing methods have been found from experience to give results tolerably correct in ordinary circumstances, though they deviate considerably from the truth in peculiar cases. To obviate this, as far as possible, we have given another method, which, it is

hoped, will prove very accurate.

In this case let B be the height of the English barometer at the lower station, b that at the upper, t, the temperature by Fahrenheit at the lower, and t' that at the upper, L the latitude of the place of observation, f the elastic force of vapour at the lower, and f' that at the upper, and H the height of the one place above the other in feet, then

$$H = 60000 \left\{ \frac{t + t'}{2} - 32 \atop 180 \right\} (1 + 0.00268 \cos 2 L) \times \left(1 + \frac{f + f'}{B + b\{1 + 0.0001(t - t')\}}\right) \log \left(\frac{B - \frac{t}{b}f}{b\{1 + 0.0001(t - t')\} - tf'}\right) \cdot (A)$$

$$\frac{t + t'}{2} - 32$$

The factors (1.375) 180 and 1+0.00268 cos. 2 L, may be reduced into tables; and, if given in logarithms, they will be very readily applied. If the centigrade thermometer be used, then

$$H = 60345.6 \left\{ (1.375)^{\frac{t+t'}{200}} (1 + 0.00268 \cos 2 L) = \left(1 + \frac{f+f'}{B+b\{(+0.00018(t-t')\}} \log \left(\frac{B-\frac{1}{4}f}{b\{1+0.00018(t-t')\}-\frac{1}{4}f'} \right) \right\} (B)$$

In which case also B, b, f, and f' may be given in reference to the French standard metre.*

The log. of the constant 60000 feet may be employed with ad-

vantage, being 4.778151.

If Laplace's constant 18393 metres, or 60345.6 feet, be taken, the constant logarithm would be 4.780646, and the factor 1+0.00268cos. 2 L must be used.

^{*} See Biot's Traité de Physique, Tome I. p. 531. + As Laplace's constant is perhaps the more accurate, it may be used in both cases.

BAROMETRIC TABLES. TABLE I.

TABLE OF THE DEPRESSION OF MERCURY IN GLASS TUBES.

| | Diam. | Ivory. | Young. | |
|---|-------------|----------------|----------|--|
| ı | | + | Laplace. | Toung. |
| I | In. 0.05 | In. 0.29494 | In. | In. 0.2964 |
| | 0.10 | 0.14028 | 0.13940 | 0.2904 |
| | 0.15 | 0.08628 | 0.08538 | 0.1424 |
| | 0.20 | 0.05811 | 0.05798 | 0.0589 |
| | 0.25 | 0.04075 | 0.04117 | 0.0404 |
| ı | 0.30 | 0.02916 | 0.02965 | 0.0280 |
| ì | 0.35 | 0.02110 | 0.02165 | 0.0196 |
| ı | 0.40 | 0.01534 | 0.01591 | 0.0139 |
| Ī | 0.45 | 0.01117 | 0.01174 | 0.0100 |
| ı | 0.50 | 0.00835 | 0.00868 | 0.0074 |
| Į | 0.70 | 0.00443 | 0.00462 | 0.0045 |
| | 0.80 | 0.00228 | 0.00244 | The state of the s |
| ı | 0.00 | 0.00119 | 0.00120 | |

This table is to be used only when two barometers, differing considerably in their internal diameters, are employed.

The expansion of the volume of mercury for 1° Fahr. = 0.000086, more correctly than 0.0001, though the difference in the nicest barometric observations is almost insensible.

TABLE II.

MR DALTON'S TABLE OF THE ELASTIC FORCE OF AQUEOUS VAPOUR.

Barometer 30 Inches.

| Temp. | Force. |
|-------|-----------------------|-------|-----------------------|-------|-----------------------|-------|-----------------------|-------|-----------------------|
| Fahr. | Inches of Mercury. |
| 0° | 0.064 | 20 | 0.129 | 40 | 0.263 | 60 | 0.524 | 80 | 1.000 |
| 1 | 0.066 | 21 | 0.134 | 41 | 0.273 | 61 | 0.542 | 81 | 1.040 |
| 2 | 0.068 | 22 | 0.139 | 42 | 0.283 | 62 | 0.560 | 82 | 1.070 |
| 3 | 0.071 | 23 | 0.144 | 43 | 0.294 | 63 | 0.578 | 83 | 1.100 |
| 4 | 0.074 | 24 | 0.150 | 44 | 0.305 | 64 | 0.597 | 84 | 1.140 |
| 5 | 0.076 | 25 | 0.156 | 45 | 0.316 | 65 | 0.616 | 85 | 1.170 |
| 6 | 0.079 | 26 | 0.162 | 46 | 0.328 | 66 | 0.635 | 86 | 1.210 |
| 7 | 0.082 | 27 | 0.168 | 47 | 0.339 | 67 | 0.655 | 87 | 1.240 |
| 8 | 0.085 | 28 | 0.174 | 48 | 0.351 | 68 | 0.676 | 88 | 1.280 |
| 9 | 0.087 | 29 | 0.180 | 49 | 0.363 | 69 | 0.698 | 89 | 1.320 |
| 10 | 0.090 | 30 | 0.186 | 50 | 0.375 | 70 | 0.721 | 90 | 1.360 |
| 11 | 0.093 | 31 | 0.193 | 51 | 0.388 | 71 | 0.745 | 91 | 1.400 |
| 12 | 0.096 | 32 | 0.200 | 52 | 0.401 | 72 | 0.770 | 92 | 1.440 |
| 13 | 0.100 | 33 | 0.207 | 53 | 0.415 | 73 | 0.796 | 93 | 1.480 |
| 14 | 0.104 | 34 | 0.214 | 54 | 0.429 | 74 | 0.823 | 94 | 1.530 |
| 15 | 0.108 | 35 | 0.221 | 55 | 0.443 | 75 | 0.851 | 95 | 1.580 |
| 16 | 0.112 | 36 | 0.229 | 56 | 0.458 | 76 | 0.880 | 96 | 1.630 |
| 17 | 0.116 | 37 | 0.237 | 57 | 0.474 | 77 | 0.910 | 97 | 1.680 |
| 18 | 0.120 | 38 | 0.245 | 58 | 0.490 | 78 | 0.940 | 98 | 1.740 |
| 19 | 0.124 | 39 | 0.254 | 59 | 0.507 | 79 | 0.971 | 99 | 1.800 |

TABLE III.

LOGARITHMS OF THE BULK OF GAS,

From the formula $\frac{x}{180} \times \log$. 0.1383027, in which x is the number of degrees above 32° Fahrenheit.

| Temp. | Log. Bulk. | Temp. | Log. B. | Temp. | Log. B. | Temp. | Log. B. |
|-------|------------|-------|----------|-------|----------|-------|----------|
| 0° | Ī.975413 | 25° | 1.994622 | 50° | 0.013830 | 75° | 0.033039 |
| 1 | .976181 | 26 | .995390 | 51 | 0.014599 | 76 | 0.033807 |
| 2 | .976950 | 27 | .996158 | 52 | 0.015367 | 77 | 0.034567 |
| 3 | .977718 | 28 | .996927 | 53 | 0.016135 | 78 | 0.035344 |
| 4 | .978486 | 29 | .997695 | 54 | 0.016904 | 79 | 0.036112 |
| 5 | .979255 | 30 | .998463 | 55 | 0.017672 | 80 | 0.036881 |
| 6 | .980023 | 31 | .999232 | 56 | 0.018440 | 81 | 0.037649 |
| 7 | .980791 | 32 | 0.000000 | 57 | 0.019209 | 82 | 0.038418 |
| 8 | .981560 | 33 | 0.000768 | 58 | 0.019977 | 83 | 0.039186 |
| 9 | .982328 | 34 | 0.001537 | 59 | 0.020745 | 84 | 0.039954 |
| 10 | .983096 | 35 | 0.002305 | 60 | 0.021514 | 85 | 0.040723 |
| 11 | .983865 | 36 | 0.003073 | 61 | 0.022282 | 86 | 0.041491 |
| 12 | .984633 | 37 | 0.003842 | 62 | 0.023050 | 87 | 0.042259 |
| 13 | .935401 | 38 | 0.004610 | 63 | 0.023819 | 88 | 0.043028 |
| 14 | .986170 | 39 | 0.005378 | 64 | 0.024587 | 89 | 0.043796 |
| 15 | .986938 | 40 | 0.006147 | 65 | 0.025356 | 90 | 0.044564 |
| 16 | .987706 | 41 | 0.006915 | 66 | 0.026124 | 91 | 0.045333 |
| 17 | .988475 | 42 | 0.007683 | 67 | 0.026892 | 92 | 0.046101 |
| 18 | .989243 | 43 | 0.008452 | 68 | 0.027661 | 93 | 0.046869 |
| 19 | .989911 | 44 | 0.009220 | 69 | 0.028429 | 94 | 0.047638 |
| 20 | .990780 | 45 | 0.009989 | 70 | 0.029197 | 95 | 0.048406 |
| 21 | .991548 | 46 | 0.010757 | 71 | 0.029966 | 96 | 0.049174 |
| 22 | .992317 | 47 | 0.011525 | 72 | 0.030734 | 97 | 0.049943 |
| 23 | .993085 | 48 | 0.012294 | 73 | 0.031502 | 98 | 0.050711 |
| 24 | .993853 | 49 | 0.013062 | 74 | 0.032271 | 99 | 0.051489 |

P. P. 1 2 3 4 5 6 7 8 9 to tenths 77 153 238 307 384 46I 538 615 691

TABLE IV. LOGARITHMIC VALUES OF 1+0.00268 cos. 2 L.

| d | Lat. | Log. | Lat. | Log. | Lat. | Log. | Lat. | Log. |
|----|------|----------|------|----------|------|----------|------|----------|
| e. | 0° | 0.001162 | 13° | 0.001045 | 26° | 0.000716 | 39° | 0.000242 |
| - | 1 | 0.001162 | 14 | 0.001027 | 27 | 0.000684 | 40 | 0.000202 |
| | 2 | 0.001160 | 15 | 0.001007 | 28 | 0.000651 | 41 | 0.000162 |
| 1 | 3 | 0.001156 | 16 | 0.000986 | 29 | 0.000617 | 42 | 0.000122 |
| | 4 | 0.001151 | 17 | 0.000964 | 30 | 0.000582 | 43 | 0.000081 |
| | 5 | 0.001145 | 18 | 0.000941 | 31 | 0.000546 | 44 | 0.000041 |
| ı | 6 | 0.001138 | 19 | 0.000916 | 32- | 0.000510 | 45 | 0.000000 |
| ı | 7 | 0.001129 | 20 | 0.000891 | 33 | 0.000473 | 46 | 9.999959 |
| | 8 | 0.001118 | 21 | 0.000864 | 34 | 0.000434 | 47 | 9.999919 |
| | 9 | 0.001106 | 22 | 0.000836 | 35 | 0.000398 | 48 | 9.999878 |
| | 10 | 0.001093 | 23 | 0.000803 | 36 | 0.000360 | 49 | 9.999838 |
| | 11 | 0.001078 | 24 | 0.000778 | 37 | 0.000321 | 50 | 9.999798 |
| | 12 | 0.001062 | 25 | 0.000747 | 38 | 0.000281 | 51 | 9.999758 |

TABLE IV .- Continued.

| Lat. | Log. | Lat. | Log. | Lat. | Log. | Lat. | · Log. |
|------|-----------|------|----------|------|----------|------|----------|
| 52° | 9.999719 | 629 | 9.999349 | 72° | 9.999059 | 82° | 9.998882 |
| 53 | 9.999679 | 63 | 9.999316 | 73 | 9.999036 | 83 | 9.998871 |
| 54 | 9.999640 | 64 | 9.999284 | 74 | 9.999014 | 84 | 9.998862 |
| 55 | 9.999602 | 65 | 9.999253 | 75 | 9.998993 | 85 | 9.998855 |
| 56 | 9.999566 | 66 | 9.999222 | 76 | 9.998973 | 86 | 9.998849 |
| 57 | 9.999527 | 67 | 9.999192 | 77 | 9.998955 | 87 | 9.998844 |
| 58 | :9.999490 | 68 | 9.999164 | 78 | 9.998938 | 88 | 9.998840 |
| 59 | 9.999454 | 69 | 9.999136 | 79 | 9.998922 | 89 | 9.998838 |
| 60 | 9.999418 | 70 | 9.999109 | 80 | 9.998907 | 90 | 9.998838 |
| 61 | 9.999383 | 71 | 9.999084 | 81 | 9.998894 | | 1-1-1 |

EXAMPLE I.

To determine the height of Arthur's Seat above the sea at Leith by the following observations, the height by levelling being 802.66 feet.

| Leith Pier 29.567 Arthur's Seat 28.704 | 55.25 5 | ther. Dew poi 4°.0 50°.0 0.5 48.5 | f = 0.375 |
|--|------------------------------|---|---|
| Fah. ther. 54°.0 50 .5 | | $0001 \times 3.5 = 0.0$ $4 + 0.010$ | f+f'=0.732 010 nearly, and =28.714 |
| Sum 104.5 Constan | t log. of 60000 | O feet | 4.778151 |
| Half 52.25 log. B B=29.567, B- \downarrow f=29.5 b=28.714, b- \downarrow f'=28.7 | 67-0.062=29. 14-0.059=28. | .505 log. 1.4698 655 log. 1.4572 | 0.015367 395 153 01 38 |
| mile. | | 0100 | 041 0 100400 |
| Difference | was the | ., .0120 | 94 log. 2.103462 |
| $1 + \frac{f + f'}{B + b} = 1 + \frac{0.732}{58.281} =$ | =1.01256 log. | | 9410g, 2.103462 138 0.006181 206 25 |
| THE THE PART OF | =1.01256 log. | | 0.006181 206 |

^{*} The t and t' in the denominators of the fractions in the formula should have been τ and τ' , the temperatures of the attached, to distinguish them from those of the detached thermometers.

| Laplace's constant log. in feet 1+0.00268 cos. 2 L for 56° Mean temperature 52.25 log. B | 4.780646 9.999566 0.015367 153 38 |
|--|---|
| Difference of logs of corrected altitudes, log | 2.103462 138 |
| 1.01256 log. | 0.005181 206 |
| | <u>25</u> |
| H =803.12 H'=802.66 | 2.904782 70 |
| Excess = 0.46 foot, or $5\frac{1}{2}$ inches | 12 |

EXAMPLE II.

Required the height of the Peak of Snowden above Caernarvon quay from the following set of observations?

| Caernarvon Quay Snowden Peak | | Att. Ther | Det. Ther. 55.25 43.00 | Dew Point. 50°.25 41.00 |
|--|-----------------------|------------------------------|---------------------------|-------------------------|
| Constant logar Correction for | latitude 53° | | (m) | 4.780646 9.999679 |
| $\frac{55^{\circ}.25 + 43^{\circ}}{2} =$ | 59°.125 log. | В | | 0.013062 |
| $B - \frac{1}{6}f = 29.92$ $b' - \frac{1}{6}f' = 26.26$ | 0 log. 1.47 32 1.4 | 7 <mark>5962</mark> 19328 | | 15 |
| Difference, $f+f'$ | 0.656 | 56634 log. | . 176 | 31 2.753047 |
| $1 + \frac{f + f'}{B + b} = 1$ | + 56.182 | = 1.01168 log | S | 0.004751 |
| H = 3561.2 | foot | | 310 0 - W | $\frac{33}{3.551592}$ |
| H' = 3555.4 | | | · · | 5.551,582 |
| Excess 5.8 | got dis - | | | |

EXAMPLE III.

Captain Sabine found the height of a hill at Spitzbergen, determined geometrically, to be 1644 feet; required its height barometrically from the following set of observations?

Observed height of the barometer at the bottom.

+0.1479

True height - 29.8214

Difference

| Observed height of the barometer, &c. at the top. | |
|--|----------------------------|
| Barometer, (diam. of tube 0.15) 28.0075 Reduction to 32° F. —0.0105 Capacity . —0.0445 Capillary action (Young) +0.0880 Attached the Detached Dew point | . 35 .4 |
| +0.0330 | |
| True height 28.0405 | |
| 0 | 4.780646 9.998907 66 |
| | $\bar{2.428135}$ |
| Mean temperature $\frac{34.9+35.5}{2}$ = 35.2 log. B | 0.002305 |
| $f + f' = 0.214 \pm 0.225 = 0.430$ | 153 0.003029 247 |
| D III 1695 | 3.213488 |
| Bar. H = 1635 Geo. H = 1644 | 0.210400 |
| Difference — 9 feet | |
| By another set of observations. | Mali |
| Attached thermometer 39°.4 35°.2 | corrected. |
| Detached 35.4 | 4 200040 |
| Constant logarithm Correction for latitude 80° | 4.780646 9.998707 |
| B $-\frac{1}{6}f$ =29.8304 -0.0374 =29.7930 log. 1.474115 b $-\frac{1}{6}f'$ =28.0624 -0.0360 =28.0264 log. 1.447569 | · / / |
| | 2.424065 |
| Mean temperature of the air $\frac{35.4+34.2}{2}$ = 34.8 log. B | 0.001537 |
| 01.01 | 615 |
| $1 + \frac{f + f'}{B + b} = 1 + \frac{.225 + .216}{57.89} = 1.00762 \log.$ | 0.003029 |
| CON API | 268 |
| Bar. H = 1618 3 Geo. H = 1644.0 | 3.209067 979 |
| Diff. — 25.7 | 88 |
| By the first set of experiments $H = 1635$ feet By the second . 1618 | |

Captain Sabine thinks there is some error in the second set of experiments, arising from the circumstance, that Mr Foster, his assistant, was obliged to hold the instruments to prevent their agitation by the

It is proper to remark, that Captain Sabine finds 1644.58 for the first and 1630.66 for the second set of observations, as stated in the Philosophical Transactions of the Royal Society of London, but the particular formula he used is not mentioned. The usual formulæ given by Roy, Shuckburgh, and Laplace may give the height more near the geometrical method in certain cases, such as in a mean state of the atmosphere, than that which we have given, though there is no doubt but that the circumstances which have induced us to give a new method, involving considerations not usually attended to in such measurements, are more conformable to the laws of nature, and will in time become more accurate as those branches of physical science on which they depend are rendered more perfect.

The dew point is supposed to be found by Daniell's hygrometer. If that instrument is not at hand, the dew point may be found by two good thermometers, one of which has its ball covered with moistened tissue-paper, as proposed by Mr Anderson, Rector of the Academy of Perth, who also gives a formula for the barometric measurement of altitudes, in which in some of the corrections I have been antici-

Let F, the elastic force of vapour by Dalton's table be thus reduced to f according to the difference between the naked and covered $\frac{0.028 \delta t \times p}{\text{=F-0.00092} \delta t \times p, \text{ in which}}$ thermometers, then $f = \mathbf{F} - \mathbf{F}$

 δt is the difference between the temperatures of the thermometers, and

p the barometric pressure.

Now let φ be the elastic force at the dew point, then $F=0.00092 p \delta t$ $\varphi = \frac{1 + 0.002084(t - t')}{1 + 0.0021(t - t')}$ nearly (1)

Here t', the temperature of the dew-point is unknown, but may be determined, first approximately from the numerator of the formula, and then substituted in the denominator, and a second approximation obtained, which will generally be sufficiently correct.

To exemplify this, let the thermometer with the dry ball show 60°F, and that covered with moistened tissue paper

T-t or δt . Now if the barometer be at 30.4 inches we have from the numera-

tor of formula (1) $f = 0.524 - 0.00092 \times 8\frac{1}{9} \times 30.4 = 0.524 - 0.238 =$ 0.286. This f corresponds, by the table of Dalton to 42° nearly, which being substituted for t' in the denominator of the formula

0.2860.286gives $\varphi = \frac{1}{1 + 0.0021(60 - 42)} = \frac{0.2756}{1.0378} = 0.2756$ which finally gives

t'=41°.3, the dew point. This is perhaps one of the best methods of determining the point of deposition, as the instruments are not, like the hygrometers of Deluc and Saussure, liable to be deteriorated by time, and besides, may still answer other purposes which none of the usual hygrometers can.

Cor.—From the same principles, may be derived a formula to determine the weight of moisture in 100 cubic inches of air or

 $0.6854 \, \varphi$ W = $\frac{1}{1+0.0021} \frac{1}{(t'-32)}$ at the freezing point. When $\phi = 2756$ and t'=41.3 we get from the expression W=0.1837 grains when the air is completely saturated with humidity. But when the temperatures 0.1837are 60° and 41° the $W = \frac{0.1057}{1 + 0.0021(60 - 41)} = 0.1767$ grains in 100 cubic inches. Perhaps this method may be conveniently compared with Mr Daniell's, to show their relative accuracy and consistency.

It may be added, that Mr Dalton states from experiments at moderate heights, that an elevation of 240 feet gives a depression of 1° temperature Fah. and an elevation of 390 feet gives a depression of 1°F. of the dew point. Hence, if t be the temperature and $\hat{\mathbf{D}}$ the dew point

$$\Delta t = \frac{\Delta H}{240}$$
, and $\Delta D = \frac{\Delta H}{390}$.

For ordinary heights, such as those usually met with in Britain, the following method, requiring no tables, which is somewhat simpler and more easily recollected than Dr Robison's, is subjoined.

Let B be the barometric altitude at the lower situation, and b that at the upper corrected for the difference of temperature in the usual manner, the atmosphere being in its mean state with regard to aqueous vapour, &c.

Then H=13100
$$\frac{(B+b)(B-b)}{Bb}$$
 $\left\{1+0.00245\left(\frac{t+t'}{2}-32^{\circ}\right)\right\}$ in feet.

Bar. in. 29.567 Att. Ther. Det. Ther. Ex.—Leith Pier 55°1 Arthur's Seat 28.704 51 3 50 글 $28.704 \times 0.0001 \times 3.5 = 0.010$, and 28.704 + 0.010 = 28.714 = b

 $1 + \left(\frac{54 + 50\frac{1}{2}}{2} - 32^{\circ}\right) \times 0.00245 = 1 + 20\frac{1}{4} \times 0.00245 = 1.04961, \text{ hence}$ $H = 13100 \times \frac{58.281 \times 0.858}{29.567 \times 28.714} \times 1.04961 = 805 \text{ feet.}$ Height by levelling

Difference 2 feet.

EXAMPLES FOR EXERCISE.

1. If the base of an oblique-angled plane triangle be 40, and the other two sides 20 and 30, what is the length of the perpendicular? Ans.—14.52369.

2. If the base of a plane triangle be 40, and the other two sides 20 and 30, what are the segments of the base made by a line bisecting the vertical angle? Ans.—24 and 16.

3. The hypotenuse of a right-angled triangle is 19630040, and one of the legs 19630000; required the two acute angles?

Ans.—6' 56".4, and 89° 53' 3".6.

4. If the sides of a plane triangle be in proportion to each other as the numbers $\frac{1}{4}$, $\frac{1}{3}$, and $\frac{1}{2}$; what are the angles?

Ans.-117° 16' 46", 36° 20' 10", and 26° 23' 4". 5. At the Observatory on the top of the Calton-hill, 350 feet above the sea at Leith, the angle of depression of the horizon marked by the sea down the frith of Forth was 18' 12" by observation. Now supposing the effect of refraction to be one-twelfth part of the whole, this must be increased by one-eleventh of itself, or the true depression would be 19' 51".28. Required the earth's diameter?

Ans.—7946 miles.

6. Suppose the height of Melville's Monument, in St Andrew's Square, Edinburgh, to be 60 feet, and that the figure placed upon the top of it is 12 feet high, at what distance from the monument may the statue be viewed under an angle of 3°, and what is the greatest angle under which it can be seen?

Ans.—It will be seen, under an angle of 3°, at the distance of 208.23, or 20.75 feet, and the greatest angle under which it can be

seen from a point in the horizontal plane is 5° 13'.

7. It is required to find the distances from the Edystone light-house to Plymouth, Start Point, and the Lizard respectively from the following data:

| | (Plymou | th to Lizard | 60 | |
|----------------------|------------|--------------|----------|-----------------|
| The distances from - | Lizard t | o Start Poir | nt 70 | miles. |
| | Start Po | int to Plym | outh 20 | |
| Plymouth | A-10 | | (North | |
| | bears fron | n Edystone | ₹ W. S. | W. |
| Start Point | | | E. by | N. |
| | - (| Lizard | 53.04) | 1-1-1 |
| Ans.—From Edys | tone to | Plymouth | 14.33 | miles. |
| | 111 | Start | 17.36 | • 12 |
| 8. Barometers. | Therm | ometers. | Required | the Altitude. |
| Lower 29.45 | Attach. | Detach. | | 09.61 fathoms, |
| Upper 26.82 | 38 | 31 | or 245 | 8 feet, by Hut- |
| | 41 | 35 | ton's r | nethod. |

EXAMPLES BY THE FRENCH MEASURES.

| Observer Humboldt. | Height of Barometer. | Attached Thermometer. | Detached Thermometer. | Dew Point. | Latitude. |
|-----------------------|-------------------------------------|--------------------------|--------------------------|---------------|----------------------------------|
| | 0 ^m .509818 0 .762944 | | 18°.75 cent. 25 .30 | | 5° 0 N. H=3543 ^m |
| | 0 ^m .377275 0 .762000 | | - 1°.6 cent. +25 .3 | | 1° 45′ N. H=5925 ^m |

Calculation of the last Example by Method III.

Constant 18393 metres log. 4.264653
$$(1.375)^{\frac{11.85}{100}} = \frac{11.85}{100} \times 0.138303 = 0.016389$$
 Latitude 1° 45′ log. 0.001161
$$B - \frac{1}{6}f = 0.759114 \log. \overline{1.880307}$$

$$b - \frac{1}{6}f' = 0.377471 \log \overline{1.576884}$$
 Difference 0.303423 log. $\overline{1.482048}$

Difference 0.303423 log. $1 + \frac{f + f'}{B + b} = 1 + \frac{0.022373}{1.136585} = 1.019686$ 0.008467

PART II.

SPHERICAL TRIGONOMETRY.

SECTION I.

Definitions, Principles, and General Properties.

1. Spherical Trigonometry is that branch of mathematics by which we are enabled, in all cases, where three of the six parts of a triangle formed by arcs of great circles in the surface of a sphere are given,

to compute or determine the other three.

2. In plane trigonometry the knowledge of the three angles is not sufficient for ascertaining the sides; for in that case the relations only of the three sides can be obtained, and not their value; whereas, in spherical trigonometry, when the sides are circular arcs, whose value depends on their proportion to the whole circle, that is, on the number of degrees they contain, the sides may always be determined when the three angles are known. Among other remarkable differences between plane and spherical triangles are,

(1.) That in the former, two known angles always determine the

third; while in the latter they never do.

(2.) The surface of a plane triangle cannot be determined from a knowledge of the angles alone; while that of a spherical triangle always can.

3. A sphere or globe is a round body formed by the revolution

of a semicircle about its diameter, which remains fixed.

4. The centre of the sphere is the same with that of the revolv-

ing sémicircle.

5. The axis of the sphere is the straight line about which the semicircle revolves.

PROPOSITION I.

6. If a sphere be cut by a plane, the section will be a circle. Let the sphere AEBF be cut by the plane ADB; then will the

section ADB be a circle. Draw the chord, or diameter of the section AB, perpendicular to the section ADB, and through the centre C draw the axis of the sphere ECGF, which will (Euc. III. 3.) bisect the chord AB in the point G. Also, join CA, CB; and draw CD, GD, to any point D in the perimeter of the section ADB.

Then, because CG is perpendicular to the plane ADB, it must be perpendicular both to GA and

GD. Hence CGA and CGD are two right-angled triangles, having

the perpendicular CG common, and the hypotenuse CA equal to the hypotenuse CD, being both radii of the same sphere; therefore their third sides GA, GD, are also equal. In like manner, it may be shown, that any other line drawn from G to the circumference of the section ADB, is equal to GA, or GB; and consequently

that section is a circle.

Cor.—If a sphere be cut by a plane through the centre, the section is a circle, having the same centre with the sphere, and equal to the circle by the revolution of the half of which the sphere was described. For all the straight lines drawn from the centre to the surface of the sphere are equal to the radius of the generating semicircle. Therefore the common section of the spherical surface, and of a plane passing through its centre, is a line lying in one plane, having all its points equally distant from the centre of the sphere, and is consequently the circumference of a circle, having for its centre the centre of the sphere, and for its radius, the radius of the sphere, that is, of the semicircle by which the sphere is described. It is therefore equal to the circle of which that semicircle is a part.

7. Any circle formed from the section of a sphere, by a plane

through its centre, is called a great circle of the sphere.

Cor.—All great circles of the sphere are equal; and any two of

them bisect each other.

They are all equal, because they have all the same radii, as has just been shewn, and any two of them bisect one another; for, as they have the same centre, their common section is a diameter of both, and therefore bisects both.*

8. The pole of a great circle of the sphere is a point in the surface of the sphere equidistant from every part of the circumference of

that circle.

9. A spherical angle is an angle on the surface of a sphere contained by the arcs of two great circles which intersect each other, and is the same as the inclination of the planes of, or tangents at the point of intersection to, these great circles.

10. A spherical triangle is a figure on the surface of a sphere formed by the intersection of three arcs of great circles, each of which is

less than a semicircle.

11. A right-angled spherical triangle has one right-angle; the sides about the right-angle are called legs, and that opposite the right-angle is called the hypotenuse.

12. A quadrantal spherical triangle has one side equal to a qua-

drant, or 90°.

13. An oblique-angled spherical triangle has none of its angles

right.

14. Spherical triangles are also called equilateral, isosceles, or scalene, according as they have three sides equal, two sides equal, or all

the three sides unequal.

15. Two arcs, or angles, when compared together, are said to be alike, or of the same affection, when both are less, or both are greater than 90°. But when one is less, and the other greater than 90°, they are said to be unlike, or of different affections or characters.

16. Every spherical triangle has three sides and three angles;

^{*} Hence the intersections of the circumferences of two great circles are two points diametrically opposite to each other.

and if any three of these six parts be given, the other three may be found.

17. A lune is a part of the surface of a sphere contained by the semicircumferences of two great circles.

18. A small circle of the sphere is that whose plane does not pass

through the centre of the sphere.

19. The small circles of the sphere do not fall under the consideration of spherical trigonometry, but such only as have the same centre with the sphere itself. And hence it is that spherical trigonometry is of so much use in practical astronomy, the apparent heavens assuming the shape of a concave sphere whose centre is the same as the centre of the earth.

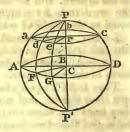
20. The sides of a spherical triangle are all arcs of great circles, which, by their intersection on the surface of a sphere, constitute

that triangle.

21. If ABDG be a great circle of the sphere whose centre is C and PCP' a diameter of the sphere perpendicular to its plane, the points P, P' are the poles of that circle. And if the small circle abcd be perpendicular to PP', we call P, P' the poles of that small circle also.

22. The great circles PAP', PGP', passing through the poles P, P' of the great circle ABDG, are called *secondaries* to that

circle.



PROPOSITION II.

23. If two arcs of circles meet each other they make two angles, which are together equal to two right-angles.

Let the arc AB meet the arc CD in the point B; then will the two angles ABC, ABD be equal to two right-angles. For, suppose the arc BE to be perpendicular to CD, then the angles EBC, EBD are right-angles.

And since the angle EBD is equal to the angles CEBA, ABD, the three angles, EBC, EBA, ABD,

are equal to the two right-angles.

But the two angles, EBC, EBA, are equal to the angle ABC; whence the two angles, ABC, ABD, are also equal to two right-angles.

PROPOSITION III.

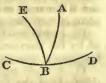
24. If two arcs of a circle intersect each other, the vertical, or opposite angles, will be equal.

Let the two arcs, AB, CD, intersect each other in E, then will the angle AEC be equal to DEB, and AED to CEB.

For since the arc AE meets the arc CD, the angles AEC, AED are together equal to two right-angles, (Prop. II.)

And because the arc DE, meets the arc AB, the angles DEB, DEA are also equal to two right-angles.

Taking away from each the common angle AED, and the re-



maining angle, AEC will be equal to DEB. In the same manner

it may be proved that the angle AED is equal to CEB.

Cor.—Hence if any number of arcs of circles intersect each other, all the angles formed about the point of intersection are together equal to four right-angles.

PROPOSITION IV.

25. The arc of a great circle, between the pole and the circum-

ference of another great circle, is a quadrant.

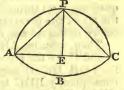
Let ABC be a great circle, and P its pole; if PC, an arc of a great circle, pass through P and meet ABC in C, the arc PC is a quadrant.

Let the circle, of which PC is an arc, meet ABC again in A, and

let AC be the common section of the planes of these great circles, which will pass through E, the centre of the sphere: Join PA, PC.

Because AP=PC, (def.), and equal straight lines in the same circle, cut off equal arcs, the arc AP = the arc PC; but APC is a semicircle, therefore the arcs AP, PC, are

each of them quadrants.



Cor. 1. If PE be drawn, the angle AEP is a right-angle; and PE, being at right-angles to every line it meets with in the plane of the circle ABC, is at right-angles to that plane. Therefore the straight line drawn from the pole of any great circle to the centre of the sphere is at right-angles to the plane of that circle; and, conversely, a straight line drawn from the centre of the sphere perpendicular to the plane of any great circle, meets the surface of the sphere in the pole of that circle.

Cor. 2. The circle APC has two poles, as has been shewn in art. 21., one on each side of its plane, which are the extremities of a diameter of the sphere perpendicular to the plane APC; and no

other points but these can be poles of the circle APC.

PROPOSITION V.

26. If the pole of a great circle be the same with the intersection of other two circles, the arc of the first circle intercepted between the other two, is the measure of the spherical angle which the same two circles make with one another.

Let the great circles AP, BP, on the surface of the sphere of

which the centre is O, intersect each other in P, and let AB be an arc of another great circle of the pole as P, AB is the measure of

the spherical angle APB.

Join PO, AO, BO; since P is the pole of AB, PA, PB are quadrants, and the angles POA, POB are right; therefore the angle AOB is the inclination of the planes of the circles PA, PB, and is equal to the spherical angle APB; but the arc AB measures the angle

A B C

AOB, therefore it also measures the spherical angle APB.

Cor. If two arcs of great circles, PA, PC, which intersect each other in P, be each of them quadrants, P will be the pole of the

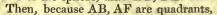
great circle which passes through A and B, the extremities of those arcs. For since the arcs PA and PB are quadrants, the angles POA, POB are right-angles, and PO is therefore perpendicular to the plane AOB, that is, to the plane of the great circle which passes through A and B. The point A, therefore, is the pole of the great circle which passes through A and B.

PROPOSITION VI.

27. An angle made by any two great circles of the sphere is equal to the angle of inclination of the planes of these circles.

Let BAE be a spherical angle made by two great circles CBA,

CEA; then will this angle be equal to the angle of inclination of the planes of those circles. For, take the arcs AB, AE, each equal to 90°, or a quadrant, and through the points B, E draw the arc of the great circle BE, and from D, the centre of the sphere, draw DB, DE.



A and C are the poles of the circle of which BE is a part, and the lines DB, DE are each perpendicular to the common section AC; consequently BDE is the angle of inclination of the planes CBA, CEA. But since DB, DE are equal, being radii of the same sphere, the angle BDE, which is measured by the arc BE, is equal to the angle BAE, which is measured by the same arc.

And if FH be drawn in the plane CBA, and FG in the plane CEA, each perpendicular to the common section AC, the angle HFG, which is equal to the angle BDE, will also be equal to the

angle BAE.

Cor. The angle BAE made by two great circles of the sphere BA, EA, is equal to the angle n A m, formed by two tangents drawn from the angular point A, one in each plane, these tangents being each perpendicular to the diameter AC.

PROPOSITION VII.

28. The distance of the poles of any two great circles of the sphere is equal to the angle of inclination of the planes of those circles.

Let AEB, CED be two great circles, and P, P' their poles; then

will the arc PP' be equal to the angle of their inclination AOC or BOD.

For, since P is the pole of the circle AEB, and P' of CED, the arc PA will be equal to PC, being each quadrants, or 90°; and if PC, A which is common to each, be taken away, the remaining arc, PP', which is the distance of two poles, is equal to CA, the measure of the angle of inclination AOC.



PROPOSITION VIII.

29. The circumference of a secondary is at right angles to the circumference of its great circle at the point of intersection.

The direction of the circumference of a great circle at any point

being the same as the diameter of its tangent at that point, the angle OBT, (figure prop. V.), is a right-angle, BT being a tangent to BP at the point B. POB is also a right-angle, and the arc PB is in the plane POB, therefore the direction of the circumference PB at B must be parallel to PO. But PO is perpendicular to the circle ABC; therefore the circle PBP' is at B perpendicular to the circle ABC; hence the arc PB at B is at right-angles to AB at B. For the same reason PAB is also a right-angle.

Cor. 1.—If a great circle, PBP', be perpendicular to ABC, and BP, BP' be taken each equal to a quadrant, or 90°, P, P' are the

poles of the circle ABC.

Cor. 2.—If any two great circles, PAP', PBP', be perpendicular to the circle ABC, they meet at the poles P, P' of that circle.

PROPOSITION IX.

30. In an isosceles spherical triangle the angles at the base are equal.

Let ABE (figure prop. VI.) be a spherical triangle, having the side

AB equal to the side AE, the spherical angles ABE, ABE are equal.*

Cor. 1.—Hence, if two of the angles of a triangle be equal, the

sides opposite to them are likewise equal.

Cor. 2.—A perpendicular drawn from the vertex of an isosceles spherical triangle to the base, bisects both the base and the vertical angle, except when the two sides are quadrants; in which case there are an indefinite number of perpendiculars.

PROPOSITION X.

31. If the three sides of one spherical triangle be equal to the three sides of another, each to each, the angles which are opposite the equal sides are equal.

PROPOSITION XI.

32. If two sides and the included angle of one spherical triangle be equal to two sides and the included angle in another, these two tringles are equal.

PROPOSITION XII.

33. If from the angles of a spherical triangle, as poles, there be described on the surface of the sphere three arcs of great circles, which, by their intersections, form another spherical triangle, each side of this new triangle will be the supplement of the measure of the angle which is at its pole, and the measure of each of its angles the supplement to that side of the primitive triangle to which it is opposite.

PROPOSITION XIII.

34. If the three angles of one spherical triangle be equal to the three angles of another, each to each, the sides which are opposite to the equal angles are equal.

PROPOSITION XIV.

35. If a side and two adjacent angles of one spherical triangle be equal to a side and two adjacent angles of another, each to each, their remaining sides and angles will be equal.

^{*} The demonstrations, which may be seen in Playfair's or Legendre's Geometry, are omitted, as they would swell this work too much, but may perhaps appear in a more complete treatise on trigonometry that has been long meditated.

PROPOSITION XV.

36. The sum of any two sides of a spherical triangle is greater than the third side; and the difference of any two sides is less than the third side.

Cor.—The shortest distance between any two points on the surface of a sphere is the arc which passes through these points.

PROPOSITION XVI.

37. The greater side of any spherical triangle is opposite to the greater angle, and the less side to the less angle.

And, in a similar manner, it may be shown that the less side is op-

posite to the less angle, and the less angle to the less side.

PROPOSITION XVII.

38. The sum of the three sides of any spherical triangle is less than the circumference of a circle, or 360°; and the difference of any two sides is less than 180°.

PROPOSITION XVIII.

39. The sum of the three angles of every spherical triangle is greater than two right-angles, or 180°, and less than six, or 540°.

Cor.—The sum of any two angles of a spherical triangle is great-

er than the supplement of the third angle.

For the angles A+B+C, being greater than two right-angles, or than ACB+ACG, if ACB or C be taken away, the sum of the remaining angles A+B, will be greater than ACG.

PROPOSITION XIX.

40. If the sum of any two sides of a spherical triangle be equal to, greater, or less than a semicircle, the sum of their opposite angles will, accordingly, be equal to, greater, or less than two right-angles; and conversely.

And, in a similar manner, it may be shown, that if the sum of the two angles B and C be equal to, greater, or less than 180°, the sum of the opposite sides AB and AC, will also be equal to, greater, or

less than 180°.

Cor. 1.—If each side of a spherical triangle be equal to, greater, or less than 180°, each of the angles will, accordingly, be right, obtuse, or acute; and conversely.

Cor. 2.—Half the sum of any two sides of a spherical triangle is

of the same kind as half the sum of their opposite angles.

PROPOSITION XX.

41. In any right-angled or quadrantal spherical triangle, the legs or sides are of the same kind or affection as their opposite angles,

and conversely.

The same will also hold if the triangle be quadrantal; for its sides and angles being the supplements of the angles and legs of the polar triangle, which in this case is right-angled, the similarity will be the same as before.

Proposition XXI.

42. In any right-angled spherical triangle the hypotenuse is less or greater than 90°, according as the two legs, or the two angles, or a leg and its adjacent angle, are alike or unlike.

what you was a man and the comment of the comment

SECTION II.

Solution of Spherical Triangles.

HAVING given a view of the general principles and properties of spherical triangles, the solution of the various problems in spherical trigonometry ought necessarily to follow. These problems may be resolved either by geometrical construction or by arithmetical calculation. There are various methods of construction, but the most simple, and generally employed, is the stereographic, in which all the circles of the sphere are represented by straight lines or circles.

Of the Stereographic Projection of the Sphere.

DEFINITIONS.

I. To project an object, as it is commonly called, is to represent every point of that object upon the same plane, as it appears to the eye in a certain position.

II. That plane upon which the object is projected is called the plane of projection, and the point where the eye is situated, the pro-

jecting point.

III. The stereographic projection of the sphere is that in which a great circle is assumed as the plane of projection, and one of its poles as the projecting point.

IV. The great circle, upon the plane of which the projection is

made, is called the primitive.

V. By the semitangent of any arc is meant the tangent of half

that arc.

VI. The line of measures of any circle of the sphere is that diameter of the primitive, produced indefinitely, which is perpendicular to

the line of common section of the circle and the primitive.

VII. The projection, or representation of any point in the sphere, is the point in which the straight line drawn from it to the projecting point intersects the plane of projection.

THEOREM I.

Every great circle of the sphere, which passes through the projecting point, is projected in a straight line, passing through the centre of the primitive; and every arc of it, reckoned from the other pole of the primitive, is projected into its semitangent.*

Cor. 1.—Every small circle, which passes through the projecting point, is projected into that straight line which is its common section

with the primitive.

Cor. 2.—Every straight line in the plane of the primitive, and produced indefinitely, is the projection of some circle on the sphere passing through the projecting point.

Cor. 3.—The stereographic projection of any point on the surface

^{*} For the investigation of the properties of this method of projection, see Gregory's or Keith's Treatises of Trigonometry, and West's Mathematics.

of the sphere, is distant from the centre of the primitive by the semitangent of the distance of that point from the pole opposite the projecting point.

THEOREM II.

Every circle of the sphere, which does not pass through the projecting point, is projected into a circle.

Cor. 1.—The centres and poles of all circles parallel to the primi-

tive, have their projections in its centre.

Cor. 2. The centre and poles of every circle, inclined to the primitive, have their projections in the line of measures.

Cor. 3.—All projected circles cut the primitive in two points di-

ametrically opposite.

THEOREM III.

The centre of the projection of a great circle is distant from the centre of the primitive by the tangent of the inclination of the great circle to the primitive, and its radius is the secant of the same.

THEOREM IV.

The centre of projection of a small circle, perpendicular to the primitive, is distant from the centre of the primitive by the secant of the distance of the circle from its nearest pole, and the radius of projection is the tangent of the same.

THEOREM V.

The projections of the poles of any circle inclined to the primitive, are in the line of measures distant from the centre of the primitive by the tangent and cotangent of half its inclination.

THEOREM VI.

Any two circles upon the sphere, passing through the poles of two great circles, intercept equal arcs upon them.

THEOREM VII.

If, from either pole of a projected great circle, two straight lines be drawn to meet the primitive and the projection, they will intercept corresponding arcs of these circles.

Solution of Right-Angled Spherical Triangles.

The solution of right-angled spherical triangles may be accomplished by formulæ investigated expressly for that purpose. We are indebted to Napier, however, for a comprehensive rule of great advantage to the memory, by reducing all the theorems employed in the solution of right-angled triangles to two. This is called the rule of the circular parts, and is perhaps one of the happiest examples of artificial memory that is known.

DEFINITIONS.

I. If in a right-angled spherical triangle the right-angle be set aside, and the five remaining parts of the triangle alone be considered, consisting of the three sides, and the two oblique angles, then, the two sides containing the right-angle, and the complements of

the other three, namely, of the two angles, and of the hypotenuse.

are called the circular parts.

II. When, of the five circular parts, any one is taken for the middle part, then, of the remaining four, the two which are immediately adjacent to it on the right and left are called adjacent parts; and the other two, each of which is separated from the middle part by an adjacent part, are called opposite parts.

This arrangement being made, the solution is obtained by the fol-

lowing

THEOREM.

In any right-angled spherical triangle, the rectangle under the radius, and the sine of the middle part, is equal to the rectangle under the tangents of the adjacent parts; or to the rectangle under the cosines of the opposite parts.

This theorem, or rule, may be easily remembered, by remarking, that the first vowels in sine, tangent, cosine, are respectively the same

as the first in middle, adjacent, opposite,

o elle or, R x sin. mid=rect. tan adj. = rect. cos. op.*

It is usual to convert the equation under consideration into an analogy having the unknown quantity for the last term, though, to those acquainted with algebra, it would be more convenient to make it alone the first term of an equation, and the remaining terms, combined properly according to the rules of algebra, the last.

PROBLEM I.

Given three of the six parts, as, for example, the hypotenuse and one of the angles of a right-angled spherical triangle, to find the sides and the remaining angle.

On the first of May 1826, the sun's longitude was 1 10 32 12", and the obliquity of the ecliptic 23 27' 40"; required the right as-

cension and declination?†

Ans.—R. A. 2h 32m 27s.3; dec. 14° 59′ 47″ N.

Construction.—With the chord of 60° describe the primitive circle EPQP' on the plane of the solstitial colure, and draw the diameters EQ and PP' at right-angles to one another, then will EQ represent the equator, and PP' the E polar axis. Lay off from the same line of chords polar axis. Lay off from the same line of chords and draw the diameter el representing the ecliptic, at right-angles to which draw plocation plane properties that the color of the

and p, p' are the poles of the ecliptic. From the line of semitangents, (Theorem I.), lay off the sun's longitude 1° 10° 32′ 12″, or 40° 32′ 2 on the ecliptic, from A to C, then C will be the place of the sun, and n c m a parallel of declination. Through the points PCP′ draw a circle of right ascension, cutting the equator EQ

^{*} Should either of the oblique angles, or hypotenuse, be one of the parts, then, instead of the word in the formula, use that derived from its complement, that is, for sine read cosine, for cosine read sine, and so on.

⁺ For the explanation of these terms the usual treatises on astronomy may be consulted. To those acquainted with the use of the globes, correct ideas relative to these problems may be readily obtained. It may be added, that the sun's longitude, and the obliquity of the celiptic, are computed from astronomical tables.

at right-angles in B, then will AB be the right ascension, BC the declination, and BCA the remaining angle or angle of position, as it is sometimes called, which, in astronomy, is seldom of much use.

- Calculation.—In the triangle ABC there are given AC=40° 32′ 12″, and the angle BAC=23° 27′ 40″, to find BC, the distance of the sun from the equator EQ, or the declination, as it is usually called. Now, since in spherical trigonometry the sines of the sides are proportional to the sines of their opposite angles,

Therefore.

| As sine ABC or radius | 100 10 11 | 10.000000 |
|--|-------------------------------|--|
| Is to sine BAC 23° 27′ 40″ | or Seal and the Real Property | 9.600021 |
| So is sine AC 40 32 12 | of the other works are my | 9.812870 |
| man and transfers of the street and of the | crown boundles on | The state of the s |

To sine BC 14 59 47

9.412891

9.894587

To find AB we may employ the method of the circular parts. In the triangle ABC are given AC and the angle BAC, to find AB the right ascension. Now, since the side CA, the angle CAB, and the side AB are all connected, that which stands in the middle or the angle A is called the middle part, and the sides AC and AB adjacent to it on each side are called the adjacent parts.*

Consequently $R \times \cos$. $A = \cot$. $AC \times \tan$. AB; and resolving this into an analogy, as is frequently done in this country, we have,

| As cot. AC | 40° 32′ 12″ | William Tolling the March | 10.067939 |
|--------------|-------------|---------------------------|-----------|
| Is to radius | | | 10.000000 |
| So is cos. A | 23 27 40 | 177901 | 9.962526 |

To tan. AB. 2^h 32^m 27^s.3 9.894587 or, since cot.; R:: R; tan., or tan.=\frac{1}{2} to radius unity (\s 35, page 11.)

| THE RESERVE OF THE PARTY OF THE | STATE OF THE RESERVE TO A STATE OF THE RESER | cot. | |
|--|--|--------------------|--|
| As radius | 10 - 10 × 10 × 10 | Charles with to an | 10.000000 |
| Is to tan. AC | 40° 32′ 12″ | | 9.932061 |
| So is cos. A | 23 27 40 | Combact Committee | 9.962526 |
| | The second second | | The state of the s |

2h 32m 27s.3

To tan. AB the same as before.

To those acquainted with algebra, it is better, after the manner of foreign mathematicians, still to retain the form of an equation thus:

tan. $AB = \frac{A \times \cos A}{\cot AC} = \cos A \times \tan AC$, the radius being represented by unity; in which case ten must be rejected in the index.

ım tan. AB 2^h 32^m 27.^s3 . . . 9.894587

To find the angle ACB, since the parts under consideration are still all connected, AC standing in the middle is assumed as the middle part, and the angles A and C are the adjacent parts, whence

It may be remarked, that if the parts are all connected, that which stands in the middle is called the middle part, and the other two are called the adjacent parts. If two only are connected, and one stands by itself, then this is called the middle part, and the other two are called the opposite parts.

cos. AC $R \times \cos$. $AC = \cot$. $A \times \cot$. C, and \cot . $C = \frac{\cos AC}{\cot A} = \cos AC \times \tan$.

A, hence

To log. cos. AC 40° 32′ 12″ Add log. tan. A 23 27 40

9.880808 9.637496

Sum = $\cot C$ 71 44 42 .2 9.518304

18 15 17 .8, is called properly the angle of posi-Or the comp. tion, sometimes useful in computing the parallaxes in solar eclipses and occultations of the fixed stars and planets by the moon.

. By assuming different parts of the triangle ABC for the middle

part, may be resolved the following

Examples for Exercise.

1. On the first of June, 1827, at noon on the meridian of Greenwich, the sun's longitude will be 2° 10° 9′ 45", the obliquity of the ecliptic 23° 27′ 36″; required the right ascension and declination?

Ans.—R. A. 4^h 34^m 7^s.6; Dec. 21° 59′ 34″ N.

2. August 12th, 1827, the obliquity of the ecliptic being 23° 27' 36", the sun's right ascension will be 9h 25m 29.3; required his longitude and declination?

Ans.-Longitude 4º 18° 56' 28", Dec. 15° 9' 32" S.

3. On the 10th November, 1828, on the meridian of Greenwich, the sun's right ascension will be 15h 2m 32s.7, and declination 17° 14' 12" S.; required the sun's longitude and the obliquity of the ecliptic?

Ans. Longitude 7° 18° 6′ 7", and obliquity of the ecliptic 23°

27' 34".

4. On the 2d of March, 1828, when the sun's declination was 7° 5′ 18" S., and obliquity of the ecliptic 23° 27′ 35"; required his longitude and right ascension?

Ans.—Longitude 11° 11° 56′ 34″; R. A. 22h 53m 24°.

PROBLEM II.

When the celestial object is not upon the ecliptic, as the moon, or the planets, and some of the fixed stars, the right ascension and declination are found by the solution of two right-angled triangles.

1. On the 17th of January, 1826, at noon, on the meridian of Greenwich, the moon's longitude was 1° 11° 5′ 14", and her latitude 2º 34' 3" N.; required her right ascension and declination, the obliquity of the ecliptic being 23° 27′ 40″? To resolve this example it is necessary to employ two right-angled spherical triangles.

In the foregoing figure, the longitude of the moon or any star S, is AD, the latitude DS, the obliquity of the ecliptic BAC, the right ascension AB and declination BS. Now, supposing a line drawn from A to S, there would be formed the right-angled spherical triangle ADS, right-angled at D, of which AD and DS are given to find the angle DAS and the side AS. If the position S of the star is without the ecliptic, then to the obliquity of the ecliptic BAC, add the angle DAS, the sum will be the angle BAS; but if S is within the ecliptic, that is between it and the equator, subtract the angle DAS from the obliquity BAC, and the remainder will be the angle BAS. Since the side AS, and the angle BAS, are now known, AB the right ascension, and BS the declination, may be found.

Calculation.—By the rule of the circular parts, first AD and DS

are given to find AS, and since the last is separated from the two first by the oblique angles, it will be the middle part, and AD and DS are the opposite parts; therefore, $R \times \cos$. AS = \cos . DS $\times \cos$. AD, or \cos . AS = \cos . DS $\times \cos$. AD to radius unity.

Log. cos. AS 1-41 9-11 9.876768

Again, to find DAS, since the right angle does not separate the parts, DA standing in the middle is called the middle part, and the side DS and the angle DAS are the adjacent parts, hence R×sin.

 $DA = \tan DS \times \cot DAS$, and, therefore, $\cot DAS = \frac{\sin DA}{\tan DS} =$

sin. DA × cot. DS, consequently

To log. cot. DS 2° 34′ 3″

Add log. sine DA 41 5 14 9.817634

Sum=log. cot. DAS 3 54 14 11.165956

Sum=log. cot. DAS 3 54 14 To this add Ob. Ec. 23 27 40

Sum = angle BAS 27 21 54

Hence AS and BAS are now known, to find AB and BS.

First to find AB. In this case the parts are connected; therefore BAS is the middle part, and AB and AS are the adjacent parts, whence

 $R \times \cos$. BAS = tan. AB × cot. AS, or tan. AB = $\frac{\cos$. BAS cot. AS, and

tan. AB = cos. BAS × tan. AS, hence
To log. cos. BAS 27° 21′ 54″
Add log. tan. AS 41 9 11 9.941505

Sum = log. tan. AB 37° 49′ 5″ 9.889965 Or in time R. A. 2° 31° 16°.3

To find BS, the angle BAS and side AS are connected, and BS is disjoined, whence $R \times \sin BS = \sin AS \times \sin BAS$, or since the sines of the sides are proportional to the sines of their opposite angles.

To sine Dec. BS 17 36 26 N. 9.480708

The foregoing method is general and applicable to any part of the ecliptic, provided proper attention be paid to the situation of the celestial object with respect to the ecliptic and equator. As this problem and its converse is of frequent occurrence in practical astronomy, rules and formulæ, and even tables, have been formed for the purpose of facilitating the computations. The following rules, given by the late Dr Maskelyne, will be found very convenient for this purpose.

PROBLEM II.

Given the right ascension, the declination, and the obliquity of the ecliptic, to find the longitude and latitude.

Let RA denote the right ascension, O the obliquity of the ecliptic, and D the declination:

Tan. D-sin. RA = tan. A, North or South as the declination is. Call O in the first six signs of RA South or S. and in the last six signs North or N.

Then A+O=B, regard being had to the algebraic signs,

A being less than 45°, and using logarithms. Sec. A+cos. B+tan. RA=tan. lon. of the same kind as RA, unless B be more than 90°, when the quantity found of the same kind as RA must be taken from twelve signs.

A being more than 45°.

Tan. $A + \csc A + \cos B + \tan RA = \tan \cos \theta$ for the same kind as RA, unless B be more than 90°, when the quantity found of the same kind as RA must be taken from twelve signs.

Lon. being nearer III. and IX. signs than O and VI. signs.

Sin. lon. + tan. B = tan. lat. of the same name as B. 15 (6.5 (Lon. nearer O and VI. signs, than III. and IX. signs.

Tan. Lon. $+\cos$ lon. $+\tan$ B = \tan lat. of the same name as B.

EXAMPLE.

On Monday the 12th of June, 1826, the moon's R. A at noon, was found by observation to be 10h 39m 31s and her declination 2° 51' 58" N.; required her longitude and latitude?

 $D = 2^{\circ} 51' 58'' \text{ N. tan. } 8.699533$

RA=10^h 30^m 31^s sine 9.536560 tan. 9.563908

8° 16′ 50″ N. tan. 9.162973 sec. 0.004551 O 23 27 40 S.

9.984575 tan. 9.433497 S. cos.

9.553034 sine 9.526946 Lon. 160 20 17 tan.

tan. 8.960443

PROBLEM III.

Given the longitude and latitude of a celestial object, and the obliquity of the ecliptic; to find the right ascension and declination.

Tan. Lat.—sine Lon.—tan. A, North or South as the latitude is. Call O North in the six first signs, and South in the six last signs.

A + O = B, as before.

A being less than 45°, sec. $A + \cos B + \tan \log C = \tan RA$ of the same kind as the longitude, unless B be more than 90°, when the quantity found of the same kind as the longitude must be subtracted from twelve signs.

A being more than 45°, tan. A + cosecant A + cos. B + tan. lon. = tan. RA of the same kind as the longitude, unless B be more than 90°, when the quantity found of the same kind as the longitude must be subtracted from twelve signs.

If RA be nearer III. signs and IX. signs, than O and VI. signs,

sine RA + tan. B = tan. Dec. of the same name as B.

And RA being nearer O and VI. signs, than III. and IX. signs, tan. RA + cos. RA + tan. B = tan. Dec. of the same name as B.*

gitude, or RA, fall upon PP', or pp', &c.

See Dr Abram Robertson's paper in the Phil. Trans. for 1816, page 138, which for

want of room cannot be given here.

These rules may, in general, be depended upon, except in peculiar circumstances. which a consideration of the figure will enable the computer to correct, as when the lon-

Example.

On the 1st of January, 1820, the mean longitude of the Star Fomalhaut was 11° 1° 19′ 34″, the mean latitude 21° 6′ 45″ S.; required the right ascension and declination, the obliquity of the ecliptic being 23° 27′ 46"?

Lat. 21° 6' 45" S. tan. 9.586721

Lon. 331 19 34 sine 9.681082 tan. 9.737901

26 S. tan. 9.905639 sec. 0.108420 A = 3849 $0 = 23 \ 27 \ 46$

S. cosine 9.667498 tan. 10.279585 B = 6217 12

9.513819 sine 9.491831 RA=341 55 14 tangent

Dec. 30 34 21

9.771416 tan.

Examples for Exercise.

1. The mean longitude of a Arietis, on the 1st January, 1820, was 1° 5° 8′ 48″, and mean latitude 9° 57′ 34″ N. when the obliquity of the ecliptic was 23° 27' 46"; what was the right ascension and declination?

Ans.—R. A. 1^h 57^m 3^s; Dec. 22° 36′ 24″ N.

2. Required the right ascension and declination of Pollux, when the longitude was 3° 20° 43′ 58", the latitude 6° 40′ 17" N. the obliquity of the ecliptic being 23° 27′ 46″?

Ans.—R. A. 7° 34° 17.5°; declination 28° 27′ 8″ N.

3. The mean longitude of Spica Virginis is 6° 21° 19′ 50″, latitude 2° 2' 24" S. and the obliquity of the ecliptic 23° 27' 46"; required the right ascension and declination?

Ans.—R. A. 13h 15m 43.5s; declination 10° 13' 4" S.

4. The mean right ascension of a Aquilæ is 19h 42m, and declination 8° 24' 4" N. the obliquity of the ecliptic being 23° 27' 46"; required the longitude and latitude?

Ans.—Longitude 9° 29° 14′ 14′, Latitude 29° 18′ 36″ N.

- 5. Required the longitude and latitude of α Pegasi, of which the right ascension is 22h 55m 48, declination 14° 14′ 21″, the obliquity of the ecliptic being 23° 27′ 46"?

Ans.—Longitude 11° 20° 58′ 47″, Latitude 19° 24′ 36″ N.

PROBLEM IV.

Given the latitude of the place, and the sun's declination, to find

his altitude and azimuth at 6 o'clock.

1. At Edinburgh, in latitude 55° 57' 20" N. on the 21st of June, 1826, the sun's declination was 23° 27′ 36" N.; required his altitude and azimuth at 6 o'clock in the morning or evening, his declination being supposed to remain the same.

Construction.—Describe the primitive HPON on the plane of the

meridian. Let HO represent the horizon, ZN the prime vertical at right angles to the former. Make OP, from a scale of chords equal to the latitude of the place, North in the present instance; draw PP', the six o'clock hour circle in this case, and at right angles to it draw the equator EQ; describe the small circle nm at the distance of 23° 27′ 36" from the equator, representing the parallel of declination, and it will cut the six



o'clock hour circle PP' in F, the sun's place at the given time.

Through Z, F, and N, describe the azimuth circle ZFN cutting the horizon in D, then FD is the altitude, FZ the zenith distance, and the angle FZP, or its measure, the arc DO, is the azimuth; consequently, the things given and required fall in either of the triangles FZP, or FDA, which are supplemental to each other. For, since OP is the latitude, PZ is the colatitude, AF is the declination; consequently, FP is the polar distance, DF being the altitude, FZ must be the zenith distance.

Calculation.—In the right-angled spherical triangle FPZ, rightangled at P, FP and PZ are given, to find the angle FZP and FZ; or in the triangle ADF, right-angled at D, there are given the angle FAD, equal to the latitude of the place, and AF, the sun's declina-

tion, to find DF, the altitude, and the side AD the azimuth.

By the rule of the circular parts FP, PZ, and PZF, are all connected, therefore PZ is the middle part, and PZF and PF are the adjacent parts, where

> $R \times \text{sine } ZP = \text{tan. } PF \times \text{cos. } PZF$, or $R \times \cos$ lat. = \cos dec. $\times \cos$ azimuth, therefore $\frac{\cos \cdot \text{lat.}}{\cos \cdot \text{dec.}} = \cos \cdot \text{lat.} \times \tan \cdot \text{dec.}$ cos. azimuth =

cos. dec. 9.748061 To log. cos. lat. Add log. tan. dec. 23 27 36

Sum = \log . cos. az. 76 20 38 9.385533 Again, to find FZ the coaltitude, the same things being given, $R \times \cos$. $FZ = \cos$. $ZP \times \cos$. FP, or sine alt. $= \sin e$ lat. $\times \sin e$ dec.

To log. sine lat. 55° 57′ 20″ Add log. sine dec. 23 27 36 9.918347 9.600002

Sum $= \log$ sine alt. 19 15 40 9.518349

PROBLEM V.

Given the latitude of the place, and the sun's declination, to find the altitude and hour when the sun is due East or West.

EXAMPLE.

At Edinburgh, on the 21st June, 1826, what was the sun's altitude and hour when due East or West, the declination being 23°

27' 36" N.

In the last figure, let ZAN meet the parallel nm in K, and suppose a circle to be drawn through the points PKP, forming the triangle ZKP, right-angled at Z, then ZK is the coaltitude, and ZPK the hour from noon; hence

 $R \times \cos$. $PK = \cos$. $ZP \times \cos$. ZK, or $\cos ZK = \frac{\cos PK}{C}$ $\frac{1}{\cos ZP} = \cos PK \times \sec PO$, or sine alt. = sine dec. \times sec. lat. Dec. 23° 27′ 36″ sine 9.600002 Lat. 55 57 20 sec. 0.081653

Alt. 28 42 55 sine 9.681655 $R \times \cos$. $ZPK = \tan ZP \times \cos PK$, or $\cos T = \cos \cdot \text{lat.} \times \tan \cdot \text{dec.}$

Dec. 23 27 36 tan. 9.637472

Time 4h 51m 48s cos. 9.467186

From noon, that is, at 7^h 8^m 12^s A. M., and 4^h 51^m 48^s P. M.

This problem is of considerable utility to the navigator and practical astronomer, for the purpose of determining time accurately when an altitude instrument is used. As the change of altitude, on which the accuracy of the determination of the time depends, is quickest when the object is on the prime vertical, the most proper time for observing an altitude for that purpose is, therefore, when the object is due East or West, as any small error in the observation has then the least possible effect on the time. Other errors are also in this case in a great degree avoided, or at least considerably lessened, particularly that arising from any small error in the estimated latitude at the time of observation. To facilitate its application, tables, corresponding to the latitude and declination (which must be of the same name with the latitude), have been given in books on Nautical Astronomy, such as those of Mendoza Rios, Mackay, and Lax. When the latitude and declination are of different names, the altitude must be as near the horizon as is consistent with accuracy, so far as depends upon the uncertainty of the horizontal refraction. Altitudes under 5° should not be used when great accuracy is required.

PROBLEM VI.

Given the latitude of the place and the sun's declination, required his amplitude and ascensional difference.*

At Edinburgh, on the 21st of June, 1826, from the data given, on

what point, and at what time, did the sun rise and set? I ha

In the triangle ABC, in the last figure, there are given the angle BAC, equal to the colatitude, and BC the sun's declination; to find AC and AB.

 $R \times sine BC = sine AC \times sine BAC$, or sine $AC = \frac{sine BC}{sine BAC} = sine BC \times cosec$. BAC.

BC, or dec. 23° 27′ 36″ N. sine 9.600002

Latitude, 55 57 20 sec. 10.251939

AC, 45 19 33 sine 9.851941
CO, 44 40 27, in which case AC is the amplitude reckoned from the East or West, to the North and South, according to the name of the declination, and CO is that reckoned from the meridian, or from the North or South, according to the name of the declination.

Again, in the same triangle AB is the ascensional difference, and $R \times sine AB = cot. BAC \times tan. BC$, or sine $AB = tan. lat. \times tan. dec.$

Lat. 55° 57' 20" tangent, 10.170286 Dec. 23 27 36 tangent, 9.637472

A. D. 2^h 39^m 52^s sine 9.807758

-8 39 52 = time of setting.
3 20 8 = time of rising, the latitude and de-

^{*} By the ascensional difference is meant the time before or after 6 o'clock the sun rises or sets. By this problem, therefore, the lengths of the day and night are determined, and the variation of the mariner's compass.

clination being of the same name, or if instead of sine we read cosine, then we would get the time of rising if the latitude and declination are of the same name, and the time of setting if of different names. This, however, is only the approximate time, as no allowance is made for the effects of a change of declination, the horizontal refraction and parallax in the case of the sun and planets. For these see Mackay on the longitude, or they may be found by the following rule. First, let the approximate time be found. To this time let the declination of the object be reduced. With it find the ascensional difference as formerly. Now, find the sum and difference of the natural cosine of the reduced declination and natural sine of the latitude, which may be carried to four places of figures only, these being sufficiently accurate for this purpose, and take half the sum of the logarithms of these quantities, to which add the constant logarithm 7.1761, and the proportional logarithm of the difference between the horizontal parallax and the sum of the horizontal refraction and dip of the horizon, the sum, rejecting 10 in the index, will be the proportional logarithm of the correction which is to be subtracted from the time of rising, or added to the time of setting, if the horizontal parallax is less than the sum of horizontal refraction and dip, otherwise the correction must be added in the first case, and subtracted in the second.

EXAMPLE.

Required the time of rising and setting of the sun on the 1st of April, 1826, in latitude 33° 42′ N., and longitude 16° 20′ W. the height of the eye, above the sea, being 28 feet.

Dec. 4° 28' N. cos. 9969 Lat. 33 42 N. sine 5548

- 3^m 10^s P. L. 1.7540

Sum 15517 log. 4.1908

The correction to be subtracted from the time of rising, or added to the time of setting. As the moon's horizontal parallax is in general greater than the effects of dip and refraction, the correction thus obtained would have been applied with a contrary sign. This method of determining time may sometimes be of use when a better cannot be obtained, and in the case of the sun or moon, a mean of the times of appearance of the upper and lower limb may be taken.*

Solution of Oblique-Angled Spherical Triangles.

The different cases of oblique-angled spherical triangles may be solved by the following theorems:—

^{*} To find the rising and setting of a star or planet, the transit over the meridian must be first computed as follows:—From R. A. of the star subtract that of the sun for noon, the remainder is the approximate time of transit. Reduce the R. A. of both to this time and the given longitude, and subtract as before, and the remainder will be the true time of transit, which, properly applied to the semidiurnal arc, will give, when corrected for dip, &c., the true time of rising or setting.

THEOREM I.

In every spherical triangle the sines of the sides are proportional to the sines of the angles opposite to them,* Or, sin. AB: sin. AC::sin. C: sin. B



THEOREM II.

In oblique-angled spherical triangles a perpendicular arc being drawn from any of the angles upon the opposite side, the cosines of the angles at the base are proportional to the sines of the segments of the vertical angle, or cos. B: cos. C:: sin. BAD: sin. CAD.

THEOREM III.

The same things remaining, the cosines of the sides are proportional to the cosines of the segments of the base, or cos. AB: cos. AC:: cos. BD:: cos. CD.

THEOREM IV.

The same construction remaining, the sines of the segments of the base are reciprocally proportional to the tangents of the angles at the base, or sin. BD: sin. CD::tan. C:tan. B.

THEOREM V.

The same construction remaining, the cosines of the segments of the vertical angles are reciprocally proportional to the tangents of the sides, or cos. BAD: cos. CAD::tan. AC:tan. AB.

THEOREM VI.

If, from an angle of a spherical triangle, there be drawn a perpendicular to the opposite side or base, the tangent of half the sum of the segments of the base is to the tangent of half the sum of the two sides of the triangle, as the tangent of half the difference of those sides to the tangent of half the difference of the segments of the base, or tan. $\frac{1}{2}$ (BD+CD): tan. $\frac{1}{2}$ (AB+BC):: tan. $\frac{1}{2}$ (AB σ AC): tan. $\frac{1}{2}$ (BD σ CD).

When the three sides or the three angles are not the given parts of the triangle, to have sufficient data for the solution of the problem, the perpendicular must be so drawn, that two of the given things in the oblique-angled triangle may be known in one of the resulting right-angled triangles.

THEOREM VII.

If a perpendicular be drawn from an angle of a spherical triangle, to the opposite side or base, the sine of the sum of the angles at the base is to the sine of their difference, as the tangent of half the base is to the tangent of half the difference of its segments: And the sine of the sum of the two sides is to the sine of their difference, as the cotangent of half the angle contained by the sides is to the tangent

^{*} See Playfair's Geometry, article Spherical Trigonometry, Prop. XXIV., or Legendre's Geometry, article LXXVI., and the following in order.

of half the difference of the angles which the same sides make with the perpendicular, or sin. (B+C): sin. (B \sim C): tan. \frac{1}{2} BC: tan. \frac{1}{2} (BD o CD). And sin. (AB + AC): sin. (AB o AC): cot. 1 A: tan. 2 (BAD of CAD), whiper of the so so his will be the enclosed

THEOREM VIII.

The sine of half the sum of any two angles of a spherical triangle, is to the sine of half their difference, as the tangent of half the side adjacent to these angles, is to the tangent of half the difference of the sides opposite to them. And the cosine of half the sum of the same angles, is to the cosine of half their difference, as the tangent of half the side adjacent to them, is to the tangent of half the sum of the sides opposite, or $\sin \frac{1}{2} (A + B) : \sin \frac{1}{2} (A \cap B) : \tan \frac{1}{2} AB : \tan$ $\frac{1}{2}$ (BC \circ AC). And $\cos \frac{1}{2}$ (A+B): $\cos \frac{1}{2}$ (A \circ B): $\tan \frac{1}{2}$ AB: $\tan \frac{1}{2}$ (BC \circ AC).

Corollary.—The sine of half the sum of any two sides of a spherical triangle, is to the sine of half their difference, as the cotangent of half the angle contained between them, is to the tangent of half the difference of the angles opposite to them: And the cosine of half the sum of these sides is to the cosine of half their difference, as the cotangent of half the angle contained between them, is to the tangent of half the sum of the angles opposite to them, tor sin. 1/2 (AB+AC): $\sin \frac{1}{2}$ $(AB \circ BC)$: $\cot \frac{1}{2}A$: $\tan \frac{1}{2}$ $(B \circ C)$ $\cos \frac{1}{2}$ $(AB \times AC)$: $\cos \frac{1}{2}$ $(AB \circ BC)$: $\cot \frac{1}{2}A$: $\tan \frac{1}{2}$ (B+C).

THEOREM IX.

It will be sometimes more easy in practice to compute an angle from the three given sides by the following formulæ and rules, than by any of those already given: thus, suppose A, B, C, are the angles as before, and a, b, c, the sides opposite; then

as before, and
$$a, b, c$$
, the sides opposite; then

Sin. $\frac{1}{2} A = \sqrt{\frac{\sin \left\{\frac{1}{2} (a+b+c)-c\right\} \cdot \sin \left\{\frac{1}{2} (a+b+c)-b\right\}}{\sin b \sin c}}$ (1)

Cos. $\frac{1}{2} A = \sqrt{\frac{\sin \left(\frac{1}{2} (a+b+c) \cdot \sin \left\{\frac{1}{2} (a+b+c)-a\right\} \cdot \sin \left\{\frac{1}{2} (a+b+c)-c\right\}}{\sin b \sin c}}$ (2)

Tan. $\frac{1}{2} A = \sqrt{\frac{\sin \left(\frac{1}{2} (a+b+c)-b\right\} \cdot \sin \left\{\frac{1}{2} (a+b+c)-c\right\}}{\sin \left(\frac{1}{2} (a+b+c)-a\right)}}$ (3)

Cos.
$$\frac{1}{2}A = \sqrt{\frac{\sin \frac{1}{2}(a+b+c)\sin \frac{1}{2}(a+b+c)-a}{\sin b \sin c}}$$
 (2)

Tan.
$$\frac{1}{2}A = \sqrt{\frac{\sin \left\{ \frac{1}{2} (a+b+c)-b \right\} \cdot \sin \left\{ \frac{1}{2} (a+b+c)-c \right\} \cdot \sin \left\{ \frac{1}{2} (a+b+c) \right\}}$$
 (3)

Rules in Words.

I, From half the sum of the three sides subtract each of the two sides which contain the required angle. Then to the cosecants of the sides which contain the required angle add the sines of the two remainders; half the sum of these foregoing logarithms will be the sine of half the required angle.

II. Find the difference between half the sum of the three sides, and the side opposite the required angle. Then to the cosecants of the two containing sides add the sines of the half sum and difference; half the sum of these four logarithms will be the cosine of half the required angle.

III. To the cosecant of half the sum of the three sides add the

^{*} This theorem forms Proposition XXX. in Playfair's Spherical Trigonometry, where it is partly erroneous. It is also given in Mr J. Wallace's edition of Brown's Logarithmic Tables. Erroneous rules and impossible triangles should always, if possible, be avoided.—See the French Edition of Cagnoli's Trigonometry, § 1038, 1108 and + Legendre, & LXXXIII.

cosecant of half that sum diminished by the side opposite the required angle, and the sines of the same half sum diminished by each of the sides containing the required angle; half the sum of these four logarithms will be the tangent of half the required angle. See remarks annexed to Case III., Plane Trigonometry.

THEOREM X.

Given two sides and the contained angle, to find the side opposite

that angle.

To twice the sine of half the contained angle, add the sines of the two containing sides, and from half the sum of these three logarithms subtract the sine of half the difference of the sides; the remainder will be the tangent of an arc, the sine of which being subtracted from the half sum of the three logarithms already found, leaves the *sine* of half the required side.

THEOREM XI.

The two sides and contained angle being given, the third side may

be found in the following manner.

To twice the sine of half the contained angle add the sines of the two containing sides; half the sum of these three logarithms, after rejecting 20 in the index, will be the cosine of an arc. Also find half the difference of the two containing sides.

To the sine of the sum of these two last arcs add the sine of their difference; half the sum of these two logarithms will be the cosine of

half the required side.

It may be remarked, that when the side is not greater than 90°, theorem X. may be used; when it is greater than 90°, theorem XI. may be employed when great accuracy is required.

THEOREM XII.

The three angles of a spherical triangle being given, to find the sides.

From half the sum of the three angles subtract each of the angles next the required side, then to the cosecants of the adjacent angles add the cosines of the two remainders; half the sum of these four logarithms will be the cosine of half the required side.

THEOREM XIII.

The same things being given; from half the sum of the three angles subtract the angle opposite the required side, then to the cosecants of the adjacent angles add the cosine of half the sum and the cosine of the difference; half the sum of these four logarithms will be the cosine of half the required side.

Either of these theorems may be employed, which will give the

more accurate result.

Having stated the theorems on which the solutions in oblique-angled spherical triangles depend, it is necessary to illustrate them by examples which will chiefly consist of those applicable to the usual cases that occur in practical astronomy and navigation.

PROBLEM I.

Given the latitude of the place, the sun's altitude and declination, to find the time and the azimuth.

At the observatory of Edinburgh, on the Calton-hill, in latitude 55° 57′ 21″ N., on the third of June, 1826, the following observa-

tions of the sun's lower limb were taken in the morning; required the time and azimuth, the barometer being at 29.56 in., and the thermometer at 64° F.?

| thermometer at 04° r.r | |
|--|--|
| Times by Watch. | Altitudes. |
| $7^{\text{h}} \cdot 1^{\text{m}} \cdot 20^{\text{s}}$ | 26° 51′ 20″ |
| 2 18 | 26 59 30 |
| 3 25 | 27 7 15 |
| 4 30 | 27 15 40 |
| COLUMN TO A STATE OF THE PARTY | |
| 5 27 | 27 23 45 |
| | OF OF OA |
| 5 17 0 | 35 37 30 |
| 5 c 1 | (Annual Company of State Company of Stat |
| Means. 7 3 24 | 27 7 30 Lower limb. |
| Or observed Z.D. | 62 52 30 |
| Z. D. 62° 52′.5 log. 8 0 . | . 2.03692 |
| Thermometer 64° F. log. | 9.98751 |
| Barometer 29.56 | 9.99358 |
| Thermometer 64.0 F. | |
| Thermometer 04.0 F. | 9.99940 |
| 7.400 7.4 | 0.07547 |
| $r = 106''.5 = 1'.46''.5 \log.$ | 2.01741 |
| Z. dist. $= 62^{\circ} 52' 30''$ | |
| Refraction + 1 46 .5 | World to the |
| The control of the co | |
| True Z. D. 62 54 16 .5 of the lower | limb. |
| Semidiameter — 15 47 .5 | Page on Strong |
| Demidiantetel — 10 47 .0 | |
| Thurs 77 D 60 20 00 of the contra | The media |
| True Z.D. 62 38 29 of the centre | |
| Approximate time, June 2d, 19h 4h | |
| Longitude in time add + 12 | West. |
| WHAT HE WAS A SECOND OF THE SE | |
| Estimated Greenwich time 19 16 | D. L. 0.09503 |
| Daily variation of dec. 7' 42" | P. L. 1.36878 |
| | Open that make by him to some |
| Prop. part. to 17 ^h 18 ^m + 6 11 | P. L. 1.46381 |
| | |
| Dec., June 2d, 22° 9 38 N. | - 3 May 27 mg 28 75 |
| 70 1 1 1 11 11 11 00 17 10 17 | . The last of the same of |
| Reduced declination 22 15 49 N. | |
| Polar distance 67 44 11 | |

1. Now in the figure, (page 70), there are given OP the latitude, and consequently ZP the colatitude, PK the polar distance, and ZK the zenith distance, the place of the sun being K near the prime vertical, as being most advantageous to determine the time with accuracy, or the three sides of the triangle KPL; to find the angle ZPK the time, and the angle PZK the azimuth from the southern meridian PEP'. This, therefore, is solved by means of theorem IX.

| √ 0 . ₹ € | Intito | DUCII | O.Li. | |
|--|---|---------------|------------------------------------|--|
| Now the latitude being | 550 571.01 | " tha | coletitude is 3 | 10 0/ 20// |
| | 104 00 6 | , me | colatitude is o | i 4 00 |
| Z. D. | 164 38 2 | | THE LABOUR DESIGNATION . | DESTRUCT |
| Colatitude | 34 2 | 39 | cosec | 0.251942 |
| Polar dist. | 67 44 | 11 | cosec | 0.033647 |
| 1 Old disc. | 0, | | | 0.00001 |
| | 104 '05 | 10 | | - 4 |
| Sum | 164 35 | 19 | . 11 | |
| 2 6 6 6 | - | | 100 | 10 |
| Half | 82 12 | 39 | 100 | A- 1 |
| First rem. | | | sine . | 9.872208 |
| | | | | |
| Second rem. | 14 28 | 20 8 | sine | 9.397850 |
| 000 7 100 | | | - 0 | |
| | | | | 19.555647 |
| e du redissionale de como reg | 2h 27 | m 9s | | Com 445 1, 10 47 |
| of the fact of the fact of | , | | sine | 0 777001 |
| 1 = 11 ho | | 4 | | 9.777824 |
| () (| | 10 | 44.0042.03 | .3.7 5 |
| Time from noon 3d | 4 54 | 42 | | umommet 3" |
| 1 | 12 | | | F arthre |
| - 8 - 4 | | ** | | |
| | - p- | 10 | . T (V TU Va) | III MITTLE A |
| App. time, A. M. | 7 5 | 18 | | |
| Time by watch | 7 3 | 24 | 1071411- | di Witan |
| | | - | S. P. D. S. W. China. | 1.10.10 |
| Watch slow | 1 | 54 | for apparent t | ima iii iii |
| waten slow | 1 | O'T | ioi apparent t | IIIC to 1315 F |
| | | - | -1-3 | |
| Again app. time | 7 5 | 18 | 7/1 14 Tel | The B. J. |
| Equation of time | _ 2 | 23 | | an-Abbured |
| Edduction of prints | | | And the same of the | -21-1112222 |
| 70.77 | 7 0 | | d the discovery as seeded deposing | |
| Mean time | 7 2 | 55 | 12 13 11 | Trung. D. |
| Time by watch | 7 3 | 24 | grant, apply of | VIII CONTROL IN |
| 1 | 0.0 | | | Lowerston |
| Watch fast | | 20 for | mean time. | THE PROPERTY |
| | h ou tho | | | W being that |
| 2. To find the azimut | n or the a | ingle ix | zir, the point | ix being that |
| in which the circles n m | | cut eac | ch other, there | are given the |
| three sides of the triang | le KPZ_ | an apparatual | | To. |
| KP, or polar dist. | 670 11 | 11" | est Class | Prop. p. Co. |
| PZ, or colatitude | 34 2 | 30 | cosec. | 0.251942 |
| 1 Zi, or colatitude | 62 38 | 00 | Cosec. | |
| ZK, or Z. dist. | 02_30 | 29_ | cosec. | 0.051515 |
| | W 12 0 | () | Sullering | Reduced |
| Sum | 164 25 | .19 | | Polar dire |
| | | | AND STORMAN INC. | |
| Half Santo | 00 10 | '20 | cino | 9.995974 |
| Tan 1 2 1 1 2 10 . II | 34 00 | 00 | Sille | |
| Difference | 9 14 ,28 | 28 5 | sine | |
| all the embreday or | sec. 202 | of the | my paried on a | The state of the s |
| TEL: p mal the | 1 1 1 1 1 1 1 2 1 1 2 1 2 1 2 1 2 1 2 1 | . 6 1 : | sound hard have - | 19.697281 |
| 2 2 2 2 | 2 2 | 1 123 | Sugar men and O | |
| de ne d'équéta in la escut que dantes au | All All 9 H | 13 | Ico. suct of | 0.040640 |
| الم و الدول الله المالية المالية المالية المالية | 40 | HILL T | cos. | 9.040040 |
| | | 2 | 7 | The street of |
| | | | | |
| | N. 90 15 | 22 | Ε. | |
| | 44 52 | | sin. or | |
| | 11 02 | | SIII. OI' | |
| | | 2 | | |
| | | | | |
| | ~ ~ ~ 4 4 | | man g | |

S. 89 44 38 E. or reckoned from the South in north latitude, or from the North in south latitude.

This problem is very useful in navigation, for the purpose of finding the variation of the compass, which is the difference between the true and observed amplitude or azimuth.

To determine this, let the observer be supposed to look directly from the centre of the card towards the point representing the true azimuth; then if the observed azimuth is to the *left* of the true azimuth, the variation is *easterly*, but if to the right it is westerly to the amount of the difference between them.

Thus let the true azimuth be S. 89° 44′ 38″ E. Observed 65 24 38

Variation 24 20 0 West. Or about 21 points westerly.

These results for time and variation have been deduced strictly from the solution of the spherical triangle formed by the data, but they may be found more readily by rules derived from it, as may be seen in various books on navigation and nautical astronomy.

When tables which have proportional parts annexed to them are used, the following method may be advantageously employed

for determining the time.

· 上下ののののとしているのののの

Rule.—When the latitude of the place and the declination are of the same name, let their difference, but, if of contrary names, let their sum, be taken. Under this difference or sum place the zenith distance, and let the half sum and half difference of these be taken; then add together the secant of the latitude, the secant of the declination, the sine of the half sum, and the sine of the half difference; half the sum of these four logarithms will be the sine of half the hour angle or time from noon, from which the apparent and mean time may be obtained as formerly.

| 128 | | | 12 | | 65 |
|------------------|-------------|--------------|------------|-------------|---|
| Latitude | | | | | 0.251877 |
| Declination | 22 15 4 | 19 N. | secant | | 0.033605 42 |
| Difference | 33 41 3 | 2 | 1 4 9 5 | | 42 |
| Zenith dist. | | | Pacana | | |
| Jan 1 | | - | | | 1 |
| Sum | 96 20 | 1 half 48 | ° 10′. 0½″ | ansine i | 9.872208 |
| Difference | 28 56 5 | 7 half 14 | 28 281 | iesine | 9.397821 |
| and william | supple from | arrive mile; | C -13 | 1 AUA (100) | 233 |
| W. W. W. W. | | | | | 19.555652 |
| Love Ser 33 | | | | | 10.0000021 |
| The Buckey | | | | | 9.777826 |
| | | | | | 681 |
| | | | | | la oralici |
| and the make | 2 27 | | | | 45 |
| | | | | | 43 |
| district Comment | | | | | June 9 - Day |
| 1-21-4-3 | | | | | od orion |
| Iron Los , To | W-110 | TO | TENTON MIT | ad not - | J 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 |
| Inne 9d | 19 5 | 17 90 P | M | RIVATION | di milan |

June 2d, 19 5 17 .90 P. M.,

In the above computation the several proportional parts are set down and summed all together, which renders the operation some-

Several variations may be made on the six things here proposed, that may serve as a useful exercise, which, by a reference to the theorems and rules already given, will be easily performed.

what more easy when our tables are employed.

PROBLEM H.

Given the latitude of the place and the sun's declination; to find the time when twilight begins and ends.

At what time will twilight begin and end at London, in latitude 51° 32′ N., on the second of May, 1827, the sun's declination being 15° 14′ N.?

In figure, (page 70), suppose a parallel n m to the equator EQ to be drawn at the distance of 15° 14' above it, while another parallel to the horizon HO is drawn at the distance of 18° below it, these two would cut one another somewhere between c and m in S, forming the triangle ZPS, in which ZP, PS, and ZS, are given to find the angle ZPS, the angle between the meridian PEP and another meridian passing through the sun at the time he is 18° degrees below the horizon, his situation when twilight begins and ends.

| Z s or zenith distance P s or polar distance PZ or colatitude | | cosecant | 0.015534 ° 0.206168 |
|---|-------------------------|--------------------------|------------------------|
| Sum | 221 14 | The second second | 1 -0 -000 |
| Half Difference | 110 37 | sine sine | 9.971256 3.659475 |
| | The makes | and confined to | 18.852433 |
| T0107250 | 4h 58m 6s 2 | cosine | 9.426216 |
| Time from noon Or at . | 9 56 12 in 2 4 48 in | the evening the morning. | 227 |

PROBLEM III.

Given the right ascensions and declinations, or the longitudes and latitudes of two celestial objects; to find their angular distance.

In this problem there are given two sides and the contained angle to find its opposite side. The contained angle is the difference between their right ascensions or longitudes, and the containing sides are the complements of the declinations or latitudes. If the sun be one of the objects, as his latitude is very small, he may be supposed to be always in the ecliptic; then the triangle so formed will be right angled if the longitudes and latitudes are used, and the computation becomes more simple. By means of this problem the lunar distances in the nautical almanac are computed.

On the 1st of June, 1828, required the distance between the moon and a Pegasi, at noon, on the meridian of Greenwich, the moon's right ascension being 295° 23' 46", and declination 16° 11' 45" S., the star's right ascension being 22h 56m 13s.85, or 344° 3' 28", and north

polar distance 75° 43′ 2″, or declination 14° 16′ 58″ N. 344° 3′ 28″—295° 23′ 46″ = 48° 39′ 42″ the angle at the pole. Instead, however, of following the operation derived from the spherical triangle, a more simple practical rule may be derived from it according to theorem IX.

To twice the sine of half the contained angle add the cosines of the moon and star's declinations, and take half the sum of these

three logarithms. From this half sum subtract the sine of half the sum of the declinations if they are of contrary names, or that of half their difference if of the same name, the remainder will be the tangent of an arc, the sine of which being subtracted from half the sum of the three logarithms already found will give the sine of half the required distance.

| Diff. of R. A. | 48° 39′ 42″ | P. CALL |
|--|--------------------------------------|---------------------------|
| ·Half | 24 19 51 sine × 2= | =19.229804 |
| Moon's declination Star's declination | 16 11 45 S. cos. 14 16 58 N. cos. | 9.982413 9.986364 |
| Sum | 30 28 43 | 39.198581 |
| Half . | 15 14 21½ sine | 19.599291 (a) 9.419717 |
| Arc | 56 31 18 tan. | 10.179574 |
| Same arc | sine | 9.921215 (b) |
| Half distance . | 28 27 29 sine 2 | 9.678076 (a—b) |
| True distance . | 56 54 58 | |

Examples for Exercise.

1. Required the distance between the moon and sun on July 2d, 1828, at noon on the meridian of Greenwich, the longitude of the sun being 3s 10° 28′ 44′, the longitude of the moon 11° 17° 59′ 39″, and latitude 2° 51′ 40″ N.?

Ans.-112° 27′ 19" east of her.

2. Required the distance between the moon and sun on the 20th January, 1828, at noon, the sun's longitude being 9° 29° 29′ 39″,

that of the moon 11° 17° 54′ 42″, and latitude 3° 24′ 28″?

3. Required the distance between the moon and & Aquilæ, at noon on the 10th of May, 1828, the right ascension of the moon being 6° 58′ 43″, the declination 4° 44′ 48″ N., the right ascension of & Aquilæ in time, being 19^h 42^m 25°.62, and north polar distance 81° 34′ 41″?

Ans.=70° 54′ 51" west of her.

4. Required the distance between the moon and Aldebaran, at midnight on the 16th of December, the moon's R. A., being 32° 31′ 30″, the declination 11° 18′ 11″ N., the R. A. of Aldebaran being 4_h 26^m 8°.67, and N. P. D. 73° 50′ 37″.4?

Ans.-33° 21′ 10″.

PROBLEM IV.

On finding the latitude by observation.

The most simple practical method of finding the latitude, is from the meridian altitude of a celestial body whose declination is known.

Should the object be the sun, moon, or some of the planets, the altitude or zenith distance of the lower or upper limb, or both, are

(L)

observed, and by the application of several corrections that of the

centre is obtained.

When reflecting instruments, such as the sextant, repeating circle, &c. with an artificial horizon, are employed, the arc read off must, from the principles of optics, be halved before the other corrections are applied.*

A meridian altitude of the sun, moon, or a planet taken at land, must be corrected for refraction, parallax, and semidiameter, and at

sea for the dip of the horizon.+

Having found the true altitude, take its complement to 90°, which gives the zenith distance, denominated north or south, according as the observer is north or south of the object.

Now, if the zenith distance and declination are of the same name, their sum is the latitude; if of contrary names, their difference is the

latitude of the same name with the greater.

Ex. 1.—Edinburgh Observatory, March 28th, 1825, with an artificial horizon and one of Troughton's best sextants, the vernier of which showed 10", Captain Pringle Stokes, R. N. found the meridian altitude of the sun's lower limb to be 73° 32′ 15", the index error being +2' 26", the barometer standing at 29.66 inches, and Fahrenheit's thermometer 56°; what was the latitude, employing the refractions in the table in the nautical almanac?

| Observed altitude | 73° | | 15" 26 | |
|---|--------------|---------------|--------------------|-------|
| Sum | 73 | 34 | 41 | |
| Half Refraction to 29.66 and 56° F. Parallax Semidiameter | 36 + + | 47 1 16 | 20 15 8 2 | Ŧ |
| True altitude | 37 | 2 | 15 | in in |
| Zenith distance | 52 2 | 57 59 | - | |
| Latitude | 55 | 57 | 28 | |

Ex. 2.—To determine from the observations of Captain Basil Hall, R. N., taken June 4th and 6th, 1822, the latitude of San Blas, that by estimation being about 21° 32½′ N., and longitude 105° 15′ W. = 7h 1m in time.

To compute the sun's declination. June 4th 1822

| | | , | TOMM! |
|---------------------|-------------------------------|-------|---------|
| Longitude in time | 7 ^h 1 ^m | D. L. | 0.53408 |
| Daily variation | 6' 56" | P. L. | 1.41433 |
| Prop. part to 7h 1m | 2' 1".6 | P. L. | 1.94841 |

Eq. to sec. diff.-23" and 7h + 2 .4

2 Correct prop. part Declination at noon G. 22° 24 41 .0

Sun's true dec. 22 26 45 .0 N.

^{*} See explanation of Table XXV. + Tables XIII. and XIV. have been computed, expressly for this purpose at sea, combinn the whole in one.

| To compute the refraction, the barometer be | ing at 29.75 inches, |
|--|---|
| and the thermometer 86° Fahrenheit, to merid | |
| Z. D | 0.0755 9.9686 |
| Bar. 29.75 | 9.9963 |
| Ther. 86° | 9.9984 |
| In the same of the | 0.000 |
| r 1".1 | 0.0388 |
| Parallax 0".2 (table 16) Face of the circle west. | t d along our forces |
| 1 lst Vernier | 88° 50′ 0″ |
| $rac{1}{2} 	ext{Readings} \left\{ egin{array}{ll} 1 	ext{st Vernier} & . & . & . & . \\ 2 	ext{d} & . & . & . & . \end{array} ight.$ | 50 10 |
| and the second of the second of the second | 88 50 5 5 |
| Obs. merid. alt. sun's l. l | + 15 47.2 |
| Refraction | 1.1. |
| Parallax | + 0.2 |
| I man a second and | 00 0 51 0 |
| True alt. sun's centre | 89 6 51.3 |
| The state of the s | 90 |
| Zenith dist. | 0 54 8.7 S. |
| Declination . , | 22 26 55.0 N. |
| The first of the same | 01 20 26 2 N |
| Latitude with face west | 21 32 36.3 N. |
| To compute the sun's declination, June | |
| Longitude in time 7 ^h 1 ^m D. L. | . 0.53408 |
| 6 9" P. L. | . 1.46640 |
| Prop. part to 7 ^h 1 ^m , 1' 48" P. L | 2.00048 |
| Eq. to sec. diff.—24" and 7" + 2.5 | |
| DOMESTIC TO COMPANY OF THE PARTY OF THE PART | o lett Hoger all. |
| Correct prop. part + 1 50.5 Dec. at noon G. 22 38 10.0 | Within salp a - |
| Dec. at 10011 G. 22 50 10.0 | 10 10 10 |
| True dec. at S. B. 22 40 0.5 N. | The first section of the section of |
| To compute the refraction, the barometer being | ng 29.8 inches, and |
| the thermometer 85° Fah., the meridian Z.D. be | ing 1° 23′.5 nearly. |
| Z. D. 1° 23′.5 log. θ 0.1926 | Parallax 0'.21 |
| Ther. 85° . log 9.9694 | |
| Bar. 29.8 9.9971 Ther. 85° 0.9085 | and property of |
| Ther. 65 . 0.9000 | A STREET STATE OF |
| r 1".44 0.1576 | 1.2.4 |
| Face of the circle east. | -10 |
| $\begin{array}{c} \text{Readings} \left\{ \begin{array}{ll} \text{1st vernier} & \cdot & \cdot \\ \text{2d vernier} & \cdot & \cdot \end{array} \right. \end{array}$ | 1° 23′ 30″ |
| 2d vernier . | 25 |
| Obs. zenith dist. suns's l. l. | 1 23 27.5 |
| Sun's semidiameter | -15 47.0 |
| Refraction | - 1.4 |
| Parallax | + 0.2 |
| True mer. Z. D. | 1 7 39.3 S. |
| A LUC MUI AND | 1 1 00.0 0. |

| True mer. Z. D. Declination | 101.70 | 2 , col | but | 1 22 | | 39.3 0.5 | |
|-------------------------------|--------|---------|-----|---------|----|--------------|----|
| Latitude, face east face west | 1.01.0 | | | | | 21.2 36.3 | N. |
| Mean latitude by sum | 1 | | | 21 | 32 | 28.7 | 5 |

When the latitude is determined by an astronomical circle, an observation is not supposed to be complete, till the observer has reversed the circle, by this means combining two sets of observations, with the face or graduated limb of the instrument alternately, as in this example, towards the east and west.

San Blas, 20th May, 1822, the barometer being at 29.78 inches, Fahrenheit's thermometer 83°, the chronometer too fast for mean time 4^h 4^m 45^s, Polaris on the meridian below the pole by chronometer at 1^h 8^m 41^s and its true apparent N. P. D. 1° 38′ 28″.46.

| Face of instru- ment. | Chronometer. | Time from the Merid. | Reduction to Merid. | Obs. Z. D. and Alts. | Altitudes. |
|--------------------------|--|-------------------------|------------------------------------|---|---|
| East | h m s 1 6 5 1 7 51 1 8 41 1 14 3 | m s 2 36 0 50 0 0 5 22 | 13".27 1 .36 0 .00 56 .55 | 70 3 34.5 3 34.0 3 35.0 19 56 19.0 | 19 56 25.5 56 26.0 56 25.0 56 19.0 |
| West-{ | 1 16 11 18 35 | 7 30 6 54 6 | 110 .44 192 .41 | 56 18.0 55 20.5 | 56 18.0 19 56 22.33 |
| | | 0 | 374 .03 62 .34 | - 10 | 1 |

To compute the correction of altitude on account of the distance of the star from the meridian.

| λ 21° 32′ 30′ | | 9.968553 |
|---------------|--|----------|
| ð 28 21 30 | | 8.457118 |
| Alt. 19 56 22 | secant | 0.026814 |
| m 62''.34 | log. | 1.794767 |
| Cor. —1 .77 | log. | 0.247252 |
| | for part II. is in this case insensible. | 0.21/202 |

To compute the refraction.

| | | THE LUIL | action. | 111 |
|---|-----------|-------------------------|---------|--|
| Z. D. 70° 3'.6 Ther. 83 Bar. 29 .78 Ther. 89 | F. | log. θ log. log. | | 2.20325 9.97112 9.99445 9.99857 |
| r 147".02 - Or 2' 27".02 | - 57 | log. | 4.00 | 2.16739 |
| Observed altitude Refraction Correction | | | 100 | 19° 56′ 22″.33 — 3 27 .02 |
| True altitude | 200 | - | • | $\frac{-1.77}{19.53.53.54}$ |

56 21.6 N.

| True altitude below the pole Polar distance | | | 53 .54 N. 28 .46 N. |
|---|----------|-----|------------------------|
| Latitude from Polaris | | | 22 .00 N. 28 .75 |
| Mean Captain Hall makes it | | | 25 .37 23 .67 |
| Difference . | (UZ e de | 01/ | 1 .70 |

Which appears to be occasioned by neglecting the application of the equation of second difference in reducing the sun's declination to

the place of observation.

It seems unnecessary to extend our remarks farther with regard to these observations, more especially if the examples in the explanation of the table XXVIII. be consulted. If the observations are taken at sea with a reflecting instrument, on the principles of Hadley's quadrant, a correction must be made for the dip in addition to these already given. This may be taken from table XI.; or the true altitude may be still more readily found from table XIII. or XIV. sufficiently correct for all the usual purposes at sea.

Ex. 1. May 1st, 1825, in longitude 64° 25' W., the observed meridian altitude of the sun's l. l. was 48° 34′ 30″, the zenith being north of the sun, and the height of the eye 14 feet; what was the la-

titude?

Latitude

| ituae: | | | |
|--|-------------|------------|-----|
| May 1st at ship, time . 0 ^h 0 ^m | Dec. 1st | 15° 4′ 19″ | N. |
| Long. in time 4 18 | P. P. | + 3 14 | |
| published who are of the property of the last | | | EDE |
| Gr. time, May 1st . 4 18 | R. D. | 15 7 33 | N. |
| Gr. time, May 1st . 4 18 Observed Altitude | 1 | 48° 34′.5 | 111 |
| Cor. to $48\frac{1}{9}$ °, 14 feet, and May | | + 11.5 | |
| | | | |
| True alt. | Avel III . | 48 46.0 | |
| Part and the second of the Part of the Second of the Secon | I OF SHORT | | |
| Z. D | THE REST OF | 41 14.0 | N. |
| Declination | | 15 7.6 | N. |
| And the property of the soul and the | | | |
| | | | |

It is unnecessary to push the calculations nearer than tenths of a minute, as any observation taken at sea is, from the indistinctness of the horizon and the uncertainty of the horizontal refraction, unless a dip section be used, liable to an error of at least one minute.

Examples for Exercise.

1. On the 1st of September, 1824, in longitude 54° W., the meridian altitude of the sun's lower limb was 79° 44′ 15″ S., the height of the eye being 24 feet; what was the latitude?

Ans.—18° 30′.9 N.

2. On the 1st of January, 1826, the meridian altitude of the star Arcturus was 60° 41′ S., the height of the eye being 24 feet; what was the latitude?

Ans.-49° 29'.8.

3. On the 14th September, 1827, in longitude 103° 18′ E., let the meridian altitude of the moon's lower limb be 51° 4′ N., and the height of the eye 20 feet; required the latitude?

Ans.-19° 48'.4 S.

4. On the 29th September, 1827, in longitude 20° 40′ W., if the observed meridian altitude of the moon's upper limb be 83° 6′ N., and the height of the eye 16 feet; required the latitude?

Ans.-21° 25'.7 S.

As the meridian altitude may, by the interposition of clouds, or other causes, be lost at sea when a knowledge of the latitude is necessary for the safety of the ship, recourse must be had to other methods, particularly to that of H double altitudes, and the time between them, as being the most practicable.* This method requires solutions in three spherical triangles. In the triangle ZPS there are given



PS the sun's polar distance at the time of the first observation, PS' that at the second, and the angle S'PS measured by the the elapsed time; to find the side S'S and the angle PS'S. Again in the triangle ZS'S there are given the zenith distance ZS at the time of the first observation, ZS' that at the second, and the side S'S already found to determine the angle ZS'S. But PS'S being already computed, ZS'P may be obtained. Whence there are in the triangle ZS'P, the sides ZS', and PS', and the contained angle ZS'P; to find the side ZP the colatitude. This is the regular method by spherical trigonometry; but if the polar distance PS be supposed to remain the same, that at the middle time, between the observations, or, as Professor Lax seems to think preferable, the same as at the time of the greater altitude, and, by combining the solutions of the several triangles in one, the operation becomes more simple. In order to render this method still more easy to practical seamen, Douwes proposed an approximate method by introducing the latitude by account, which, when properly restricted according to the rules of Maskelyne or the tables of Lax, will generally give the desired result sufficiently correct for nautical purposes, and the computations may be very readily performed by the tables of Lynn.

When the common tables are used, Mr Ivory's solution is the best, particularly in the form that Mr Riddle has given it, which we shall

adopt here.

Find the sun's declination for the time of the greater altitude, and the true altitudes, reducing the less if necessary for the ship's run to what it would have been had it been taken at the same place with the greater. This is accomplished by observing the sun's bearing by compass, at the time of taking the less altitude, and, finding the angle contained between that and the ship's course by compass, corrected for leeway if she makes any, in the interval between the observations. With this angle as a course enter a traverse table, and the difference of latitude, answering to the distance run during the elapsed time, will be the reduction of altitude.

If the less altitude be observed in the forenoon, the reduction of altitude must be added to it, if the angle between the ship's course and the sun's bearing be less than eight points; but if that angle be greater than eight points, the reduction is to be subtracted from the less altitude. If the less altitude be observed in the afternoon, the

^{*} On the authority of a very distinguished practical navigator, I am informed, that double altitudes are not of such importance as is generally supposed.

+ A circle is supposed to pass through PS' P' similar to PSP'.

reduction is to be subtracted from it, if the angle between the ship's course and the sun's bearing is less than eight points; but if greater, the reduction is to be added to the less altitude. With the corrected altitudes, the elapsed time, and the declination, the latitude at the time of the observation of the greatest altitude will be found, which may be reduced to noon by means of the dead reckoning.

1. Take half the interval between the observations, and call it

the half elapsed time.

2. To the sine of the half elapsed time add the sine of the sun's polar distance, the sum, rejecting always ten in the index, will be arc first.

3. To the secant of arc first add the cosine of the polar distance, the sum will be the cosine of arc second, which will be of the same

affection or character as the polar distance.

4. To the cosecant of arc first, add the cosine of half the sum of the true altitudes, and the sine of half their difference, the sum will be the sine of arc third.

5. Add together the secant of arc first, the sine of half the sum of the true altitudes, the cosine of half their difference, and the secant

of arc third, the sum will be the cosine of arc fourth.

6. The difference of arc second and arc fourth is arc fifth, when the zenith and the elevated pole are on the same side of the great circle, passing through the places of the sun at the times of observation, otherwise their sum is arc fifth.

7. To the cosine of arc third add the cosine of arc fifth, and the

sum will be the sine of the latitude.

Ex. 1.—On the 6th of June, 1828, in latitude 58° N., and longitude 48° W., by account, at $10^{\rm h}$ 53° $20^{\rm s}$ A. M. per watch, the altitude of the sun's lower limb was 52° 20′, and at $1^{\rm h}$ 17° 8°, the altitude of the same limb was 52° 54′, and the bearing per compass S. W. by W. The ship's course during the elapsed time was S., the wind E.S.E., and hourly rate of sailing 8 knots, and the ship making $1\frac{1}{2}$ pts of lee-way. Required the true latitude at the time of observation of the greatest altitude, the height of the eye being 16 feet?

Ship's apparent course S. or 0^{pts} Lee-way $1\frac{1}{2}$

Ship's true course S. by W. $\frac{1}{2}$ W. $= 1\frac{1}{2}$ pts S. W. S. W. by W. = 5 pts S. W.

Contained angle $3\frac{1}{2}$ Interval between the observations $= 2^h \cdot 23^m \cdot 48^s = 2^h \cdot 4$ Distance run $= = 2^h \cdot 4 \times 8 = 19.2$ miles.

Now to course $3\frac{1}{2}$ points and distance 19'.2, the difference of latitude is 14'.84, and since the least altitude was observed in the afternoon, and the angle between the ship's course and sun's bearing is less than eight points, this reduction is *subtractive*.

^{*} Should there be any doubt whether the zenith and elevated pole are on the same side of the great circle, passing through the places of the sun, the latitude may be computed on both suppositions, which, being compared with that by account, the true latitude will, in general, be readily discovered with little additional trouble, for it is only are fourth and its cosine that will require alteration.

| 00 | | |
|--|---|--------------------|
| First observed alt. 53° 20' | | |
| Cor. table XIII. + 11 | ·2 · · · · · · · · · · · · · · · · · · | 11.2 |
| 1. True alt 53 31 | .2 Reduction . — | 14.8 |
| The state of the state of | 2 True alt 59 | 2 50 .4 |
| 1. True alt . 53 | ° 31′.2 | a More |
| 2 | 50.4 | 904 |
| | transfer and a second | 20.00 |
| Sum . 106 | 21.6 half 53° $10'.8 = 53^{\circ}$ | 10' 48" |
| and the second s | | 145 |
| | 40.8 half $0.20.4 = 0$ | |
| Tim on | me \cdot $10^{h} 53^{m} 20$ |)° A. M. |
| 13 17 8 Lo | ong. W 3 12 | 10 5 500 |
| 7 0 00 10 | 14 | |
| Elapsedt. 2 23 48 | |) A. M. |
| | n 6th at . 2 5 20 | 0 P. M. |
| H. E. T. 1 11 54 Ann. time 2 ^h 5 ^m 20 ^s | D. T. 100 | 200 |
| 1100. 011110 | D. L. 1.060 | |
| Daily variation - 5' 55" | P. L. 1.483 | 320 |
| D | 0 31 . 2.543 | 250 |
| Prop. part Dec. at noon or 6th | 2.540 22° 41′ 17″ N. | 550 |
| Dec. at noon or our | 2 41 1/ N. | |
| Reduced dec 2 | 2 41 48 N. | |
| 200000000000000000000000000000000000000 | 7 18 12 | |
| Folar dist. | 7 10 12 | To the last |
| | | THE REAL PROPERTY. |
| 9.489404 sin. 1 ^h 11 ^m 54 ^s H. E. T. 9.965055 sin. 67 12 12 pol. dist. cos. | 9.586422 | - |
| | | Calen. |
| 9.454459 sin. 16 32 37 arc 1st sec. | 0.018362 cosec | 0.545624 |
| 66 15 52 arc 2d cos. | 9.604784 | - T |
| | 0.018362 sec. arc 1 | |
| | 9.903374 sin. 53° 10′ 48″ cos. | 9.777646 |
| | 9.999993 cos. 0 20 24 sin. | 7.773187 |
| | 0.000034 sec.3d 0 42 56 sin. | 8.096457 |
| 33 22 8 arc 4. cos. | 9.921763 3d . cos. | 9.999966 |
| 32 52 44 arc 5. cos. | | 9.924104 |
| Latitude 57 5 51 N. arc 6. sine | 111 0 30 102 10 10 10 | 9.924070 |
| | | 0.022010 |

In this example the computation is carried to seconds, but such a

degree of accuracy is unnecessary at sea.

2. On the 6th of March, 1827, in latitude 60° N. by account, and longitude 105° E., the altitude of the sun's lower limb was observed to be 19° 42' at 40h 4m 20s in the forenoon, his centre bearing S. S. E. by compass, and at 1h 32m 36s afternoon it was 21° 8'. The ship's course during the elapsed time was N. W. by N., sailing at the rate of 9 knots per hour, and the height of the eye 16 feet. Required the ship's latitude at the time of taking the greater altitude? Ans.—60° 37′ N.

3. August 31, 1827, in latitude 12° 40' S. by account and longitude 165° E. at 11h 13m 30° A. M., the altitude of the sun's lower limb was 66° 9′ 30″, and at 1° 15^m 12° P. M. it was 62° 0′ 15″, bearing at the same time N. W. & W. During the elapsed time the ship was sailing S. W. by W. at the rate of 4 knots per hour, and the height of the observer's eye was 28 feet. Required the latitude at the time of taking the first altitude?

Ans.—11° 37′ Š.

PROBLEM VI.

On finding the Longitude. I. BY LUNARS.

Since the rotation of the earth about its axis is performed in a day, the sun appears to pass over 360° in 24 hours, and, consequently, over 15° in one hour; therefore, it is obvious, that the difference of time between any two places will give the difference of longitude be-

tween those places.

A variety of methods have been proposed for determining the longitude of a place, but almost all of them depend upon one general principle, the comparison of the relative times under two different meridians; so that, if the time on two different meridians be known, the difference of these times turned into degrees, at the rate of 15° to an hour, will give the difference of longitude between these meridians.

As the sun apparently moves from the east towards the west, it is evident, that all places lying to the eastward of any meridian will have noon, or any other hour, sooner, or if westward, later, by the precise time the sun takes to pass from the meridian of the one place to that of the other. Hence, if the time on the meridian of Greenwich, the place from which our longitude is reckoned, and that of any other place at the same instant be known, the longitude of the latter place from Greenwich is also known, by turning the difference of time into degrees, at the rate of 15° to an hour.

Among the heavenly bodies which frequently present themselves for observation, there is none whose apparent velocity is so rapid with regard to the sun, planets, and fixed stars near the ecliptic, as that of the moon; the diurnal motion of that object being at a mean rate about 13°11′. Hence, her distance from these bodies is continually changing in proportion to the time, and an error of 2″ in the distance between the moon and any of these bodies will produce an error of about 1′ only of longitude. Of all the various modes, then, which have been proposed to determine the longitude at sea, it is probable the method by lunar observations will continue to be the most practicable. It appears also from the numerous observations lately made by several of our most distinguished navigators, that a series of lunars taken at land with good instruments, will, when great nicety in the requisite observations and calculations is attended to, give the longitude with singular accuracy.

The instruments generally employed are a good chronometer for connecting observations taken at different times with one another, two good quadrants for obtaining the altitudes, and a sextant or reflecting circle for taking the distance. These instruments are all described in our usual treatises on navigation and nautical astro-

nomy

If the sun or star be at a sufficient distance from the meridian at the time of taking the distance, the true altitude of either of these objects will serve to compute the apparent time at the ship, and this compared with the Greenwich time, derived from the lunar distance, will give the longitude. The same thing may be obtained from the moon's altitude, but less readily, as her right ascension and declination must be very accurately computed by applying the equation of second difference.

This method will be rendered familiar by the following examples.* Ex. 1.—September 24, 1827, in latitude 48° 50' south, and longitude by account 120° west, at 8h 18m 30s A. M., the following observations were made to obtain the true longitude; the height of the eyes of the observers being 30 feet above the surface of the sea, the angular instruments being perfectly adjusted when the English barometer stood at 29.4 inches, and Fahrenheit's thermometer at 60°.

The mean of five distances between the moon and sun's nearest limbs was 44° 33′ 45″, the altitude of the sun's lower limb 22° 4′ 15″,

| and the altitude of the moon's upper limb 6° 6′ 0″. |
|--|
| Time at ship 23 ^d 20 ^h 18 ^m 30 ^s To this time by estimation. |
| Longitude in time 8 0 0 the sun's semidiameter is 15' 59" |
| the moon's . 16 2 |
| Ext. Green. time 24 4 18 30 augmentation 2 |
| Obs. dist. n. l. 44° 33′ 45″ hor. parallax . 58 49 |
| Sun's semidia. + 15 59 reduction to lat. 49° S 7 |
| Mann's semidia + 16 0 reduced reveller 50 40 |
| Moon's semidia. + 16 2 reduced parallax . 58 42 Augmentation + 2 |
| Augmentation + 2 |
| App. cent. dist. 45 5 48 |
| Alt. sun's l. l. 22° 4′ 15" alt. moon's u. l. 6° 6′ |
| 67 55 45 |
| Z. D. log. \$2.15567 83 54 1. \$2.70124 |
| Thermometer 66°.0 F. 9.99104 |
| Barometer 29 .4 E. 9.99123 |
| Thermometer 60 .0 F 9.99957 |
| 10000 |
| r = 137''.25 . 9.98184 . 9.98184 |
| Or $2' 17''.25$ 2.13751 $r' = 482''.3$ 2.68308 |
| For the sun $or = 8' 2''.3$ |
| $-0.104 \times (60-50) = \cdot 104 \times 10 = -1.04$ |
| $+0.15 \times (30-29.4) = .15 \times .6 = +0.09$ |
| The state of the s |
| True refraction for the moon = 8 1 .35 |
| Alt. sun's l, l. 22° 4′ 15" Alt. moon's u. l. 6° 6′ 0" |
| Dip to 30 feet — 5 27 — 5 27 |
| The state of the s |
| 21 58 48 |
| Semidiameter + 15 59 Semidiameter augm. — 16 4 |
| 20 14 4 |
| App. alt. 22 14 47 App. altitude . 5 44 29 |

The necessary computations are readily and very accurately performed, according to the rules of spherical trigonometry from the tables contained in this work. There are several collections of tables, such as those of Mendoza Rios, Lax, Lynn, and Thomson, which, for general practice at sea, by abating something of rigorous accuracy, render the calculations more simple. Some of them, however, are rather bulky and expensive.

| App. alt. Refraction | | 14' 47 2 17 | App. altitude Refraction | . 5° 44′ 29 — 8 1 |
|----------------------------|------|------------------|---|---------------------------------|
| Parallax , | + | 3 | Parallax in alt. | 5 36 28 + 58 22 |
| Sun's T. alt. | 22 | 12 33 | Moon's true alt. | |
| Alt. moon's u Red. par. | | 6° 6′ 0 58 42 | y' | Secant 0.60247 P. L. 0.48663 |
| Par. in alt. | AP 4 | 58 22 | Mag sub-To-entimo assum sel virini a | P. L. 0.48910 |

The reduction of the apparent to the true distance is effected by the solution of two spherical triangles. First the angle at the zenith is found from the triangle formed by the apparent zenith distances and apparent distance. Next the true distance is computed from the angle at the zenith and the true zenith distances, and these two may be combined in the following manner.

| App. dist. | 45 | 0 5 | 48 | / // | | | |
|--|------|-------|-------|-----------------------|--|---------------------------------|-------------------|
| App. alt. ① | | 14 | | | secant | | 0.033593 |
| | 5 | | 29 | | secant | | 0.002188 |
| App. alt.) | J | ** | 49 | | secant | | 0.002100 |
| a | HO | - | 4 | | EN 1903 | | 1002 |
| Sum . | 73 | 5 | 4 | | No. Land | | III.AVG |
| | - | | | | | | |
| Half . | 36 | 32 | 20 | -d la 19 | cosine | | 9.904942 |
| Difference | 8 | 33 | | | | | 9.995141 |
| Difference | 0 | 33 | 10 | | cosine | | 9.993141 |
| win Mail | | 20 | - | | | | 0.000 |
| True alt. ① | 22 | 12 | | | cosine | | 9.966522 |
| True alt.) | 6 | 34 | 50 | - | cosine | | 9.997129 |
| THE PARTY OF THE P | - | | | | 30 3 | 10120 133 | A & B |
| Sum . | 28 | 47 | 23 | | | | 19.899515 |
| Half . | 14 | 23 | 42 | | | | |
| Arc | 27 | 1 | 55 | 200 | cosine | 1 100 | 9.949757 |
| Arc | 41 | 1 | 00 | - | cosine | | 3.343131 |
| 0 | | ~ - | | | | | |
| Sum | 41 | 25 | | 100 | sine | | 9.820638 |
| Difference | 12 | 38 | 13 | 1304 | sine | 100 | 9.339993 |
| | | | | 1,45 | | -22 HIN | Charles (COCK) |
| | | | | | | | 19.160631 |
| | | | 6 6 | A TI SUM | 0.6- 22 | | 10.100002 |
| 1 Dist. | 99 | 21 | 51 | - 1000 - | sine | | 0.500016 |
| g Dist. | 24 | 21 | - | | sine | | 9.580316 |
| | . 10 | | 2 | | | | Difference |
| Marie III | _ | - | - | The Secretary Section | | - | |
| True dist. | 44 | 43 | 30 | CAL PROF | West Later | | - MANAGE |
| Dist. at 3h | 44 | 1 | 21 | 0° 4 | 2' 9" | P. L. | 0.63048 |
| 6 | 45 | 38 | 36 | 1 8 | 37 15 | P. L. | 0.26738 |
| | | | | | 10 | 1 . 24. | 0.20700 |
| Time nest 2h | 11 | 18" | 1 1 5 | | | n r | 0.26210 |
| Time past 3 ^h | _ | 10 | 1 | | | P. L. | 0.36310 |
| Preced. time | 3 | 120-1 | | AT 10 STREET, | NAME OF THE OWNER, OWNE | STREET, STREET, STREET, STREET, | O'THE ME |
| Application to a | 4 | | - | | ST | DISTRIBUTION NAMED IN | O SP LIXER IN |
| Approx. time | 4 | 18 | 1 | OF THE PARTY. | - | - | Table of the Park |

wines all we show the same of the same of

| THE RESERVE AND ADDRESS OF THE PERSON OF THE | 1st Diff. | 2d Diff. | - Mean. |
|--|-----------|----------|---------|
| Dist. at noon 42° 24′ 13″ | 1° 37′ 8′ | 7" | |
| $-3^{\rm h} \ 44 1 21$ $-6 45 38 36$ | 1 37 15 | 7 | +7" |
| 9 47 15 58 | 1 37 22 | 4 | 150 017 |

 $(1^h 18^m 1^s) \times 4 = 5^h 12^m 4^s$, to which and second difference 7" we get (from table XXVII.) 1" of motion, that at a mean rate gives 2 seconds of time.

This, from the explanation of the table, because the first differences are all increasing, must be subtracted from the approximate distance, and consequently added to the approximate time.

To the approximate time 4^h 18^m 1^s Add cor. from sec. diff. + 2^s

True T. at Greenwich 24d 4 18 3

Computation of the time derived from the figure in page 70, Theorem IX., page 75 after the examples in page 78.

| Sun's T. alt. Sun's pol. dist. Latitude . | 22° 12′ 33″ 89 40 33 48 50 0 | cosecan | 94 10 5 | 0.000007 0.181608 |
|---|------------------------------------|----------------|--------------|--|
| Sum . | 160 43 6 | | 0 100 | nues |
| Half . Diff | 80 21 33 58 9 0 | cosine sine | bi G h | 9.223941 9.929129 |
| | | | FE 91.00 | 19.334685 |
| 1 Time from noon | 1h 50m 48s.6 | sine | OS POLITY | 9.667343 |
| | 2 | | Z Z 1 | |
| Time from noon | 3 41 37.2 24 | | 8 F W | |
| App. time 23 ^d App. T. Green. 24 | 20 18 23.0 4 18 3.0 | | 50 AS 44- | 100 mm 11/07 |
| Lon. in time Lynn gives | | | | n his copious autical tables. |
| Difference . | | 9 | 45 | |
| | | | Act with the | Andrew Street, |

Ex. 2.—On September 12th, 1823, in latitude 26° 30′ N., longitude by account 24° 30′ W. at 5^h 34^m P. M. by watch, the altitude

^{*} The equation of second difference happens to be small in this example. It may amount to 6 seconds of distance, 12 seconds of time, or 3' of longitude in some cases. The correction of second difference is taken from the usual table, and its effects estimated according to the moon's mean motion. It is performed more correctly, however, by means of Tables 3d and 4th immediately following this article, which have been computed by the author expressly for this purpose.

| of the sun's lower limb was 7° 37', that of the moon's lower limb |
|---|
| was 35° 35', the distance of their nearest limbs 95° 19' 58", the baro- |
| meter being 30.28 inches, and the thermometer 72°.4 Fahrenheit, the |
| height of the eye being 25 feet; what was the longitude? |
| Time per watch 5 ^h 34 ^m |

| Time per watch Longitude 24° W. in time + 1 36 |
|--|
| Estimated Greenwich time Moon's semidiameter at noon Correction for Greenwich time 7 10 P. M. 14' 52" parallax correct for 7h 10m — 5 |
| Augmentation . 14 50 equatorial par. 54 26 - 2 |
| True semidiameter 14 58 red. hor. par. 54 24 Alt. of sun's l. l. 7° 37′ Moon's 35° 35′ Moon's 35° 35′ |
| Z. D. 82 23 log. \$\epsilon 2.61313 \ \text{Z. D.} 54 25 log. \$\epsilon 190970 \ \text{P.P. 5'} 133 |
| Thermometer 73 4 log. 9.98020 . 9.98020 |
| Barometer 30 28 log. 0.00289 0.00289 |
| Thermometer 72 4 log. 9.99902 9.99902 |
| 110111011101101111111111111111111111111 |
| r 398".1 2.59898 r 78".3 log. 1.89428 |
| Or $6'$ 38".1 or 1' 18".3 060 × + 22.4 = - 1 .3 alt. moon's l. l. 35° 35' secant 0.08977 |
| $+.09 \times +.28 = + 0.0$ red. hor. par. 54' 24' P. L. 0.51967 |
| Total III - ALL TOTAL III - AL |
| r . 6 36 .8 parallax in alt. 44 14 P. L. 0.60944 |
| Alt. sun's l. l. 7° 37′ 0″ alt. of moon's l. l. 35° 35′ 0″ |
| Dip to 25 ft. — 4 58 dip. to 25 feet — 4 58 |
| 38 30 2 |
| 7 32 2 semidiameter + 14 58 |
| Semidiameter + 15 56 app. altitude . 35 45 0 |
| refraction — 1 18 |
| App. alt. 7 47 58 parallax . + 44 14 |
| Refraction $-$ 6 37 Parallax $+$ 9 moon's true alt. $\phantom{aaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaa$ |
| |
| Sun's true alt. 7 41 30 |
| Observed distance 95° 19′ 58″ |
| Sun's semidiameter + 14 58 |
| Moon's semidiameter + 15 56 |
| App. central dist. 95 50 52 |

P. only in the colony S. V. It's the state of the state o

Equation of the damps - P.L.

| A dist | 95° 50′ 52″ | When your land | |
|--|--|--|--|
| App. dist. | 7 47 58 | secant . | 0.004036 |
| Sun's app. alt. | | THE RESIDENCE OF THE PARTY OF T | |
| Moon's app. alt. | 35 45 1 | secant | 0.090672 |
| 1-2 | | | THE RESERVE |
| 0 | 139 23 50 | | |
| Sum · | 100 20 00 | and the second | Water 1947 months |
| • | 20 47 55 | - State 10 - 77 | 0 7 400 7 |
| Half . | 69 41 55 | cosine . | 9.540277 |
| Difference . | 26 8 57 | cosine . | 9.953107 |
| | 7 41 30 1 | cosine . | 9.996075 |
| Sun's true alt. | | THE RESERVE OF THE PARTY OF THE | |
| Moon's true alt. | 36 27 56 | cosine . | 9.905372 |
| | | | |
| Sum . | 44 9 26 | | 19.489539 |
| Sum | 177 7 776 | | |
| The same of the same of the same of | 00 4 40 | | CAN THE PARTY OF T |
| Half . | 22 4 43 | | 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 |
| Arc . | 56 14 50 | cosine | 9.744770 |
| | 411 | | A second and the |
| G 1997 | MO 10 22 | sine . | 9.990922 |
| Sum . | 78 19 33 | | |
| Difference . | 34 10 7 | sine . | 9.749450 |
| 1 | When the same of t | 95.47.60 | |
| | | 100000 | 19.740372 |
| CONTRACTOR OF THE PARTY OF THE | - Inchina | 1000 100 | 10.710072 |
| | (L-(2-m) | It can be | 0.000000 |
| Half dist. | 47 52 13 | sine . | 9.870186 |
| PAY | 2 | | |
| | E-10860 | | ANALYSIS STREET |
| cm - 11 - | 05 44 00 | | |
| True dist. | 95 44 26 | 2 L 1000 | a aa ma a |
| True distance 95 | 5° 44′ 26″ 0° | 36' 9" P.L. | 0.69716 |
| Dist. at 6h 95 | 8 17 1 | 21 56 P.L. | 0.34181 |
| | 30 13 | | 310 22-02 |
| | 00 10 | TOW OF D.T. | OOFFOR |
| Time past 6 ^h | | 19 ^m 25 ^s P.L. | 0.35535 |
| Time of first distanc | e . 6 | A SECTION | 1.11.100 |
| 44.05 | - NI | and the second | 100 |
| A 4: | mo at Cuant H | 10 95 | A SANGER AND |
| Approximate app. ti | me at Green. | 19 20 | - 10 CO |
| To find | the corection for | or second differen | |
| | 1st Diff. | 2d Diff. | Mean. |
| Dist. at 3h 93° 46' 1 | 111 | | A Lord Co. and |
| | 0 0,00 | // H | |
| 6 95 8 1 | 1 21 21 | - 77 | - 7" |
| 9 96 30 13 | - | -7 | 100 |
| I2 97 52 9 | 1 21 49 | 1 - OL W | Delin bright |
| the second secon | 10 m. 20 m. | | |
| To the annuarima | to time (In Onm | VA on 5h 00m | and the moon |

To the approximate time $(1^h \ 20^m) \times 4$, or $5^h \ 20^m$, and the mean second difference — 7", the equation from Table XXVII. is 0".9 or about 1", which, since the second difference is negative, ought to be added to the proportional part of the distance computed by even proportion for the approximate time, and consequently it must be subtracted from the approximate time, or in general this correction for the time must be applied with a contrary sign to that which is employed when correcting an arc, or with the same sign as that of the second difference.

Now 1° 21′ 56″: 1″:: 3h: 2s of time nearly.

Equation of 2d diff. 2°

Or this operation may be performed by proportional logarithms, thus,

Equation of sec. diff. 1"

Variation in 3^h, 1° 21′ 56"

P.L. 3.03342

P.L. 0.04181

2.69161

P.L.

| From approximate apparent time Subtract equation now found | 778-368 Y | 7 ^h 19 ^m 25 ^s 2 |
|---|-----------|--|
| True apparent time at Greenwich | | 7 19 23 |

| To find the apparent time at the place of observation. | | | |
|--|--------------------------------|------------------|-------------------------------|
| The reduced declina | tion is found as in th | he explanation | of Table |
| IX. and XXVII., then Latitude 26° 30′ 0″ | N. secant | 528 8.6 | 0.048209 |
| Declination 4 17 7 | N. secant | | 0.001214 |
| Difference 22 12 53 Zenith dist. 82 18 30 | the grant on | The state of the | |
| Sum 104 31 23 Difference 60 5 37 | half 52 15 42 half 30 2 48 | | 9.8980 7 5 9.699582 |
| ed seeming to the | 0 | man (7 melas) | 9.647080 |
| 2 ^h | 47 ^m 4 ^s | sine | 9.823540 |
| App. time 5 Greenwich time 7 | 34 8 19 23 | 1/2 | |

Longitude in time 1 45 15 W. = 26° 18′ 45″ West.

Or about two miles less than Mr E. Riddle makes it in his treatise on navigation, a very useful work, combining theory with practice, a method too much neglected in the present plan of nautical instruction.

Ex. 3.—On the 14th of June, 1827, in latitude 28° 31′ 10″ N., and longitude 144° W. by account, at about 20° 32°, the distance between the sun and moon was observed to be 97° 22′ 40″; when the altitude of the sun's lower limb was 44° 36′ 40″, the altitude of the moon's upper limb was 35° 38′ 20″, the height of the eye being 20 feet; required the longitude, the barometer being at 29.68 inches, and Fahrenheit's thermometer at 68°.

| Longitude 144° W. in time | - F. F. | | 36 |
|--|---|--------------------------------------|-------------------------------|
| Approximate Greenwich time, To this time moon's semidiame Augmentation to 36° alt. | ter is 15' 37" h | or. par. ed. to lat. $28\frac{1}{2}$ | 8 57′ 18″ — 2 |
| Correct semidiameter Alt. of sun's l.l. 44° 36′.7 | | or. hor. par. u.l. 35° 38′.3 | 57 16 |
| Barometer 29.7 9 | 77198 Z. D. .98401 .99563 .99922 | 54 21.71o. | 9.98401 9.99563 9.69922 |

1.75084, r 1' 17".4

1.88873

r 56".3

89

h-s = 44

| Sun's semidiameter 15' 46" Parallax in alt. 6 | moon's alt. 35° 38' hor. par. 57' 16" | sec. 0.09004 P.L. 0.49737 |
|---|---|--|
| Alt. sun's <i>l. l.</i> Dip. to 20 feet — 4 26 Semidiameter + 15 46 | par. in alt. 46 32 moon's alt. u. l. semidiameter | P.L. 0.58741 35° 38′ 20″ — 4 26 — 15 46 |
| App. alt. 44 48 0 Refraction — 56 Parallax + 6 | app. alt. refraction parallax | 35 18 8 - 1 18 + 46 32 |
| True alt. 44 47 10 Observed distance of nearest lim Sun's semidiameter Moon's semidiameter | | 36 3 22 97° 22′ 40″ + 15 46 + 15 46 |
| Apparent central distance Now to compute the correction Dr Young's method, there are given as the second of the | n of the oblique semi iven. | 97 54 12 diameters, by |
| $\begin{array}{ccc} s' & = \frac{45}{36} \\ \hline 178 \end{array}$ | E TO THE | on tour |

As these give in Table II. 1" for the sun and 1" for the moon, or 2" in all, it is necessary to subtract them from the apparent or even true distance when they are so small.

=924

= 84

8

924

90

14

| Apparent distance Sun's app. altitude Moon's app. altitude | 97° 54′ 12 ′′ 44 48 0 secant 35 18 8 secant | 0.149004 0.088248 |
|--|--|--|
| Sum | 178 0 20 | |
| Half Difference Sun's true alt. Moon's true altitude | 89 0 10 cosine 8 54 2 cosine 44 47 10 cosine 36 3 22 cosine | 8.240647 9.994739 9.851100 9.907648 |
| Sum . | 80 50 32 | 18.231386 |
| Half Are | 40 25 16 82 30 0 cosine | 9.115693 |
| Sum Difference | 122 55 16 sine 42 4 44 sine | 9.923979 9.826174 |
| COUNTRY STORY | A CONTRACTOR OF THE PERSON NAMED IN | 19.750153 |

| BANKARO SE NAS JAMES NAS | Dinuteur a mo | | 19.750153 |
|---------------------------|---------------------------|---|-----------|
| Half dist. | 48° 35′ 33½″ | , | 9.875076 |
| TOOL 15 00 01 10 - 7000 | 2 2 | 00 01 0 | o 10 m3 |
| Cor. for oblique semidia. | 97 11 7 | | 9 0 HE |
| Address a grown T off (2) | | grado selo v | a wold |
| True dist 6 | 97 11 5 97 18 52 | 0° 7′ 47″ P.L. | 1.36411 |
| Dist. at 9 | 95 47 0 | 1 31 52 P.L. | 0.29211 |
| E V | | 0 ^h 15 ^m I5 ^s P.L. | 1.07200 |
| 1 - | | 1/4/ | |
| Dist. at 3h 98° 51′ 7″ | 1. 60/ 15// | 6 15 15 | - 4 |
| 6 97 18 52 | 1° 32′ 15″ 1° 31° 52 — | - 23" Mean. - 23 — 23" | |
| 9 95 47 0 12 94 15 31 | 1 31 29 | - 23 — 23" | ann's |

To 15^m and 23" the equation of second difference is 1", which, for a variation of 1° 32' nearly, gives 2° of time to be subtracted, whence the true time is 6^h 15^m 13° of the 15th of June, or 30^h 15^m 13° after the noon of the 14th.

| To con | mpute the time. | | |
|--|---|--------------------|---|
| True altitude | 44° 47′ 10″ | 4 No. 191 | |
| Polar distance . | 66 41 10 | cosecant 0.036999 | 2 |
| Latitude | 28 31 20 | secant 0.056193 | 3 |
| EBOUNE O | | £ 1.013 E | |
| Sum | 139 59 40 | | |
| Wildows. | | | _ |
| Half | 69 59 50 | cosine 9.534111 | |
| Difference | 25 12 40 | sine 9.629364 | 1 |
| all the W seems Worldon | a Monagar | 10 origan | - |
| OLIGERAL TALL TO THE PARTY OF T | 7 7 1 | 19.256660 | , |
| II-le- | 1 ^h 40 ^m 35 ^s .3 | 0.600000 | - |
| Half | 1" 40" 55".5 | sine 9.628330 | |
| Control 1 Property | | 109 | , |
| Time from noon | 3 21 10 .6 | 4 - Jys) (7 a) 221 | |
| Time nom noon | 24 | 199 | _ |
| 10-64-55 | 145 | II diament | |
| App. time 14th | 20 38 49 4 | 8 1:11-22 |) |
| App. time at Greenwich | 30 15 13 .0 | April - Continues | |
| Appliante at often with | | Lyue J Style U 3 | |
| Longitude | 9 36 23 .6 = | = 144 6' W. | |
| Advis Garage | 20 10 2 | | |

4. On the 29th of March, 1826, in latitude 56° 12′ S., and longitude by account 97° W. at about 7° 20° P. M., the observed distance, between the moon's nearest limb and the star Fomalhaut, was, from a mean of five sets of observations, 61° 56′ 30″; the observed altitude of the moon's lower limb was 32° 4′; the observed altitude of the star 6° 16′; the barometer being 29.2 inches, the thermometer 42° F., and the height of the eye 20 feet: what was the true longitude?

(N)

| Est. time 7 ^h 2 ^m moon's equatorial hor. par. 58' 14" sun's 9" |
|--|
| |
| Long. in time 6 28 reduction for lat. 56° S. — 8 |
| TRUCTURE - THE TRUCTURE OF THE AREA TO THE |
| Est. G. time 13 30 reduced hor. par. 58 6 |
| moon's semidiameter 15 52 |
| augmentation to 32° + 9 |
| augm. semidiameter 16 1 |
| Now to correct the oblique semidiameter by Dr Young's method |
| Now to correct the oblique semidiameter by Dr. roung's method |
| from Tables I. and II. we have |
| $d = 62^{\circ}$ gives $A = 5$ in Table I. |
| s = 6 |
| 20 |
| $f_{0} = \frac{32}{3}$ |
| 100 |
| ger in middle Printed Scholands |
| $h = \overline{50} \qquad = 81 \qquad .$ |
| |
| h-s = 44 = 84 |
| I/O since Con _ O in table II |
| Sum . 170 give Cor. = 0 in table II. |
| Observed distance 61° 56′ 30″ |
| Moon's aug. semidiameter + 16 1 |
| Drug Comment of the C |
| App. central distance |
| Alt. of star 6° 16′ alt. of moon's l. l. 32° 4′ |
| NOT ANY ANY AND ADDRESS OF THE PARTY OF THE |
| Z. D. 83 44 log. # 2.69110, Z. D. 57 56 log. # 1.96844 |
| Thermometer 42° F 0.00730 |
| |
| |
| |
| Thermometer 42° . 9.96020 |
| Thermometer 42° . 0.06034 |
| |
| Thermometer 42° . 0.06034 9.99590 . 9.99590 9.99590 |
| Thermometer 42° . 0.06034 $9.99590 	 . 	 9.99590 	 9.99590$ $r' = 486''.4 2.68700 	 . 	 r = 1' 32'' \log. 1.96434$ |
| Thermometer 42° . 0.06034 $9.99590 	 9.99590 	 9.99590$ $r' = 486''.4 	 2.68700 	 r = 1' 	 32'' 	 \log. 	 1.96434$ Or = 8' 6 .4 |
| Thermometer 42° . 0.06034 $9.99590 	 9.99590 	 9.99590$ $r' = 486''.4 	 2.68700 	 r = 1' 	 32'' 	 \log. 	 1.96434$ $Or = 8' 	 6 	 .4$ $-0''.1 \times -8 = + 	 0 	 .8 	 Moon's 	 alt. 	 32^{\circ} 	 4' 	 secant 	 0.07190$ |
| Thermometer 42° . 0.06034 $9.99590 	 9.99590 	 9.99590$ $r' = 486''.4 	 2.68700 	 r = 1' 	 32'' 	 \log. 	 1.96434$ Or = 8' 6 .4 |
| Thermometer 42° . 0.06034 9.99590 . 9.99590 9.99590 $r' = 486''.4 \ 2.68700 . r = 1' \ 32'' \ \log. 1.96434$ Or = 8' 6 .4 -0''.1 \times -8 = + 0 .8 Moon's alt. 32° 4' secant 0.07190 0''.14 \times \cdot 8 = + 0 .1 Hor. par. $58'$ 6" P.L. 0.49110 |
| Thermometer 42° . 0.06034 9.99590 . 9.99590 9.99590 $r' = 486''.4 \ 2.68700 \cdot r = 1' \ 32'' \ \log. 1.96434$ Or = 8' 6 .4 -0''.1 \times -8 = + 0 .8 Moon's alt. 32° 4' secant 0.07190 0''.14 \times \(8 = + 0 \) .1 Hor. par. $58'$ 6" P.L. 0.49110 $r = 8 \ 7 \ .3$ Par. in alt. $49' \ 14''$ P.L. 0.56300 |
| Thermometer 42° . 0.06034 9.99590 . 9.99590 9.99590 $r' = 486''.4 \ 2.68700 \cdot r = 1' \ 32'' \ \log. 1.96434$ Or = 8' 6 .4 -0''.1 \times -8 = + 0 .8 Moon's alt. 32° 4' secant 0.07190 0''.14 \times \(8 = + 0 \) .1 Hor. par. $58'$ 6" P.L. 0.49110 $r = 8 \ 7 \ .3$ Par. in alt. $49' \ 14''$ P.L. 0.56300 |
| Thermometer 42° . 0.06034 9.99590 . 9.99590 9.99590 $r' = 486''.4 \ 2.68700 \cdot r = 1' \ 32'' \ \log. 1.96434$ Or = 8' 6 .4 -0''.1 \times -8 = + 0 .8 Moon's alt. $32^{\circ} \ 4' \ \text{secant}$ 0.07190 0''.14 \times \(8 = + 0 \) .1 Hor. par. $58' \ 6'' \ \text{P.L.}$ 0.49110 $r = 8 \ 7 \ .3$ Par. in alt. $49' \ 14'' \ \text{P.L.}$ 0.56300 Alt. of star $6^{\circ} \ 16' \ 0'' \ \text{alt. of moon's } l. \ l.$ $32^{\circ} \ 4' \ 0''$ |
| Thermometer 42° . 0.06034 9.99590 . 9.99590 9.99590 $r' = 486''.4 \ 2.68700 \cdot r = 1' \ 32'' \ \log. 1.96434$ Or = 8' 6 .4 -0''.1 \times -8 = + 0 .8 Moon's alt. 32° 4' secant 0.07190 0''.14 \times \(8 = + 0 \) .1 Hor. par. $58'$ 6" P.L. 0.49110 $r = 8 \ 7 \ .3$ Par. in alt. $49' \ 14''$ P.L. 0.56300 |
| Thermometer 42° . 0.06034 9.99590 9.99590 9.99590 $r' = 486''.4 \ 2.68700 \cdot r = 1' \ 32'' \ \log. \ 1.96434$ Or $= 8' \ 6 \ .4$ $-0''.1 \times -8 = + \ 0 \ .8$ Moon's alt. $32^{\circ} \ 4'$ secant 0.07190 0''.14 $\times \cdot 8 = + \ 0 \ .1$ Hor. par. $58' \ 6''$ P.L. 0.49110 $r = 8 \ 7 \ .3$ Par. in alt. $49' \ 14''$ P.L. 0.56300 Alt. of star $6^{\circ} \ 16' \ 0''$ alt. of moon's $l. \ l.$ 32° 4' 0" Dip. to 20 feet $-4 \ 26$ dip. to 20 feet $-4 \ 26$ |
| Thermometer 42° . 0.06034 9.99590 9.99590 9.99590 $r' = 486''.4 \ 2.68700 \cdot r = 1' \ 32'' \ \log. \ 1.96434$ Or $= 8' \ 6 \ .4$ $-0''.1 \times -8 = + \ 0 \ .8$ Moon's alt. $32^{\circ} \ 4'$ secant 0.07190 0''.14 $\times \cdot 8 = + \ 0 \ .1$ Hor. par. $58' \ 6''$ P.L. 0.49110 $r = 8 \ 7 \ .3$ Par. in alt. $49' \ 14''$ P.L. 0.56300 Alt. of star $6^{\circ} \ 16' \ 0''$ alt. of moon's $l. \ l.$ $32^{\circ} \ 4' \ 0''$ Dip. to 20 feet $-4 \ 26$ dip. to 20 feet $-4 \ 26$ |
| Thermometer 42° . 0.06034 9.99590 9.99590 9.99590 $r' = 486''.4 \ 2.68700 \cdot r = 1' \ 32'' \ \log. \ 1.96434$ Or $= 8' \ 6 \ .4$ $-0''.1 \times -8 = + \ 0 \ .8$ Moon's alt. $32^{\circ} \ 4'$ secant 0.07190 0''.14 $\times \cdot 8 = + \ 0 \ .1$ Hor. par. $58' \ 6''$ P.L. 0.49110 $r = 8 \ 7 \ .3$ Par. in alt. $49' \ 14''$ P.L. 0.56300 Alt. of star $6^{\circ} \ 16' \ 0''$ alt. of moon's $l. \ l.$ 32° 4' 0" Dip. to 20 feet $-4 \ 26$ dip. to 20 feet $-4 \ 26$ |
| Thermometer 42° . 0.06034 9.99590 . 9.99590 9.99590 $r' = 486''.4 \ 2.68700$. $r = 1' \ 32'' \ \log$. 1.96434 Or $= 8' \ 6 \ .4$ $-0''.1 \times -8 = + \ 0 \ .8$ Moon's alt. $32^{\circ} \ 4'$ secant 0.07190 $0''.14 \times \cdot 8 = + \ 0 \ .1$ Hor. par. $58' \ 6''$ P.L. 0.49110 $r = 8 \ 7 \ .3$ Par. in alt. $49' \ 14''$ P.L. 0.56300 Alt. of star $6^{\circ} \ 16' \ 0''$ alt. of moon's $l. \ l.$ 32° $4' \ 0''$ Dip. to 20 feet $-4 \ 26$ dip. to 20 feet $-4 \ 26$ App. alt. $6 \ 11 \ 34$ Refraction $-8 \ 7$ semidiameter $+16 \ 1$ |
| Thermometer 42° . 0.06034 9.99590 . 9.99590 9.99590 r' = 486''.4 2.68700 . $r = 1'$ 32" log. 1.96434 Or = 8' 6 .4 -0".1 × -8 = + 0 .8 Moon's alt. 32° 4' secant 0.07190 0".14 × ·8 = + 0 .1 Hor. par. 58' 6" P.L. 0.49110 r = 8 7 .3 Par. in alt. 49' 14" P.L. 0.56300 Alt. of star 6° 16' 0" alt. of moon's $l.$ $l.$ 32° 4' 0" Dip. to 20 feet — 4 26 dip. to 20 feet — 4 26 App. alt. 6 11 34 semidiameter + 16 1 True alt. of star 6 3 27 app. alt. centre 32 15 35 |
| Thermometer 42° . 0.06034 9.99590 . 9.99590 9.99590 r' = 486''.4 2.68700 . $r = 1'$ 32" log. 1.96434 Or = 8' 6 .4 -0".1 × -8 = + 0 .8 Moon's alt. 32° 4' secant 0.07190 0".14 × ·8 = + 0 .1 Hor. par. 58' 6" P.L. 0.49110 r = 8 7 .3 Par. in alt. 49' 14" P.L. 0.56300 Alt. of star 6° 16' 0" alt. of moon's l. l. 32° 4' 0" Dip. to 20 feet — 4 26 dip. to 20 feet — 4 26 App. alt. 6 11 34 semidiameter + 16 1 True alt. of star 6 3 27 app. alt. centre refraction — 32 15 35 — 1 32 |
| Thermometer 42° . 0.06034 9.99590 . 9.99590 9.99590 r' = 486''.4 2.68700 . $r = 1'$ 32" log. 1.96434 Or = 8' 6 .4 -0".1 × -8 = + 0 .8 Moon's alt. 32° 4' secant 0.07190 0".14 × ·8 = + 0 .1 Hor. par. 58' 6" P.L. 0.49110 r = 8 7 .3 Par. in alt. 49' 14" P.L. 0.56300 Alt. of star 6° 16' 0" alt. of moon's $l.$ $l.$ 32° 4' 0" Dip. to 20 feet — 4 26 dip. to 20 feet — 4 26 App. alt. 6 11 34 semidiameter + 16 1 True alt. of star 6 3 27 app. alt. centre 32 15 35 |
| Thermometer 42° . 0.06034 9.99590 . 9.99590 9.99590 $r' = 486''.4 \ 2.68700 \cdot r = 1' \ 32'' \ \log. 1.96434$ Or $= 8' \ 6.4$ $-0''.1 \times -8 = + 0.8$ Moon's alt. $32^{\circ} \ 4'$ secant 0.07190 $0''.14 \times \cdot 8 = + 0.1$ Hor. par. $58' \ 6''$ P.L. 0.49110 $r = 8 \ 7.3$ Par. in alt. $49' \ 14''$ P.L. 0.56300 Alt. of star $6^{\circ} \ 16' \ 0''$ alt. of moon's $l. \ l.$ 32° $4' \ 0''$ Dip. to 20 feet $-4 \ 26'$ dip. to 20 feet $-4 \ 26'$ App. alt. $6 \ 11 \ 34$ semidiameter $+16 \ 1$ True alt. of star $6 \ 3 \ 27$ app. alt. centre refraction par. in alt. $+49 \ 14$ |
| Thermometer 42° . 0.06034 9.99590 . 9.99590 9.99590 r' = 486''.4 2.68700 . $r = 1'$ 32" log. 1.96434 Or = 8' 6 .4 -0".1 × -8 = + 0 .8 Moon's alt. 32° 4' secant 0.07190 0".14 × ·8 = + 0 .1 Hor. par. 58' 6" P.L. 0.49110 r = 8 7 .3 Par. in alt. 49' 14" P.L. 0.56300 Alt. of star 6° 16' 0" alt. of moon's l. l. 32° 4' 0" Dip. to 20 feet — 4 26 dip. to 20 feet — 4 26 App. alt. 6 11 34 semidiameter + 16 1 True alt. of star 6 3 27 app. alt. centre refraction — 32 15 35 — 1 32 |
| Thermometer 42° . 0.06034 9.99590 . 9.99590 9.99590 $r' = 486''.4 \ 2.68700 \cdot r = 1' \ 32'' \ \log. 1.96434$ Or $= 8' \ 6.4$ $-0''.1 \times -8 = + 0.8$ Moon's alt. $32^{\circ} \ 4'$ secant 0.07190 $0''.14 \times \cdot 8 = + 0.1$ Hor. par. $58' \ 6''$ P.L. 0.49110 $r = 8 \ 7.3$ Par. in alt. $49' \ 14''$ P.L. 0.56300 Alt. of star $6^{\circ} \ 16' \ 0''$ alt. of moon's $l. \ l.$ 32° $4' \ 0''$ Dip. to 20 feet $-4 \ 26'$ dip. to 20 feet $-4 \ 26'$ App. alt. $6 \ 11 \ 34$ semidiameter $+16 \ 1$ True alt. of star $6 \ 3 \ 27$ app. alt. centre refraction par. in alt. $+49 \ 14$ |
| Thermometer 42° . 0.06034 9.99590 . 9.99590 9.99590 $r' = 486''.4 \ 2.68700 \cdot r = 1' \ 32'' \ \log. 1.96434$ Or $= 8' \ 6.4$ $-0''.1 \times -8 = + 0.8$ Moon's alt. $32^{\circ} \ 4'$ secant 0.07190 $0''.14 \times \cdot 8 = + 0.1$ Hor. par. $58' \ 6''$ P.L. 0.49110 $r = 8 \ 7.3$ Par. in alt. $49' \ 14''$ P.L. 0.56300 Alt. of star $6^{\circ} \ 16' \ 0''$ alt. of moon's $l. \ l.$ 32° $4' \ 0''$ Dip. to 20 feet $-4 \ 26'$ dip. to 20 feet $-4 \ 26'$ App. alt. $6 \ 11 \ 34$ semidiameter $+16 \ 1$ True alt. of star $6 \ 3 \ 27$ app. alt. centre refraction par. in alt. $+49 \ 14$ |

The state of the s

¥5.

CHI

the 1 ff my all he happed with him

| SPREMICAL INTONOMETRY. | 99 |
|--|--------------------|
| App. dist. 62° 12′ 31″ | Second of such St. |
| 211 | 0.002542 |
| Moon's app. alt. 32 15 35 secant | 0.072816 |
| | |
| | |
| 200 00 10 | Emr's IL |
| Half . 50 19 50 cosine | 9.805067 |
| Diff 11 52 41 cosine . | |
| | 9.997568 |
| Moon's t. alt. 33 3 17 cosine | 9.923322 |
| all Addition to the soul | |
| Sum . 39 6 44 = 3 | 19.791915 |
| and the second s | - |
| Half . 19 33 22 | Director |
| Arc . 38 5 49 cosine . | 9.895957 |
| | |
| Sum . 57 39 11 sine | 9.926766 |
| Diff 18 32 27 sine | 9.502400 |
| 20 02 21. | 0.002100 |
| | 19.429166 |
| The state of the s | 10.120100 |
| $31 13 6\frac{1}{9} sine$ | 9.714583 |
| 2 | 5.71.1000 |
| 2 | |
| True dist. 62 26 13 | + |
| | 0.00004 |
| | 0.60724 |
| 15 61 41 45 1 28 56 P.L. | 0.30621 |
| 15 20 10 10 10 10 10 10 10 10 10 10 10 10 10 | 0.00100 |
| 1 ^h 30 ^m 0 ^s P. L. | 0.30103 |
| Preceding hour 12 | 1 |
| 18 10 W 10 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 | 1 |
| Approximate app. time 13 30 0 at Greenwich. | |
| 64° 40′ 19 | |
| 05 10 41 1 29 56 - 42" - 43" 5 or - 44 | 1" nearly |
| $\begin{array}{cccccccccccccccccccccccccccccccccccc$ | Lincarry |
| 60 13 35 | A CONTRACTOR |
| Now to approximate time 1 ^h 30 ^m , and second difference | -44", the |
| equation of second difference is 5".5, to which and varia | tion 1° 29' |
| nearly in 3 hours, the final equation in time is about 11' t | o be sub- |
| tracted. Whence from 13h 30m this equation of 11s being s | subtracted, |
| the true apparent time is 13 ^h 29 ^m 49 ^s at Greenwich. | 100 |
| To compute the apparent time at ship. | 1 |
| Star's true alt. 6° 3′ 26″ | |
| Polar dist. 59 27 40 cosecant . | 0.064853 |
| Latitude 56 12 0 secant . | 0.254694 |
| Datitude 00 12 0 secant . | 0.20 200 X |
| Sum 121 43 6 | |

| Star's true alt. Polar dist. Latitude | 59 27 40 56 12 0 | | cosecant . | 0.064853 0.254694 |
|---------------------------------------|------------------------|-------------------------------------|-------------|--|
| Sum . | 121 43 6 | 285 MI 98 | 和 班 以 由 | |
| Half . Diff. | 60 51 33 54 48 7 | 10 Oct 10 | cosine sine | 9.68 74 92 9.91 23 09 |
| 4 10 | 101 4 100 101 4 100 | 1 10 10 | | 19.919348 |
| 0 10 | 101 2 10 | 4 ^h 22 ^m 45½° | sine | 9.959674 54 |
| Star's merid. | dist. E. | 8 45 31 | 性 化 机物 | 20 |

SEV. C

1000

THE P

TVILLE

松一個

| Star's merid. distance E. Star's R. A. | . 8 ^h 45 ^m 31 ^s 22 48 1 |
|--|---|
| R. A of merid. Sun's R. A. | 31 33 32 24 32 26 |
| App. time at ship App. time at Green. | 7 1 6 13 29 49 |
| Long. in time Without Eq. 2d diff. | 6 28 43 = 97° 10′ 45″ W. 6 28 54 = 97 13 30 W. |
| Error | 2 45 · W. |

TABLE I.

CORRECTION FOR THE OBLIQUE SEMI-DIAMETER. For Argument A.

| _ | | | | 10, | Argi | men | | | | | |
|---|----------------|----------|-----|-----|------|-----|----|-----|-----|----------|------|
| | For h h- | s | d | For | hh- | 5 | d | For | hh- | <u> </u> | |
| i | ~ | - | | | ~ | | | | ~ | | |
| ۱ | | - | 1 | | - | ~ | - | _ | | ~ | - |
| | ° A | 0 | A | 0 | A | 0 | A | 0 | A | 0 | A |
| | 89 924 | 1 | 176 | 59 | 71 | 31 | 29 | 29 | 94 | 61 | 6 |
| | 88 954 | 2 | 146 | 58 | 72 | 32 | 28 | 28 | 95 | 62 | 5 |
| 1 | 87 972 | 3 | 128 | 57 | 74 | 33 | 26 | 27 | 95 | 63 | 5 |
| | 86 984 | 4 | 116 | 56 | 75 | 34 | 25 | 26 | 95 | 54 | 5 |
| | 85 994 | 5 | 106 | 55 | 76 | 35 | 24 | 25 | 96 | 65 | 4 |
| | | _ | | 54 | 77 | 36 | 23 | 24 | 96 | 66 | 4 |
| | 84 2 | 6 | 98 | 53 | 78 | 37 | | 23 | 96 | 67 | 4 |
| | 83 9 | 7 | 91 | 52 | 79 | 38 | 21 | 22 | 97. | 68 | 3 |
| - | 82 14 | 8 | 86 | 51 | 80 | 39 | | 21 | 97 | 69 | 3 |
| 1 | 81 19 | 9 | 81 | 50 | 81 | 40 | 19 | 20 | 97 | 70 | 3 |
| | 80 24 | 10 | 76 | - | 50 | | | 100 | 100 | 10.0 | - 61 |
| 3 | WO 00 | | | 40 | 00 | 47 | 10 | 70 | | | |
| | 79 28 | 11 | 72 | 49 | 82 | 41 | 18 | 19 | 98 | 71 | 2 |
| | 78 32 | 12 | 68 | 48 | 83 | 42 | 17 | 18 | 98 | 72 | 2 |
| 7 | 77 35 | 13 | 65 | 47 | 83 | 43 | 17 | 17 | 98 | 73 | 2 |
| Ñ | 76 38 | 14 | _62 | 46 | 84 | 44 | 16 | 16 | 98 | 74 | 2 |
| | 75 41 | 15 | 59 | 45 | 85 | 45 | 15 | 15 | 98 | 75 | 2 |
| | 74 44 | 16 | 56 | 44 | 86 | 46 | 14 | 14 | 99 | 76 | 1 |
| | 73 47 | 17 | 53 | 43 | 86 | 47 | 14 | 13 | 99 | 77 | 1 |
| • | 72 49 71 51 | 18 19 | 51 | 42 | 87 | 48 | 13 | 12 | 99 | 78 | 1 |
| | 70 53 | 20 | 49 | 41 | 88 | 49 | 12 | 11 | 99 | 79 | 1 |
| | 10 33 | 20 | 47 | 40 | 88 | 50 | 12 | 10 | 99 | 80 | 1 |
| | 69 55 | 21 | 45 | 39 | 89 | 51 | 11 | 9 | 99 | 81 | 1 |
| | 68 57 | 22 | 43 | 38 | 90 | 52 | 10 | 8 | 100 | 82 | 0 |
| | 67 59 | 23 | 41 | 37 | 90 | 53 | 10 | 7 | 100 | 83 | 0 |
| | 66 61 | 24 | 39 | 36 | 91 | 54 | 9 | 6 | 100 | 84 | 0 |
| | 65 63 | 25 | 37 | 35 | 91 | 55 | 9 | 5 | 100 | 85 | o |
| | 64 64 | 26 | 36 | 34 | 92 | 56 | 8 | 4 | 100 | 46 | 0 |
| - | 63 66 | 27 | 34 | 33 | 92 | 57 | 7 | 3 | 100 | 87 | 0 |
| | 62 67 | 28 | 33 | 32 | 93 | 58 | 7 | 2 | 100 | 88 | ŏ |
| | 61 69 | 29 | 31 | 31 | 93 | 59 | 7 | 1 | 100 | 89 | 0 |
| | 60 70 | 30 | 30 | 30 | 94 | 60 | 6 | ō | 100 | 90 | 0 |
| | | | | | 200 | | | | | - | |

TABLE II.

CORRECTION FOR THE OBLIQUE SEMI-DIAMETER.

DIMINUTION OF THE SEMI-DIAMETER.

Argument A(h)+A(h-s)+A(d).

| -1 | 2.34. | - | - | 1.14.0 | A | ltitud | le. | | 111 | | 07.1 | | - | |
|------------|------------------|-----|-----|--------|----|--------|-----|-----|-----|-----|---------|-----|-----|-----|
| Sum of A | 5° | 6° | 70 | 80 | 9° | 10° | 11° | 12° | 140 | 16° | 18° | 20° | 30° | 45° |
| 0" | 25" | 19" | 14" | 11" | 9" | 8" | 6" | 5" | 4" | 3" | 3" | 2" | 1" | 1" |
| 20 | 24 | 18 | 14 | 11 | 9 | 7 | 6 | 5 | 4 | 3 | 2 | 2 | î | 0 |
| 40 | 23 | 17 | 13 | 10 | 8 | 7 | 6 | 5 | 4 | 3 | | 2 | ī | 0 |
| 60 | 21 | 16 | 12 | 9 | 8 | 6 | 5 | 5 | 3 | 3 | 2 2 2 2 | 2 | 1 | 0 |
| 70 | 20 | 15 | 12 | 9 | 8 | 6 | 5 | 5 | 3 | 3 | 2 | 2 | 1 | 0 |
| 80 | 19 | 14 | 11 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 2 | 2 | 1 | 0 |
| 90 | 17 | 13 | 10 | 8 | 7 | 6 | 5 | 4 | 3. | 2 | 2 | 2 | 1 | 0 |
| 100 | 16 | 12 | 9 | 7 | 6 | 5 | 4 | 4 | 3 | 2 | 2 | 1 | 1 | 0 |
| 110 | 14 | 10 | 8 | 6 | 5 | 4 | 3 | 3 | 2 | 2 | 1 | 1 | 1 | 0 |
| 120 | 11 | 9 | 7 | 5 | 4 | 3 | 2 | 2 | 2 | 1 | 1 | 1 | 0 | 0 |
| 130 | 9 | 7 | 5 | 4 | 3 | 3 | 2 | 2 | 1 | 1 | 1 | 1 | 0 | 0 |
| 135 | 7 | 6 | 4 | 3 | 2 | 2 2 | 2 | 1 | 1 | 1 | 1 | 0 | 0 | 0 |
| 140 | 6 | -5- | 4 | 3 | 2 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 |
| 145 | 5 | 4 | 3 | 2 | 2 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 |
| 150 | 3 | 3 | 2 | 2 | 1 | i | 1 | 1 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 155 | 3 | 2 | 2 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 160 | 0 | 1 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0. | 0 | 0 | 0 | 0 | 0 |
| 170 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 178 180 | | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 182 | 2 3 4 5 | 2 | 2 | 1 | i | î | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 184 | 1 | 3 | 2 | 2 | i | î. | î | 1 | 1 | i | 0 | 0 | 0 | 0 |
| 186 | 5 | 4 | 3 | 2 | 2 | 2 | î | î | 1 | ī | 1 | 1 | 0 | _ |
| 188 | 7 | 6 | 4 | 3 | 2 | 2 | 2 | i | î | î | î | î | 1 | |
| 190 | 9 | 7 | 5 | 4 | 3 | 3 | 2 | 2 | î | î | î | î | î | _ |
| 191 | 10 | 8 | 6 | 4 | 4 | 3 | 3 | 2 | 2 | 1 | 1 | ī | î | _ |
| 192 | 11: | 9 | 7 | 5 | 4 | 4 | 3 | 3 | 2 | 2 | 1 | ī | 1 | |
| 193 | 12 | 9, | 7 | 5 | 5 | 4 | 3 | 3 | 2 | 2 | 2 | 1 | 1 | |
| 194 | 14 | 10 | 8 | 6 | 5 | 4 | 4 | 3 | 2 | 2 | 2 | 2 | 1 | |
| 195 | 15 | 11 | 9 | 6 | 6 | 5 | 4 | 4 | 3 | 2 | 2 | 2 | - | |
| 196 | 17 | 13 | 10 | 7 | 6 | 6 | 5 | 4 | 3 | 3 | 2 | 2 | - | |
| 197 | 19. | 14 | 11 | 8 | 7 | 6 | 5 | 5 | 3 | 3 | 2 | 2 | - | - |
| 198 | 21 | 16 | 12 | 9 | 8 | 7 | 6 | 5 | 3 | 3 | 3 | - | - | - |
| 199 | 23 | 17 | 13 | 10 | 8 | 8 | 6 | 5. | 4 | | - | | - | |
| 200 | 25. | 19 | 14 | 11 | 9 | | - | 110 | - | - | - | - | - | - |
| Alt | 5° | 60 | 70 | 30 | 90 | 10° | 11° | 12° | 140 | 160 | 18° | 20° | 309 | 45° |

TABLE III.

EQUATIONS OF SECOND DIFFERENCE FOR THREE HOURS.

| 1 | COLUMN TO SERVICE SERV | _ | W | , | | | 10 | -11 | - | -50 | | Seco | nd I | iffe | ren | ce. | | | . 0 | 000 | MILI | 10 | | 1 |
|---|--|----|----------|--------------|-----|------|------|------|--------------|------------|----------------|------------|--------------|------------------|-----|--------------|------|------|-----|-----|------|------|----------------|----|
| ı | Tir | ne | | " | " | " | 1 " | 11 | 1 " | " | " | " | " | 1" | [" | " | " | " | " | " | " | " | M. | |
| ı | | | _ | 10 | 20 | 30 | 40 | 50 | 60 | 70 | 80 | 90 | 100 | 1 | 2 | 3 | .4 | 5 | 6 | -7 | 8 | 9 | 171. | ı |
| ı | h. m. | | | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0,0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 06 | 6 |
| 1 | 3 | | | 0.1 | 0.2 | 0.2 | 0.3 | 0.4 | 0.5 | 0.6 | 0.7 | 07 | 0.8 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.1 | 0,1 | | 1 5 | 9 |
| ı | 6 | | 54 | | | | | | 1.0 | | 1.3 | 1.5 | | | | 0.0 | | | | | | | 2 5 | 81 |
| ı | 9 12 | | | | | | | | 1.5 | | 1.9 | 2.1 | | | | $0.1 \\ 0.1$ | | | | | | | 3 5 | |
| 1 | 15 | | 45 | 0.4 | 08 | 1.1 | 1.5 | 1.9 | 23 | 2.7 | 3.1 | 3.4 | 38 | 00 | 0.1 | 0.1 | 0.2 | 0.2 | 0.2 | 0,3 | 0.3 | 0.3 | 5 5 | 5 |
| ı | 18 | | | | | | | | 2.7 | | 3.6 | 4.1 | | | | 0.1 | | | | | | | 6 5 | 44 |
| ı | 21 24 | | | $0.5 \\ 0.6$ | 1.9 | 1.7 | 2.1 | 2.0 | 3.1 3.5 | 4.0 | 4.1 | 4.6 5.2 | 5.8 | 0.1 | 0.1 | $0.2 \\ 0.2$ | 0.2 | 0.3 | 0.3 | 0.4 | 0.4 | 0.5 | 7 53 8 55 | 3 |
| 1 | 27 | | | 0.6 | 1.3 | 1.9 | 2.6 | 3.2 | 3.8 | 4.5 | 5.1 | 5.7 | 6.4 | 0.1 | 0.1 | 0.2 | 0.3 | 0.3 | 0.4 | 0.4 | 0.5 | 0.6 | 95 | i |
| J | 0 30 | 2 | 30 | | 1.4 | 2.1 | 2.8 | 3.5 | 4.2 | 4.9 | 5.6 | 6.3 | 6.9 | $\overline{0.1}$ | 0.1 | | | | | | 0.6 | | 10 5 | ō |
| 1 | 33 | | | | | | | | 4.4 | | 6.0 | 6.7 | | | | 0.2 | | | | | | | 11 49 | |
| 1 | 36 | | 24 21 | 0.8 | 1.6 | 2.4 | 3.2 | 4.0 | 4.8 5.1 | 5.9 | 6.4 | 7.2 | 8.0 | 0.1 | 0.2 | 0.2 | 0.3 | 0.4 | 0.5 | 0.6 | 0.6 | 0.7 | 12 44 13 4/ | 3 |
| ı | 42 | | 18 | 0.9 | 1.8 | 2.7 | 3.6 | 4.5 | 5.4 | 6.3 | 7.2 | 8.1 | 8.9 | 01 | 0.2 | 0.3 | 0.4 | 0.4 | 0.5 | 0.6 | 0.7 | 0.8 | 14 4 | 6 |
| ı | 45 | | | | | | | | 5.6 | | 7.5 | 8.4 | 9.4 | 0.1 | 0.2 | 0.3 | 0.4 | 0.5 | 0.6 | 0.7 | 0.8 | 0.8 | 15 45 | 5 |
| ı | 48 51 | | 12 | | | | | | 5.9 6.1 | | 7.8 8.1 | 8.8 9.1 | | | | | | | | | | | 16 44 17 43 | |
| ı | 54 | | 6 | | 2.1 | 3.2 | 4.2 | 5.3 | 6.3 | 7.4 | 8.4 | 9.5 | 10.5 | 0.1 | 0.2 | 0.3 | 0.4 | 0.5 | 0.6 | 0.7 | 0.8 | 1.0 | 18 45 | 2 |
| ١ | 57 | | 3 | 1.1 | 2.2 | _ | _ | - | 6.5 | | 8.7 | 9.7 | - | | | | | | _ | | | | 19 4 | |
| ı | 1 0 | 2 | 0 | 1.1 | 22 | 3.3 | 4.4 | 5.6 | 6.7 | 7.8 | 8.9 | | 11.1 | | | | | | | | | | | |
| ı | 6 | | 57 | 1.1 | 2.3 | 3.4 | 4.5 | 5.8 | $6.8 \\ 7.0$ | 8 1 | 9.1 | | 11.4 | | | | | | | | | | | |
| 1 | 9 | | 51 | 1,2 | 24 | 3.5 | 4.7 | 5.9 | 7.1 | 8.3 | 9.5 | 10.6 | 11.8 | 0.1 | 0.2 | 0.4 | 0.5 | 0.6 | 0.7 | 0.8 | 0.9 | 1.11 | 23 3 | 7 |
| 1 | 12 | | | | 2'4 | | | | | 8.4 | | | 12.0 | | | | | | | | | | | |
| ١ | 15 | | 45 | | 2.5 | | | | | 8.5 8.6 | | | 12·2 12·3 | | | | | | | | | | | |
| ١ | 21 | 1 | 39 | 1.2 | 2.5 | 3.7 | 5.0 | 6.2 | 7.4 | 8.7 | 9.9 | 11.1 | 12.4 | 0, 1 | 0.2 | 0.4 | 0.5 | 0.6 | 0.7 | 0.9 | 1.0 | 1.1 | 27 33 | 3 |
| 1 | 24 | | 36 | | | | | | | 8.7 | 10.0 | 11.2 | 12.4 | 0.1 | 0.2 | 0.4 | 0.5 | 0.6 | 0.7 | 0.9 | 1.0 | 1.1 | 28 32 | |
| 1 | 27 | 1 | 30 | 1.3 | 2.5 | 3.7 | 5.0 | 6.3 | 7.5 | 88 | $10.0 \\ 10.0$ | 11.2 | 12.5 | 0.1 | 0.2 | 0.4 | 0.5 | 0.6 | 0.7 | 0.9 | 1.0 | 1.1 | 30 30 | |
| | 1 00 | 14 | 200 | | 700 | 1000 | ,000 | 10.0 | 1.0 | 0.0 | 10.0 | AAHO | TWAN | O. I | VO | U. T | 0.01 | 0.01 | 0.0 | 0.0 | 4.01 | 7-11 | 00 | |

TABLE IV.

CORRECTION OF APPARENT TIME FOR EQUATION OF SECOND DIFFERENCE.

| Varia. Capaciton of second Difference. Capaciton of second Difference | . 113 11 |
|--|----------|
| hours, 1 2 3 4 5 6 7 8 9 10 0.1 0.2 0.3 0.4 0.5 0.6 0.7 1 0 0.3 0.6 0.7 1 0 0.1 0.2 0.3 0.4 0.5 0.6 0.7 1 0 3.0 6.0 9.0 12.0 15.0 18.0 21.0 24.0 27.0 30.0 0.3 0.6 0.9 1.2 1,5 1.8 2.2 2.9 5.8 8.7 11.6 14.5 17.4 20.3 23.2 26.1 29.0 0.3 0.6 0.9 1.2 1,5 1.8 2.5 4 2.8 5.6 8.3 11.2 14.1 16.9 19.7 22.5 25.3 28.1 0.3 0.6 0.8 1.1 1.4 1.7 2.6 6 2.7 5.5 8.2 10.9 1.3 6 16.4 19.1 21.8 24.5 27.3 0.3 0.6 0.8 1.1 1.4 1.7 1.6 1.5 8 2.7 5.8 7.9 10.6 13.2 15.9 18.5 21.2 23.8 26.5 0.3 0.5 0.8 1.1 1,4 1.6 1.5 | . 10: 11 |
| 7 (8, 8, 8, 8, 8, 8, 8, 8, 8, 8, 8, 8, 8, 8 | |
| $ \begin{array}{cccccccccccccccccccccccccccccccccccc$ | 0.8 0.9 |
| 2 2.9 5.8 8.7 11.6 14.5 17.4 20.3 23.2 26.1 29.0 0.3 0.6 0.9 1.2 1 5 1.7 2.6 4 2.8 5.6 8.4 11.2 14.1 16.9 19.7 (22.5 52.3 28.1 0.3 0.6 0.8 1.1 1.4 1.7 2.6 6 2.7 5.5 8.2 10.9 13.6 16.4 19.1 21.8 24.5 27.3 0.3 0.6 0.8 1.1 1.4 1.7 2.6 8 2.7 5.3 7.9 10.6 13.2 15.9 18.5 21.2 23.8 26.5 0.3 0.5 0.8 1.1 1.3 1.6 1.5 | 8. 8. |
| 4 2.8 5.6 8.4 11.2 14.1 16.9 19.7 22.5 25.3 28.1 10.3 0.6 0.8 1.1 1.4 1.7 2.6 2.7 5.5 8.2 10.9 13.6 16.4 19.1 21.8 24.5 27.3 0.3 0.6 0.8 1.1 1.4 1.61.5 2 2.7 5.3 7.9 10.6 13.2 15.9 18.5 21.2 3.8 26.5 0.9 3.0 5.0 8.1 11.3 1.61.5 | 2 4 2.7 |
| 6 2.7 5.5 8.2 10.9 13.6 16.4 19.1 21.8 24.5 27.3 0.3 0.6 0.8 1.1 1.4 1.6 1.9 8 2.7 5.3 7.9 10.6 13.2 15.9 18.5 21.2 23.8 26.5 0.3 0.5 0.8 1.1 1.3 1.6 1.5 | 2.3 2.6 |
| 8 2.7 5.3 7.9 10.6 13.2 15.9 18.5 21.2 23.8 26.5 0.3 0.5 0.8 1.1 1.3 1.6 1.9 | 2.2 2.5 |
| | 2.2 2.3 |
| | |
| 12 2.5 5.0 7.5 10.0 12 5 15.0 17.5 20.0 22.5 25.0 0.3 0.5 0.8 1.0 1.3 1.5 1.8 | 2.023 |
| 14 2.4 4.9 7.3 9.7 12.2 14.6 17.0 19.5 21.9 24.3 0.2 0.5 0.7 1.0 1.2 1.5 1.7 | 2.0 2.2 |
| 16 2.4 4.7 7.1 9.5 11.8 14.2 16.6 18.9 21.3 23.7 0.2 0.5 0.7 1.0 1.2 1.4 1.7 | 1.9 2,1 |
| 18 2.3 4.6 6.9 9.2 11.5 13.8 16.2 18.5 20.8 23.1 0.2 0.5 0.7 0.9 1.2 1.4 1.6 | 1.9 2.1 |
| 20 2.2 4.5 6.7 9.0 11.2 13.5 15.7 18.0 20.2 22.5 0.2 0.5 0.7 0.9 1.1 1.4 1.6 | 1.8 2.0 |
| 1 22 2 2 4 4 6.6 8.8 11.0 13 2 15.4 17.6 19.8 21.9 0.2 0.4 0.7 0.9 1.1 1.3 1.5 | 1.8 2.0 |
| 24 2.14.3 6.4 8.6 10.7 12.9 15.0 17.1 19.3 21.4 0 2 0.4 0.6 0.9 1.1 1.3 1.5 | 1.7 1.9 |
| 26 2.1 4.2 6.3 8.4 10.5 12.6 14.7 16.7 18.8 20.9 0.2 0.4 0.6 0.8 1.1 1.3 1.5 | |
| 28 2.0 4.1 6.1 8.2 10.2 12.3 14.3 16.4 18.4 20.5 0.2 0.4 0.6 0.8 1.0 1.2 1.4 | |
| 30 2.0 4.0 6.0 8.0 10.0 12.0 14.0 16.0 18.0 20.0 0.2 0.4 0.6 0.8 1.0 1.2 1.4 | |
| 32 2.0 3.9 5.9 7.8 9.8 11.7 13.7 15.6 17.6 19.5 0.2 0.4 0.6 0.8 1.0 1.2 1.4 | 1.0 1.8 |
| $\begin{array}{c ccccccccccccccccccccccccccccccccccc$ | 1.5 1.7 |
| | 1.5 1.7 |
| | 1.4 1.6 |
| 1 42 1.8 3.5 5.3 7.1 8.8 10.6 12.4 14.1 15.9 17.6 0.2 0.4 0.5 0.7 0.9 1.1 1.2 | |
| 44 1.7 3.5 5.2 6.9 8.7 10.4 12.1 13.8 15.6 17.3 0.2 0.4 0.5 0.7 0.9 1.0 1.2 | |
| 46 1.7 3.4 5.1 6.8 8.5 10.2 11.9 13.6 15.3 17.0 0.2 0.3 0.5 0.7 0.9 1.0 1.2 | |
| 48 1,7 3,3 5,0 6.7 8,3 10,0 11,7 13,3 15,0 16,7 0,2 0,3 0,5 0,7 0.8 1,0 1,2 | 1.3 1.5 |
| 50 11.6 3.3 4 9 6 5 8.2 9.8 11.5 13.1 14.7 16.4 0.2 0.3 0.5 0.7 0.8 1.0 1.2 | 1.3 1.5 |
| 52 1.6 3.2 4 8 6.4 8.0 9.6 11.2 12.9 14.5 16.1 0.2 0.3 0.5 0.6 0.8 1.0 1.1 | |
| 54 1.6 3.2 4.7 6.3 7.9 9.5 11.1 12.6 14.2 15.8 0.2 0.3 0.5 0.6 0.8 1.0 1.1 | |
| 56 1.6 3.1 4.6 6.2 7.8 9.3 11 0 12.4 14.0 15.5 0.2 0.3 0.5 0.6 0.8 0.9 1.1 | 1.2 1.4 |
| 58 1.5 3.1 4.6 6.1 7.6 9.2 10.7 12.2 13.7 15.2 0.2 0.3 0.5 0.6 0.8 0.9 1.1 2 0 1.5 3.0 4.5 6.0 7.5 9.0 10.5 12.0 13.5 15.0 0.1 0.3 0.4 0.6 0.7 0.9 1.6 | 1.2 1.4 |

In the practice of lunars four persons are frequently employed in making the observations, the first to take the distance, the second to take the altitude of the sun or star, the third to take the altitude of the moon, and the fourth to write down the observations. One person, however, may make the whole himself, according to the following method, which was obligingly communicated by that distinguished practical navigator Captain Basil Hall. Speaking of his own practice, he says,-" I always take all my altitudes and distances with the same instrument. First the altitudes of the sun, then those of the moon, then several distances; next the altitudes of the moon, then those of the sun, and interpolating by proportional logarithms for the altitudes at the mean time of the distances.* At night I never take an altitude, unless it be about twilight, when it can be done with accuracy and ease."

"The method which I use to connect lunars and chronometers is not very general, but infinitely the best, and ought to be universally adopted, as it renders all allowance for the distance run in the in-

terval of little or no consequence."

"The use of lunars at sea I conceive is, in a great degree, to check the chronometers: the method by lunars being infallible, though not very nice; that by chronometers being fallible, but as nice as possible. So that a number of lunars are necessary to check a chronometer, and the object is to bring the whole of such lunars to bear rigorously on the chronometer without making use of the

logboard.

W Description "This will be best illustrated by an example. At noon, or any other hour during the day most convenient for taking a lunar, I observe a set, or half dozen sets of lunars with the sun, carefully noting what the chronometer shows, but without taking any account of the actual time. At any other hour when the sun is near the prime vertical, or most suitable for determining the time, I take altitudes expressly with this view, from which I discover the error of the same chronometer used for the lunars. Again, during the night I take lunar distances with the stars, on both sides of the moon if possible, at the moments most favourable, but never mind the exact time, only carefully recording what the chronometer shows. Now by the sights for absolute time I ascertain what was the error of the chronometer on apparent time at that meridian, and this same error, corrected for rate during the interval, I apply to each of the different times by the chronometer when the lunars were taken. By this means I get the apparent times due to the meridian, on which the absolute time sights were taken, with as much accuracy as if the whole, lunars and all, had been taken at that fixed meridian. The distances give the several times at Greenwich, and thus they all concur in settling the difference of time, between the first meridian and that chosen for taking the time, with a view of seeing what longitude the chronometer gives. Hence, if there had been an unseen current of some miles an hour of which no account could possibly be taken, still the result would not be vitiated thereby, but all the lunars would be found to contribute to the same end, thus making, according to Dr Wollaston's simile, the moon serve the purpose of a great Greenwich clock in the heavens. After having

^{*} This is si . ' .r to the method given in Norie's Navigation.

determined the true longitude and error of the chronometers when within a few days sail of the land, I run the remainder of the voyage, in a great degree, by the chronometers alone."

On finding the Longitude. II. BY CHRONOMETERS.

The foregoing method of finding the longitude by lunars is very valuable at sea, on account of the frequent opportunities which occur for observation. About the time of new moon, and in unsteady weather, the necessary observations for the practice of this method cannot be obtained, and the dead reckoning is not to be depended on for any length of time, therefore recourse must be had to other methods.

On account of the very high degree of perfection to which chronometers have been brought, the longitude determined by a mean of three or four of these delicate machines merits great confidence. If the rate of a chronometer be determined on shore, or rather perhaps on board in the situation it is intended to occupy during the voyage, where the various causes which act upon it, and are likely to alter its rate, are in operation, it is likely this rate will remain pretty uniform for some time, and the amount of the gain or loss, being allowed for on the time indicated by it at any future period, the true time may be obtained at the meridian of the place where its rate and original error was determined, with as much accuracy as if it had been adjusted to go accurately to mean solar time on that meridian. Hence, it is obvious, that if the original error, and the gain or loss in 24 hours, called the daily rate, of a chronometer, be known, on any meridian, such for example as that of Greenwich; by making proper allowance for these, the mean time at Greenwich may be readily known to such a degree of accuracy as the going of the chronometer will warrant.

It is now only necessary to find the apparent time at ship, by an altitude of any celestial body properly situated, by some of the methods already given; to which the equation of time being taken from the Nautical Almanac and properly applied, the result will be the mean time to be compared with that at the given meridian to

show the longitude of the ship.

The rate of a chronometer is readily obtained, by observing daily, if possible, the altitude of one or more celestial objects near the prime vertical, from which the mean time may be accurately determined, and, being compared with that shown by the chronometer, its gain or loss in 24 hours, and also its error on the day of the last observation, called the original error, will become known.*

Ex. 1.—Near Falmouth, in latitude 50° 8′ 48″ N., and longitude 20^m 10° W., at about 18^h 47^m 20°, the following altitudes of the sun's lower limb were taken, with an artificial horizon, in order to ascertain the daily rate of a chronometer previously set to Greenwich time. The observations were made with a sextant of which the index error was + 1′ 30″, the barometer 29.6 inches, and the thermome-

ter 56° Fahrenheit.

[•] These would be more accurately performed on shore by using an artificial horizon and the method of equal altitudes. In this case a pocket chronometer should be employed, to be compared with those on board, which ought to be as numerous as possible.

| SIMERICAL INIGONOMETRI. | 100 |
|--|--|
| Times by Chronometer. Double Alt. alt. 19° 3' | only hard |
| And respect to the first of the property of the state of the | 201 |
| 19 ^h 10 ^m 35 ^s 37° 48′ 45″ Z. D. 70 57 log. | 281 |
| 19 ^h 10 ^m 35 ^s 37° 48′ 45″ Z. D. 70 57 log. 12 45 38 4 30 ther. 56° log. | 9.99460 |
| 14 58 38 20 15 bar. 29.6 log. | 9.99417 |
| ther. 56° log. | 9.99974 |
| 3 8 18 3 13 30 | |
| r 163".4 | 2.21282 |
| Means 19 12 46 38 4 30 = 2' 43".4 I. E. + 1 30 sun's parallax 8". | 100 |
| I. E. + 1 30 sun's parallax 8". | 75 - FF |
| 2 38 6 0 | |
| THE PART OF THE PA | Lawrence of the |
| 19 3 0 | 1012-1 |
| Time at Falmouth 18h 47m 20s | Investors. |
| Longitude in time + 20 10 | My 188 |
| 10 ft 00 TO T | 0.0004 |
| Greenwich time 19 7 30 D. L. Daily variation 17' 58" P. L. | 0.09861 1.00080 |
| Daily variation 17' 58" P. L. | 1.00000 |
| Prop. part to 19 ^h 7½ ^m 14 19 P. L. | 1.09941 |
| Dec. at noon, May 1st 15 8 49 | |
| and the second s | |
| | 01 011 |
| | 3' 0" |
| Semidiameter + Refraction + - | 15 53 3 2 43 .4 |
| | 8.1 |
| some trippings | |
| True altitude . 19 | 16 18 |
| Sun's true dec. 15° 23′ 8″ N. secant . | 0.015850 |
| Latitude 50 8 48 N. secant . | 0.193260 |
| 310) L (r | 70 - 01 |
| Difference 34 45 40 | A CONTRACTOR OF THE PARTY OF TH |
| Zenith dist. 70 43 42 | · · · · · · · · · · · · · · · · · · · |
| Sum . 105 29 22 half 52° 44′ 41″ sine | 9.900884 |
| | 9.489599 |
| 103100000 | 3641 |
| | 19.599593 |
| Oh Odm Ode O | O'HOOHOO |
| 2 ^h 36 ^m 23 ^s .8 sine | 9.799796 |
| 2 | |
| Time from noon 5 12 47.6 | |
| 24 | - 444 |
| The state of the s | 13 TOL |
| Apparent time at Falm. 18 47 12.4 | |
| Equation of time — 3 10.9 | T SEC |
| Mean time at Falm. 18 44 1.5 | |
| Time by chronometer 19 12 46.0 | of Second |
| Address of the state of the sta | 1000 |
| Chronometer for Falm. 28 44.5 fast | DE LA |
| | (0) |
| | |

Again, on the 11th of May, 1824, the altitude of the sun's lower limb taken with the same instruments as before, the index error being constant, was 19° 9′ 50″, when the chronometer showed 18h 57m 56°. This gives the mean time at Falmouth 18h 30m 23.5, and the error of the chronometer for the meridian of the place 27m 32.5.

| Whence, on May 1st, the error was | | 10.51 | 28 ^m 44 ^s .5 |
|--|------|--------------|------------------------------------|
| 11th · yg | 81 1 | 81.5 | 27 32.5 |
| The loss in ten days is Or in one day it is | L 10 | 10 11 01 | 1 12 7.2 |
| Hence the daily rate is | I . | 11 1 . 4 . 1 | -7.2 |

It is to be observed, that the altitudes should be taken nearly at the same time of the day, otherwise an allowance must be made for

the rate during the interval.

1. On the 22d of May, 1824, in latitude 32° 36′ N., and longitude by account 16° 40′ W., the altitude of the sun's lower limb at sea was 37° 24′, when the chronometer showed 5^h 12^m 24°.5, the height of the eye being 20 feet; required the longitude?

| Time per. watch | 5 ^h 12 ^m 24.5 Daily rate | 7°.2 |
|--|--|----------------------|
| Original error | - 28 44.5 Loss in 111 days | \[\frac{79.2}{1.8} |
| Loss in 11 days 5 | 4 43 40.0 | 60 81.0 |
| Greenwich M. ti. Alt. sun's l. l. Cor. table XIII. | | 20° 26′ N. + 2 |
| True alt. | 39 · 36 cor. dec. Z. D. | 20 28 N. 69 32 |
| True alt Pol. dist Latitude | 39° 36′ 69 32 cosecant | 0.028318 0.074455 |
| Sum . | 141 44 | Alle Rings |
| Half | 70 52 cosine | 9.515566 9.715186 |
| TO POST OF THE STATE OF THE STA | American Company | 19.333525 |
| - (| 1 ^h 50 ^m 39 ^s sine | 9.666762 583 |
| App. time Eq. of time | 3 41 18 — 3 40 | 179 |
| Mean T. at ship M. T. at Green. | 3 37 38 4 45 1 | miles of the |
| Long. in time | $\overline{1}$ $\overline{7}$ $\overline{23}$ = 16° 51' W. | Property of the |

For the usual computations at sea it is unnecessary to push the calculations farther than the nearest minute.

2. On the 11th of October, 1824, at noon, on the meridian of Greenwich, a chronometer was 11^m 19.4 fast, and the daily rate was + 4.1. On the 21st of October, at 6^h 42^m 10. A. M. by the same chronometer, the observed altitude of the sun's lower limb was 42° 17′ 20″, and the height of the eye 20 feet; required the longitude?

Ans.-33° 25' E.

3. On the 16th August, 1828, in latitude 38° 20′ S., the mean of several altitudes of Antares west of the meridian was 14° 29′, the height of the eye being 12 feet, and the mean of the times per watch 11^h 41^m 38° P. M., which had been compared with mean time at the Cape of Good Hope on the 22d of June, and was found to be 1^h 10^m 28° too slow, and gaining 3°.54 a day; required the longitude of the ship?

Ans.-17° 36' E.

· EQUATION TO EQUAL ALTITUDES.

In ordinary cases the error and rate of a chronometer may be determined by single altitudes; but when great accuracy is required equal altitudes are very superior, especially when a transit instrument cannot be obtained. On this account various tables have been computed to facilitate this operation, though it is believed few of them afford great advantage in actual practice. To those who would prefer such a table, that of D. Josef S. Cerquero, given in the thirteenth volume of the Journal of Science, is perhaps the most commodious and exact. By this means, however, tables would be multiplied to any extent without giving much advantage, on account of the inconvenience of taking proportional parts; and from this consideration it is often better to give an easy practical rule, requiring the use of the ordinary tables, where neither double entries, different signs, nor proportional parts are necessary.

The equation of equal altitudes is a correction for the change of declination of the celestial body during the interval of observation, to be applied to the middle time between the instants shown by a chronometer, at which, on a given day, that body has equal altitudes; to find the true time by the chronometer when the object

was upon the meridian.

Rule.*

To the cosine of half the interval between the times of observation add the cotangent of the latitude, the sum, rejecting 10 in the index, will be the tangent of arc first, the difference between which,

and the polar distance, will be arc second.

Now to the constant logarithm 5.364517, add the cotangent of half the elapsed time, the cosecant of arc first, the cosecant of the polar distance, the sine of arc second, the logarithm of the elapsed time in minutes, the logarithm of the daily variation of the declination in seconds, the sum will be the logarithm of the equation of equal altitudes in seconds of time, which, when applied to NOON, is additive if the polar distance is increasing, and subtractive if it is decreasing.

^{*} See Dr Mackay's or Mr Riddle's Navigation for a similar rule, analogous in principle, though perhaps in the detail somewhat less simple.

If the equation is applied to MIDNIGHT, it is additive if the polar distance is decreasing, and subtractive if the polar distance is increas-

ing.*

Ex. 1.—On the 23d of March, 1809, at Pisa in latitude 43° 43' 11'' N. equal altitudes of the planet Venus were taken before and after transit, the elapsed time between which was $8^{\rm h}$ $50^{\rm m}$; required the equation of equal altitudes when her declination was 20° 42' 40'' N., and her daily variation +20' 5'' or +1205'' increasing, and consequently the polar distance decreasing?

| Latitude | 43° 43′ | | 019462 | C. L. | 5.364517 |
|-----------------|--------------------------------|----------|-------------|---------------|----------|
| H. E. T. | 4 ^h 25 ^m | cos. 9. | 605032 | cot. | 9.643463 |
| Sto ou mirror | m attended to be | 79.1 | March 41 / | | 100000 |
| Arc 1. | 22° 50′ | tan. 9.6 | 524494 | cosec. | 0.411110 |
| Pol. dist. | 69 17 | cosecan | it . | | 0.029030 |
| | - | | 0.00 | The sales | 110 |
| Arc 2. | 46 27 | sine | | | 9.860202 |
| Elap. time | $8^{\rm h} 50^{\rm m} = 3$ | 530m log | Se Constitu | Hall to the | 2.724276 |
| Daily var. dec. | | | | | 3.080987 |
| - 100 | | 0.0 | F.(1 m) | | 0.0000 |
| Eq. E. Alts - | - 12°.99 | 77.5 | rul 1 | le organisma. | 1.113585 |
| -1 | | | | | 7.77000 |

Or subtractive, because the polar distance is decreasing and is to be

applied to noon.

Ex. 2—On the afternoon of the 17th of September, 1810, altitudes of the sun were observed at Marseilles, in latitude 43° 17′ 50″ N., and equal altitudes were taken on the forenoon of the 18th, after an interval of 21^h 50^m, the sun's declination for the 17th at midnight being 2° 14′ 23″ N., and daily variation of declination — 23′ 14″ = —1394″; required the equation of equal altitudes?

Ans.—Equation of equal altitudes — 136°.70.

Or subtractive, for the polar distance is increasing, and is to be ap-

plied to midnight.

Ex. 3.—At Florence, in latitude 43° 46′ 40″ N., on the 8th of April, 1809, equal altitudes of the planet Mars were taken at an interval of 8^h 20^m when his declination was 5° 9′ 40″ S., decreasing at the rate of 6′ 38″ daily; required the correction for the planet's superior passage?

Ans.—Equation of equal altitudes — 5.196.

Or subtractive, because the polar distance is decreasing, and is to be applied to the superior transit.

TO FIND THE ERROR OF A CHRONOMETER BY EQUAL ALTITUDES.

By the Sun.—The sun is in general the most convenient object for determining the error of a chronometer by equal altitudes, and the forenoon and afternoon of the same civil day are often preferred, though the evening and succeeding morning may sometimes be employed with advantage.

In the morning when the sun is more than two hours distant from the meridian, in mean latitudes, let a set of observations be taken with the corresponding times by a chronometer. In the afternoon

^{*} By polar distance in the computation, is meant the distance of the object from the elevated pole, which may be either referred to the north or south pole, according to the name of the latitude.

observe the instants when the sun comes to the same altitude, writ-

ing each time down opposite its corresponding altitude. of de it may

Now half the sum of any two times, answering to the same altitude, will be the approximate time of noon. Find the mean of all the times of noon in this manner from each corresponding pair of observations; to which the equation of equal altitudes being applied, the result will be the time of apparent noon, or the instant that the sun's centre is on the meridian by the chronometer. The difference between this and noon is the error of the chronometer, which will be fast or slow according as the time of noon thereby is greater or less than twelve hours.

Ex. 1.—On the 29th of January, 1826, in latitude 57°9' N., the following equal altitudes of the sun were observed; required the er-

ror of the chronometer?

| Altitudes. | Times A. M. | 7 | imes P. M. |
|--|--------------------------|---|---|
| 8° 5′ | 21h 35m 8s | Y THE | 2h 55m 43s |
| 8 10 8 15 | 36 8 37 9 | Ti li | 54 42 53 42 |
| 8 20 | 38 9 . | 52.55 | 52 41 |
| 8 25 | 39 10 | 10 m | 51 40 |
| WTMOA: | 35 44 | | 15 8 |
| Means. | 21 37 8.8 | 26.1 | 2 53 41.6 |
| | 2 53 41.6 | | 1 37 8.8 |
| Elapsed time | 5 16 32.8 | Sum 2 | 4 30 50.4 |
| Н. Е. Т. | 2 38 16.4 | Half I | 2 15 25.2 |
| Sun's declination at noon, | | | 7° 59′ 15″ S. |
| Daily variation or decreas | se of polar distance | A - 2 - 2 - 2 - 2 - 2 - 2 - 2 - 2 - 2 - | - 16 15 N. |
| Latitude 57° 9′ | cot. 9.810025 | C. L. | 5.364517 |
| H. E. T. 2 ^h 38 ^m | cos. 9.887406 | cot. | 0.083896 |
| Arc 1. 26 29 | tan. 9.697431 | çosec. | 0.350726 |
| Pol. dist. 107 59 | cosecant | Line ton | 0.021753 |
| Arc 2. 81 30 | sine | -1. 1 | 9.995203 |
| | 316 ^m .5 log. | | 2.500374 |
| Daily var. dec. 16' 15" = | 975" log. | of common s | 2.989005 |
| Eq. equal alts — 20°.2 | and the little and | n neighbo | 1.305471 |
| Half sum or approximate | time of noon | -41- | 12h 15m 25°.2 |
| Equation of equal altitude | es . | , | |
| ALC: NO CONTRACTOR OF THE PARTY | | A DATE A | 10 15 5 6 |
| Time of apparent noon by Equation of time with con | trary sign | ing may be a | $ \begin{array}{cccccccccccccccccccccccccccccccccccc$ |
| Marie Contract Contra | | 360 | dia you street |
| Time of mean noon by ch | ronometer | المتالية | 12 1 37.1 |
| Hence the chronometer | was 15" of fast for | apparent | noon, and 1 ^m |

37:1 fast for mean time.

Ex. 2.—On the 24th of July, at Pendennis castle near Falmouth, in latitude 50° 8′ 48″ N., Dr Tiarks, with a sextant of ten inches radius by Mr Troughton, and an artificial horizon, together with a

chronometer by Morice, found the double altitude of the sun's upper limb to be 69° 47′ 20″, at 8^h 29^m 13° A. M., and 4^h 25^m 5°.3 P. M.; required the time of apparent noon by the chronometer?*

| Time after noon 23d per chronometer 20 ^h 29 ^m 13 0 |
|--|
| 24 4 25 $5 \cdot 3$ |
| Sum |
| Half sum, or approximate noon . 12 27 9.15 |
| Difference, or elapsed time |
| Half elapsed time |
| The declination of the sun, at noon 24th, is 19° 58′ nearly. Daily variation 12′ 39″ S., or increasing the polar distance. |
| Latitude 50° 9′ cot. 9.921503 C. L. 5.364517 H. E. T. 3 ^h 58 ^m cos. 9.705469 cot. 9.770148 |
| Arc 1. 22° 57′ tan. 9.626972 cosec. 0.409016 Pol. dist. 70 2 cosecant 0.026922 |
| Arc 2. 47 5 sine 9.864716 |
| Elap. time $7^{\text{h}} 56^{\text{m}} = 476^{\text{m}} \log$. 2.677607 Daily var. dec. $12' 39'' = 759'' \log$. 2.880242 |
| |
| Eq. eq. alts. +9'.844 log 0.993168 To approximate noon |
| Add the equation of equal altitudes . + 9.844 |
| Apparent noon |
| Ex. 3.—On the 24th of July, 1822, at 3 ^h 5 ^m 38 ^s .7 P. M., and 25th July, at 9 ^h 49 ^m 59 ^s .7 A. M. at the same place, the double altitude of |
| the sun's upper limb was 93° 40'; required the apparent time of |
| midnight by the chronometer? Time after noon, July 24th |
| 24 |
| Sum |
| Half sum, or approximate midnight . 12 27 49.2 |
| Elapsed time |
| Half elapsed time 9 22 10.5 |
| Declination at midnight 19° 52′ N., daily variation 12′ 39″ S. Or increasing the polar distance, and the equation is therefore negative for midnight. |

[•] See a Report on Chronometrical Observations to ascertain the longitude of the island of Madeira, by J. L. Tiarks, 1822.

| Latitude 50° 9′ cot. 9.921503 C. L. | 5.364517 | | | | | |
|--|----------------------------------|--|--|--|--|--|
| H. E. T. 9 ^h 22 ^m cos. 9.887406 cot. | 0.083896 | | | | | |
| Arc 1. 32 47 tan. 9.808909 cosec. Pol. dist. 70 8 cosecant | 0.266431 0.026648 | | | | | |
| Arc 2. 37 21 sine | 9.782961 3.050766 2.880242 | | | | | |
| Eq. eq. alts. — 28°.54 log. 1.455461 From approximate midnight 12h 27m 49°.20 Subtract the equation of equal altitudes 28.54 | | | | | | |
| | 27 20 66 | | | | | |

Proceeding in this manner till a considerable number of observations are made, the error of a chronometer may be determined with great accuracy. If this chronometer is compared with any given number of them, all their errors and rates may be found as has been done by Dr Tiarks.

The same thing may be done by the stars, though rather less con-

veniently.

The following method of comparing a chronometer with mean time by Dr Tiarks, communicated by Captain Basil Hall, R. N.,

will be found very useful.

The difference of a chronometer from the mean time at a place. being known at three different instants, to find that difference for any intermediate instant with a proper regard to the change of rate which may have taken place between the first and second, and between the second and third times.

Let the difference at the

times
$$o = a$$

 $t' = a+b$
 $t'' = a+b+c$

So that b is the difference between the first and second states of the chronometer, and c the difference between the second and third states of the same chronometer, the state of a chronometer, (namely, its difference from the mean time of a given place), at the moment t will be

$$+ \left\{ \frac{t}{t'} \frac{(t-t'')}{(t'-t'')} + \frac{t}{t''} \frac{(t-t')}{(t''-t')} \right\} b + \frac{t}{t''} \frac{(t-t')}{(t''-t')} c; \text{ or}$$

$$a + \left\{ \frac{t}{t' \cdot t''} \frac{t}{(t''+t'-t)} \right\} b + \frac{t}{t''} \frac{(t-t')}{(t''-t')} c = \text{correction}$$

If t is less than t', $\frac{t(t-t'')}{t(t'-t'')}$ is positive and $\frac{t(t-t')}{t''(t''-t')}$ is negative, and

if t is greater than t' both are positive.

EXAMPLE.

The difference of a chronometer from the mean time of a certain place was known on the following days:

| 112 | | IN INODE | CIION. | |
|--|-------------------|---------------------|--|-------------------------------------|
| 3 (4) | 4 | Differe | nces. | Days. |
| August 9d.5243 | 21 8003 | And the second | | and 2d=21.8903 |
| 31.4146 | 4.5104 | Dinere | l l | and $3 = 26.4007$ |
| Sept. 4.9250 | | 10.) | THE PERSON NAMED IN | |
| Hence $o = 0$. | | • | Armenia . | n 0, 100 m |
| $\begin{array}{c} t' = 21. \\ t'' = 26. \end{array}$ | 4007 | | and a later | No. 10 |
| | 2007 | i inf | William M. | |
| t' + t'' = 48. | 2910 | - Pul | | |
| It is now requi | ired to fin | nd the sta | te of the chrono | meter for August |
| 17th, at 11h 7m | $44^{\circ} = 17$ | ^d .4637. | Deducting Aug | ust 9d.5243 from |
| August 17°.4637 | we have | the interv | al $t = 7^{\circ}.9394$. | |
| t' + t'' = 48.29 | 910 - | V 000400 | t' = 21.8903 | log. 1.340252 |
| 1900 7.98 | 194 log. | 0.899788 | t'' = 26.4007 | log. 1.421616 |
| t'+t'-t = 40.35 | 16 lor | 1 605861 | # v # 10m | 2.761868 |
| 1 To -1 -1 10100 | To log. | 1.000001 | , X, 10g. | 2.701000 |
| $t \times (t'+t''-t)$, or nu | im. log. | 2.505649 | Well on the least | A september of the street, and |
| t'xt" or denominat | tor, log. | 2.761868 | manage Francisco | -704 L 334 A 119 |
| | . , . | | . 70 mg 11 mg 11 mg | and the second |
| . t smin | 1 Tor | 0 743781 | or factor of b | right some little |
| $\frac{t}{t'\times t''}\times (t'+t''-t)$ | | | | . Latintonia. |
| t = 7.9394, | log. | 0.899788 | t'' = 26.4007 | log. 1.421616 |
| t' = 21.8903 | C MINNING | 1 Set 1920 H | t' = 21.8903 | TE-14 3/1 up-19 |
| t'=t=139509 | low | 1 144600 | W W A 510A | 107 0 654015 |
| | | | | |
| numerator | log. | 2.044390 | t'' $(t''-t')$ denor | n. log. 2.075831 |
| denominator | log: | 2.075831 | The state of the s | Senie Land Line |
| | 0 | | and with hom ! | most officernt |
| $\frac{t (t-t')}{t'' (t''-t')} \log.$ | | 9 968559 | or factor of c v | hich is negative, |
| | 11.7 | 0.000000, | of factor of c v | men is negative, |
| because t is less the | nan t' . | 91 | | 1-1-3 D: M |
| August 9th, 126 | 95m -10 | | 1 Elm E#s 9E | Diff. |
| | | | | a legicol z |
| 31st, 9 | DOTAL TO SERVICE | alele ed) | . 54 10.33 | |
| Sept. 4th, 22 | | o cho mi | 54 39.16 | 28.83 c |
| What is the diff | ference, | August 17 | 7th, 11 ^h 8 ^m . | William I |
| $b = 132^{\circ}.98$ | log. 2.1 | 23782 | c = 28.83 | log. 1.459845 |
| factor b. | log. 9.7 | 43781 | factor c | log. 9.968559 |
| $(f) b = +73^{\circ}.72^{\circ}$ | log 18 | 67563 | (f) 6-96 | 82 log. 1.428404 |
| (f) c = -26.82 | Tog. Tio | (1 | 0 10-20 | 02 10g. 1.120101 |
| (1) | | | / V | The second second |
| cor. = + 46.90 | to be ap | plied to | the error of the | chronometer at |
| the time a . | | 1,614 | | |
| August 9th, 12 ^h 3 | | | ow for M. T. | 51 ^m 57 ^s .35 |
| | correc | ction | | . + 46.90 |
| Chronometer clow | for mean | n time | | . 52 44.25 |
| On August 17th, | at 11h 7m | 448 * | and of the latest terminal | . 52 77.20 |
| On aluguet a full, | | 1 5 CON 125 T | | 2 - 7 9 6 4 1 2 |

^{*} For Rossel's method of correcting the error in rate of a chronometer, see Biot's Astronomie, vol. III., or Myer's translation of this, page 95.

| | Tabl Decimal Fraction | ~ ~- | Day of 24h. | Deci | Table II. Decimal Parts of an Hour. | | Table III. To convert Decimals of Time into Degrees at 15° to an Hour. | | |
|----|---|--|---|--|---|--|--|--|--|
| N. | T. Decimal. | 7 | . Decimal. | T | Decimal. | T, | Arc. | | |
| | 1 ^h 0. ^h 041667 2 0. 083333 3 0. 125000 4 0. 166667 5 0. 208333 6 0. 250000 7 0. 291667 8 0. 333333 9 0. 375000 | 20 30 40 50 1 2 | h.006944 .013889 .020833 .027778 .034722 .000694 .001389 .002083 | 20 30 40 | h.166667 .333333 .500000 .666667 .833333 .016667 .033333 .050000 | 0.2 0.3 0.4 0.5 0.6 0.7 | 1".5 3 .0 4 .5 6 .0 7 .5 9 .0 10 .5 12 .0 13 .5 | | |
| | 10 0. 416667 11 0. 458333 12 0. 500000 13 0. 541667 14 0. 583333 15 0. 625000 | 5 6 7 8 9 10 ^s 20 30 40 | .003472 .004167 .004861 .005556 .006250 .000116 .000232 .000348 .000464 .000580 .000012 .000023 .000035 | 5 6 7 8 9 10 ^s 20 30 40 | .083333 .100000 .116667 .133333 .150000 | 0.01 0.02 0.03 0.04 0.05 0.06 0.07 0.08 0.09 0.001 0.002 0.003 0.003 | 0 .15 0 .30 0 .45 0 .60 0 .75 0 .90 1 .05 1 20 1 .35 0 .015 0 .030 0 .045 0 .060 0 .075 | | |
| ŀ | For 12 ^h double that for 24 ^h . | 4 5 6 7 8 9 | .000046 .000058 .000069 .000081 .000092 .000104 | 4 5 6 7 8 9 | .0011110 .0013890 .0016670 .0019440 .002222 .002500 | 0.007 | 0 .090 0 .105 0 .120 0 .135 | | |

Explanation.

Table I. contains the decimal fraction of a day of 24^h. It is useful for finding what part of a day any number of hours, minutes, and seconds are, and consequently may be conveniently employed in many calculations where daily differences are necessarily involved, such as the daily rate of a clock, the change of which, in any given number of hours, &c. may be thereby readily obtained. It is also very useful in the preceding method of comparing chronometers, and other purposes.

Table II. serves the same purpose when an hour is taken for

unit, and is useful in several astronomical operations.

Table III. is supplementary to the general Table V. which serves to convert time into degrees if less than 6^h or 90°. But as 6^h answers to 90°, 12^h to 180° and 18^h to 270°, this table will easily be applied to 24^h or 360°, the whole circle to every four seconds of time, and

by the proportional parts at the bottom to every single second. Whence it is only necessary to convert the decimal part of the time into degrees by this table to complete the whole.

III. BY OCCULTATIONS AND ECLIPSES.

The moon in her periodical revolution frequently passes between the earth and a fixed star, of which she intercepts the spectator's

view, thus, producing what is called an occultation.

Since the instant of disappearance and reappearance of the star can be ascertained without the use of any instrument liable to error, the longitude may be determined more accurately by an observation of this phenomenon, than by a lunar distance. An observer possessed of an ordinary telescope, a chronometer, and an instrument to determine its error and rate,* can readily make the observations; and the necessary calculations are far from difficult. Several rules have been proposed for this purpose independent of the method of determining the parallaxes by the nonagesimal, and comparatively much more simple. Of these, Dr Inman's of Portsmouth, which we shall in the mean time adopt with some alterations, appears to us the most convenient.

At the instant of the disappearance or reappearance of the star, the apparent right ascension and declination of the point of the moon's limb in contact with the star is the same as the right ascension and declination of the star, which can be obtained with great facility and accuracy from tables. The apparent right ascension and declination of this point being corrected for parallax, its true right ascension and declination will be determined. Now since the distance of this point from the moon's centre, which is equal to her semidiameter, and the declination of the centre for the estimated time at Greenwich, may be found by the Nautical Almanac, the true right ascension of the moon's centre is easily computed. Should there be an uncertainty in the estimated Greenwich time amounting to about one minute, the operation must be repeated, till the estimated and computed Greenwich time be very nearly the same.

Rule.

By applying the estimated longitude in time to the observer's apparent time, the reduced Greenwich time to the nearest minute will be obtained.

To this time take from the Nautical Almanac the sun's R. A., the moon's R. A. and their declinations corrected for second differences, together with the variation of declination for 10°, for the purpose of repeating the operation when supposed necessary; and the moon's semidiameter, and the horizontal parallax corrected for the spheroidal figure of the earth.

Take also the moon's R. A. for 3h after the first estimated time

corrected as formerly.

Find from the Nautical Almanac, or from other tables, the apparent R. A. and D. of the observed fixed star; and reduce the given latitude for the spheroidal figure of the earth.

^{*} If the observations are made at sea, an allowance must be made for the rate of the chronometer between the disappearance and reappearance of the star and the run of the ship, as in lunars.

To the apparent time add the sun's R. A., and from the sum, increased if necessary by 24^h, subtract the star's R. A.; the remainder, if less than 12^h, will be the hour angle; if greater than 12^h, its com-

plement to 24h will be the hour angle.

Now write down the proportional logarithm of the reduced horizontal parallax under the numbers (1), (2), and (3). Under (1) and (2) put the secant of the reduced latitude; under (3) the cosecant of the same; under (1) the cosecant of the hour angle (a), and take the sum of these.

Below the sum of the three logarithms under (1) put the constant logarithm 1.17609, and the cosine of the star's declination; at the same time under (2) put the cosecant, and under (3) the secant of the same; the sum of these three logarithms under (1) will be the proportional logarithm of arc first, or the parallax in R.A. in time, nearly; one half of which (b) is to be subtracted from the hour an-

gle (a), giving (a-b), the corrected hour angle.

Under (2) put the secant of the hour-angle thus corrected. sum of the logarithms under (3) will be the proportional logarithm of the first part of the parallax in declination, and that under (2) the second. The first part must be applied with such a sign as to diminish the star's distance from the elevated pole: the second must be applied with the same sign as the first, if the hour-angle and polar distance are the one greater, and the other less than 90° or 6h; otherwise with a contrary sign. The result will the true declination of the observed point of the moon's limb. Take the difference between this true declination of the observed point and the declination of the moon's centre, found from the Nautical Almanac, under which put the moon's horizontal semidiameter properly corrected, and take the sum and difference. Add together the proportional logarithm of this sum and difference, and take half the sum, to which add the cosine of the mean of the two declinations just found, the sum will be the proportional logarithm of the moon's semidiameter in R. A. nearly.

Under (4) put the constant logarithm 1.17609, the first sum under (1), and the cosine of the declination of the observed point, the sum will be the proportional logarithm of the exact parallax of R. A. in time. This being added to the star's R. A. when west of the meridian, but subtracted if east, will give the true R. A. of the point observed. To the true R. A. thus obtained add the moon's semidiameter in R. A., or subtract it therefrom, according as the reappearance or disappearance of the star has been observed, and the result will be the true R. A. of the moon's centre deduced from observa-

tion.

If this differs considerably from the R. A. taken from the Nautical Almanac, alter the moon's declination by as many seconds as will make a corresponding variation in the first R. A. such as the Nautical Almanac would give for the same alteration in declination. Repeat the operation till this is the case, and the last R. A. will be that required.

Under this put the moon's (1) R. A. taken from the Nautical Almanac for the Greenwich time, and then the moon's R. A. three hours after, or the (2) R. A. Take the difference between the first and second, and the difference between the second and third. Then from the proportional logarithm of the first difference subtract that of the second, the remainder will be the proportional logarithm of a

portion of time which must be added to the Greenwich time when the first R. A. is greater than the second; otherwise subtracted; and the result will be the Greenwich apparent time. The difference between this and the apparent time of the observer will be the longitude in time.

Ex. 1.—On the 3d of March 1823, at Bahia, in latitude 12° 57′ 17″ S., and longitude by estimation 38° 30′ W., the reappearance of Antares from the dark limb of the moon was observed at 15^h 30^m

0°.3; Required the true longitude?

| Bahia, March | 3d, | $15^{\rm h}$ | $30^{\rm m} 0^{\rm s}.3$ | Moon's 1st R.A. 244 | ° 27 | 29 | ″.75 |
|---------------|-----------------|--------------|--------------------------|---------------------|-------------|-------|---------|
| Lon. in time | | 2 | 34 | 2d R.A. 246 | 6 | 16 | .82 |
| D + 1 | | | | Dec. 25 | 55 | 15 | .6 S. |
| G. est. time | | 18 | 4 | var. for 10°+ | | | .63 S. |
| To this time. | | | | hor. S.D. | 14 | 50 | 3 |
| Sun's R.A. | 22^{h} | $56^{\rm m}$ | 58s.64 | eq. par. | 54 | 26 | .5 |
| Antares R.A. | 16 | 18 | 35.8 | red. to 13° | | 0 | .5 |
| Dec | 26 | 1 | 50.1 | 11971 - 11971 - 1 | | 1 | |
| 1000 | | | | red. par. | 54 | 26 | .0 |
| App. time | 15 ^h | 30 | 0.3 | and the same | | | |
| Sun's RA. | 22 | 56 | 58.64 | latitude | 120 | 57' | 17" S. |
| | | | | red. to 13° S. | _ | 5 | 0 |
| Sum . | 38 | 26 | 58.94 | | | | THE CO. |
| Antares R.A. | 16 | 18 | 35.82 | red. lat. | 12 | 52 | 17 |
| | | V. | | | 3. | - EM | 6 |
| Diff | 22 | 8 | 23.12 | | > | YORK | 81 |
| | 24 | - 1% | | | | | 1000 |
| 1111 | | | | 8.1. | or house | | 707 |
| Hour angle | 1 | 51 | 36.88 | | * - | | A SOR |
| 0 | | | | | Section All | V - 7 | Table 1 |

As it is convenient that the work should follow from beginning to end in regular order, that of the foregoing example has been transferred to the two following pages, and to avoid unnecessary waste of room, the remainder of this has been filled with the following example for exercise:—

Ex. 3.—On the 26th of May, 1822, at San Blas in latitude 21° 32′ 25″ N., and longitude by estimation 105¼° W., at 9h 22m 41° 3, A.T. the immersion of a Leonis was observed by Lieutenant H. Foster, then Master's Mate of his Majesty's ship Conway; what was the true longi-

the second secon

AND THE RESERVE THE RESERVE THE PERSON NAMED IN

- Charles I to the first the second to

And the second s

The state of the said of the said of the

MINE A STORY BUT THE

tude?

Ans.—105° 18′ 27″ W.

| G. L. 1.17609 | 0.86021 | | | 9.95415 | 1.99045 | 244 11′ 21″ |
|---|-------------------------------|---------------------------------------|---|--|---|--------------------------------|
| (3) 0.51941 0.65216 0.04645 | 1.21802 | | A SELLIN | Separate Sep | (4) 0 ^h 1 ^m 50°.4 P. L. | 16 18 35.8 16 16 45.4 = |
| 941 P. L. 104 cosec. 768 sec. | . P. L. | | 276 | 089 P. L. | (4) 0 ^h | **s R. A. 16 T. R. A. 16 |
| P. L. 0.51941 ** dec. S. 0.35768 | | 12' 43 .8 S. | 0.05276 | (3) 0 20 37 .5 N. 0.94089 25 52 6 .3 cosine | 25 55 15 .6 | 3 9 .3 14 50 .0 17 59. 3 |
| (1) 0.51941 0.01104 0.32976 | 0.86021 | 1.17609 26° 12′ 43 .8 S. 1.98975 | (a) | 8.8 | 25 | Difference)'s semidia.]Sum |
| 26" P. L. secant 36'.9 (a) cosec. | P. L. | C. L. 1" 50.6 P. L. | 0. 0 55.3 (b) 1 50 41.6 (a-b) secant | | nation | 2 |
| Moon's h. par. 0° 54' 26'' Reduced lat. 12 52 17 Hour angle 1° 51" 36'.9(a) | Sum **s declina. 26° 1′ 50″.1 | Arc (1) 0 ^h 1 ^m | Half . 0, 0 Difference 1 50 | Moon's true declination | Moon's reduced declination | B 4 3 7 1 1 1 1 |

Est. time 18

| Sum Sum | | 17' 59".3 | P. L. | P. L. 1.00028 | T. R. A. arc (5) | T. R. A. 244° 11 21" arc (5) + 16. 7 | 110 |
|---------------|-------------------|-----------|-------|--------------------------|---|--|-----|
| Differ Sum | ence | 11 49 .7 | P. L. | P. L. 1.18790 2.18818 | C. R. A. 1 | C. R. A. P. 244 27 28 Jst R. A. 244 97 30 | |
| Half | . 44 | 2.8 | | 1.09409 | 2d R. A. | 2d R. A. 246 6 16 | |
| Cos | Cosine | • | | 9.95405 | 9.95405 3.73239 P.L. 1st diff. 0° 0′ 2″ | 00 00 5% | |
| Arc | Arc (5) . 16 6 .7 | 16 6 .7 | P. L. | P. L. 1.04814 | 0.26066 P.S. 2d diff. | 1 38 46 | |
| | | | | | 3.47173 P.L. P. P. | Oh Om 38.7 | |

Green, T. 18 3 56.3 Bahia T. 15 30 0.3 L. in T. 2 33 56.0 in deg. 38° 29′ 0″ W.

Ex. 2.—On the 20th of July 1823, at Rio Janeiro, in latitude 22° 54' 10" S., and estimated longitude 43° 15' W. the disappearance of A Sagittarii behind the moon's dark limb was observed at 6th 49th 9.2; What was the true longitude?

| Rio Janeiro, Ju | aly 20, 6 ^h 49 ^m 2 53 | Moon's 1st R.A. 2d R.A. 2 | 273° 16′ 59″ 274 54 48 |
|-----------------|--|---------------------------|-----------------------------|
| Lon. in time | . 2 03 | var. in 10° | + 5.44 |
| Est. Greenwich | | dec. | 25 39 21 S. |
| To this time. | | var. in 10° | - 0.3S. |
| Sun's R.A. | 7 ^h 57 ^m 23' .7 | hor. S.D. | 14' 52" |
| Star's R.A. | 18 17 7 .3 | eq. par. | 53 58 |
| Dec. | 25° 30 31".0 | red. to 23° | _ 2 |
| App. time | 6 ^h 49 ^m 9 ^s .2 | 1 | |
| Sun's R.A. | 7 57 23 .7 | red. par. | 53 56 |
| 1 1 | | latitude | 22° 54′ 10″ S. |
| Sum . | 14 46 32 .9 | reduc. | — 8 12 |
| Star's R.A. | 18 17 7 .3 | | |
| | | red. lat | 22 45 58 S. |
| Diff. | 20 29 25 .6 | 19 | |
| | 24 | | |
| | 0.00.04.4 | | |
| Hour angle | 3 30 34 .4 | | = 1 3,0 = 1 |
| | The state of the s | | |

It is hardly necessary to give the variation of the sun's R. A. and D. in 10°, as it is very small, and as the true time must differ but a few seconds from the estimated, on repetition the longitude cannot vary much on this account.

Ex. 4.—On the 3d of January, 1825, at Port Bowen, in latitude 73° 13′ 40′ N., and longitude by estimation 5h 56m W, the immersion of z Geminorum of the 4th magnitude was observed at 6th 14th 23.26 M. T., and the emersion at 7 11 12.17 M. T., by Lieutenant Henry Foster, R. N.; what was the true longitude?

Ans.—By immersion the longitude is 5h 55m 48, and by emer-

sion it is 5^h 55^m 35^s W.

It was intended, if room would have permitted, to put the whole of the calculation on one page, and, though not done here, may readily enough be so placed by the calculator. This little attention ought not to be slighted, as a neat form, like a convenient formula, will be found of some service in accurate computations.

| 1.17609 | | ant und | 9.95511 | 1.78954 | | 3, 0,, |
|--|------------------------|---------------------------|-----------------------------------|--------------------|------------------------|---------------------------------------|
| i | | | | .3 P.L. | ر ب | *'s T. R. A. 18 14 12.0 = 273° 33′ 0″ |
| (3) 0.52342 0.41231 0.04454 | -ger -ger man | ii. | | arc (4) 0h 2m 55.3 | 18 17 7 | 18 14 12 |
| P. L. cosec. secant P. L. | lar | 0.1 | 20 os 10 71 01 | arc (4) | **s E. R. A. 18 17 7.3 | "s T. R. A. |
| (2) 0.52342 0.03522 0.36588 | | 0.21337 | 1.13789 cosine | | | |
| . L | 25 49 21 S. | al . | 13 7 N. 25 36 14 S. | 25 39 21 | 3 7 | 17 49 |
| $\begin{array}{c} (1) \\ 0.0352342 \\ 0.09970 \\ \hline 0.09970 \\ \hline 0.056334 \\ \hline 0.056334 \\ \hline 0.117609 \\ \hline (2) \\ 0.0187 \\ \hline 0.08234 \\ \hline 0.0910 \\ 0.0910 \\ \hline 0.0910 \\ 0.0910 \\ \hline 0.0910 \\ 0.0910 \\ \hline 0.0910 \\ 0.0910 \\ \hline 0.0910 \\ 0.0910 \\ \hline 0.0910 \\ 0.0910 \\ \hline 0.0910 \\ 0.0910 \\ \hline 0.0910 \\ 0.0910 \\ \hline 0.0910 \\ 0.0910 \\ \hline 0.0910 \\ 0.0910 \\ \hline 0.0910 \\ 0.0910 \\ \hline 0.0910 \\ \hline 0.0910 \\ 0.0910 \\ \hline 0.0910 \\ 0.0910 \\ \hline 0.0910 \\ \hline 0.0910 \\ 0.09$ | und wa | | (3) | 25 | D. | |
| 00 010 1 | 9.95545 | secant | moordi njenoron i reflessie | | Diff. Moon's S D | Sum |
| 9° 53° 56° P. L. 29° 45° 58 secant 3° 30° 34° .4(a) cosec. P. L. C. L. | 31 cos. 55.2 P. L. | 1 27.6 (b) 9 6.8 (a—b) | 14" | 21 | 15 35 | 37 47 .5 |
| 0° 53' 56" 22 45 58 3° 30° 34 | 25 30 31 2 55 | 2 29 | s. 25° 36′ 14″ | . 25 39 21 | 51 15 | 25 37 |
| Ys R. hor. par. Red. latitude Hour angle | Moon's dec. Arc (1) | · · | Moon's true dec. | Moon's est. dec. | | . JI |
|)'s Red Hou | Mo | Half | Mo | Mc | Sum | Half |

9h 42m

Est. time

Long. in T. Or in degrees

G. T. July 20 Rio Jan. T.

| 0,, | 99 | 4 | 69 | 8 | 20 | 6 | |
|-------------|---------------|----------------------|---------------------|-----------|-----------------------------|----------------------------------|--|
| 273° 33′ 0″ | - 15 56 | C. R. A. P. 273 17 4 | lst R. A. 273 16 59 | 274 54 48 | 71 | 0.26486 = 2d diff. P. L. 1 37 49 | රී |
| | 1 | 273 | 273 | 274 | + | r. 1 | + |
| = 0 | 5) | A. P. | . A. | 2d R. A. | iff. P.] | iff. P. 1 | cor. |
| 18 14 12.0= | arc (5) | C. R. | 1st B | 2d R | 3.34445 = 1st diff. P. L. + | 2d di | 3.06959 P. L. cor. + |
| 18 14 | | | | | 445 = | 486= | 959 |
| 1 | | | | | 3.34 | 0.26 | 3.06 |
| | 0445 | 1.19144 | 2.19589 | 1.09794 | 9.95502 | 1.05296 | |
| , | P. L. 1.00445 | 1.1 | 2.1 | 101 | 6.6 | 1.0 | |
| | P. L | P.L. | | ١. | • | | lmost |
| -6 | | | | The I | * | | it is a |
| 45 | 17 49 | 35 | | 3) | | • | : 0".3, |
| . 14 42 | 17 | 11 35 | | 1 | | 26" | about |
| 01 0 | | - 7 | | | 51. | Arc (5) — 15' 56" | aly be |
| ('s S. D. | m | # | В | H | Cosine | c (5) | o plu |
| | Sum | Diff. | Sum | Half | | Are | 9° wo |
| | | r 0 | | | | | on for |
| 7 47. | | 5 | | - | | _ / | linati |
| 25 37 47.5 | 1 | | B Th | 33 | | - Marie | in dec |
| | - 1 | | | | 179 | 25 | As the variation in declination for 9 would only be about 0".3, it is almost |
| 6.3 | | 34 | | | | 1 140 1 140 | e varia |
| lalf | - | | 8 | - | -13 | 1 | As th |

As the variation in declination for 9° would only be about 0.3, it is almost unnecessary to repeat the final part of the work, unless the operations were carried to fractions of a second.

(Q)

BY AN ECLIPSE OF THE SUN.

An eclipse of the sun depends upon the same cause as an occultation, his light being intercepted by the body of the moon passing between him and the spectator. The beginning and end of a solar eclipse is easily observed by a telescope of moderate power properly prepared, when the point of contact of the limbs being nearly known, and the rule for computing the longitude is similar to that now given for an occultation. If the semidiameter of the moon passing through that point of the sun and moon, apparently in contact, be supposed to be produced to the centre of the sun, as seen from the observer, and conceiving this centre to be at the distance of the fixed stars, so as to have no sensible parallax, then it is manifest, that the rule for an occultation must apply by substituting for the moon's semidiameter the sum of the sun and moon's semidiameters, considering the sun to be at the same distance as the moon when seen from the earth's centre,—that is, subtracting the augmentation for the sun's semidiameter as if it were the moon's from it, as found in the Nautical Almanac. In the supposition just made, the sun's centre was supposed to have no parallax; but, as it has a horizontal parallax of about 8".7, in finding the apparent place we cannot proceed exactly as for a fixed star. The sun's right ascension and declination, as seen from the centre, must be taken from the Nautical Almanac, which, corrected for parallax, will give the apparent right ascension and declination, thus reducing the case of a solar eclipse to a similarity with that of an occultation. The apparent right ascension and declination of the sun's centre must now be corrected, using the horizontal parallax of the moon in the computation. This would evidently give the same true place as if, taking the right ascension and declination of the sun's centre from the Nautical Almanac, we considered these elements as apparent, and corrected them for parallax, instead of the moon's horizontal parallax employing the difference between the horizontal parallaxes of the sun and moon.

Whence the true right ascension of the point answering to the sun's centre is obtained, and consequently, as formerly, the true right ascension of the moon's centre, from which the Greenwich apparent time is determined. The apparent time of the observer is found by means of a chronometer, whose error and rate have been determined by double altitudes if possible, if not, by altitudes both

to the east and west of the meridian.

Rule.

By applying the estimated longitude in time to the observer's apparent time expressed astronomically, the Greenwich time will be obtained to the nearest minute. For this time take from the Nautical Almanac the sun's right ascension and declination, the sun's semidiameter diminished by the augmentation, the moon's right ascension and declination, semidiameter and horizontal parallax corrected for the spheroidal figure of the earth, and diminished by the sun's horizontal parallax. Take also the moon's R. A. for 3 hours after the first R. A., or estimated Greenwich time.

Find the hour angle, which, in the afternoon, is the observer's apparent time, and in the morning its complement to 24 hours.

Employing the moon's diminished horizontal parallax, correct the

sun's right ascension and declination, as if for some point on the moon extended, proceeding as formerly, only putting the sum of the sun's semidiameter, diminished by augmentation and the moon's semidiameter, instead of the moon's semidiameter alone. If the resulting Greenwich time differ from the estimated, the sun's R. A. and declination must be corrected for the difference, repeating the operation as often as necessary, till the Greenwich time by computation and estimation agree.

Ex.—On the 7th of September, 1820, at the Royal Naval College, Portsmouth, in latitude 50° 48′ 3″ N., and longitude by estimation 1° W., the end of a solar eclipse was observed at 3^h 12^m 55°; requir-

ed the true longitude?

| ca die dae longi | aude. | | | | | |
|------------------|----------------------------------|-------------------------|---------------|-----|-----|---------|
| Ports. Sept. 7. | 3 ^h 13 ^m M | loon's (1) R. A. | 166° | 54' | 47" | Silver |
| Lon. in time | 4 | var. in 10 ^s | | | 4" | . 4 |
| | 2 40 | (2) R. A | 168 | 13 | 26 | 15 KIS |
| Est. G. T. | 3 7 . | dec. | 6 | 21 | 4 | N. |
| To this tin | | var. in 10° | | | 1 | .84 S. |
| Sun's R. A. 11h | 4m 13s.60 | hor. S. D. | | 14 | 42 | .7 |
| Var. in 10s | 0.025 | equa. par. | | 53 | 56 | .0 |
| Dec 5° ! | 58' 22" N. | red. to lat. | | - | 6 | .3 |
| Var. in 10° | 0 .16 | | | - | | - |
| Semidia. | 15 54 . 8 | red. par | | 53 | 49 | .7 |
| Hor. par | 8.6 | sun's hor. par. | ٠. | | 8 | .6 |
| Alt. 30° nearly | | A I | | | | Company |
| App. time 3h 12m | $55^{\circ} = H.A.$ | difference | | 53 | 41 | .1 |
| | | latitude . | 50 | 48 | 3 | N. |
| | 1 10 | Reduction | - | 11 | 15 | |
| | | | | | _ | |
| | | Red. lat | 50 | 36 | 48 | |
| | 2 1 | Sun's S. D. | | | 54 | |
| - 1- 10 St 1- | 81 6 71 | Aug. to 30° | | - | 7 | .8 |
| | 1 21 | 0 | | - | | - |
| | | Red. S. D. | | 15 | 47 | .0 |
| fals is | | Moon's S. D. | b. 8 | | 42 | |
| J 2 7 3 | | | | 76 | 1 | 616 - |
| 0.00 | 1000 | Sum . | | 30 | 29 | .7 |
| | | | | | | |

| (4) 1.17609 0.85031 | | | | 9.99709 | 2.02349 | | 166° 28′ 58″ | + 56 0 | 166 54 58 |
|--|--|---------------|------------------------|-----------------------------|--------------------|------------------------|--------------|---------------|---------------|
| 543 C. L. 188 | 2967 | | 9.0 | | 2 P. L. | 42 | 55.84= | arc. (5) | red. R. A. |
| P. L. cosec. secant | P. L. 0.63967 | | | 2 500 | 0h 1m 42°.2 | sun's R. A. 11 4 13.64 | 11 5 55.8 | | |
| (2) 0.52543 0.19751 8.98273 | | | 2/ 22" S. P.L. 1.88030 | V. cosine | - 1 | sun's R. | 19 | P. L. 0.58596 | P. L. 1.09994 |
| cant 0.52543 P. L. cant 0.19751 Sec. 0.12737 \odot 's dec. N. \odot 0.85031 cosec. | 1.17609 (2) 41" 16' N. 9.99763 6° 39 38 N. | | . 22. 25 8 | T. dec. 60 37 16 N. cosine. |)'s dec. 6 21 4 N. | 16 12 | 30 30 | 46 42 | 14 18 |
| P. L. 0.52545 secant 0.19751 cosec. 0.12737 P. L. 0.85031 | C. L. 1.17609 cos. 9.99763 | P. L. 2.02403 | secant | T. de |)'s de | Diff. | | Sum | diff. |
| P se (a) co | | (%) | 3 12 3.9 (a—b) | | 15' 47" | 14 43 | 30 30 | | 16" |
| ٠ ت | 5° 58′ 22″ | 1m 42°.2 | 3 12 | | | | 106 | | . 6° 37′ 16″ |
| Diff. of par. Red. lat. Hour angle | Sun's dec. | Arc 1. | Diff. | | Sun's S. D. | Moon's S. D. | Sum | | True dec. |

| 166 54 47 168 13 26 1 18 39 0 0 0 25 3 17 25 3 12 55 4 30 1 7' 30" | 166° 54′ 47″ + 11 166 54 58 |
|--|--|
| 24 R. A. 299203 P. L. 0.35957 P. L. 2.63246 P. L. to est. time G. T. app. T. lon. in time in deg. | 3.55630 0.35957 3.19673 var. in 25' cor. |
| | P. L. P. L. P. L. = 1° 5′4 |
| sum 1.68 half 0.84 . 9.99 P. L. 0.84 166° 28° 1 166° 28° 1 A.cor. 166° 54 | 3 17 18 5 3 17 3 17 17 18 5 12 12 12 12 12 12 12 12 12 12 12 12 12 |
| cosine Arc (5) 26′ 0′ Repetition R. A. arc (5) | diff. 0.58518 1.10247 est. T. 1.68765 G. T. 0.84382 Ap. T. 9.99721 lon. in T. 8.84183 |
| . 4 2 6 9 9 | 16 17 30 30 46 47 P.L. 14 13 P.L. Sum Half 6° 29′ 10″ cos. 25 57 .4 P. L. |
| Moon's dec. 6 21 4 Sum . 12 58 20 Half . 6 29 10 Moon's dec. 6° 21' Cor. dec.) 6 20 8 True dec. 6 37 1 | Diff. Sum S. D. 3 Sum Diff. 1 Sum 1 25 |

On the 7th of July, 1823, at Dunglass House, the seat of Sir James Hall, Bart., in latitude 55° 56′ 32″ N., and longitude by estimation 9^m 30° W., Captain Basil Hall, R.N., observed the end of a solar eclipse at 17^h 55^m 34°.1 mean time; required the true longitude of Dunglass?

| July 7th, 17 ^h 55 ^m 34 ^s J | uly 7th, Mean Time, 17h 55m 34s 1 |
|---|--|
| | qu. of time to $18^{\rm h}$ $1^{\rm m}$ $-$ 4 28.7 |
| Eq. of T. at noon, — 4 21 | |
| a a | pparent time at D. 17 51 5.4 |
| Approx. G. T. 18 0 43 | 24 |
| Or . 18 l nearly. | |
| | our angle, . 6 8 54.6 |
| To this time. | |
| Sun's R. A. 7h 6m 2s.55 | Moon's (1) R. A. 106° 14′ 5″.8 |
| Var. in 10 ^s , 0.03 | (2) R. A. 108 16 16 .4 |
| Sun's dec. 22° 35′ 40″.2 | var. in 10°, + 6.8 |
| Var. in 10 ^s , — 0 .05 | dec. 23 48 55 .7 |
| Sun's S. D. 15' 45".5 | var. in 10^{8} — 1.3 |
| Aug. to 20° alt. — 5.5 | S. D. 16 43 |
| | equat. par. 61 20 .5 |
| Cor. S. D. 15 40 .0 | red. to 56° — 8.1 |
| Hor. par. 8 .54 | |
| Latitude, 55° 56′ 32″ | red. par. 61 12 .4 |
| Reduction, — 10 40 | sun's par. 8.4 |
| | |
| Red. lat. 55 45 52 | diff. par. 61 4.0 |

| C. L. 1.17609 0.71960 | | | 14 15 7 8 | | - W 624 10 | 9.96279 | L. 1.85848 | -0.00 | : 105° 53′ 15″.0 | + 20 46 .0 | 106 14 1.0 | 106 14 5 .8 | 108 16 16 .4 |
|---|-------------|---------|-----------|------------------------------------|-----------------------|---------------------------|-----------------------|-----------------|------------------|---------------|---------------|-------------|--------------|
| (3) Cosec. 0.08264 secant 0.03468 P. L. 0.58679 | | 8 | | | | | — 2m 29'.6 P. L. | A. 7 6 2.6 | 7 3 33.0 = | arc (5) = | T. R. A. | (1) R. A. | (2) R. A. |
| (2) 0.46847 P. 0.24980 cos 0.41544 sec | | | | 1.47491 | 26½ P. L. 2.60962 | cosine | arc (4) | sun's R. A. 7 6 | | P. L. 0.48750 | P. L. 1,46405 | 1.95155 | 0.97577 |
| P. L. secant (O's dec. N.) 222 35′ 40″ (2) 46 37 | 23 22 17 | | | | (3) $26\frac{1}{2}$ P | $23 \ 22 \ 43\frac{1}{2}$ | $23 48 55\frac{1}{2}$ | 26 12 | 32 23 | 58 35 | 6 11 1 | wns | half |
| (1) 0.46947 0.24980 0.00033 0.71960 1.17609 | 9.96532 | 1.86101 | | nt . | | lec. | moon's dec. | | | 0.19 | 0.750 | | |
| P. L. secant cosec. P. L. C. L. C. L. | cosine | P. L. | | -b) seca | | T. dec. | moo | diff. | | Sum | diff. | | |
| 1° 1′ 4″ P. L. 55 45 52 secant 6 th 8 th 54′.6 (a) cosec. P. L. C. L. | 22° 35′ 40″ | 2m 28.8 | 1 14.4(6) | $6^{\text{h}} 7 40.2 (a-b)$ secant | 7 | おから からか | .15′ 40″ | 16 43 | 32 23 | Jan | 23° 22′ 44″ | 23.48 56 | 47 11 40 |
| Diff. par. Red. lat. Hour angle | Sun's dec. | Arc 1 | Half | Special property | | 1000 | Sun's S. D. | Moon's S. D. | Sum | 0-1-0 | Sun's T. dec. | Moon's | Sum . |

Lon. in time in degrees

| 120 | | | | | | | | | | | | | |
|--|--|---|----------------------------|--|---|-----------------------------|---------------------------|---------------------|----------------------------|----------------------------------|------------------------------------|---|---|
| | | | | `` | | | | | | | | | |
| ထဲ | 9 | 0.0 | 0. | 4. 6. | rly | 0. | 0. | 0. | 0. | 0. | 0.5 | 70 4 | 17 |
| 4 | 2 | 100 | 53 | 6 4 | lea | 15" | 15 | 0 | _ | - | 53 | 52 | 47 |
| | C1 | 3.18554 P. L. arc (6) - 7.0 est. G. T. 18° 1' 0.0 | T.A.G.T. 18 0 53.0 | A. Dungl. T. 17 51 5.4 Lon. in T. 9 47.6 W. | in deg. 2° 27' nearly | sun's C. R. A. 105 53 15".0 | + 20 45 .0 | 106 14 0 .0 | 106 14 1 .0 | 1970 | - 0°.5 18 0 53.0 | 18h 0 52.5 17 51 5.4 | 9 47.1 |
| 1 | 63 | ۱۵۵ | 8 | 10 | 87 | 50 | C/1 | 3 1 | 1 | | | 487 | |
| 1 | | 17 | 1 = | H | CA | 105 | + | 100 | 106 | | 182 | HH | 1 |
| liff. | diff. | 9 | T. | 1 2 | 60 | | | | | | | | |
| 1) | 5 | arc T | 5 | ngl in 7 | n d | | | + | A | | ı T | H | 35 |
| • | ن | L. G | Y. | Du | -= | * A | | sun's T. R A. | moon's C. R. A. | 4.03342 P. L. 0.16829 | 3.86513 P. L. Est. Greenwich T. | Cor. G. A. T. App. Dunglass T. | e |
| P. I | Д. | P. est | E | A. Lo | | 25 | arc (5) c. | [.] | C | П | Peny | A. | Lon. in time |
| 65 | 63 | 54 | | | | ,s | 5 | S | on | 23 | 313 | ಚಿ ದ | ii. |
| 538 | 89 | 185 | | | | sur | arc | sur | mo | 4.03342 | 865 st. | or. | on. |
| 33 | 0. | 60 | | | - | | | | | 4.0 | | | - 17 |
| 9.96288 3.35383 P. L. (1) diff. — 4 .8 | 0.93785 .0.16829 P. L. (2) diff. 2 2 10 .6 | , | | • | 110 | | | | | | th | nis a- | |
| 879 | 378 | | - | | 37 | 22 | 26 | 130 | 80 | 37 | W | s tl | |
| 9.6 | 0.0 | | | | 187 | 165 | 1.95259 | 0.97629 | 9.96208 | 0.93837 | EW, | A | |
| | | | | | 0.4 | 1, | 1 | 0 | 6 | 0.0 | Ä | N. | |
| | P.L. | | | | P. L. 0.48737 | P. L. 1.46522 | - | | ٠. | , | ick | a lo | |
| • | 14 | | | | 4 | Д | | | | 20′ 45″ P. L. | erw | an , an , | |
| | _ | 73 | 53 | | 1 | | • | | • | " | m, | 21 21 21 31 31 | n |
| | 46′ | 43 | 56 | 13 | 36 | 10 | | | | 45 | rth | tal 20 | |
| | 20' 46" | 55 | 88 | 26 13 32 23 | 58 36 | 01 9 | | | | 20, | Ž, | r is | e e |
| | | sun's C. dec. 23 22 43 .5 | moon's C. dec. 23 38 56 .5 | | | 10. | | | | | at | owe Jul | tud |
| • | | 63 | c. 2 | | ı | | | | | | and | th s to the | ngi |
| | | dec | de. | diff. sum of S. D. | | | mns | half | • | | SS | rlas of | f 10 |
| | _ | Ü | S | 3 2 | | | S | þ | | 9 | ngla | ung ors | 0 ,0 |
| | arc (5) | n,s | noc | r. m | E | £ | | | | arc (5) c | Dur | f D | at 5 |
| | arc | sul | E | diff. | sum | diff. | | -6 | | ar | at] | e of | poor |
| 0.0 | | | • • • • • • | | • • • • • • | | | | | 4 | all | tud et, | to |
| 23 35 50 cosine. | | | | | | | | 8 | | 14. | H | ngi rre | nt |
| 00 | | 55 | 94 | 5 51 | 0 | 1 20 | 8 | 8 | 10 | 27 | 3 tain | ars, | nou |
| 50 | E13 | Ç | 0.04 | 7 6 2.5] | 0 | 23 22 43 .5 | 5 | 4 | 1 | 23 48 55 .7 + 0 .9 | 23 48 56 6 aken by Capts | the ery | an |
| 35 | | 3m | | 2,4 | | 2 | 4 | | - | 55 | 3 5 | t al | ınsı |
| 9 | | on. | | 30 | 31 | C.1 | | -9 | 17 | 4 | 184 u | S, the | ", m |
| CA | -11 | titi 7 | | 1 24 | TI | 1 23 | 106 | - | 18 | + 53 | 23 ake | ligh ace | he |
| | | ebe | 5 | | 005 | | Ą. | 3 | | 3 | ss t | ay pl | get |
| | | 2 | 000 | 53 | 0,0 | | R | 6 | Y. | 600 | ngle | tter | n to |
| | | ** | × | Om lec. | × | c. | (I) | 0× |) R | de | c. | e of | kei |
| Ç. | | S | 1 | 18 18 d | 1- | de, | s,uc | 1 | C | on's | de ron | Isk two | s ta |
| Half | | Repetition. | Cor.—7'×0'005=— | Cor. R. A. For 18^{h} 0 ^m 53 ^s $\left\{\begin{array}{c} 7-6 & 2.51 \\ 23^{\circ} 22' 43''.5 \end{array}\right\}$ Sun's dec. | $Cor7^{\circ}\times-0^{\circ}005=+$ 0.0 | Cor. dec. | Moon's(1)R.A. 106 14 5 .8 | Cor7*x0".68= - 4 .8 | Cor. (1) R. A. 106 14 1 .0 | Moon's dec. 23 Cor7*x-0".3= + | Cor. dec. From a | the Isle of May light, it appears, on comparison with the latitudes and longitudes of the two latter places, that the longitude of Dunglass tower is 2° 21′ 42″ W. As this result is conceived to be very correct, the errors of the lunar tables, and the observa- | tions taken together, must amount to about 5' of longitude. |
| _ | | | | | | | - | | | | | 4 4 4 | 3 |

IV. BY THE MOON'S TRANSIT.

The method of finding the longitude by the culmination of the moon and stars, is now considered very convenient and accurate.

Since the observations require a transit instrument, and the clock used with it generally shows siderial time; the difference of the times is supposed to be siderial time. If it is not, it must be reduced to siderial time by Table XXXI. If the moon had no motion, the difference of times between her transit and that of a fixed star would be the same at both places.

The difference of the differences arises from, and is equal to the increase (I) of the moon's right ascension in time, in the interval

between the passages over the meridian at each place.

Hence, if the increase (N) of the moon's R.A. in one hour of siderial time be known N: I:: lh: X, the angle described by the western meridian in the interval of the passages of the moon.

This is equal to the difference of longitude + I.

Hence, the difference of longitude is equal to $X-I = \frac{1}{N}-I$. By the Nautical Almanac the moon's right ascension is given at every noon and midnight; whence its increase in an hour of siderial time may be found nearly in the middle of the interval including the observations.

Assume the difference of longitude = L' as nearly as can be estimated, and compute the increase (E) of the moon's R. A. in the siderial time L', then

As E:I:: L': $X = \frac{IL'}{E}$, (1) and the exact difference of longitude

 $=\frac{IL'}{E}$ —I (2). But this exactness is only necessary when the places differ considerably in longitude.

The moon's limb is observed by a transit instrument, and not the centre, which makes some little difference when the difference of

longitude is considerable.

When great accuracy is required, it would then be necessary to make an allowance for the moon's alteration of distance, that changes her apparent diameter, and also for change of declination, which changes her semidiameter in R. A.*

Ex.—June 13th, 1791, the following observations of the passage of the moon and & Serpentis were made at the observatories of Green-

wich and Dublin; required their difference of Longitude?

At Greenwich, R. A.)'s 1st limb
R. A. \alpha serpentis

15^h 5^m 3' 52 at 9^h 36^m App. T.
15 33 34.70

28 31.18
At Dublin
R. A.)'s 1st limb
\alpha serpentis
28 31.18
15^h 6^m 12' 49
15 33 36.91

2d Difference
27 24.42

^{*} For a more complete solution of this method, see Dr Brinkley's Article in the first number of the Dublin Philosophical Journal, and Mr Baily's Memoir in the Transactions of the Astronomical Society.

| Difference Daily rate of clock—16*.88 prop. part | AND DESCRIPTION OF THE PERSON NAMED IN | 24.°42 0.32 |
|--|--|----------------|
| 2d cor. diff. | 27 | 24.74 |

Difference of 1st and 2d differences 6.44 = 16' 36''.6.

As the places do not differ much in longitude, it is unnecessary to reduce apparent to mean time.

This difference 16' 36".6 is the increase of the moon's R. A., in the interval of its passages of the meridians of the observations of Greenwich and Dublin.

By the Nautical Almanac, we find the following differences of the right ascensions of the same limb of the moon, and the star at about the same time.

| the day market make a feet | | 7.11. | Di | ff. | |
|----------------------------|--------|---------|--------|---------------|----------|
| June 12, midnight 213 | 3° 15′ | | 70 23 | 7 1 1 1 1 1 1 | 10 10 10 |
| | 0 38 | The son | | | H SEE |
| - 13, midnight 22 | 8 11 | | . 7 33 | (| #0 OF F |
| | 5 53 | | 7 42 | 1 | 7° 37′.5 |
| 14, midnight 24 | 3 43 | | . 7 40 | an mile | |

If the places differ much in longitude, the motion in R. A. should be calculated to seconds, though, in the present case as the second differences are sufficiently uniform, the mean first difference containing the interval will be sufficiently accurate for the rate of increase in 12 hours at the middle time.

Hence, by formula (1) 7° 37'.5:16' $36''.6:12^{\circ}$ $x = 1568^{\circ}.42$, and when the difference of longitude is not considerable $x + \frac{x}{6 \times 60} =$

$$\frac{1568^{\circ}.42 + \frac{1568^{\circ}.42}{6 \times 60}}{6 \times 60} = 26^{\circ} 12^{\circ}.77, \text{ consequently } 26^{\circ} 12^{\circ}.77 - 1^{\circ} 6^{\circ}.44$$

$$= 25^{\circ} 6^{\circ}.33 = 6^{\circ} 16' 35'' \text{ W}.$$

If It be the increase of the moon's R. A. during the interval between the transits, then $x + \frac{x}{365} - r$ must be used when the difference of longitude is considerable.

It would extend this article too much to give Baily's or Brinkley's methods, which are more accurate and complete, and can only be fully treated in a work on astronomy.

In the foregoing example the difference of R. A. between the moon and star was determined at both places by observation, but for ordinary purposes that at Greenwich may be found by the Nautical Almanac.

OF THE TRANSIT INSTRUMENT.

A transit instrument is a telescope properly placed in the meridian for the purpose of observing the times at which the celestial bodies pass this circle. If the clock or chronometer by which the time is marked be adjusted to show siderial time, then their right ascensions will be found. This is perhaps the best method of determining the rates of chronometers.

The telescope is fitted to an axis, of which the ends tapered into points turn in notches, from their shape called Vs or Ys. This axis is made hollow, opposite one of the ends of which is placed a lamp

for illuminating the wires in night observations.

These wires, generally five in number, are placed in the telescope equidistant from each other, and perpendicular to the horizon, having also a horizontal wire bisecting them, near or upon which the

transits are observed.

When properly adjusted, the middle vertical wire coincides with the meridian, and the instant that the centre of any heavenly body passes this wire, is called its transit. The other parallel wires are intended to correct or verify the observation by taking a mean between the transits over the first and last, the SECOND and FOURTH, and comparing it with the third or meridian wire; or, what is more correct, a mean of the whole called the reduction of the wires.

There are five principal adjustments necessary in placing a transit instrument, three relative to the telescope and two to the axis.

1. The wires should be set perfectly vertical.—This is verified by observing that any distant object cut by a wire does not change its position relative to that wire, on moving the instrument up and down. If it does, the wires must be all turned till the object is kept upon them, when moved through their whole extent, and the

adjustment is then complete.

2. The telescope should have no parallax.—When any distant object is bisected by the horizontal wire, if, on moving the eye up and down a little, the object should appear to separate from the wire, the instrument is said to have a parallax. This must be corrected by placing the object and eye glasses at such a distance from each other, that their foci may meet in the point of intersection of the wires. When the object-glass has been properly fixed by the instrument-maker, the observer has only to adjust the eye-glass.

3. The line of collimation should be correct.*—This is known by bisecting any object by the meridian wire, and if, on reversing the axis, the object still remains bisected as before, the line of collimation is correct. If not, it must be adjusted by means of the small screws in the sides of the telescope. This is effected by easing the one screw and tightening the other till the error appears one half diminished, when the axis is again reversed, and the operation is repeated till the adjustment is properly effected.

4. To level the axis.—This is performed by means of a screw placed under one of the Ys or notches, which raises or depresses that end of the axis at pleasure, while the true horizontal position is

ascertained by a spirit-level.

5. To bring the telescope to the meridian.—This is accomplished by means of a horizontal screw acting on one end of the axis, by which it is moved backward or forward till its proper position is obtained.

As the problem of bringing a transit instrument into the meridian is one of considerable difficulty, it is proposed to treat it at some length.

To take a Transit.

With the latitude of the place and the declination of the object compute its meridian altitude.

When it is known to approach the meridian, elevate the telescope

^{*} The line of collimation is an imaginary straight line supposed to join the centre of refractions of the object glass, and the intersection of the meridian and horizontal wire in the centre of the telescope.

to the given altitude by the circle attached to the end of the axis. Now, because the telescope inverts objects, the object will appear to come into the field of view from the west and move towards the east.

Mark the time of transit over each wire, using a dark glass to save the eye when the sun is observed.

FROM THE GREENWICH OBSERVATIONS.

| 1816. | | Wires. | | | | | Reduc. Star. | |
|-------|---|--|--|---|---------|--------|--------------------------|--|
| Nov. | I. | _ II. | 111. | 1V. | - V. S, | Wires. | | |
| 3d | 1.4 22.6 | | 21 ^h 55 ^m 38 ^s .5 0 29 27 .5 | 5°.5 0.0 | | | ∡ Aquarii. ∡ Cassiop. | |
| 4th | 0.4 | 18.4 | 21 55 37.2 | 55.7 | 14.1 | 37.16 | ∡ Aquarii. | |
| 8th | 51 ^m 29 ^s .4 53 45.0 | 51 ^m 48 ^s .5 53 4.3 | 14 ^h 52 ^m 7 ^s .6 14 54 23.4 | 52 ^m 26 ^s .7 54 42.5 | | | Sun's 1 L. Sun's 2 L. | |

| By taking the means as directed. | EV UN |
|--|---|
| That of the 3d will be | 21 ^h 55 ^m 38 ^s .30 |
| 4th | 0 29 27.16 14 53 15.50 |
| By the Nautical Almanac the sun's } right ascension that day was | 14 54 4.70 |
| The error of the clock on the 8th is slow, or Suppose the observation had been made with middle one only, then | |
| To | |
| Add semidiameter, Table XV. | + 1 7.6 |
| | 14 53 15.2 |
| Mean of the whole | 14-53 15.5 |
| Difference only | |
| The error of the clock may readily be determine if one of those whose true places are given in the Na observed. Otherwise the corrections must be appriate tables. | autical Almanac is |
| Observed transit on 3d | 21 ^h 55 ^m 38 ^s .30 |
| α Aquarii R. A. by tables | 21 56 24.35 |
| Error of clock by the star slow, on the 3d On the 8th | - 46.05 - 49.20 |
| Loss in 4.71 siderial days Or the daily loss is | 3.15 0.67 |

TO BRING A TRANSIT INSTRUMENT INTO THE MERIDIAN.

To perform this problem, the time should be accurately determined by an altitude near the prime vertical, or still better by equal altitudes as already explained. Bring the telescope to any celestial object when nearly passing the meridian, and, by turning the horizontal screw, make the middle wire bisect the object at the instant of its transit, then is the instrument in the meridian.

Should the object be the sun, as it cannot be accurately bisected, either limb must be observed when on the meridian by allowing for the time his semidiameter takes to pass the meridian. This is found most accurately in the Nautical Almanac, or, if it is not at hand,

from Table XV.

To find the Time that any Star takes to pass from one wire to another in a Transit Instrument, that of the Equinoctial being known.

Rule.—To the cosine of the star's declination add the proportional logarithm of the time at the equinoctial, the sum is the proportional

logarithm of the time by the given star.

Ex.—On the 10th of April, 1826, by a transit telescope which gave 25.4 for the passage of a star on the equinoctial from wire to wire; what would be the time by Antares, having 26° 2' S. declination?

| Declination Time | 26° 2′ 25°.4 | cosine P. L. |) i ha | 9.95354 2.62867 |
|------------------|-----------------|-----------------|--------|--------------------|
| Reduced time . | 28.26 | P. L. | -1-0- | 2.58221 |

Or this would be more readily performed by considering the seconds minutes, and converting the decimals into thirds to be estimated seconds, then the answer will come out in minutes and seconds to be estimated seconds and thirds.

| Declination Time | 26° 2′ 25°. 4, or 25 ^m 24° | cosine P. L. | - an | 9.95354 0.85044 |
|---------------------|--|-----------------|------|-------------------|
| -10-10-10-1 | STREET SAN THEORY AND PERSON | | | |
| | 28 27 or 28 16 | P. L. | | 0.80308 |

Hence the star's expected time of approach to the other wires becomes known after its contact with the first is observed.

One of the most convenient methods of fixing the transit telescope in the meridian in mean northern latitudes is by means of Polaris.

It is required to set a transit instrument by Polaris, on the 1st of March, 1826, at Edinburgh, in latitude 55° 57′ 21″ N. By a reference to the Nautical Almanac its altitude at its superior transit will be 57° 34′, and at its inferior 54° 21′; and its R. A. is 0° 58° 12° 20. It must therefore pass the meridian about 2° 8°, and 14° 8° at the altitudes stated above, which serve as a guide to advertise the observer to be prepared.

Now let the clock be regulated to siderial time, and when it shows 0^h 58^m 12.2 make the middle wire bisect Polaris, then will the instrument be in the meridian. If, however, the time first assumed was not known with sufficient accuracy, the error of the clock can now be found very nearly by the transit of the sun or a star. By repeatedly observing Polaris, and correcting in this manner, the instrument will at last be truly in the meridian. This may be verified in several ways. One of the most general methods is by observing that the semirevolutions of circumpolar stars are equal, sup-

posing that the rate of the clock is uniform. Should the observer not choose to trust to that, he may select two circumpolar stars whose right ascensions differ nearly 12h, as it requires in this case only a few minutes perfect regularity in the clock. Take the difference between the transits of circumpolar stars by the clock, which are nearly in the same azimuth, the one above the other below the pole; repeat the operation 12 hours after successively, when the stars have reversed their positions, and if there be a variation in their differences, it shows a deviation in the instrument, which may be corrected by substituting half the difference for the error, and repeating the trial by approximation till the adjustment is complete.

If some of those stars whose apparent places are given in the Nautical Almanac be selected, the operation will be comparatively easy. These in pairs are; 1, & Cassiopeiæ and & Ursæ Majoris; 2, Polaris and & Ursæ Majoris; 3, Polaris or & Arietis and & Draconis; 4, Capella and & Herculis; 5, & Tauri and & Draconis; 6, & Aurigæ and y Draconis; 7, Pollux and y Aquilæ. No doubt some of these can only be so observed in very high northern latitudes; and, therefore, recourse must be had in some instances to other tables, such

as those of Dr Pearson.*

It sometimes happens that an observer has not a command of the whole meridian, especially if he has not an observatory properly adapted to the purpose, yet may find it necessary to take transits for the regulations of clocks or chronometers. In this case recourse must be had to the sun, and to pairs of high and low stars having nearly the same right ascension. Having, by the sun and a good watch or chronometer, placed the instrument nearly in the meridian, observe the transits of two stars having nearly the same right ascension, but differing at least 30° or 40° of declination. Now if the interval between their passing the meridian in siderial time be exactly equal to their difference of right ascension, the instrument is truly placed; if not, it wants correction.

If, when the latitude is N. and the stars S. of the zenith, the highest star come first to the meridian and the interval between the transits be too great, it deviates towards the west; if too small, towards

the east.

But if the lowest star come first to the meridian, and the interval between the transit be too great, it deviates towards the east; if too small, towards the west. In either case there is required a correc-

tion, which may be computed in the following manner:-

Rule.—To the secant of the star's declination add the sine of the difference of the latitude and declination, if they are of the same name, or the sine of their sum, if they are of different names; of the sum of which find the natural numbers. To the logarithm of the sum of these add the arithmetical complement of the logarithm of their difference, and the logarithm of the difference between the excess of the right ascension of one star above that of the other, and the observed interval of time between the transits, the sum will be the logarithm of an arc in time.

Half the sum of the excess of the right ascension of the one star above the other and the foregoing arc, will be the deviation at the

^{*} Perhaps the catalogue in the Nautical Almanac might be extended and the selection more judicious. For example, the places of some of the smaller stars in Orion might be properly exchanged for either circumpolar or high and low stars.

lowest star, and half the difference between these will be the devia-

tion at the highest.

The deviation in time at each star being now known, the instrument may be easily rectified by either, or both of them on the following night, or still more readily by a third star on the same evening; or, if the telescope is sufficiently powerful to show stars in the day, all the corrections may be performed at any time in a few successive hours. For the deviation of one star being known, that at another may be computed by the following-

Rule.—To the logarithm of the given deviation add the cosine of the corresponding star's declination, the secant of the declination of the third star, the cosecant of the sum of the latitude and declination of the first star if they are of different names, or of their difference if they are of the same name, and the sine of the sum of the latitude and declination of the third star if they are of different names, or of their difference if they are of the same name; the sum of these will be the logarithm of the deviation in seconds of time at the third star.

Ex.—On the 1st of March, 1826, at the observatory of Edinburgh, in latitude 55° 57' 21" N., I observed the transits of Capella and Rigel, on the same evening, about a quarter past 6, and found the interval between the two transits 2.5 less than the difference between their true apparent right ascensions, as given in the Nautical Almanac; required the deviation of the instrument at either star, and also at a third, as Sirius?

55° 57′ N. 55° 57′ N. Latitude

Dec. of Capella 45 48 N. sec. 0.156664 Rig. 8 25 S. sec. 0.004703 sin. 9.246069 sum 64 22 10

Difference sin. 9.955005 1. Nat. number 0.2528 9.402733 ...9.959708

2. Nat. number 0.9114

75

1.1642 log. 0.065953 0.6586 ar. co. 1.181478 Difference Diff. of R. A. and \2.5 log. 0.397940 Obs. interval

Arc in time

4.42 log. 1.645346

Sum

6.92 half = $3^{\circ}46$ = the deviation at Rigel.

Difference

1.92 half = 0.96 = the deviation at Capella.

Now since the highest star comes first to the meridian, and the interval between the transits is too short, the deviations are easterly. If the stars had been between the zenith and the north pole, the

deviations would have been westerly.

Since it has been found necessary to fix the instrument as soon as possible, we shall proceed to compute the deviation at the third star, which can be easily done, as we have an hour and three quarters nearly to perform the calculations and complete the arrangements; thus:

| Declination of Rigel (a) | 8° 25′ S. | cosine † | 9.995297 |
|---|-------------------------|----------|----------------------------------|
| Latitude . (b) Declination of Sirius (c) | 55 57 N. 16 29 S. | secant | 0.018226 |
| Second sum, or $(b+c) =$ | 64 22 72 26 3°.46 | cosecant | 0.044995 9.979260 0.539076 |
| Deviation at Sirius | 3.7745 | log. | 0.576854 |

After having corrected the instrument by means of Sirius, I observed the transits of Castor and Procyon, and again those of Procyon and Pollux, and found the interval of time to agree with their difference in right ascension, from which I concluded, that in the space of about three hours I had placed my transit instru-

ment exactly in the meridian.

As it is rather a difficult operation to fix a transit instrument accurately in the meridian, these operations should be repeated a considerable number of times to insure the utmost possible accuracy. After the observations prove satisfactory, a meridian mark may be put up in a horizontal direction at a considerable distance, with which the central wire may be frequently examined and rectified previous to any very nice observation. This mark may be of various constructions, such as a copper-plate with a hole in it, so as a small segment of light may be seen on each side of the vertical middle wire, or a small notch in a building, or even a post at some distance. A thin slip of brass or copper painted black, with white lines or divisions at every inch, and numbered throughout, will also be found very convenient, and by knowing its distance the deviation upon it may be computed.*

The transit instrument being now properly rectified, it will be found the most accurate of all for determining the error and rate of a clock or chronometer, by taking the transit of the sun or stars daily, and marking the difference regularly in a column prepared for that purpose. If a star be observed, siderial time must be reduced

to mean solar time by Table XXXI. when necessary.

- Ex. 1.—The observed times of the sun's passing the meridian of the observatory were as follows:—What was the original error on the last day of observation and the daily rate?

| | 1826. | Obs. Time. Sun's Transit. | Mean Time, App. Noon. | Chronometer too fast. | Daily Rate. | | |
|---|--|------------------------------------|---|-----------------------|---|--|--|
| | March 1 2 3 4 5 6 | 0 25 16.6 0 25 5.4 0 24 54.0 | 0 ^h 12 ^m 40 ^h .7 0 12 28.6 0 12 16.0 0 12 3.0 0 11 49.5 0 11 35.6 | | + 1.6 + 1.4 + 1.6 + 1.5 + 1.7 | | |
| ı | Mean daily rate is therefore +1.56 And the original error at noon, on the 6th of March, 1826, is 0h 12m 54*2 fast. | | | | | | |

[•] Hor. deviation = sec. alt. × cos. dec. × obs. diff. of time × 15, to radius 1. On Captain Kater's plan, by contracting the diameter of the object-glass by some contrivance for that purpose, the meridian mark may be only a few feet distant.—See his paper on the Floating Collimator.

Hence its error, supposing the rate to remain uniform, may, at any

moderately distant future time, be determined.

Ex. 2.—On the same evenings the star Rigel passed the meridian as follows:—Required the daily rate and the original error on the sixth at the time of observation, about 6 o'clock in the evening?

| 1826. | Obs. Time. Sun's Transit. | Daily Diff. of Star's Transit. | Diff. of Mean and Siderial Time. | Daily Rate, | |
|-----------------|------------------------------|---|---|-------------|--------|
| March 1 | 6h 42m 56s.6 | 0 | | | |
| 1 3 | 6 39 2.3 6 35 7.8 | 3 ^m 54 ^s .3 3 54.5 | 3 ^m 55 ^s .9 3 55.9 | + 1.6 + 1.4 | |
| . 4 | 6 31 13.4 | 3 54.4 | 3 55.9 | + 1.5 | |
| 5 6 | 6 27 19.2 6 23 25.0 | 3 54.2 3 54.2 | 3 55.9 3 55.9 | + 1.7 + 1.7 | |
| | 0 25 25.0 | 3 34.2 | 9.00 6 | | I |
| 1 | | Sales and | | 5 7.9 | |
| Rate by the sta | | not lo | • 6 - 50 • | +1.58 | algain |
| By the su | in . | and and | 0.507 0 1 | +1.56 | Broad |
| | . The come of | I la year | SPECIAL CONTRACTOR | 2 3.14 | 47.0 |
| Mean rate by h | ooth . | Trible | | + 1.57 | 170 |
| Sun's R. A. at | | | . 28 | | |
| Prop. part of d | laily var., to | ^b , . | + | 55 | .5 |
| Reduced R. A. | | • | . 2 | 3 7 16 | |
| Star's R. A. by | Nautical Alr | manac | 110376 | 5 6 12 | .5 |
| Apparent time | of transit | | | 58 55 | .6 |
| Equation of tin | ne ji , | 100-00 | + | 11 35 | .6 |
| Mean time of t | ransit of star | Lugar e | | 3 10 31 | .2 |
| Time of transit | by chronome | eter on the 6 | 6th 6 | 3 23 25 | .0 |
| Error of chron | ometer, fast b | v star. | . 0 | 12 53 | .8 |
| Allowing for c | | | | | _ |
| 1 | - S 6 13, 19 | There is | September 1 | 8 | .4 |
| Mean error at | Sh foot | | |) 12 54 | 9 |
| With a daily ra | - | | . + | | .57 |
| | | | | | - |

As opportunities may not occur daily for celestial observations, it is in that case necessary to compare a chronometer with a good clock, the rate of which can be depended on, and is occasionally ascertained by the heavenly bodies.

 E_x . 3.—Given the daily difference between a chronometer and a clock, the rate of the clock being occasionally determined by celestial observations; to find the error and rate of the chronometer?

17. A 4. 1. S. L.

| 1826. | Clock before Mean Time. | Chron, differs from Clock. | Chron. before Mean Time. | Daily Rate. |
|-----------------|--|---|---|-----------------------------------|
| May 1 2 3 4 5 6 | + 8.5 * + 8.9 + 9.4 + 9.8 * + 10.1 | + 2°.5 + 3.8 + 5.2 + 6.5 + 7.9 + 9.3 | + 11°.0 + 12.7 + 14.6 + 16.3 + 18.0 + 19.8 | + 1°.7 + 1.9 + 1.7 + 1.7 |

5 + 8.8

Mean daily rate + 1.76 And on the 6th at noon, the original error was fast 19.8

Hence the error of the chronometer may be found at any moderate distance of time, so far as its steady rate can be depended on.

The clock was examined by celestial observation, only where the asterisks are placed, or on the 1st, 4th, and 6th, and these are sufficient to ascertain, with the requisite precision, the rate of the chronometer when the clock is good. It is in a somewhat similar manner that the prize chronometers are tried at Greenwich.

Table of the variations of the sun's R. A. and dec. in 1° for every month in the year.

| Month. | Var. in R. A. for 1 Second. | Var. in Dec. for 1 Second- |
|----------|--------------------------------|-------------------------------|
| January | 0°.0029 | 0".008 N. |
| February | 0.0027 | 0 .014 N. |
| March · | 0.0025 | 0 .016 N. |
| April | 0.0026 | 0 .014 N. |
| May | 0.0028 | 0 .009 N. |
| June | 0.0029 | 0 .000 |
| July | 0.0028 | 0 .006 S. |
| August | 0.0026 | 0 .013 S. |
| Sept. · | 0.0025 | 0 .016 S. |
| October | 0.0026 | 0 .015 S. |
| Novem. | 0.0028 | 0 .010 S. |
| December | 0.0031 | 0 .002 S. |

This table will be useful when the change of the sun's R. A or D. for a few seconds only is wanted.

who to the property of the state of the stat

PART III. mainly laws made in bould

MENSURATION, SURVEYING, &c.

SECTION I.

Mensuration of Surfaces.

Mensuration is the application of Arithmetic to Geometry, by which the values of geometrical magnitudes are obtained in numbers.

In this case some determinate magnitude of the same kind with that to be measured is assumed, as unit, and the number of times this unit is contained in the given magnitude is the measure of that magnitude.

See Leslie's Geometry, Book V. Prop. XXV.

1. To find the area of a parallelogram, multiply the length by the

perpendicular breadth.

2. Triangle.—Multiply the base by the perpendicular altitude; half the product is the area. Or take half the product of the two sides and the natural sine of the contained angle. Or when the three sides are given, multiply half the sum of the three sides, and the differences between that half sum and the three sides together, the square root of this product will be the area. This may be performed readily by logarithms.

3. Trapezium.—Multiply the base into half the sum of the per-

pendiculars.

4. Trapezoid.—Multiply half the sum of the parallel sides by the perpendicular distance between them.

5. Irregular Polygon.—Divide it into triangles, find their areas,

the sum of these will be the area.

6. Regular Polygon.—Multiply the square of the side given into the proper multiplier for areas from the table, page 142, for that purpose, and the product will be the area. Or, divide the polygon into triangles; find the area of one of them by some of the foregoing rules. Multiply this by the number in the whole polygon, the product is the area.

7. Circle.—The diameter is to the circumference as 1 to 3.1415926536,

or 1 to 3.141593 nearly.

The circumference is to the diameter as 1 to 0.318309.

The area is equivalent to the square of the diameter multiplied into 0.785398.

The area is equivalent to half the diameter multiplied into half

the circumference.

8. Circular Arc.—The length of a circular arc is equivalent to the radius of the circle multiplied by 0.0174533 and by the number of degrees in the arc.

Or, from eight times the chord of half the arc subtract the chord of the whole arc, one third of this remainder is the length of the

arc nearly.

9. Circular Sector.—The area is equivalent to the radius multipli-

ed into half the length of the arc.

10. Circular Segment.—Multiply the square of the radius by either half the difference of the arc of the segment and its sine, or by half their SUM, according as the segment is less or GREATER than a semicircle, and the product will be the area.

11. Parabola.—The area is equivalent to two-thirds of the pro-

duct of its base and altitude.

12. Ellipse.—The area is equivalent to the product of the transverse axis into the conjugate axis multiplied by 0.785398. Periphery.—Multiply the square root of half the sum of the squares of the two axes by 3.141593, the product will be the periphery nearly.

Examples for Exercise.

1. Required the area of a square of which the side is 5 feet 9 inches?

Ans.—33.0625 feet.

2. Required the area of a rectangle, if the length is 1375 links and

the breadth 950? Ans.—13° 0° 10°.

3. Required the area of a rhombus, of which the length of the side is 12.24 feet and height 9.16 feet?

Ans.—112.1184 square feet.

4. Required the area of a rhomboid, of which the length is 7 feet 9 inches, and height 3 feet 6 inches?

Ans. -27ft. 1in. 6pa.

5. Required the area of a rhomboid, of which the adjacent sides are 2535 and 1040 links, and the contained angle 30°?

Ans.—13ac. Or. 29p.

6. Required the area of a triangle, of which the base is 1225 links and altitude 850?

Ans.—5 ac. 0r. 33p.

7. Required the area of a triangle, of which two of the sides are 30 and 40 and the contained angle 28° 57′ 18″?

Ans.—290.47356.

8. Required the area of a triangle, of which the three sides are 20, 30, and 40 feet?

Ans.—290.4737 square feet.

9. How many acres are there in a triangle, of which the three sides are 380, 420, and 765 yards?

Ans.—9ac. 0r. 38p.

10. A ladder, 50 feet long, being placed in a street, reached a window 28 feet from the ground on one side; and, by turning it over, without removing the foot, it reached another window 36 feet high on the other side; required the breadth of the street?

Ans.—76.1233 feet.

11. How many acres are there in the trapezium, of which the diagonal is 475 links, and the two perpendiculars falling upon it on opposite sides, 225 and 360 links respectively.

Ans.-13ac. 2r. 25p.

12. Required the area of a regular hexagon, one of whose equal sides is 14.6 feet and the perpendicular from the centre 12.64 feet.

Ans.—553.632 feet.

13. If the diameter of a circle be 17, what is the circumference? Ans.—53.4072.

14. If the circumference of the earth be 24850 miles, what is the liameter?

Ans.—7910.

15. If the chord of an arc be 30, the height or versed sine 8, what is the length of the arc?

Ans. -351.

16. Required the length of an arc of 57° 17′ 44″.8; the diameter of the circle being 25 feet?

Ans.—12.5, which is equal to the radius.

17. Required the area of a circle, of which the diameter is $15\frac{1}{4}$ Ans.—81.1798.

18. Required the radius of a circle in yards, of which the area is

Ans. $-39\frac{1}{4}$ yds.

19. The diameters of two circles are 16 and 10; what is the area of the ring formed between these two circles, the centre being common to both? Ans.—122.5224.

20. Required the area of the sector, whose height or raised sine is

4 and the diameter of the circle 16?

Ans.-33.5103.

21. Required the area of the segment of a circle, of which the chord is 16 and the diameter of the circle $16\frac{9}{3}$?

Ans.-70.7083.

22. Let ABCD be a four-sided field, and from the side AB to the points C, D, let fall the perpendiculars PC and QD. Now the measure of AP is 110 links, PC is 352 links; AQ is 745 links, QD is 595 and AB is 1110 links; required the area of the field?

Ans .- 3ac. 3r. 35p.

TO FIND THE AREAS OF CIRCULAR SEGMENTS.

Rule.—Divide the height of the segment by the diameter, and find the quotient in the column of heights in the following table: Take out the corresponding area in the next column on the righthand; and multiply it by the square of the circle's diameter, for the area of the segment.

| TABLE OF THE AREAS OF CIRCULAR SEGN | MENTS. |
|-------------------------------------|--------|
|-------------------------------------|--------|

| Height. | Area of the Segment. | Height, | Area of the Segment. |
|---------|-------------------------|---------|-------------------------|---------|-------------------------|---------|-------------------------|---------|-------------------------|
| 01 | .00133 | | .04701 | | .11990 | .31 | .20738 .21667 | | |
| .03 | .00687 | .13 | .06000 | .23 | .13646 | .33 | .22603 | .43 | .32293 |
| .04 | .01468 | .15 | .07387 | .25 | .15354 | .35 | .24498 | .45 | .34278 |
| .06 | .02417 | .17 | .08853 | .27 | .17109 | .37 | .26418 | .47 | .36272 |
| .08 | | | | | | | | | |
| ,10 | .04088 | .20 | .11182 | .30 | .19817 | .40 | .29337 | .50 | .39270 |

Ex. 1.—Taking as an example the chord 12, and the radius 10, or diameter 20.

And having found the perpendicular from the centre upon the chord = 8; then 10-8=2. Hence, by the rule, = $2 \div 20 = 1$ the tabular height. This being sought in the first column of the table, the corresponding tabular area is found = 04088. Then $04048 \times 20^{\circ} = 04088 \times 400 = 16.352$, the area.

The use of the following tables will be readily understood, from considering that the areas of similar figures are as the squares of

their like dimensions, and their SOLIDITIES as the CUBES.

TABLE OF POLYGONS.

| No of Sides. | Names. | Multipliers for areas. | Radius of circum. circle. | Factors for sides. |
|-----------------|---------------------|------------------------|------------------------------|--------------------|
| 3 | Trigon | 0.4330127 | 0.5773503 | |
| 4 | Tetragon, or Square | 1.0000000 | 0.7071068 | 1.414214 |
| 5 | Pentagon | 1.7204774 | 0.8506508 | 1.175570 |
| 6 | Hexagon | 2.5980762 | 1.0000000 | 1.000000 |
| 7 | Heptagon | 3.6339124 | 1.1523824 | |
| - 8 | Octagon | 4.8284271 | 1.3065628 | |
| 9 | Nonagon | 6.1818242 | 1.4619022 | 0.684040 |
| 10 | Decagon | 7.6942088 | 1.6180340 | 0.618034 |
| 111 | Undecagon | 9.3656399 | 1.7747324 | 0.563465 |
| 12 | Dodecagon | 11.1961524 | 1.9318517 | 0.517638 |

SECTION II.

Mensuration of Solids.

1. Prism. (1.) Surface. Multiply the perimeter of one end by the length or height, the product will be the surface of the sides. To this add the areas of the two ends, and the sum will be the whole surface.

(2.) Solidity or Capacity. Multiply the area of the base by the height, the product will be the solid content. The same rules de-

termine the surface and capacity of a cylinder.

2. Pyramid or Cone. (1.) Surface. Multiply half the perimeter of the base by the slant height. To this add the surface of the base, the sum is the whole surface.

(2.) Capacity. Multiply the area of the base by one-third the

perpendicular height.

3. Frustum of a Pyramid. (1.) Multiply half the sum of the perimeters of the two ends by the slant height. To this add the areas

of the two ends, the sum will be the whole surface.

(2.) Capacity. Add a diameter or side of the greater base to one of the less; from the square of the sum subtract the product of these two sides or diameter; multiply the remainder by a third of the height, and this last product by the proper number for the circle, .785398, or polygon, the last product will be the content.

4. Sphere. (1.) Surface. Multiply the square of the diameter

by 3.141593, the product is the surface.

(2.) Capacity. Multiply the cube of the diameter by 0.5236, or the cube of the circumference by 0.016887.

5. Spheric Segment. (1.) Surface. Multiply the circumference

of the sphere by the height of the segment.

(2.) Capacity, or $c = 0.5236 \ h^2$ (3 $d = 2 \ h$), in which d is the diameter of the sphere and h the height; or $c = 0.5236 \ h^2$ (3 $r^2 + h^2$); in which r is the radius of the base of the segment and h its height.

6. Paraboloid, or solid formed by the rotation of a parabola about

its axis.

Capacity. Multiply the base by its height, half the product is the content.

7. Spheroid, or solid formed by the revolution of an ellipse about one of its axes.

· Capacity. Multiply the square of the revolving axis by the fixed axis, and the product by 0.5236, the result will be the content.

8. Regular, or Platonic bodies, as they are sometimes called, are contained under like, equal, and regular plane figures, of which the solid angles are all equal. The names and descriptions of these bodies, together with their multipliers, the side of each being unity, are contained in the following tables:-

Surfaces and Solidities of Regular Bodies, the Side being Unity, or 1,

| No of Sides. | Name. | Surface. | Solidity. |
|-------------------------|---|--------------------------------------|-----------|
| 4 6 8 12 20 | Tetraedron Hexaedron Octaedron Dodecaedron Icosaedron | 6.0000000 3.4641016 20.6457288 | |

| The diam, of a sphere being 1; the side of a | That may be in- scribed in the sphere, is | That may be circum- scribed about the square, is | That is equal to the sphere, is | .0 |
|---|--|--|---|----|
| Tetraedron Hexaedron Octaedron Dodecaedron Icosaedron | 0.816497 0 577350 0.707107 0.525731 0.356822 | 2.44948 1.00000 1.22474 0.66158 0.44903 | 1.64417 0.88610 1.03576 0.62153 0.40883 | |

Examples for Exercise.

1. Required the solidity of a cube, of which the side is 5 feet 3 inches? Ans. 144,7 feet.

2. What is the solidity of a block of marble, of which the length

is 10 feet, breadth $5\frac{\pi}{4}$ feet, and depth $3\frac{1}{6}$ feet? Ans. $201\frac{1}{4}$ feet.

3. Required the solidity of a prism, of which the base is a hexagon, each of the equal sides being 1 foot 4 inches, and the length of the prism 15 feet? Ans. 69.282 feet.

4. Required the convex surface of a cylinder, of which the circumference is 8 feet 4 inches, and length 14 feet? Ans. 1162 feet.

5. What is the solidity of a cylinder, of which the length is 5 ft. and diameter of its base 2 feet? Ans. 15.708 feet.

6. The diameter of the base of a right cone is $4\frac{1}{2}$ feet, and the slant height 20 feet; required the convex surface? Ans. 141.372

7. Required the convex surface of a frustum of a right cone, the circumference of the greater end being 30 feet, that of the less 10 feet, and the slant height 20 feet? Ans. 400 feet.

8. What is the solidity of a triangular pyramid, of which the

height is 30, and each side of its base 3? Ans. 38.97.

9. What is the solidity of a cone, of which the circumference of the base is 40 feet, and its height 50 feet? Ans. 2122 feet.

10. What is the solidity of the frustum of a cone, of which the diameter of the greater end is 5 feet, that of the less 3 feet, and the perpendicular height 9 feet? Ans. 115.454 cubic feet.

11. What is the solidity of a frustum of a square pyramid, one side of the greater end being 18 inches, that of the less 15 inches.

and the height 5 feet? Ans. 16380 cubic inches.

12. Required the convex superficies of a sphere, of which the diameter is 17 inches? Ans. 907.92 square inches.

13. Required the solidity of the same? Ans. 1.48868 cubic feet.

- 14. Required the solidity of the earth, considering it as a perfect sphere, of which the diameter is 7910 miles? Ans. 259136798136 cubic miles.
- 15. What is the solidity of the segment of a sphere, of which the diameter of the base is 20 feet, and its height 9 feet? Ans. 1795.4244 cubic feet.

SECTION III.

Surveying.

In landsurveying, the instruments commonly employed for the ordinary purposes are—

Gunter's chain, and ten iron pins.
 Cross-staff, and signal staves.

3. Field-book, or paper.

4. Case of mathematical instruments.

5. Plotting scales.

6. Parallel ruler, and beam compasses.

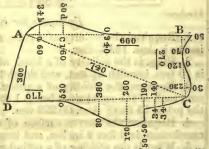
7. A small quadrant, if a theodolite is not at hand, to reduce

the hypotenusal to their horizontal measure.

It would exceed our present limits to describe all these, as well as some others, which may however appear perhaps in a work proposed with that view.

An Example of Laying Off a Field.

Having set up poles at A, B, C, and D, so as with the different dotted lines to reduce the body of the field to a quadrilateral form, and drawn a sketch of it, into which the measures when taken may be inserted; begin at any point A, measuring the successive distances A a, A c, &c., on the chainline A B, and the corre-



sponding offsets ab, cd, &c., and marking them as in the figure till a complete circuit A B C D A of the field and the diagonal A C are measured; these afford data for planning it, and computing the area. For the various portions may be considered either as trapezoids or triangles, whose contents may be ascertained by the rules given for that purpose.* The area computed in this manner will be 2.4295 acres, or 2 ac. 1 ro. 28.72 po., though it is better in general to retain it in acres and decimals. It is necessary to take an account of the roads, dikes, ponds, &c., of which the contents must all be stated distinctly by themselves when a whole estate is surveyed. In the case of the sale of crops, that in tillage only must be measured.

Required the plan and area of the field, from the following fieldbook, in which the angles were measured, with the pocket-box, sextant, and the distances with the chain, beginning the operations

at the gate near the south-east corner?

[•] Many landsurveyors first construct an accurate plan, from which, by scale and compass, the area is obtained with sufficient precision; and this is at least a good method of checking the result by computation.

Field-Book.

| Left hand Offsets, &c. | 11) | Stations, Distances, and Angles. | Right-hand Offsets, &c. |
|--|--------|--|--|
| 12 | Links. | | |
| Hedge. | 0 | 0 | Remark. The chain- |
| 177 | 38 | the state of the s | line bears nearly west |
| Zeminik (1000) | 00 | | along the north side |
| THE HOURS OF DIG TO | 73 | | of Bitterick Syke. |
| Deadriggs* or | 83 | 240 | of Bitteriek byke. |
| Crosshall lands | 70 | 300 | A TOTAL OF THE STATE OF THE STA |
| on the south or left | | | all a track to sail some |
| | 34 | 400 | and the delication of the same |
| hand | 0 | 480 | the state of the state of the |
| Market of the state | 0 | 510 | doing the to- |
| A second to the second to the | 44 | 650 | free trans to be a first |
| | 42 | 726 | the same time to design |
| | 100 | and the second s | 000000000000000000000000000000000000000 |
| 1 | | ⊙2d 85° 43′ 30″ N. | |
| Boundary. | 0 | 0 | The chain-line bears |
| The state of the s | 2 | 200 | nearly north. |
| AND MANUAL VISION NAMED | 5 | 400 | 100 100 100 100 100 100 100 100 100 100 |
| AND THE PROPERTY OF | 3 | 600 | man (manual) village (st. |
| 100 L 701 LECT MAY 140 | 0 | 800 | and and and fuller |
| The court make the | 10 | 860 | Million War / The Million |
| controlly burns. To Jeson | | 866 | send not have to be |
| ALL THE STATE OF T | 0 | The second secon | |
| ** 1 | | ⊙ 3d 73° 8′ 0″ E. | The state of the s |
| Hedge. | 0 | 0 | |
| | 50 | 100 | |
| Hardacres land | 66 | 200 | The chain-line bears |
| on the north | 83 | 264 | nearly east. |
| or left hand | 30 | 350 | |
| 1/3/12/2 | 66 | 456 | |
| and much bed to | 5 | 544 | |
| A STATE OF THE RESERVE | 130 | 700 | |
| Section 14 House Sea Sec. | 0 | 755 | |
| | - | ⊙ 4th101° 23′0″ S. | The chain-line bears |
| | 0 | 100 | almost south along |
| | | the contract of the contract o | |
| The second second | 12 | 200 | the road from Green- |
| V | 38 | | law to Eccles. The |
| | 65 | | diagonal from O 1st |
| m - 1 | 108 | 500. | to o 3d, measuring |
| To O 1st, or | 143 | 600 | 1053 links, was also |
| | 7 | W. E. S. L. CO. O. | taken, that the area |
| 4 | 0 | Area = 6.14537 ac. | might by the three |
| | 1 4 | | sides of the triangles |
| All the second s | | | be a check upon that |
| A CHARLES TO A COLUMN TO THE REAL PROPERTY AND A COLUMN TO THE REAL PROPER | 100 | | determined from us- |
| The state of the s | | | ing the angles. |
| | - | | 8 |

If there are dikes, ditches, or fences of any kind, they must be measured during the survey, and their amount stated. Also plantations, roads, commons, lakes, ponds, &c., must be all surveyed and classed separately from the arable land. For these we cannot here enter into detail.

[•] This place is mentioned in Sir Walter Scott's Minstrelsy of the Scottish Border.

الرا الأراف المائمي أاردا

on River

ing in an ing

Levelling.

It is often necessary to ascertain the difference of elevation of one point above another, for the purpose of conveying a stream of water to drive machinery. This may be performed in several ways, but the readiest and most acurate is by means of a spirit-level of the best construction. It must be accompanied by a pole, or rod divided into feet, and at least hundredths of a foot. On this rod a sliding vane is fitted, capable of moving easily up and down, and having a dark strong line or other well-defined mark upon it, by which the telescope, or in common levels the sight, may be directed. The slider must be moved upwards or downwards on the rod, till the mark coincide with the intersections of the cross hairs in the focus of the telescope. When this is accomplished, and the level being properly adjusted, the height in feet and hundredth parts is to be carefully read off and marked in a book for the purpose. Now, by means of a chain or measuring tape, let the pole-bearer place it at equal distances, alternately on each side of the level, such as about one or two hundred yards, if convenient, if a level with a good telescope be used. If an ordinary level with a plain sight be used, the distance must be reduced to as many feet. The heights taken with the telescope turned towards the place whence the observer set out, are called the back observations; and those taken towards the place where he means to finish, are called fore observations, for the sake of distinction. Since the pole is always placed at equal distances from the level, no allowance need be made for the curvature of the earth.*

EXAMPLE.

ATTEM SALTING

| Ва | ick. | For | re. |
|--------|--------------------|--------------------|--------|
| Dist. | Height on Pole. | Height on Pole. | Dist. |
| Links. | Feet. | Feet. | Links. |
| 10.0 | 2.92 | 4.68 | 100 |
| 100 | .1.56 | 3.79 | 100 |
| 200 | 0.48 | 5.63 | 200 |
| 200 | 1.35 | 4.86 | 200 |
| 150 | 1.27 | 3.74 | 150 |
| 150 | 1.34 | 2.56 | 150 |
| 100 | 2.36 | 3.94 | 100 |
| 50 | 3.28 | 4.36 | 50 |
| 1050 | 14.56 | 33.56 | |
| 2 | | 14.56 | 2- |
| 2100 | | 19.00 | |

Hence the difference of level on a sloping height of 2100 links of Gunter's surveying chain, or $2100 \times 0.66 = 1386$ feet, is 19 feet. When a spirit-level exactly adapted to this purpose, is not at hand, if there is a theodolite to be had, it will perform the operation, though it is not quite so convenient.

The difference of level is about 8 inches in a mile, which increases as the square of the distance. The difference of level in feet allowing for refraction, is 5 of the square of the distance in English miles.

In case of levelling for canals, the process is not different, only the canal is carried on an exact level, by judiciously choosing the situation winding round rising grounds, conveying it across ravines by aqueduct bridges, and allowing it to descend at particular points, by means of locks. Roads ought to be carried along a level line as nearly as possible, and only having gentle acclivities and declivities. This may be readily obtained by following routes somewhat circuitous in uneven parts of the country, taking the advantage of ravines, water courses, and the sides of lakes; for a greater distance on a road nearly level, is productive of less expense of animal strength, than by passing over considerable elevations. All very quick turns in the road, particularly when entering upon a bridge, ought to be avoided, as the danger from centrifugal force, which may be readily estimated by the formula, Part III., Sec. IV., is considerable. The justice of these remarks may be readily appreciated by considering many parts in most of our public roads which have hitherto been constructed upon the very worst principles, having been entrusted to what are called practical men, who are frequently the mere slaves of custom.

SECTION IV.

Rules and Formulæ.

When two angles of a plane triangle are known the third may be found, consequently, for general purposes, it is unnecessary to measure the third angle. But when great accuracy is required, or when the sides on the surface of the earth are large, they become spherical arcs, and then the third angle should always be measured as a check upon the results. In conducting geodetical operations, the triangle should be so chosen, if possible, as to produce the most accurate conclusions. To diminish the probability of error, the following rules should be observed:—

I. When one side only of a triangle is to be determined, the mea-

sured base should be nearly equal to the required side.

II. When two sides of a triangle are to be determined, the triangle

should, if possible, be equilateral.

III. When the base cannot be equal to one or to both the required sides, it should be as long as possible, and the two angles at the

base equal, and not less than twenty or thirty degrees.*

IV. When the centre of the instrument cannot be placed in the vertical line occupied by the axis of a signal, the observed angles must be reduced to it by an appropriate formula. Let C be the centre of the station, such as a tower, P the place of the centre of the instrument, by which the angle subtended by A B at

P is to be measured. Let the angle A P B be observed, and the distance C P be measured, it is required to find C, the measure of the angle A C B? Suppose A P B = P, B P C = p, C P = d, A C = D and B C = D'.

Since the exterior angle of the triangle A P I is equal to the sum of the two interior and opposite C P angles, A I B = P+I A P, and of the triangle B I C, the exterior angle A I B = C+C B P. Making these two values of A I B equal, by transposition, we have C-P=I A P-C B P. But

^{*} For a demonstration of these properties, see vol. 111. of Hutton's Course of Mathematics.

the triangles C A P, C B P give sin. C A P = sin. I A P = $\frac{C P}{A C}$ sin. A P C= $\frac{d \sin (P+p)}{D}$, sin. C B P= $\frac{C P}{B C}$ sin. B P C = $\frac{d \sin p}{D}$. And since the angles C A P, C B P, are, by hypothesis, always very small, their sines may be substituted for their arcs, hence, C= $\frac{d \sin (P+p)}{D}$ = $\frac{d \sin p}{D}$, which in seconds becomes $\frac{d}{\sin N}$ { $\frac{\sin (P+p)}{D}$ = $\frac{\sin p}{D}$ }; or R" being the length of an arc in seconds equal to the radius, or 206264".8, then C= $\frac{N}{N}$ = R" $\frac{N}{N}$ d × { $\frac{\sin (P+p)}{D}$ = $\frac{\sin p}{D}$ }. The use of this formula cannot be embarassing, provided the signs of sin. $\frac{N}{N}$ and sin. (P+ $\frac{N}{N}$) be properly attended to, as is illustrated by the following example:—Let the observed angle P be 43° 52" 49".44, $\frac{N}{N}$ = 264° 41′ 24", $\frac{N}{N}$ d = 10.706 feet, D = 57508 feet and D' = 66750 feet, required the reduction?

When signals are circular or polygonal towers, various methods may be employed to find the true angle, from a due consideration of the nature of the case, which, to any one possessing a knowledge of the elements of geometry, will readily occur.

V. The angles measured in an inclined plane, should be reduced

to the horizontal plane.

In this case the altitudes must be also observed, and then there is formed a spherical triangle, of which the three sides are given to compute the angle at the zenith, which may be performed by the

rules of spherical trigonometry.

VI. A spherical triangle being proposed, of which the three sides are very small compared with the radius of the sphere; if from each of its angles, one-third of the excess of the sum of its three angles, above two right angles be subtracted, the angles so diminished may be taken for the angles of a rectilineal triangle, whose sides are equal in length to those of the proposed triangle.

To find the spherical excess when the three sides are given in feet.

1. Rule.—To the constant logarithm 1.349380, add the logarithm of half the sum of the three sides, the logarithms of the three differences between these sides and that half sum, half the sum of these five logarithms will be the logarithm of the spherical excess in seconds.

2. To the logarithm of the area of the triangle taken as a plane one in feet, add the constant logarithm 0.674690; the sum is the lo-

garithm of the excess above 180° in seconds.

3. If the base and perpendicular of a triangle be given. To the logarithm of the base in feet, add the logarithm of the perpendicular, and the constant logarithm 0.373660; the sum will be the logarithm of the spherical excess in seconds.

The spherical excess amounts to one second for an area of 76 English square miles, whence, if the area in square miles be known, the spherical excess may be readily obtained by dividing it by 76.

VII. To reduce a base on an elevated level to that at the surface

of the sea.

Let r represent the radius of the earth, corresponding to the base b at the level of the sea, and r+a the radius referred to the level of the measured base B; then it is obvious that r+a:r::B:

$$b = B \times \frac{r}{r+a}$$
. Hence, $B - b = B - B \frac{r}{r+a} = B \times \frac{a}{r+a} = B \times \frac{a}{r+a}$

 $\left(\frac{a}{r} - \frac{a^2}{r^2} + &c\right)$. But the radius of the earth being very great in comparison of the difference of level a, we have the correction & sufficiently accurate, by retaining the first term. Hence, $\delta = B \times \frac{a}{a}$.

Rule.—By logarithms. To the logarithm of the measured base in feet, add the logarithm of its height above the sea, and the constant logarithm 2.680110; the sum will be the logarithm of a number of feet which, taken from the measured base, will be that at the level of the sea required.

VIII. To determine the horizontal refraction from observation.

Rule.—From the measure of the intercepted terrestrial arc, subtract the sum of the two depressions at its extremities; half the remainder is the refraction. If by reason of the smallness of the contained arc, one of the objects has an elevation instead of a depression, then the depression must be taken from the sum of the contained arc and elevation; half the remainder is the refraction.

FORMULÆ.

$$R = \frac{c - d - d'}{2} = \frac{c - (d + d')}{2} \qquad (1.)$$

If -d' becomes an elevation, it changes its sign, and becomes

The exact quantity of terrestrial refraction is very variable. It is estimated by Dr Maskelyne at one-tenth of the intercepted arc, by Delambre at one-eleventh, by General Mudge at one-twelfth, and by Legendre at one-fourteenth at a mean state of the atmosphere. In peculiar circumstances it varies very considerably from this, as from one-sixth to one-eighteenth of the contained arc.

IX. To find the angle made by a given line with the meridian.

With a good instrument measure the greatest and least angular distance of the pole star from the vertical plane in which the given line is situated; half the sum of these two measures will the angle

This may also be done, though less accurately, by computing the azimuth of the sun, or a star, when on the line, from an altitude

taken for that purpose.

X. In addition to what has already been said relative to finding the latitude of the place, we may add here, that the same thing may be very accurately obtained, by observing the greatest and least altitude or zenith distance of a circumpolar star, and correcting them for the effects of refraction; half the sum of the altitudes, thus corrected, will be the latitude, or half the sum of the zenith distances will be the colatitude.

XI. To determine the ratio of the earth's axes, and their actual magnitude from the measure of a degree of the meridian in two given distant latitudes, supposing the earth a spheroid generated by

the rotation of an ellipse about its minor axis.*

Let d and d' be the measure of two degrees, d being the least, or that nearest the equator, l and l' the latitudes of their middle points, t the semitransverse axis of the meridian or radius of the equator, c the semiconjugate or semipolar axis, c the excess of the equatorial radius above the polar semiaxis, and $r^{\circ} = 57^{\circ}.2957795$, the number of degrees in an arc are equal to the radius.

Then,
$$e = \frac{r^{\circ} (d'-d)}{3\sin(l'+l) \times \sin(l'-l)}$$
 (1.)

And
$$\frac{e}{t} = \frac{a-a}{3 \text{ d sin. } (l'+l) \times \sin. (l'-l)}$$
 (2.)

If
$$\frac{e}{t} = \epsilon$$
, ellipticity or compression, $t = \frac{r \cdot a}{1 - \frac{\epsilon}{a} - \frac{5}{a}\epsilon \cos 2l}$ (3.)

of degrees in an arc are equal to the radius.

Then, $e = \frac{r^{\circ} (d'-d)}{3 \sin.(l'+l) \times \sin.(l'-l)}$ (1.)

And $\frac{e}{t} = \frac{d'-d}{3 d \sin.(l'+l) \times \sin.(l'-l)}$ (2.)

If $\frac{e}{t} = \mathfrak{s}$, ellipticity or compression, $t = \frac{r^{\circ} d}{1 - \frac{\mathfrak{s}}{2} - \frac{\mathfrak{s}}{2}\mathfrak{s}} \cos.2l$ (3.)

When l is nothing, or when one of the degrees is at the equator from formula (1.) $e = \frac{r^{\circ} (d'-d)}{3 \sin.^{2} l}$ (4.) from formula (1.)

Therefore, the excess of the degree in any latitude above this degree at the equator, when divided by the square of the sine of the latitude, should always give the same quotient; or the excess of the degrees of the meridian above the degree at the equator, should be

 $d'-d=\frac{3}{r^{\circ}}\sin(2l+1)\sin(1)$, and since the sine of one degree is

0.017453,
$$d'-d = \frac{3 e \times 0.017453}{r^{\circ}} \sin. (2 l + 1^{\circ})$$
 (6.)+

The contiguous degrees therefore differ, by a quantity proportional to the sine of twice the middle latitude. The difference is a maximum when $2 l+1^{\circ} = 90^{\circ}$, or when the middle latitude is 45°.

From five different measures combined so as to produce the most accurate result, Mr Playfair found $\epsilon = 0.0032 = \frac{1}{312.5}$ nearly, and the equation representing the degrees of the meridian setting out from 45°, will be

 $D = 60759.472 - 290.576 \cos 2 l_{\ddagger}^{\dagger}$ (7.)

in fathoms, or,

• Playfair's Outlines of Natural Philosophy, Vol. II. Art. 59. † Using logarithms, d-d=0C. L. 1.0084715 + log. sin. (2 $l+1^\circ$) in fathoms,

or d-d=C. L. 1.7866228+log. sin. (2 $l+1^{\circ}$) in feet, where e=11158.8 fathoms, or 66952.8 feet respectively, and d = 60460 fathoms, or 362760 feet. \pm In toises D = 57011-272.65 cos. 2 l.

 $D = 69.044 - 0.3299 \cos 2 l$ (8.) in English miles.

Hence, e = 11158.8 = 12.680 t = 3486858.8 = 3962.349c = 3475700.0 = 3949.669

The radius of curvature for the parallel of $45^{\circ} = t - \frac{e}{2} = 2481279.4$ fath. = 3956.009 miles. The circumference of the meridian is therefore equal to the product of the mean degree at 45° by 360 = 24855.84 miles; and the circumference of the equator is 24896.16 miles, or about 40 miles more than the preceding.

A geographical mile is therefore 1012.6 fathoms, or 6075.6 feet.

tude is l, and D a degree of the curve perpendicular to the meridian at the same point, then, $e = \frac{r^{\circ}}{2}$ (D—d) sec. 2 l. (10.)

$$t = r^{\circ} D - \frac{r^{\circ}}{2} (D - d) \tan^{2} l.$$
 (11.)

$$\frac{e}{t} \text{ or } = \frac{2}{D-d} = \frac{D-d}{2 D \cos^2 l} = \frac{D-d}{2 D} \times \sec^2 l. \quad (12.)$$

For exercise the following measures of degrees of latitude are given.

| | Observers. | Lat. | Degrees in Toises. | Deductions. |
|---|------------|-----------|-----------------------|---------------------------------|
| d | Bouguer | 0° 0′ 0′′ | 56753 | Radius of the equator |
| | Condamine | 0 0 0 | 56749 | 3271691 toises. |
| 4 | Lambton | 12 5 ON. | 56761 | Semipolar axis. |
| | Lacaille | 35 18 OS. | 57037 | 3260964 toises, |
| ı | Mason | 39 12 0N. | 56888 | $\varepsilon = \frac{1}{304}$. |
| Н | Boscovich | 43 1 0N. | 56979 | Q = 5130740 toises. |
| 1 | Delambre | 46 12 ON. | 57021 | 1 toise = 1.949037 metre. |
| 1 | Mudge | 52 2 20N. | 57069 | 1 French foot = 144 lines. |
| | | 66 20 ON. | 57168 | 1 Englishfoot=135.073 lines. |

Let these be solved by the foregoing theorems, and the various consequences drawn.

Ex. 1.—In the Philosophical Transactions for 1795, D the degree perpendicular to the meridian, is given equal to 61182 English fathoms; d = 60851, and $l = 50^{\circ}$ 4′ N. By formula. (12.)

 $s = \frac{331}{2 \times 61182} \times \text{sec.} \ ^2 50^{\circ} \ 41' = \frac{1}{148.4} \text{ nearly, and much too great.}$

Ex. 2.—The length of a degree in latitude 52° 2′ 20″ N. is 57074 toises, that in 11° 0′ N. is 56755 toises; required the ellipticity by formula (2.)?

| $l' = 52^{\circ} \ 2' \ 20'' \text{ const. log.}$ | 9.522879 |
|---|----------------------|
| l'+l = 63 	 2 	 20 cosecant, | 0.049969 0.182718 |
| d' = 57074 $d = 56755$ ar. co. log | 5.245996 |
| d'—d 319 log | 2.503791 |
| $= 0.003202 \log 1$ | 7.505353 |
| or $=\frac{32}{10000} = \frac{1}{312.5}$ nearly. | - 3 2 |

If L = the length of a degree of longitude, then

$$L = \frac{\cos l}{r^{\circ}} (1 + \epsilon \sin^{2} l + \frac{3}{4} \epsilon^{2} \sin^{4} l). \qquad (13.)^{*}$$

If the value of the degree is wanted in toises, fathoms, or feet, the second member of this equation must be multiplied by the semitransverse axis in the same measure.

Ex. 1.—Required the length of a degree of latitude at Edinburgh, in 56° N.?

By formula (7), $D = 60759.472 + 290.576 \times \sin 22^{\circ} = 60759.427$ $+290.576 \times 0.374607 = 60868.3$ fathoms.

Ex. 2.—Required the length of a degree of longitude in latitude 56° N., the ellipticity being $\frac{1}{300}$?

By formula (13), $L = \frac{0.559193}{57.2957795} \left\{ 1 + \frac{1}{300} \times 0.68694 \right\}$; or L = $0.009760 \times 1.00229 \times 20918750 = 204635$ feet, or, taking in the second term mentioned in the note, it is 204648 feet. These formulæ are useful for fixing the latitude and longitude of a particular point when referred to some object whose situation has been well determined, such as many places in Britain are by the trigonometrical survey In this case any amateur observer may verify the latitude and longitude of his observatory deduced from his own observations, by a comparison with some point well settled in that work, when properly connected by trigonometrical operations. Even by taking a few angles with great care, the situation of a particular point may be well settled by spherical trigonometry, as in the following example communicated by Captain Hall.

Ex. 2.—Given the latitude of the Staff on North Berwick Law, 56° 3′ 8" N., longitude 2° 42′ 11" W., and the latitude of the Isle of of May light 56° 11′ 22" N., longitude 2° 32′ 47" W.; the angle at North Berwick Law, between the Isle of May and Dunglass Tower, 87° 41′ 1″, that at Dunglass, between the Isle of May and North Berwick Law, being 37° 20′ 13″; required the latitude and longi-

tude of Dunglass Tower?

Ans. Lat. 55° 56′ 31″.7 N., Long. 2° 21′ 42″ W.

^{*} If great accuracy is not required, 3 : 2 sin. 4 l. may be omitted in the quantity within the parenthesis.

If p be the length of a degree perpendicular to the meridian, t the equatorial radius, c the semipolar axis, t-c=d the difference of these, r° the length of an arc in degrees equal to radius, or $57^{\circ}.2957795$,

and
$$l$$
 the latitude, then $p = \frac{t + d \sin^{2} l}{r^{\circ}}$ nearly. . . . (14)

Ex. 5.—1f t = 3486850 fathoms, d = 11160 fathoms, and $l = 56^{\circ}$. $\frac{3486850 + 11160 \times 68694}{57,90578} = 60991$ fathoms.

If p be the measure of a degree of a great circle perpendicular to a meridian at a certain point, m that of the corresponding degree on the meridian itself, and o the length of a degree on an oblique arc, making an angle a with the meridian, then

$$o = \frac{p m}{p - (p - m) \sin^{2} a} = \frac{m}{1 - \frac{p - m}{p} \sin^{2} a} \qquad (15)$$

Ex. 6.—If p = 61182 fathoms, m = 60850 fathoms, and $a = 81^{\circ}56'$ 53", therefore

$$o = \frac{60850}{1 - \frac{332}{61182} \times 0.98038} = \frac{60850}{1 - 0.00532} = \frac{60850}{0.99468} = 61175.45 \text{ the}$$

length of the oblique degree in fathoms.

For an extension of this subject, see Mr Ivory on the properties of a line of the shortest distance traced on the surface of the oblate spheroid, in the sixty-seventh volume of the Philosophical Magazine. It is rather too long and difficult to be inserted in this place.

SECTION V.

Rules and Formulæ. SPECIFIC GRAVITY.

The difference between the absolute weight of a body, and its weight when entirely immersed in a fluid, is the same with the

weight of a quantity of the fluid equal in bulk to the body.

If W be the weight of a body in vacuo, (which is nearly the same as that in air,) and W' its weight in water, then W-W' is the weight of a quantity of water equal in bulk to the body; and since the weight of any body divided by an equal bulk of water, measures the specific

gravity, S, of the body, then
$$S = \frac{W}{W - W'}$$
 (1)

The specific gravities of bodies are determined by the hydrostatic balance, the hydrometer, &c. described in books on Natural Philo-

sophy.

To compute the specific gravity of air under given circumstances. It is shown in Playfair's Outlines, vol. I. § 333, that if the elasticity or tension at the freezing point, be denoted by unity and x, any number of degrees above that point, then the elastic force f at

that point, will be $f = (1.375)^{-\frac{1}{180}}$ of Fahrenheit's scale, or

$$\log f = \frac{x}{180} \times \log. (1.375) = \frac{x}{180} \times 0.138303$$
 (2)

This also gives the bulk of gas in like circumstances. But the specific gravity is reciprocally as the bulk, therefore the reciprocal of the bulk or the natural number answering to the arithmetical complement of the log. f, will be the specific gravity of permanently elastic fluids. Thus let the bulk and specific gravity of air at 32° F. = 1, then at 52° F. they will be 1.036, and 0.9652 respectively.

From the experiments of Gay Lussac, it may be shown that 0.4545 will be the specific gravity of aqueous vapour, when compared with atmospheric air, at 32° F. Now, when the temperature is given, the specific gravity of aqueous vapour is directly as its temperature, and the tension being given, the specific gravity is reciprocally as its bulk, the specific gravity s of aqueous vapour, (that of water being 1), in saturated air at any temperature t, and elastic force f, (from Dalton's table) will be obtained from the following formula, the barometer being at 30 inches.

rometer being $\frac{f}{s} = 0.4545 \times \frac{f}{30} \times \frac{660}{448+t} = \frac{10 f}{448+t}$ (3)

If it be not saturated, and
$$t'$$
 being the dew point
$$s = \frac{10 f}{448 + t} \times \frac{448 + t}{448 + t'} = \frac{10 f}{448 + t} \times \left(1 + \frac{t - t'}{448 + t'}\right) \tag{4}$$

The quantities in this expression are all known except f, which is to be taken from any good table, such as Dalton's or Ure's. See Table

II., page 48.

If, therefore, s' be the specific gravity of air fully saturated with moisture, a the specific gravity of dry air obtained from formula (2), and s the specific gravity of aqueous vapour in saturated air, derived from formulæ (3), then from the law of expansion discovered by

Dalton and Gay Lussac, that $v = \frac{p}{p-f,*}$, p being the barometric pressure, f the elastic force, and v the volume,

$$s' = a + \left(0.4545 \times \frac{660}{448 + t} - a\right) \times \frac{f}{30}$$
, or by simplication,

$$s' = a + s - \frac{af}{30} \tag{5}$$

If t' be the dew point, and s" be the specific gravity, according to the actual state of the atmosphere,

$$s'' = \left(a + s - \frac{af}{30}\right) \left(1 + \frac{t - t'}{448 + t'}\right) \tag{6}$$

in which a and s are got from the following table, page 165, and f from Dalton's.

Ex.—Required the specific gravity of air saturated with moisture,

By formula (2), $\frac{60}{180} \times 0.138303 = \frac{1}{3} \times 0.138303 = 0.046101$, ar. co.

of which is 9.953899. To this the natural number is
$$0.89929 = a$$
. But by formula (3), $s = \frac{10f}{448 + t} = 0.02782$, and $\frac{af}{30} = 0.04502$.

Now, $s' = a + s - \frac{af}{30}$ by formula (5); therefore, s' = 0.89929 +0.02782-0.04502=0.88209 the specific gravity of air saturated with moisture, at 92° F. If the air is not saturated. Suppose 87° F. the dew point represented by t', then the factor $1 + \frac{t-t'}{448+t'}$ in formula

[•] Daniell and Tredgold, contend that this formula should be $\frac{p+f}{n}$. The difference in a moderate range, however, is not great. The elasticity in the example, was not taken from Dalton. It is difficult to obtain correct formulæ for these researches.

(6), becomes $1 + \frac{92 - 87}{448 + 92} = 1 + \frac{1}{108}$, therefore, $0.88209 + \frac{0.88209}{108} =$

0.88209 + 0.00817=0.89026, the specific gravity of air in the given

circumstances, that of dry air at 32° F. being unity.

It is shown in Playfair's Outlines, vol. I., art. 256, that if the specific gravity of air be called m, that of water being 1; if W be the weight of any body in air, and W' its weight in water, then W+m (W—W') is its weight in vacuo very nearly. In a mean state of the atmosphere at 30 inches of the barometer and 60° F. m=0.00122 nearly, which may be reduced to any other temperature by the foregoing formula (4), and to any other pressure by multiplying $\frac{p}{30}$

If s be the specific gravity of a body ascertained by weighing it in air and water, and m the specific gravity of the air at the time when the experiment was made; the correct specific gravity s', or that which would have been found if the body had been weighed in a vacuum instead of air, or

s' = s + m (1—s). (7) Where the body is heavier than water, this correction is subtrac-

tive; when lighter it is additive.

Ex.—The weight of Captain Kater's experimental pendulum was carefully determined in air, by Barton's balance from the Mint, and found to be 66904 grains. The trough, which had been previously placed under the pendulum, was then filled with distilled water, and the weight of the water displaced was 9066 grains. The small portion of iron wire which was immersed in the water was carefully noted; the weight of the wire by which the pendulum was suspended was 56 grains, and the weight of water equal in bulk to that part of the wire which was immersed was 2.5 grains. The temperature of the water was 68° F., that of the atmosphere 62° F., and the ba-

rometer 29.9 inches. Now since $s = \frac{w}{w - w'}$, w being the weight in air, and w' that in water, then

 $s = \frac{66848}{90635} = 7.37552$ at 29.9 bar. and 62° F., and s' = 7.37552 + 0.00120678 (1—7.37552) = 7.36783 at 68° Fahrenheit.

But the specific gravity of water oat 68° is 99936, that at 62° be-

ing 1; and, therefore

 $\frac{1}{\sigma}$ × s' = $\frac{1}{0.99936}$ × 7.36783 = 7.37254 at 62° F.

Biot's experiments give at 30 inches bar., and 60° F, the specific gravity of air 0.00122, or $\frac{1}{820}$, water being 1.

Mr S. Rice, from Sir G. Shuckburgh's experiments, deduces 0.0012085, not differing much from Biot's, and generally supposed the more correct. According to Gay Lussac, the expansions of fluids from 32° to 212° F. is 0.375, whence $\frac{375}{180} = \frac{1}{480}$ for 1° F.

Now suppose c = the first correction of the length of the pendulum, c' the second, l the measured length of the pendulum, p the barometric pressure, the standard being 30 inches; and l the difference of temperature from the standard, then

If l' = the corrected length of the pendulum l, from a mean of Captain Kater's experiments at London in air, then $l' = l + \frac{l}{s(c + c')}$ (10), s being the specific gravity of the pendulum.

s being the specific gravity of the pendulum. Whence $c = \frac{24600}{29.786} = 826$, and $\delta t = 69^{\circ}.62 - 62^{\circ} = 7^{\circ}.62$, hence $c' = \frac{826 \times 7.62}{480} = 13$, therefore c + c' = 839.

Hence by formula (10) $l' = l + 39.13284 \times \frac{1}{839} \times \frac{1}{7.37254} = l + 0.00633$.

It is now only necessary to correct for the height above the sea,

which is 92.5 feet.

The correction for this height found by the formula, which will

presently be given, is 0.00023.

Hence l''=39.13284+0.00633+0.00023=39.13940. In this case no allowance is made for the hygrometer. Now if the air were supposed half saturated with moisture, since Captain Kater does not give the state of the hygrometer, and the mean between Biot's and Rice's specific gravity of air taken, the true length would come out 39.13938, which differs from Captain Kater's result by 0.00009 in excess.

It is shown by writers on mechanics, that when the semiare described by a pendulum is 1°, the time lost by oscillating in a circular, instead of a cycloidal or infinitely small arc, is $\frac{1}{52524}$ in each second, and that in different small arcs of the same circle, the time lost varies nearly as the square of the arc; hence if a pendulum makes v vibrations in 24^h , when vibrating in very small circular arcs, of which the mean at the commencement and termination of each experiment is d degrees, it would, in the same time, make $v + \frac{d^2v}{d^2}$

52524 infinitely small vibrations. Hence to correct the oscillations of a pendulum for the arcs of vibration, multiply the square of the mean arc when it makes

 Daily
 86000 oscillations by
 1.637

 86100
 1.639

 86200
 1.641

 86300
 1.643

 86400
 1.645

 86500
 1.647

 86600
 1.649

Since the force of gravity varies directly as the length of the pendulum, or inversely as the squares of the number of vibrations, and the diminution of the force of gravity, arising from the buoyancy of the atmosphere, is $\frac{1}{m}$ past; therefore if v be the number of vibration in air, and V those in a vacuum, then

$$V = \left\{ v^2 \left(1 + \frac{1}{m} \right) \right\}^{\frac{1}{4}} = v \left\{ 1 + \frac{1}{2m} - \frac{1}{8m^2} + \&c. \right\}$$
 (10)

V = v + c, and hence $c = \frac{v}{2m}$ nearly.

In Captain Kater's experiments at Unst, the specific gravity of the pendulum, to that of air, was as 7099 to 1, hence $\frac{1}{m} = \frac{1}{7099}$, and

therefore $\frac{v}{2m} = \frac{86090.77}{14198} = 6.07$ nearly.

If n' be the number of oscillations performed in 24^h by the experimental pendulum, n the true number, e the expansion for a change of one degree Fahrenheit, t the standard temperature, and t' the observed, then

 $n = n' + \frac{1}{2} n' e (t' - t)$

In Captain Kater's pendulum e=0.00001 of an inch nearly, whence

 $n = n' + \frac{1}{2}n' \times 0.00001 \ (t' - t)$.

Hence if v = 86058.82, $t' = 71^{\circ}.6$ and $t = 62^{\circ}$, the number of vibrations at the latter temperature are $n = 86058.72 + \frac{1}{2} \times 86058.72 \times \frac{1}{2}$ $0.00001 \times 9.6 = 86082.77$.

To reduce the length of the pendulum from any height to the level of the sea, the true length being denoted by l, the observed by l', the height above the sea by a, and the radius of the earth by r,

$$l = l' + \frac{2 a l'}{r} \tag{12}$$

Some allow one-third for the effect of the dense strata immediate-

ly under the pendulum, in which case $l = l' + \frac{4 \cdot a \cdot l'}{3 \cdot r}$

In a similar manner
$$v = v' + \frac{2v'a}{3r}$$
 . (14)

At Unst $\frac{2 v' a}{3 r} = 0.06$, therefore

86090.77 + 6.07 + 0.06 = 86096.90 = the number of oscillations of the pendulum in a mean solar day at the level of the sea in vacuo.

These formulæ are sufficient for most purposes. Biot has, how, ever, demonstrated, that if c be the correction in seconds for the mean arc of vibration, n the number of oscillations, M the logarithmic modulus, a the arc of vibration at the commencement of the interval, and b that at the end, then

 $c = \frac{n'\sin(a+b)\sin(a-b)}{2}$ (15)32 M log. (a)

These arcs being small, their lengths will not differ sensibly from their sines, whence if a and b are given in degrees, the lengths of these arcs will be $0.0174533 \ a$ and $0.0174533 \ b$, and M = 2.302585, these values being substituted for a, b, and M, equation (15) will be-

come $c = \frac{n'(a+b)(a-b)}{241886 \log. (\log. a - \log. b)}$, and adopting logarithms, we come $c = \frac{1}{241886} \log (\log a - \log b)$ finally have $\log c = \{\log n' + \log (a+b) + \log (a-b)\}$

| To apply this to practice let marked E, and we have $a=1^{\circ}.21$ $a+b=2.30 \log$. $a-b=0.12 \log$. $n'=86056.47 \log$. | and $b=1^{\circ}.09$, whence | th experiment e.361728 .079181 .934785 |
|---|-------------------------------|---|
| Sum | | .375694 |
| Diff 0.045359 log | 100 mg/m 15 200 mg | E pisan/2 to 1 |
| Sum (B) | Is I have all the | .040274 (B) |

 $(A - B) = \log c = 2^{s}.165.$

Hence n = n' + c = 86056.47 + 2.165 = 86058.635. Captain Kater thinking this an unnecessary refinement in practice, multiplies the square of the mean arc by 1.638 Table (A); thus $1.15 \times 1.15 \times 1.638 = 2^{\circ}.166$ nearly the same as before; and, by selecting the proper number, this is sufficiently correct for almost any purpose,

and much more simple.

If the length of a pendulum oscillating seconds of mean time at one place or point on the earth's surface be known, its length at another place, where the same invariable pendulum makes a different number of vibrations, may readily be found. For if l be the length at the first place, l' that at the second, v the number of vibrations at the first place in 24 hours, and v' that at the second, then as is shown by writers on mechanics,* $l:l'::v^2:v'^2$. (17) consequently if three of these be known the fourth may be found.

As this is rather laborious, an approximate rule may be obtained sufficiently correct for most purposes where the difference of oscillations does not exceed 30 or 40, or in an arc of five or six degrees. If ΔL represent a small variation of the length of the pendulum, and ΔN that in the number of oscillations, then ΔL , $\frac{L}{\Delta N}$

and
$$\Delta N = \frac{\frac{1}{2} N \Delta L}{L}$$
. (18)

Let δ L be the variation of L for one degree of Fahrenheit's thermometer, and n the number of degrees of change of temperature, for this then Δ L = n δ L × L, and Δ N = $\frac{1}{2}$ N n δ L . (19)

Since the variation of brass from expansion is nearly 0.00001 inch

for 1° Fah.
$$\triangle$$
 N = 0.432 n , and \triangle L = $\frac{n \text{ L}}{100000}$. (20)

EXAMPLE I.

Captain Kater found the experimental pendulum made at London in latitude 51° 31′ 8″ N. 86061.52 oscillations at 62° Fah. in a mean solar day, while at Unst in latitude 60° 45′ 28″ N., it made 86096.90 oscillations in the same time; required the length of the pendulum at Unst, that at London being 39.13929 inches?

^{*} See Gregory's Mechanics, vol. I., section II., for this and other formulæ and corrections more simple than those given here.

Here $86096.90 - 86061.52 = 35.38 = \Delta N$. Now $\Delta L = \frac{L \Delta N}{\frac{1}{4} N}$

formula (18) = $\frac{39.13929 \times 35.38}{43048.45}$ = 0.03217, consequently 39.13929

+ 0.03217 = 39.17146 inches, the length at Unst.

Ex. 2.—Captain Hall found an experimental pendulum, making 86235.98 oscillations at London at 62° Fah., made 86101.34 oscillations at Galapagos at the temperature of 68°. Hence from the number of oscillations at London (since 68°-62°=6°,) we must subtract (formula 20) $0.432 \times 6 = 2.59$ oscillations from that at London, which becomes 86233.39.

Now by formula (17), as the places are very distant, $v^2: v'^2::l:$ l':: 39.13929: 39.01951, the length of the pendulum at Galapagos.

Of late the figure of the earth has been determined with great accuracy by means of the pendulum. It is demonstrated by the theory of gravitation, that the length of the pendulum is augmented from the equator to the pole, proportionally to the square of the sine of the latitude, in such a manner that if the length of the equatorial pendulum be represented by z, and its absolute variation from the equator to the pole by y, then l, its length in any other latitude, L will be represented by the following equation:-

 $l = z + y \sin^2 L$

If we have two equations of this form, in which l and L are determined by observation, we can obtain the values of z and y.

$$l = z + y \sin^2 L$$

$$l' = z + y \sin^2 L'$$

hence
$$y = \frac{l'-l}{\sin (L'+L)\sin (l'-L)}$$
 (2)

And
$$z = l - y \sin^2 L$$
 . (3)

Consequently 2 represents the diminution of gravity from the pole to the equator.

Now by the doctrine of central forces if f denote the centrifugal force; # the circumference of a circle to diameter unity; r the radius of the given circle in which a body revolves; t the time of re-

volution, and g the gravitating force, then $f = \frac{4\pi}{r} \frac{^2 r}{t^2}$. But by the

theory of the pendulum, if l is its length, $g = \pi^2 l$; hence

$$f = \frac{4 r}{t^2 l} = \frac{r}{\left(\frac{1}{2}\right)^2 l} \qquad . \tag{4}$$

The ratio of the centrifugal force to gravity may be expressed by $\frac{f}{1+f}$, and the ellipticity of the meridian or flattening of the earth is from theory equal to 5* of the ratio of the centrifugal force to gravity, diminished by the fraction obtained from dividing the difference of the lengths of the pendulum at the pole and equator by its length at the equator. Wherefore if & denote the ellipticity,

^{*} This fraction is obtained by approximation, and is not perfectly correct. By taking in the quantities of the second order, the ellipticity would vary about $\frac{1}{200}$ from the first approximation. It is difficult to solve the equations involving these. Still, however, no error should be allowed, if possible, to affect the final results, but what unavoidably belongs to the observations.

$$\epsilon = \frac{5}{2} \times \frac{f}{1+f} - \frac{y}{z}$$

 $\epsilon = \frac{5}{2} \times \frac{f}{1+f} - \frac{y}{z}$ By substituting the value of f from equation (4)

$$\varepsilon = \frac{5}{2} \times \frac{r}{r + (\frac{1}{2})^2 l} - \frac{y}{z} \qquad (5)$$

As t in these investigations denotes the time which the earth takes to perform a rotation about its axis, or 86164.0908; $\frac{1}{2}$ $t^2 =$ 1856062632, r, the radius of the equator, is 20918750 feet, l, the length of the equatorial pendulum by numerous observations, is 39.013 inches, or 3.25108 feet, and y = 0.20712 inch.

Whence
$$\varepsilon = 0.008638 - \frac{y}{z}$$
 (6)

By combining a great number of the best observations I have found $\epsilon = 0.003333 = \frac{1}{300}$ nearly.

From these we may get a formula to compute the length of the pendulum at any latitude.

Commencing at the equator $l = 39.013 + 0.20712 \sin^2 L$ Setting out from 45°, $l = 39.11656 - 0.10356 \cos^2 L$ (\mathbf{B})

Ex.—Required the length of the pendulum at Leith, in latitude 55° 58′ 39″ N. ?

Ans.—39.1555 inches.

Since $g = \pi^2 l = 32.2$ feet.

Hence the length of the pendulum and force of gravity may be found at any latitude.

But the force of gravity may be found more readily by a particu-

lar formula for that purpose.

Since g is equal to 32.172 feet, or 9.8058 metres at 45°, then G at any other latitude will be

 $G = g (1 - 0.00268 \cos^2 L)$ (7)Or $G = 32.172 (1 - 0.00268 \cos^2 L)$ in feet.

Let L be the length of the sexagesimal pendulum and l that of the French decimal-metrical pendulum, then

L = 52.74079 l(8)of Sir George Shuckburgh's scale,

or L = 52.740564 l(9)

of Bird's Parliamentary Standard of 1758.

Let v be the velocity of sound at 30 inches of the English barometer, 60° of Fahrenheit's thermometer and 14° of Mr Goldingham's hygrometer which he used at Madras, also let a be the change of velocity for a variation of one inch of the English barometer, & for that of one degree of Fahrenheit's thermometer, y that for one degree of Mr G's hygrometer, w the velocity of the wind, and \varphi the angle which the direction of the wind makes with that of the sound, and V the true velocity under given circumstances, then

 $V = v + \alpha (p' - p) + \beta (t' - t) + \gamma (h' - h) + \omega \cos \varphi$ in which p = 30 inches, $t = 60^{\circ}$ Fah. $h = 14^{\circ}$ hygrometer, and p', t'and h', the observed states of the barometer, thermometer, and hy-

grometer, respectively.

From an examination of Mr Goldingham's experiments at Madras, I have found $\alpha = 18.8$ feet, $\beta = 1.14$ feet, and $\gamma = 2.87$ feet. The values of ω and φ not being stated in any set of experiments which I have seen, have not been exactly verified. They must be known, however, at the time of computing the velocity as they undoubtedly affect it. Without these it becomes

 $V = 1100 + 18.8 (p' - 30) + 1.14 (t' - 60^{\circ}) + 2.87 (h' - 14^{\circ}) (11)$

Required the velocity at Port Bowen, the Bar. being at 30.398 in. Fahrenheit's Ther. — 38°.5., the state of the hygrometer, and velocity and exact direction of the wind being unknown?

Ans.—995.19, differing about 19 feet from observation from want

of the other parts of the data.

Or, if V be the velocity, t the temperature, f the elastic force of vapour by Dalton's table for the dew point, obtained by Daniell's hygrometer, or otherwise by formula, page 53, p the barometric pressure, λ the latitude of the place of observation, and ω cos. ϕ the same as before,

 $V = \{104.0885 + 0.10831 (t - 32^{\circ})\} \left(1 + \frac{f}{5\frac{1}{3}} p - 2f\right) (10.2738 - 0.01378 \cos 2 \lambda) + \omega \cos \varphi, \text{ in English feet.}$ (12)

Ex.—On the 19th of July, 1826, in mean latitude 56° N., longitude 3° 10′ W., several experiments were tried on the velocity of sound, when the guns on Edinburgh Castle were fired in honour of his Majesty's coronation. They were made on the coast of Fife at the distance of 42546 feet, the barometer standing at 29.96 inches, the thermometer at 72°, the dew point by Daniell's hygrometer, or by a thermometer, having its bulb moistened with tissue paper, (page 53) at 66°, the velocity of the wind by an anemometer was 15 miles per hour, or 22 feet in a second, making an angle of 60° with that of the sound; required the true rate per second and the difference between theory and experiment, when the arithmetical mean of a number of experiments gives 37.448 seconds for the time elapsed between seeing the flash and hearing the report?*

$$V = \{104.0885 + 4.3324\} \left(1 + \frac{0.635}{158.52}\right) (10.2738 + 0.1136) + 22 \times 0.5 = 108.4209 \times 1.004 \times 10.3874 + 11 = 1141.715$$

Experiment gives
$$\frac{42546}{37.448} = \frac{1136.189}{5.526}$$
Difference $\frac{42546}{37.448} = \frac{1136.189}{45.526}$

or excess of the formula.

In a river or open canal, let v be the velocity of the stream measured by the inches it moves over in a second of time; r a constant quantity, called the radius of the section, and obtained by dividing the area of the transverse section of the stream expressed in square inches by the boundary or perimeter of that section, diminished by the superficial breadth of the stream expressed in linear inches. Also let λ be the length of an open canal or of a close pipe; δ the difference of the level of its extremities, d the diameter in the case of a pipe, h the height of the water in the reservoir above the upper orifice of the pipe, and h' the height above the lower orifice, at which the water stands in the cistern into which it is emptied.

Now let $\frac{\delta}{\lambda} = i$ or the sine of inclination and $\frac{h + \delta - h'}{\lambda} = k$. The formula for the velocity of water in pipes, per second, will be $v = \{32806.6 \ d \ k + 0.023751\}^{\frac{1}{2}} - 0.154113$. (13)

(x)

^{*} If a series of experiments are made by a gun at each end of the measured base, the geometrical means of the times should be taken. See Bulletin de Sciences for 1826.

Ex. Let
$$\delta = 65$$
 feet, $d = 19$ inches, $\lambda = 18300$ feet, $\frac{\delta}{\lambda} =$

 $\frac{65}{18300}$ = 0.00352 = k, therefore

 $v = \{32806.6 \ d \ k + 0.020751\}^{\frac{1}{2}} = 0.154113 = 46.9$ inches the velocity per second.

In rivers and other canals, the formula is

 $v=\{32806.6\ r\ i+0.023751\}^{\frac{i}{2}}-0.154113$. . . (14) These formulæ have been simplified, and are tolerably correct.

Suppose v, d, δ , and λ , are all expressed in feet,

$$v=50\left\{\frac{d\delta}{\lambda}\right\}^{\frac{1}{2}}$$
 nearly the velocity in feet, per second. (15)

Let D be the discharge per minute in cubic feet, then

$$D=2356 d^2 \left(\frac{d \delta}{\lambda}\right)^{\frac{1}{2}} \qquad . \qquad . \qquad . \qquad (16)$$

To find the fall in a river caused by obstruction, such as the piers of a bridge, &c.

Let v be the velocity of the stream in feet per second, b the whole breadth of the channel in feet, c the contracted breadth between the obstacles, and f the fall, then

$$f = \left\{ \left(\frac{25 \ b}{21 \ c} \right)^2 - 1 \right\} \frac{v^2}{64} = \frac{1.42 \ b^2 - c^2}{64 \ c^2} \times v^2 \text{ very nearly} \qquad (17)$$

Let, as is nearly the case with the old London Bridge, $v=3\frac{1}{6}$, b=926, c=200,

Hence
$$f = \frac{1.42 \ b^2 - c^2}{64 \ c^2} \times v^2 = 0.46 \times 10^{-1}_{36} = 4.73$$
 feet, or 4 ft. 8^{3}_{4}

inches by the formula, while that by experiment was 4 feet 9 inches.

TO FIND THE TONNAGE OF A SHIP BY LOGARITHMS, ACCORDING TO THE COMMON METHOD.

Rule.—If the vessel is a ship of war, let fall a perpendicular from the fore-side of the stem, at the height of the hause holes; but if a merchantman, the perpendicular is to be let fall from that part of the fore-side of the stem which is at the same height above the keel, as the wing transom; also let fall another perpendicular from the back of the main post, at the height of the wing transom. Find the distance between these two perpendiculars, from which subtract three-fifths of the extreme breadth; and also, the product of the height of the wing transom above the upper edge of the keel, by $2\frac{1}{2}$ inches, and the remainder is the length of the keel for tonnage. To the logarithm of which, add the logarithm of the breadth, and that of the half-breadth, and the constant logarithm 8.02687;* the sum, rejecting 10 from the index, will be the logarithm of the tonnage required.

Ex.—Let the length between the perpendicular at the fore-part of the stem, and the back of the post, be 100 feet: the extreme breadth 271 feet, and the height of the wing transom 15 feet. Required the

tonnage?—Ans. 321 tons.

The arithmetical complement of the logarithm of 94, being the common divisor for finding the tonnage. This method is far from being correct. See papers on Naval Architecture, published by Morgan and Creuze. G. B. Whittaker, London. 1826.

TABLES OF SPECIFIC GRAVITY.

| 801 | ZIDS. |
|--|--|
| Principle March Street Committee (1947) | Control of the last of the las |
| Platina | Marble, green Campanian 2.742 |
| Gold, pure, hammered 19.362 | , Parian . 2.837 , Norwegian . 2.728 |
| Guinea of George III. 17.629 | , Norwegian . 2.728 |
| Tungsten . 17.600 Mercury, at 32° Fahren. 13.598 | , green Egyptian 2.668 Emerald 2.775 Pearl 2.752 |
| Mercury, at 32° Fahren. 13.598 | Emerald 2.775 |
| Lead | Pearl 2.752 |
| Palladium 11.300 | Chalk, British . 2.784 |
| Rhodium 11.000 | Jasper 2.710 |
| Virgin Silver . 10.744 | Coral 2.680 |
| Shilling of George III. 10.534 | Rock Crystal 2.653 |
| Bismuth, molten . 9.822 | English Pebble . 2.619 |
| Copper, wire-drawn 8.878 | Limpid Feldspar . 2.564 |
| Red Copper, molten 8.788 | Glass, green . 2.642 |
| Molybdena . 8.611 | —, white 2.892 |
| Rhodium | , bottle 2.733 |
| . 0.213 | Porcelaine, China . 2.385 |
| Uranium 8.109 | , Limoges 2.341 |
| Steel from 7.769 to 7.816 | Native Sulphur . 2.033 |
| Cobalt, molten 7.812 | Ivory 1.917 |
| Bar Iron 7.788 Pure Cornish Tin . 7.291 Ditto hardened | Ivory 1.917 Alabaster, 1.874 |
| Pure Cornish Tin . 7.291 | Alum 1.720 |
| Ditto hardened . 7.299 | Conal onaque 1.140 |
| Cast Iron 7 907 | Sodium 073 |
| Zinc 6.869 | Oak heart of 950 |
| Antimony 6.719 | Alabaster, 1.874 Alum 1.720 Copal, opaque 1.140 Sodium 973 Oak, heart of 950 Ice 930 Potassium 866 Beech 852 Ash 845 Apple-Tree 793 Orange-Wood 705 Pear-Tree 661 |
| Tellurium 6.115 | Potaggium 966 |
| Chromium 5 000 | Rocch 959 |
| Spar heavy 1420 | Ach 045 |
| Jargon of Covion | Apple Tree |
| Oriental Pulser 4.410 | Apple-Tree |
| Samphine Oriental 2004 | Orange-wood 705 |
| Ditto Progilian 2.191 | Pear-Tree |
| Zinc | Pear-Tree 661 Linden-Tree 604 |
| Oriental Topaz . 4.019 Oriental Beryl . 3.549 | Cypress |
| Diamond for 0 501 | Cedar 561 |
| Diamond . from 3.501 to 3.531 | Fir |
| English Flint Glass 3.329 Tourmalin . 3.155 Asbestus . 2.996 | Cypress 598 Cedar 561 Fir 550 Poplar 383 Cork 240 |
| Achaeta 3.155 | Cork 240 |
| Asbestus 2.996 | No. of the Contract of the Con |
| | IIDS. |
| Liqu | The second secon |
| Sulphuric Acid . 1.841 | Burgundy Wine . 991 |
| Sulphuric Acid . 1.841 Nitrous Acid . 1.550 Water from the Dead Sea 1.240 | Olive Oil |
| Water from the Dead Sea 1.240 | Muriatic Ether . 874 |
| Nitric Acid . 1.218 Sea-Water . 1.026 Milk 1.030 | Oil of Turpentine . 870 |
| Sea-Water . 1.026 | Liquid Bitumen . 848 |
| Milk 1.030 | Alcohol, absolute . 792 |
| Distilled Water . 1.000 | Sulphuric Ether 716 |
| Distilled Water 1.000 Wine of Bourdeaux 944 | Air at the Earth's sur, about 12 |
| | The state state of the state of |

^{1.} Since a cubic foot of water, at the temperature of 40° Fahrenheit, weighs 1000 ounces avoirdupois, or 62½ pounds, the numbers in the preceding tables, omitting the decimal points, exhibit very

nearly the respective weights of a cubic foot of the several substances

in avoirdupois ounces.

2. If the weight of a body be known in avoirdupois ounces, its weight in Troy ounces will be found in multiplying it into 91145. And, if the weight be given in Troy ounces, it will be found in avoirdupois by multiplying it into 1.0971.

| | _ | | |
|----------------------------|-----------------------------|------------------------------|---------|
| | GAS | SES. | 200E |
| Atmospheric air* | 1.0000 | Muriatic acid-gas | 1.2474 |
| Vapour of hydriotic ether | 5.4749 | Sulphuretted hydrogen | 1.1912 |
| oil of turpentine | 5.0130 | Oxygen-gas | 1.1036 |
| Hydriotic acid-gas . | 4.4430 | Nitrous-gas | 1.0288 |
| Fluo-silicic acid-gas . | 3.5735 | Olefiant-gas | 0.9784 |
| Vapour of sulph. of carbon | 2.6447 | Azote, or nitrogen-gas | 0.9691 |
| sulphuric ether | | Oxide of carbon . | 0.9569 |
| Chlorine | 2.4700 | Hydro-cyanic vapour | 0.9476 |
| Fluo-boric gas | 2.3709 | Phosphuretted hydrogen | 0.8700 |
| Vapour of muriatic ether | 2.2190 | Steam of water | 0.6235 |
| Sulphurous acid-gas . | 2.1920 | Ammoniacal-gas . | 0.5967 |
| Cyanogen | 1.8064 | Carburetted hydrogen | 0.5550 |
| Vapour of absolute alcohol | 1.6133 | Arseniated hydrogen | 0.5290 |
| Nitrous oxide | 1.5204 | Hydrogen-gas | 0.0732 |
| Carbonic acid | 1.5196 | Charles | 1 - 1 |
| * Air 0.00122 water | being = | 1, hence Gas S. G. x 0.00122 | = S. G. |
| Water = 1. | | | CODICE |
| | The second name of the last | | |

Specific gravity of Distilled Water at different temperatures, that at 62° being taken as unity.

| | | | | | | | | 1:00102 | |
|----|---------|----|---------|----|---------|----|----|---------|----|
| 68 | 0.99936 | 60 | 1.00018 | 52 | 1.00076 | 28 | 44 | 1.00107 | 36 |
| 66 | 0.99958 | 58 | 1.00035 | 50 | 1.00087 | 30 | 42 | 1.00111 | 38 |
| 64 | 0.99980 | 56 | 1.00050 | 48 | 1.00095 | 32 | 40 | 1.00113 | 40 |

MISCELLANEOUS COMPUTATIONS AND EXPERIMENTS.

The pendulum vibrating seconds of mean solar time at London in a vacuum, and reduced to the level of the sea, is 39:1393 inches; consequently the descent of a heavy body from rest in one second of time, in a vacuum, will be 193.145 inches. The logarithm 2:2858828.

A platina metre at the temperature of 32°, supposed to be the ten millionth part of the quadrant of the meridian, 39 3708 inches. The ratio to the imperial measure of three feet, as 1 09363 to 1, the logarithm 0 0388717.

The following standards, accurately measured, give these results:—Gen. Lambton's scale, used in the Trig. Surv. of India, 35 99934 inches.

Sir G. Shuckburgh's scale (which for all purposes may be considered as identical with the imperial standard)

Gen. Roy's 'scale 36.00088

Royal Society's standard 36.00135

Ramsden's bar 36.00249

Weight of a cubic inch of distilled water in a vacuum at the temp. 62°, as opposed to brass weights in a vacuum also, 252 722 grains

log. 2·4026430

| Consequently a cubic foot 62:3862 pounds avoir- | x |
|---|---|
| Weight of a cubic inch of distilled water in air at | |
| 62° of temperature with a mean height of the log. 2.4021857 barometer 252.456 grains | |
| Consequently a cubic foot 62:3862 pounds avoir- dupois | × |
| And an ounce of water 1.73298 cubic inches log. 0.2387924 | |
| Cubic inches in the imperial gallon, 277.276 log. 2.4429124 Diameter of the cylinder containing a gallon at one log. 1.2739112 | |
| inch high, 18.78933 | |

SPECIFIC GRAVITY OF DRY AND SATURATED AIR.

That at 30 in. Bar., and 32° Fahr. being 1.

| Temp. Fahr. Specific Grav. of Saturat. Air. Fahr. Fahr. Specific Grav. of Saturat. Air. Specific Grav. of Saturat. Air. 32° 1.00000 0.99750 67° 0.93996 0.93164 33 0.99824 0.99568 68 0.93829 0.92968 34 0.99647 0.99385 69 0.93664 0.92772 35 0.99471 0.99203 70 0.93499 0.82576 36 0.99294 0.99021 71 0.93333 0.92380 37 0.99119 0.98339 72 0.93168 0.92184 38 0.98769 0.98470 74 0.92839 0.91792 40 0.98595 0.98286 75 0.92675 0.91596 41 0.98470 74 0.92347 0.91203 43 0.98073 0.9717 77 0.92347 0.91203 43 0.98073 0.97358 80 0.91859 0.90811 45 0.97256 0.97358 80 </th <th></th> <th></th> <th>10000</th> <th></th> <th></th> <th>4</th> <th></th> | | | 10000 | | | 4 | |
|--|----|--------|--|-------------------|-------|----------------|------------------|
| 32° 1.00000 0.99750 67° 0.93996 0.93164 33 0.99824 0.99568 68 0.93829 0.92968 34 0.99647 0.99385 69 0.93664 0.92772 35 0.99471 0.99203 70 0.93499 0.82576 36 0.99294 0.99021 71 0.93333 0.92380 37 0.99119 0.98839 72 0.93168 0.92184 38 0.98769 0.98470 74 0.92839 0.91792 40 0.98595 0.98286 75 0.92675 0.91596 41 0.98420 0.98101 76 0.92511 0.91400 42 0.98246 0.97917 77 0.92347 0.91203 43 0.98073 0.97731 78 0.92184 0.91005 44 0.97900 0.97545 79 0.92021 0.90811 45 0.97256 0.97358 80 0.91859 <t< th=""><th></th><th></th><th>Specific Grav.</th><th>Specific Grav.</th><th></th><th>Specific Grav.</th><th>Specific Grav.</th></t<> | | | Specific Grav. | Specific Grav. | | Specific Grav. | Specific Grav. |
| 33 0.99824 0.99568 68 0.93829 0.92968 34 0.99647 0.99385 69 0.93664 0.92772 35 0.99471 0.99203 70 0.93499 0.82576 36 0.99294 0.99021 71 0.93333 0.92380 37 0.99119 0.98654 73 0.93004 0.91883 38 0.98769 0.98470 74 0.92839 0.91792 40 0.98595 0.98286 75 0.92675 0.91596 41 0.98426 0.97917 77 0.92347 0.91203 42 0.98246 0.97917 77 0.92347 0.91203 43 0.98073 0.97731 78 0.92184 0.91005 44 0.97900 0.97545 79 0.92021 0.90811 45 0.97726 0.97358 80 0.91859 0.90609 46 0.97553 0.97172 81 0.91656 | ı | raiii. | of Dry Air. | of Saturat. All. | rani. | of Dry Air. | or Saturat, Air. |
| 33 0.99824 0.99568 68 0.93829 0.92968 34 0.99647 0.99385 69 0.93664 0.92772 35 0.99471 0.99203 70 0.93499 0.82576 36 0.99294 0.99021 71 0.93333 0.92380 37 0.99119 0.98654 73 0.93004 0.91883 38 0.98769 0.98470 74 0.92839 0.91792 40 0.98595 0.98286 75 0.92675 0.91596 41 0.98426 0.97917 77 0.92347 0.91203 42 0.98246 0.97917 77 0.92347 0.91203 43 0.98073 0.97731 78 0.92184 0.91005 44 0.97900 0.97545 79 0.92021 0.90811 45 0.97726 0.97358 80 0.91859 0.90609 46 0.97553 0.97172 81 0.91656 | ı | 32° | 1.00000 | 0.99750 | 67° | 0.93996 | 0.93164 |
| 34 0.99647 0.99385 69 0.93664 0.92772 35 0.99471 0.99203 70 0.93499 0.82576 36 0.99294 0.99021 71 0.93333 0.92380 37 0.99119 0.98389 72 0.93168 0.92184 38 0.98769 0.98470 74 0.92339 0.91792 40 0.98595 0.98286 75 0.92675 0.91596 41 0.98420 0.98101 76 0.92511 0.91203 43 0.98073 0.97917 77 0.92347 0.91203 43 0.98073 0.97545 79 0.92021 0.90811 45 0.97726 0.97358 80 0.91859 0.90609 46 0.97553 0.97172 81 0.91656 0.90411 47 0.97381 0.96986 82 0.91534 0.90213 48 0.97038 0.96610 84 0.9121 0 | ı | 33 | | | 68 | 0.93829 | 0.92968 |
| 36 0.99294 0.99021 71 0.93333 0.92380 37 0.99119 0.98839 72 0.93168 0.92184 38 0.98944 0.98654 73 0.93004 0.91988 39 0.98769 0.98470 74 0.92839 0.91792 40 0.98595 0.98286 75 0.92675 0.91596 41 0.98420 0.98101 76 0.92511 0.91400 42 0.98246 0.97917 77 0.92347 0.91203 43 0.98073 0.97731 78 0.92184 0.91005 44 0.97900 0.97545 79 0.92021 0.90811 45 0.97726 0.97358 80 0.91859 0.90609 46 0.97553 0.97172 81 0.91656 0.90411 47 0.97381 0.96986 82 0.91534 0.90213 48 0.97209 0.96798 83 0.91373 | | 34 | | -1.0. | 69 | | 0.92772 |
| 37 0.99119 0.98839 72 0.93168 0.92184 38 0.98944 0.98654 73 0.93004 0.91988 39 0.98769 0.98470 74 0.92839 0.91792 40 0.98595 0.98286 75 0.92675 0.91596 41 0.98420 0.98101 76 0.92511 0.91400 42 0.98246 0.97917 77 0.92347 0.91203 43 0.98073 0.97731 78 0.92184 0.91005 44 0.97900 0.97545 79 0.92021 0.90811 45 0.97726 0.97358 80 0.91859 0.90609 46 0.97553 0.97172 81 0.91656 0.90411 47 0.97381 0.96986 82 0.91534 0.90213 48 0.97209 0.96798 83 0.91373 0.90013 49 0.96866 0.96421 85 0.91050 | | 35 | 0.99471 | 0.99203 | 70 | 0.93499 | 0.82576 |
| 37 0.99119 0.98839 72 0.93168 0.92184 38 0.98944 0.98654 73 0.93004 0.91988 39 0.98769 0.98470 74 0.92839 0.91792 40 0.98595 0.98286 75 0.92675 0.91596 41 0.98420 0.98101 76 0.92511 0.91400 42 0.98246 0.97917 77 0.92347 0.91203 43 0.98073 0.97731 78 0.92184 0.91005 44 0.97900 0.97545 79 0.92021 0.90811 45 0.97726 0.97358 80 0.91859 0.90609 46 0.97553 0.97172 81 0.91656 0.90411 47 0.97381 0.96986 82 0.91534 0.90213 48 0.97209 0.96798 83 0.91373 0.90013 49 0.96866 0.96421 85 0.91050 | | 36 | 0.99294 | 0.99021 | 71 | 0.93333 | 0.92380 |
| 38 0.98944 0.98654 73 0.93004 0.91988 39 0.98769 0.98470 74 0.92839 0.91792 40 0.98595 0.98286 75 0.92675 0.91596 41 0.98420 0.98101 76 0.92511 0.91400 42 0.98246 0.97917 77 0.92347 0.91203 43 0.98073 0.97731 78 0.92184 0.9105 44 0.97900 0.97545 79 0.92021 0.90811 45 0.97726 0.97358 80 0.91859 0.90609 46 0.97553 0.97172 81 0.91656 0.90411 47 0.97381 0.96986 82 0.91534 0.90213 48 0.97209 0.96798 83 0.91373 0.90013 49 0.9738 0.96610 84 0.91211 0.89614 50 0.96686 0.96421 85 0.91050 0. | | 37 | 0.99119 | 0.98839 | 72 | 0.93168 | |
| 40 0.98595 0.98286 75 0.92675 0.91596 41 0.98420 0.98101 76 0.92511 0.91400 42 0.98246 0.97917 77 0.92347 0.91203 43 0.98073 0.97731 78 0.92184 0.91005 44 0.97900 0.97545 79 0.92021 0.90811 45 0.97726 0.97358 80 0.91859 0.90601 46 0.97553 0.97172 81 0.91656 0.90411 47 0.97381 0.96986 82 0.91534 0.90213 48 0.97209 0.96798 83 0.91373 0.90013 49 0.96866 0.96421 85 0.91050 0.89615 51 0.96695 0.96233 86 0.90839 0.89415 52 0.96524 0.96045 87 0.90728 0.89216 53 0.9634 0.95855 88 0.90567 0 | 1 | 38 | 0.98944 | 0.98654 | 73 | 0 93004 | 0.91988 |
| 40 0.98595 0.98286 75 0.92675 0.91596 41 0.98420 0.98101 76 0.92511 0.91400 42 0.98246 0.97917 77 0.92347 0.91203 43 0.98073 0.97731 78 0.92184 0.91005 44 0.97900 0.97545 79 0.92021 0.90811 45 0.97726 0.97358 80 0.91859 0.90601 46 0.97553 0.97172 81 0.91656 0.90411 47 0.97381 0.96986 82 0.91534 0.90213 48 0.97209 0.96798 83 0.91373 0.90013 49 0.96866 0.96421 85 0.91050 0.89615 51 0.96695 0.96233 86 0.90839 0.89415 52 0.96524 0.96045 87 0.90728 0.89216 53 0.9634 0.95855 88 0.90567 0 | | 39 | 0.98769 | 0.98470 | 74 | 0.92839 | 0.91792 |
| 42 0.98246 0.97917 77 0.92347 0.91203 43 0.98073 0.97731 78 0.92184 0.91005 44 0.97900 0.97545 79 0.92021 0.90811 45 0.9726 0.97358 80 0.91859 0.90609 46 0.97553 0.97172 81 0.91656 0.90411 47 0.97381 0.96986 82 0.91534 0.90213 48 0.97209 0.96798 83 0.91373 0.90013 49 0.97038 0.96610 84 0.91211 0.39814 50 0.96866 0.96421 85 0.91050 0.89615 51 0.96695 0.96233 86 0.90839 0.89415 52 0.96524 0.96045 87 0.90728 0.89216 53 0.9634 0.95855 88 0.90567 0.89014 54 0.96183 0.95665 89 0.90408 0. | | 40 | 0.98595 | 0.98286 | | 0.92675 | 0.91596 |
| 43 0.98073 0.97731 78 0.92184 0.91005 44 0.97900 0.97545 79 0.92021 0.90811 45 0.97726 0.97358 80 0.91859 0.90609 46 0.97553 0.97172 81 0.91656 0.90411 47 0.97381 0.96986 82 0.91534 0.90213 48 0.97209 0.96798 83 0.91373 0.90013 49 0.97038 0.96610 84 0.91211 0.39814 50 0.96866 0.96421 85 0.91050 0.89615 51 0.96695 0.96233 86 0.90389 0.89415 52 0.96524 0.96045 87 0.90728 0.89216 53 0.96354 0.95855 88 0.90408 0.88813 55 0.96183 0.95665 89 0.90408 0.88413 55 0.99544 0.95955 92 0.89929 | ۱ | | 0.98420 | 0.98101 | 76 | 0.92511 | |
| 44 0.97900 0.97545 79 0.92021 0.90811 45 0.97726 0.97358 80 0.91859 0.90609 46 0.97553 0.97172 81 0.91656 0.90411 47 0.97381 0.96986 82 0.91534 0.90213 48 0.97209 0.96798 83 0.91373 0.90013 49 0.97038 0.96610 84 0.91211 0.39814 50 0.96866 0.96421 85 0.91050 0.89615 51 0.96695 0.96233 86 0.90839 0.89415 52 0.96524 0.96045 87 0.90728 0.89216 53 0.96354 0.95855 88 0.90408 0.88813 55 0.96183 0.95475 90 0.90248 0.88611 54 0.96183 0.95285 91 0.90089 0.88410 57 0.95674 0.95095 92 0.89929 | | | | | | | 0.0 |
| 45 0.97726 0.97358 80 0.91859 0.90609 46 0.97553 0.97172 81 0.91656 0.90411 47 0.97381 0.96986 82 0.91534 0.90213 48 0.97209 0.96798 83 0.91373 0.90013 49 0.97038 0.96610 84 0.91211 0.89814 50 0.96866 0.96421 85 0.91050 0.89615 51 0.96695 0.96233 86 0.90839 0.89415 52 0.96524 0.96045 87 0.90728 0.89216 53 0.96354 0.95855 88 0.90567 0.89014 54 0.96183 0.95665 89 0.90408 0.88813 55 0.96013 0.95475 90 0.90248 0.88611 56 0.95843 0.95285 91 0.90089 0.88410 57 0.95674 0.95095 92 0.89929 | | | | 0.97731 | 78 | | |
| 46 0.97553 0.97172 81 0.91656 0.90411 47 0.97381 0.96986 82 0.91534 0.90213 48 0.97209 0.96798 83 0.91373 0.90013 49 0.97038 0.96610 84 0.91211 0.89814 50 0.96866 0.96421 85 0.91050 0.89615 51 0.96695 0.96233 86 0.90399 0.89415 52 0.96524 0.96045 87 0.90728 0.89216 53 0.96354 0.95855 88 0.90567 0.89014 54 0.96183 0.95665 89 0.90408 0.88813 55 0.96013 0.95475 90 0.90248 0.88611 56 0.95843 0.95285 91 0.90089 0.88410 57 0.95674 0.95095 92 0.89929 0.88208 58 0.95336 0.94710 94 0.89612 | | | | | | | |
| 47 0.97381 0.96986 82 0.91534 0.90213 48 0.97209 0.96798 83 0.91373 0.90013 49 0.97038 0.96610 84 0.91211 0.39814 50 0.96866 0.96421 85 0.91050 0.89615 51 0.96695 0.96233 86 0.90839 0.89415 52 0.96524 0.96045 87 0.90728 0.89216 53 0.96354 0.95855 88 0.90567 0.89014 54 0.96183 0.95665 89 0.90408 0.88813 55 0.96013 0.95475 90 0.90248 0.88611 56 0.95843 0.95285 91 0.90089 0.88410 57 0.95674 0.95095 92 0.89929 0.88208 58 0.95504 0.94902 93 0.89770 0.88006 59 0.95336 0.94710 94 0.89612 | | - | | | | | |
| 48 0.97209 0.96798 83 0.91373 0.90013 49 0.97038 0.96610 84 0.91211 0.39814 50 0.96866 0.96421 85 0.91050 0.89615 51 0.96695 0.96233 86 0.90839 0.89415 52 0.96524 0.96045 87 0.90728 0.89216 53 0.96354 0.95855 88 0.90567 0.89014 54 0.96183 0.95665 89 0.90408 0.88813 55 0.96013 0.95475 90 0.90248 0.88611 56 0.95843 0.95285 91 0.90089 0.88410 57 0.95674 0.95095 92 0.89929 0.88208 58 0.95504 0.94902 93 0.89770 0.88006 59 0.95336 0.94710 94 0.89612 0.87803 60 0.95168 0.94518 95 0.89453 | ī | | | | 20.00 | | |
| 49 0.97209 0.9610 84 0.91211 0.89814 50 0.96866 0.96421 85 0.91050 0.89615 51 0.96695 0.96233 86 0.90839 0.89415 52 0.96524 0.96045 87 0.90728 0.89216 53 0.96354 0.95855 88 0.90567 0.89014 54 0.96183 0.95665 89 0.90408 0.88813 55 0.96013 0.95475 90 0.90248 0.88611 56 0.95843 0.95285 91 0.90089 0.88410 57 0.95674 0.95095 92 0.89929 0.88208 58 0.95504 0.94902 93 0.89770 0.88006 59 0.95336 0.94710 94 0.89612 0.87803 60 0.95168 0.94518 95 0.89453 0.87602 61 0.94999 0.94326 96 0.89295 0 | ř. | | | 7 3 3 | | | |
| 50 0.96866 0.96421 85 0.91050 0.89615 51 0.96695 0.96233 86 0.90839 0.89415 52 0.96524 0.96045 87 0.90728 0.89216 53 0.96354 0.95855 88 0.90567 0.89014 54 0.96183 0.95665 89 0.90408 0.88813 55 0.96013 0.95475 90 0.90248 0.88611 56 0.95843 0.95285 91 0.90089 0.88410 57 0.95674 0.95095 92 0.89929 0.88208 58 0.95504 0.94902 93 0.89770 0.88006 59 0.95336 0.94710 94 0.89612 0.87803 60 0.95168 0.94518 95 0.89453 0.87602 61 0.94999 0.94326 96 0.89295 0.87401 62 0.94831 0.94134 97 0.89137 | | | | | - | | 0.0.0 |
| 51 0.96695 0.96233 86 0.90889 0.89415 52 0.96524 0.96045 87 0.90728 0.89216 53 0.96354 0.95855 88 0.90567 0.89014 54 0.96183 0.95665 89 0.90408 0.88813 55 0.96013 0.95475 90 0.90248 0.88611 56 0.95843 0.95285 91 0.90089 0.88410 57 0.95674 0.95095 92 0.89929 0.88208 58 0.95504 0.94902 93 0.89770 0.88006 59 0.95336 0.94710 94 0.89612 0.87803 60 0.95168 0.94518 95 0.89453 0.87602 61 0.94999 0.94326 96 0.89295 0.87401 62 0.94831 0.94134 97 0.89137 0.87199 63 0.94664 0.93940 98 0.88979 | | | | | | | |
| 52 0.96524 0.96045 87 0.90728 0.89216 53 0.96354 0.95855 88 0.90567 0.89014 54 0.96183 0.95665 89 0.90408 0.88813 55 0.96013 0.95475 90 0.90248 0.88611 56 0.95843 0.95285 91 0.90089 0.88410 57 0.95674 0.95095 92 0.89929 0.88208 58 0.95504 0.94902 93 0.89770 0.88006 59 0.95336 0.94710 94 0.89612 0.87803 60 0.95168 0.94518 95 0.89453 0.87401 61 0.94999 0.94326 96 0.89295 0.87401 62 0.94831 0.94134 97 0.89137 0.87199 63 0.94664 0.93940 98 0.88979 0.86995 64 0.94329 0.93552 100 0.88664 <td< th=""><th></th><th></th><th>1</th><th>0.0</th><th></th><th></th><th></th></td<> | | | 1 | 0.0 | | | |
| 53 0.96354 0.95855 88 0.90567 0.89014 54 0.96183 0.95665 89 0.90408 0.88813 55 0.96013 0.95475 90 0.90248 0.88611 56 0.95843 0.95285 91 0.90089 0.88410 57 0.95674 0.95095 92 0.89929 0.88208 58 0.95504 0.94902 93 0.89770 0.88006 59 0.95336 0.94710 94 0.89612 0.87803 60 0.95168 0.94518 95 0.89453 0.87602 61 0.94999 0.94326 96 0.89295 0.87401 62 0.94831 0.94134 97 0.89137 0.87199 63 0.94664 0.93746 99 0.88821 0.86790 64 0.94329 0.93552 100 0.88664 0.86585 | | ~ - | The second second | | | | |
| 54 0.96183 0.95665 89 0.90408 0.88813 55 0.96013 0.95475 90 0.90248 0.88611 56 0.95843 0.95285 91 0.90089 0.88410 57 0.95674 0.95095 92 0.89929 0.88208 58 0.95504 0.94902 93 0.89770 0.88006 59 0.95336 0.94710 94 0.89612 0.87803 60 0.95168 0.94518 95 0.89453 0.87602 61 0.94999 0.94326 96 0.89295 0.87401 62 0.94831 0.94134 97 0.89137 0.87199 63 0.94664 0.93940 98 0.88979 0.86995 64 0.94329 0.93746 99 0.88621 0.86790 65 0.94329 0.93552 100 0.88664 0.86585 | | ~ ~ ~ | 0.000.00 | | | | |
| 55 0.96013 0.95475 90 0.90248 0.88611 56 0.95843 0.95285 91 0.90089 0.88410 57 0.95674 0.95095 92 0.89929 0.88208 58 0.95504 0.94902 93 0.89770 0.88006 59 0.95336 0.94710 94 0.89612 0.87803 60 0.95168 0.94518 95 0.89453 0.87602 61 0.94999 0.94326 96 0.89295 0.87401 62 0.94831 0.94134 97 0.89137 0.87199 63 0.94664 0.93940 98 0.88979 0.86995 64 0.94329 0.93552 100 0.88664 0.86585 | | | 0.0000 | 0.0.0.0.0 | | | 1 |
| $\begin{array}{cccccccccccccccccccccccccccccccccccc$ | | ~ ~ | | | | | |
| 57 0.95674 0.95095 92 0.89929 0.88208 58 0.95504 0.94902 93 0.89770 0.88006 59 0.95336 0.94710 94 0.89612 0.87803 60 0.95168 0.94518 95 0.89453 0.87602 61 0.94999 0.94326 96 0.89295 0.87401 62 0.94831 0.94134 97 0.89137 0.87199 63 0.94664 0.93940 98 0.88979 0.86995 64 0.94496 0.93746 99 0.88821 0.86790 65 0.94329 0.93552 100 0.88664 0.86585 | | | | The second second | | 1 | |
| $\begin{array}{c ccccccccccccccccccccccccccccccccccc$ | | | 0.00 | 0.0 | | | |
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$ | | | | 0.000 | | | |
| 60 0.95168 0.94518 95 0.89453 0.87602 61 0.94999 0.94326 96 0.89295 0.87401 62 0.94831 0.94134 97 0.89137 0.87199 63 0.94664 0.93940 98 0.88979 0.86995 64 0.94496 0.93746 99 0.88821 0.86790 65 0.94329 0.93552 100 0.88664 0.86585 | | | | | | | |
| 61 0.94999 0.94326 96 0.89295 0.87401 62 0.94831 0.94134 97 0.89137 0.87199 63 0.94664 0.93940 98 0.88979 0.86995 64 0.94496 0.93746 99 0.88821 0.86790 65 0.94329 0.93552 100 0.88664 0.86585 | | | 1 11 21 21 21 21 | | - | | |
| 62 0.94831 0.94134 97 0.89137 0.87199 63 0.94664 0.93940 98 0.88979 0.86995 64 0.94496 0.93746 99 0.88821 0.86790 65 0.94329 0.93552 100 0.88664 0.86585 | | | | 1 0 10 10 | | 1 | |
| 63 0.94664 0.93940 98 0.88979 0.86995 64 0.94496 0.93746 99 0.88821 0.86790 65 0.94329 0.93552 100 0.88664 0.86585 | | | 1 1 1 1 1 1 1 1 | EL ST. ST. ST. | 10.00 | | |
| | | | 1 | 0 0 0 0 | | | |
| 65 0.94329 0.93552 100 0.88664 0.86585 | | | | | | | |
| 100 0.00004 0.00000 | | | The state of the s | | | | |
| 00 0 34102 0.33330 110 0.87110 0.84329 | | | 010 110110 | | | 1 | |
| | | 00 | 1 0 34102 | 1 0.90000 | 1110 | 0.87110 | 0.84329 |

EXPANSIONS OF SOLIDS, AND LIQUIDS AT DIFFERENT TEMPERATURES, FROM 32° to 212° Fah.

| · · · · · · · · · · · · · · · · · · · | Means. |
|--|--|
| Olam tuha limaan | |
| Glass tube, linear . | 1.000822 |
| Plate glass, | 1.000878 |
| Deal, | 1.000808 |
| Platina, | 1.000911 |
| Cast iron, | 1.001110 |
| Steel, | 1 001213 |
| Iron, | 1.001249 |
| Gold, | 1.001458 |
| Copper, | 1.001796 |
| Brass, . | 1.001873 |
| Silver, | 1.002002 |
| Tin, | 1.002372 |
| Lead, | 1.002858 |
| Zinc, . | 1.002976 |
| Mercury, volume, | 1.018100 |
| Water, | 1.044660 |
| Alcohol, | 1.105000 |
| Fixed Oils, | 1.075000 |
| AND DESCRIPTION OF THE PROPERTY OF THE PROPERT | The second secon |

TABLE FOR COMPUTING THE FLEXIBILITY AND STRENGTH OF TIMBER.*

| The second secon | | - | | - | | |
|--|----------------|----------------|-------------|-------------|--------------|-------------|
| Name of the kind of Wood. | Spec. Grav. | Value of U. | Value of E. | Value of S. | Value of S'. | Value of C. |
| Teak | 745 | 818 | 9657802 | 2462 | 2488 | 15550 |
| Poon | 579 | 596 | 6759200 | 2221 | 2266 | 14787 |
| Eng. Oak | 969 | 598 | 3494730 | 1181 | 1205 | 9836 |
| Do. Spec. 2. | 934 | 435 | 5806200 | 1672 | 1736 | 10853 |
| Canadian Oak | 872 | 588 | 8595864 | 1766 | 1803 | 11428 |
| Dantzic Oak . | 756 | 724 | 4765750 | 1457 | 1477 | 7386 |
| Adriatic Oak . | 993 | 610 | 3885700 | 1583 | 1409 | 8808 |
| Ash | 760 | 395 | 6580750 | 2026 | 2124 | 17337 |
| Beech | 696 | 615 | 5417266 | 1556 | 1586 | 9912 |
| Elm | 553 | 509 | 2799347 | 1013 | 1042 | 5767 |
| Pitch Pine | 660 | 588 | 4900466 | 1632 | 1666 | 10415 |
| Red Pine | 657 | 605 | 7359700 | 1341 | 1368 | 10000 |
| New Eng. Fir | 553 | 757 | 5967400 | 1102 | 1116 | 9947 |
| Riga Fir | 753 | 588 | 5314570 | 1108 | 1131 | 10707 |
| Do. Spec. 2. | 738 | | 3962800 | 1051 | 1081 | 0700 |
| Mar Forest Fir | 696 | 588 | 2581400 | 1144 | 1168 | 9539 |
| Do. Spec. 2. | 693 | 403 | 3478328 | 1262 | 310 | 10691 |
| Larch | 531 | 411 | 2465433 | 653 | 890 | - |
| Do. Spec. 2. | 522 | 518 | 3591133 | 832 | 850 | HOEK |
| Do. Spec. 3. | 556 | 518 | 4210830 | 1127 | 1149 | 7655 |
| Do. Spec. 4. | 560 | 518 | 4210830 | 1149 | 1172 | 7352 |
| Norway Spar . | 577 | 648 | 5832000 | 1474 | 1492 | 12180 |

^{*} From Barlow on the Strength of Timber.

Solution of Practical Problems, from the preceding Data.

Prob. I.—To find the Strength of Direct Cohesion of a Piece of Timber of any given Dimensions.

Rule.—Multiply the area of the transverse section, in inches, by the value of C, in the preceding table of data, and the product will be the strength required.

Note.—If the specific gravity be not the same as the mean tabular specific gravity; say, as the latter is to the former, so is the above product to the correct result.

Ex.—What weight will it require to tear asunder a piece of teak 3 inches square, the specific gravity being 745?—Ans. 139.95 lbs.

Prob. II.—To compute the Deflection of Beams fixed at one End and loaded at the other with any given Weight.

Rule 1.—Multiply the tabular value of E by the breadth and cube of the depth of the given beam, both in inches.

2.—Multiply also the cube of the length in inches by the given

weight, and that product again by 32.

3.—Divide the latter product by the former, for the deflection sought.

Ex.—An ash batten, 3 inches square, is fixed in a wall, and projects from it 4 feet. If a weight of 200 lbs. be hung on its extremity, how much will it be deflected?—Ans. $1\frac{1}{3}$ inches.

Note.—The same rule will apply, when the weight is distributed throughout the length, by multiplying the second product by 12 instead of 32.

PROB. III.—To compute the Deflection of Beams, supported at each End, and loaded in the Middle with any given Weight.

Rule 1.—Multiply the tabular value of E by the breadth and cube

of the depth, both in inches.

2.—Multiply also the cube of the length, in inches, by the given weight in lbs.; then divide the latter product by the former for the deflection sought.

Ex.—A square beam of English oak, whose side is 6 inches, is supported on two walls, 20 feet distant, and is to be loaded at its middle point with 1000 lbs., what will it be deflected?—Ans. 1.8 inch.

Note.—If the beam be fixed at each end, the deflection will, with equal weights, be two-thirds of that found by the above rule.

Prob. IV.—To compute the Deflection of Beams supported at each End, and loaded uniformly throughout their Length with a given Weight.

Rule.—Compute the deflection the same as in the last problem. Multiply that result by 5, and divide the product by 8, and the quotient will be the answer.

Ex.—A uniform bar of Adriatic oak, 2 inches square, is rested upon two props, distant 24 feet, how much will it be deflected by its own weight, its specific gravity being 960, or 60 lbs. to the cubic foot?—Ans. 9½ inches.

PROB. V .- To compute the ultimate Deflection of Beams or Rods, before their Rupture.

Note.—The beams are supposed to be supported at each end.

Rule.—Multiply the tabular value of U, in the preceding table of data, by the depth of the beam in inches, and divide the square of the length, also in inches, by that product, for the ultimate deflection sought.

Ex.—A square inch rod of ash, 6 feet long, is broken by a weight applied to its centre: how much will it be deflected before it breaks? Ans. 13.1 inches.

PROB. VI.—To find the ultimate transverse Strength of any rectangular Beam of Timber, fixed at one End and loaded at the other.

Rule I.—Multiply the value of S, in the preceding table of data, by the breadth and square of the depth, both in inches, and divide that product by the length, also in inches, and the quotient will be the weight in lbs. This is approximative.

Rule II.—1. Take the ultimate deflection 8 times that of the last problem, and divide the deflection by the length, which will give

the sine of the angle; whence, by a table find the secant.

2. Multiply the secant by the breadth and square of the depth in inches, and the product again by the value of S' in the table of data.

3. Divide this last product by the length in inches, and the quo-

tient will be the answer in lbs.

Ex. 1.—What weight will it require to break a piece of Mar forest fir, fixed by one end in a wall, and loaded at the other; the breadth being 2 inches, depth 3 inches, and length 4 feet?—Ans. 518 lbs.

Prob. VII.—To compute the ultimate transverse Strength of any rectangular Beam, when supported at both Ends and loaded in the Centre.

Rule I.—Multiply the tabular value of S by 4 times the breadth and square of the depth in inches, and divide that product by the

length, also in inches, for the weight.

Rule II.—1. Compute the ultimate deflection by Prob. V.; square that deflection, and divide it by the square of half the length of the beam, and add the quotient to 1, for the square of the secant of deflection; which multiply by the length in ihches.

2. Multiply the tabular value of S' by 4 times the breadth, and the square of the depth; and divide that product by the former an-

swer in lbs.

Ex.—What weight will be necessary to break a piece of larch similar to the third specimen, the length being 8 feet 4 inches, the breadth 8 inches, and depth 10 inches; being supported at each end, and loaded in the middle?—Ans. 36676 lbs.

EXPLANATION OF THE TABLES.

TABLE I.—The Miles and Parts of a Mile in a Degree of Longitude at every Degree of Latitude, supposing the Earth to be a Sphere.

The first column of this table contains degrees of latitude, the second the miles and hundredth parts of a mile in a corresponding degree of longitude, -of these the remaining columns are a continuation. If the given latitude consists of degrees and minutes, a proportional part of the difference between two contiguous degrees, the one greater and the other less than the given latitude must be applied to the miles, &c. corresponding to either of the adjacent degrees, by addition or subtraction, according as it is greater or less than the given latitude.

Example 1.—Required the number of miles in a degree of longitude

at the Isle of May, in latitude 56° 11' 22" N.

Miles in a degree of longitude in latitude 56°=33.55 \cdot · · · in latitude 57 = 32.68

.87 Difference

Then 60': 11' 22":: 87: 165, which, subtracted from 33.55, gives 33.385; the measure of a degree of longitude in latitude 56° 11' 22".

. Ex. 2.—Suppose the error of a chronometer to be half a minute, after a voyage from Leith to the West-Indies and back, how many geographical miles would that amount to at the mouth of the frith of Forth, near the Isle of May?"

Since 1° of longitude is equal to four minutes of time, then half a minute will be the eighth part of a degree, and \(\frac{1}{8}\) of 33.385=4.178,

or about 4½ miles.

Ex. 3.—What is the distance in geographical or nautical miles between Stockholm in longitude about 189 E., and Petersburgh in longitude 30° E., the common latitude being 60° N. nearly?

 30° — 18° = 12° , and 12×30 =360 miles nearly, since at 60 one

degree is 30 miles.

TABLE II.—Logarithms of Numbers.—Part I. contains the logarithms of all numbers from 1 to 100, inclusive, with their proper indices prefixed. Part II. contains the decimal part of the logarithms of all numbers from 100 to 10,000, without their indices. The indices are easily supplied by the computist, being always one unit less than the number of integers in the given natural num-The index of the logarithm of a number in which there are any integers is always positive; but, if the number be properly a fraction, the index is negative, usually marked by the sign - either

before, or more generally above the index. If the first effective figure of the decimal fraction be adjacent to the decimal point, the index is $\bar{1}$; if there be one cipher between them, the index is $\bar{2}$; if two ciphers, the index is $\bar{3}$; and, in general, the number denoting the place of the first significant figure from the decimal point will be the negative index. Instead of negative indices, their arithmetical complements are frequently used, especially by those unacquainted with the first principles of Algebra.

The decimal parts of the logarithms of numbers consisting of the same figures are the same whether the number be integral, frac-

tional, or mixed, which may be illustrated as follows:— Numbers 546800 Logarithms 5.737829

| 546800 | Logarithms | 5.737829 |
|-----------|----------------------|-----------------------|
| 54680 . | | 4.737829 |
| 5468 . | Or and the second | 3.737829 |
| 546.8 | | 2.737829 |
| 54.68 | | 1.737829 |
| 5.468 | The same of the same | 0.737829 |
| 0.5468 | | 1.737829, or 9.737829 |
| 0.05468 | 13 - 25 H | 2.737829, or 8.737829 |
| 0.005468 | | 3.737829, or 7.737829 |
| 0.0005468 | | 4.737829, or 6.737829 |

PROBLEM I .- To find the Logarithm of any given Number.

RULE.—If the given number be under 100, its logarithm is found in the first page of the table immediately opposite to it.

If the number consist of three figures, find it in the first column of the following or second part of the table, opposite to which, and

under or above 0, is its logarithm.

If the given number contains four figures, the three first are to be found, as before, in the side-column; and under the fourth at the top, or above it at the bottom, will be found the logarithm required.

To this prefix the proper index, and the whole is completed.

If the given number exceeds four figures, find the difference between the logarithm answering to the first four figures of the given number, and the next immediately following; multiply this difference by the remaining figures in the given number, point off as many figures to the right hand as there are in the multiplier, and the remainder added to the logarithm, answering to the first four figures, will be the logarithm required nearly. The logarithm of a vulgar fraction is found by subtracting the logarithm of the denominator from that of the numerator; and that of a mixed quantity is found by reducing it to an improper fraction, and proceeding as before; or the vulgar fractions may be reduced to decimals, and the logarithms found as usual.

Ex. 1.—What is the logarithm of 56?

In the first part of the table, opposite to 56, and under N. is 1.748188.

Ex.—What is the logarithm of 366?

In the second part of the table, opposite to 366, and under 0, is 2.563481, supplying the index. The first two figures are understood to be supplied in the blank space, till the change takes place at 57; and this must be attended to throughout the whole of this table, as well as several others that follow.

Ex. 3.—Required the logarithm of 7854?
Opposite to 785, and under 4 is 3.895091

WHEN THE WAY

Ex. 4. Required the logarithm of 100176? The log. of 1001 is 000434 1002 is 000868

The difference is 434

Then 434×76 is 32984. From this cut off two figures, because the difference has been multiplied by two figures, 76, and it becomes 329.84. If the figure next the decimal point is less than 5, the whole may be rejected; but, if greater, increase the figure before the point by unity, and consequently, in the present case, 329.84 would become 330. Whence to 000434

Add 330, and supply the index 330

And the log. of 100176 will be 5.000764

In general the difference may be taken from the right-hand column, under D, unless the logarithms vary very rapidly, which happens only near the commencement of the table, as in the preceding example, where the difference under D is 432, the mean difference of the whole line, instead of 434 by actual subtraction. This would cause a difference of two units, in the last decimal place, less than that found above, or the logarithm would turn out to be 5.000762,

instead of 5.000764.

To facilitate the method of obtaining proportional parts, there has been added to these tables an additional column on the left-hand side of the page, under P. P. In the column under N, the two first figures are omitted, and the third alone retained, by which means a regular series of the arithmetical digits, beginning with 1 and ending with 9, are obtained between each bar, or line across the page. Hence the proportional parts corresponding to the mean difference within the space marked out by each pair of cross bars, answering to any of the nine digits, can be placed opposite to each, which, in these tables, has been accordingly done. By this means the logarithm corresponding to any number extended to five or six places of figures, may be very readily obtained with sufficient accuracy, excepting, perhaps, when it falls in the second and third pages, where the differences vary rapidly.

Ex. 5.—Required the logarithm of 546876.

| od arrea or | TO TO THE TOT | TITLE OF O TOO! | O. | |
|-------------|---------------|-----------------|-------|--------|
| Log. of | 546800 is | 5.737829 , | or 5. | 737829 |
| Prop. par | | | | 56 |
| | for 6 | 48, | or | 5 |
| | | | or - | |

Log. of 546876 is 5.7378898, or 5.737890

If the number consists of one figure more than four, or five figures altogether, the proportional part may be added at sight.

Ex. 6.—Required the log. of $\frac{15}{17}$?

Required the log. of $7\frac{6}{8}$, or $6\frac{1}{8}$, or 7.625? Log. of 7.625 is

Required the logarithms of 24, 56, 102, 546, 7854, 78653, 54.4768, 97685.46, 0.001546, 0.176804, 0.00043689, 31, 315, 7681, 485713, 3976635, 854615;

PROBLEM II.—To find the Number answering to any given Logarithm.

Find the logarithm next less than that given in the column marked 0 at the top, and continue the sight along that horizontal line till a logarithm the same as that given, or as near as possible, be found; then the three first figures of the corresponding natural number will be found opposite to it in the side-column, and the fourth immediately above at the top or below at the bottom of the page. If the index of the given logarithm be 3, the four figures thus found are integers; if the index be 2, the three first figures are integers and the fourth is a decimal, and so on, as may be easily understood by consulting Problem I. If the given logarithm cannot be exactly found in the table, and if more than four figures be wanted in the corresponding natural number, then find the difference between the given and the next less logarithm. To this annex on the right-hand as many ciphers as there are figures required above four in the natural number. Divide the whole by the difference between the next less and next greater logarithm, and the quotient annexed to the four figures formerly found will be the natural number required. The same thing may be done by the table of P. P. by subtracting a part corresponding to each unit from the difference between the given logarithm and the next less, and annexing these units successively in order to the number previously found.

Ex. 1.—Required the natural number corresponding to the loga-

rithm 2.495544?

This logarithm is found opposite to 313 and under 0, and, as the

index is 2, then 313 is the number required.

Ex. 2.—What is the number answering to the logarithm 3.828338? The logarithm is found 673, and under 5, therefore, since the index is three, the natural number is 6735. If the index had been 2, then it would have been 673.5, or the natural number must always consist of one integer (if there are integers) more than the index expresses.

Ex. 3.—Required the natural number answering to the logarithm

 $\bar{2.627980}$?

The natural number corresponding to this is 4246; but the index being $\overline{2}$, one cipher must be prefixed, from what has been said in

Prob. I., and it becomes 0.04246.

Ex. 4.—What is the number answering to the logarithm 5.687956? The nearest less logarithm than this is 687886, corresponding to which will be found the number 4874. The difference between 687956 and 687886 is 70, to this annex two ciphers, and it becomes 7000, which being divided by 89, the difference of the columns found under D gives 79. This being subjoined to 4874 gives 487479, the number required. Or the same may be performed thus:—

| | 487400 | corresponds to | | | | 37886 |
|-------|--------|--------------------|------|-----|-------|----------|
| gives | . 70 | Diff. in P. P. for | 1.19 | | | 70 63 |
| gives | . 8 | remainder as diff. | ٠ | 100 | . 700 | 7 72 |

or in all 487478, differing only one unit in the last place from the former number.

LOGARITHMIC ARITHMETIC.

PROBLEM III.—To perform Multiplication by Logarithms.

RULE.—Add the logarithms of the factors, and the sum is the lo-

garithm of the product.

If there are both negative and affirmative indices, their sum is taken according to the rules of algebra; or the arithmetical complements of the negative indices may be used, rejecting the tens in their sum.

The arithmetical complement of the logarithm of any number is found by subtracting the given logarithm from 10, or by subtracting each of its figures beginning at the left-hand from 9, and the last effective figure from 10. When the arithmetical complement of the index alone is wanted, it is found by subtracting it from 10.

| Ex. 1.—Multiply 6564 by 85 Factors $\begin{cases} 6564 \text{ logarithm} \\ 836 \text{ logarithm} \end{cases}$ | 36 | 3.817169 3.922206 |
|---|-----|----------------------|
| sum 5487000 correspon | | 6.739375 6.739335 |
| gives diff. in P | . P | . 40 |

or in all 5487500, which agrees as nearly with the real product 5487504, as tables extending to six places of decimals will give.

Ex. 2.—Multiply the numbers 43.68, 0.534, and 0.007685 together

logarithmically.

Factors $\begin{cases} 43.68 & \text{log. } 1.640283, \text{ or } 1.640283 \\ 0.534 & \text{log. } \overline{1.727541} - 9.727541 \\ 0.007685 & \text{log. } \overline{3.885644} - 7.885644 \end{cases}$

Product 0.179254 1.253468 9.253468
PROBLEM IV.—To perform Division by Logarithms.

RULE.—From the logarithm of the dividend subtract the logarithm of the divisor, the remainder is the logarithm of the quotient.

Ex. 1.—Divide 5486 by 96.

Dividend 5486 log. 3.739256 Divisor 96 log. 1.982271 Quotient 57.146 1.756985 40

Ex. 2.—Divide 0.07856 by 0.003482.

Dividend 0.07856 . . $\log \overline{2}.895201$ Divisor 0.003482 . . $\log \overline{3}.541829$

Quotient 22.5617 1.353372

33 19

14

PROBLEM V.—To perform Proportion by Logarithms.

Rule.—From the sum of the logarithms of the second and third terms, subtract the logarithm of the first term; the remainder will be the logarithm of the answer. Or, instead of subtracting the logarithm of the first term, its arithmetical complement may be added to the other two, which, in many cases, is more convenient.

Ex.—A merchantman distant twenty miles, going at the rate of 5 knots or miles an hour, is pursued by a privateer, sailing at the rate of 7 miles; after three hours chase the breeze freshened, the merchantman's rate was increased to 6 knots, and the privateer's to 10. In what time will the privateer come up with the merchantman?

As the privateer gained 2 miles an hour on the merchantman, at the end of the first 3 hours, the distance between them is obviously 14 miles. During the remainder of the chase the hourly gain of the

privateer was 4 knots. Hence,

To the time required 3^h.5 or 3^h 30^m 0.544068 Consequently, from the time the breeze freshened, the privateer would come up with the merchantman in three hours and a half, or in six hours and a half from the commencement of the chase.

PROBLEM VI.—To perform Involution by Logarithms.

RULE.—Multiply the logarithm of the given number by the index of the power, and the product will be the logarithm of the power required.

Ex. 1.—What is the square of 64?
Given number 64
Index of the power

log. 1.806180

Square 4096. 3.612360

Ex. 2.—What is the third power of 24?
Given number 24 log. 1.380211

Third power 13824 4.140633 508

198

PROBLEM VII.—To perform Evolution by Logarithms.

RULE.—Divide the logarithm of the given number by the index of the root, supposed to be expressed by an integer, as, for example, the square root by 2, the cube root by 3, and the quotient will be the logarithm of the root.

If the given number be a decimal, and the arithmetical complement of the negative index be used, then prefix I to that index for the

square root, 2 for the cube root, 3 for the fourth root, &c.

If the index of the root be expressed by a fraction of which the numerator is not unity, then multiply the logarithm of the given number by the numerator, and divide it by the denominator of that index.

Ex. 1.—What is the square root of 1296?

Given number 1296 log. 3.112605 Square root 36 1.556302 Ex. 2.—Required the cube root of 0.0009261?

Given number 0.009261 log. 3.966658, or 7.966658 Cube root 0.21 1.322219, or 9.322219

What is the fourth root of 0.00007634?

Given number 0.00007634 log. $\overline{5}.882752$ Given index . $\frac{1}{4}$

Log. of the root 0.0934734 $\overline{2}.970688$

In this example, because the index of the root 4 is not contained in the negative index $\overline{5}$ a certain number of times exactly, the logarithm $\overline{5}.882752$ is resolved into its equivalent $\overline{8}+3.882752$, and the product of this by $\frac{1}{4}$ is $\overline{2}.970688$ the logarithm of the root required.

TABLE III.—The Angles which every Point and Quarter Point of

the Compass makes with the Meridian.

This table is useful for reducing the points of the mariner's compass to degrees, and conversely. It is divided into seven columns; in the two first and two last columns are contained the names of the several points; the third and fifth contain the corresponding points and quarter points reckoned from the meridian; and the fourth the degrees, minutes, and seconds, answering to them. Its use is obvious.

TABLE IV .- Logarithmic Sines, Tangents, and Secants, to every

Point and Quarter Point of the Compass.

In performing calculations relative to navigation, it will be found convenient to take the logarithmic sines, tangents, and secants, from this table, thereby saving the trouble of reducing them to degrees, &c., by the preceding table. The manner of using it is easy, and will be readily understood from the explanation of the table which immediately follows.

TABLE V.—Logarithmic Sines, Tangents, and Secants.

This table contains the logarithms of the natural sines, tangents, and secants, to each degree and minute of the quadrant in the usual manner. To facilitate calculations in which time is involved, the degrees and minutes have been converted into time at the rate of 15° to an hour, and annexed at the top and bottom of the page and in two additional side-columns.* These, together with proportional parts to each second of time, or to every fifteen seconds of a degree, at the bottom of each page, will, it is hoped, render this table still more easy and general in its use than those of a similar kind usually given.

The degrees are numbered at the top of the table, in a direct order, from 0° to 45°, and, at the bottom of the table, in a retrograde order, from 45° to 90°. The minutes are contained in two of the marginal columns. The minutes in the left-hand column belong to the degree at the top of the page, and those in the right-hand column belong to the degree at the bottom. In like manner, the minutes and seconds of time in the first left-hand column belong

^{*} This table will therefore convert degrees into time, and conversely.

to the hour at the top, and those in the right-hand column belong to the hour at the bottom. To promote perspicuity, it is recommended to mark minutes and seconds of the circle always by accents, and those of time by m and s, as is done in the tables.

PROBLEM I .- To find the Sine, Cosine, &c. answering to any given

Degree or Minute.

Rule.—Find the given degrees at the top of the page if less than 45°, and the minutes in the left-hand column; opposite to which, and under the word sine, cosine, &c. is the number required. But if the given degrees be greater than 45° and less than 90°, find them at the bottom, and the required sine, cosine, &c. will be found above the word sine, cosine, &c. opposite to the given number of minutes in the right-hand column. If the given arc exceed 90°, find the sine, cosine, &c. of its supplement, or, which comes to the same thing, and will be more easy in practice, to find the sine of an arc above 90°, reject 90°, and take the cosine of the remainder. To find the cosine of an arc above 90° reject 90°, and take the sine of the remainder. The same method may be pursued for the tangents and secants both for arcs and time, recollecting that 90° corresponds to 6°.

Ex. 1.—Required the log. sine of 23° 28'?

Under the word sine in the page marked 23° on the top, and opposite to 28′ in the left-hand column, is 9.600118, the sine required.

Ex. 2.—What is the cotangent of 55° 57′?

In the page marked 55°, at the bottom and opposite 57' in the right-hand side-column, is 9.829805, the cotangent of 55° 57'.

Ex. 3.—Required the secant of 125° 40'?

The supplement of 125° 40′ is 54° 20′, the secant of which is 10.234280, or, which comes to the same thing, the cosecant of 35° 40' the excess of 125° 40′ above 90° is 10.234280, the secant required. Hitherto the given arc has been supposed not to exceed 180°; but, in several astronomical calculations, it frequently happens that arcs through the whole circle are employed; consequently, if the arc lie between 180° and 270°, diminish it by 180°; if between 270° and 360°, take its explement to 360°, and take the logarithmic sines, &c. as before. Otherwise, for the log. sine, &c. of an arc between 270° and 360°, take the log. cosine, &c, of its excess above 270°, and for the log. cosine, &c. of an arc between 270° and 360°, let the sine, &c. of its excess above 270° be taken. And for the log. sine, &c. of an arc between 180° and 270° let the log. sine of its excess above 180° be taken. Thus the log. sine of 300° 28' is the log. sine, &c. of 30° 28′, the excess above 270°; and the log. sine of 220° 18′ is the same as that of 40° 18', and so on. The same may be done when time is employed, recollecting that 6^h corresponds to 90°, 12^h to 180°, 18^h to 270°, and 24^h to 360°.

PROBLEM II .- To find the Sine, Tangent, &c. of an Arc expressed in

Degrees, Minutes, and Seconds.

RULE.—Find the sine, tangent, &c. corresponding to the given degree and minute, and also that answering to the next greater minute, multiply the difference between them by the given number of seconds, and divide the product by 60; then the quotient added to the sine, tangent, &c. of the given degree and minute, or subtracted from the cosine, cotangent, &c. will give the quantity required nearly. To facilitate this process the difference, to 100", has been given in the column marked D. Multiply this difference by the

number of seconds, cut off two figures from the right, and add the remainder to the sine, tangent, &c. of the given degree and minute, or subtract it from the cosine, &c., and the quantity required will be obtained nearly.

Ex. 1.—Required the log. sine of 23° 27′ 40″?

Log. sine of 23° 27′ is 9.599827

23 28 is 9.600118

Difference 291
Seconds 40

60 | 11640
194

Log. sine of 23° 27′ 9.599827
Proportional part for 40″ 194

Striking off two figures on the right gives 194,00 The same as before.

If no very great precision is required, then the proportional part for the nearest fifteen seconds may be taken from the small table at the bottom of the page.

Ex. 2.—Required the logarithm tangent of 2^h 24^m 46^s?

Log. tangent of 2^h 24^m 44^s is 9.864180 Proportional part for 2^s is 132

Log. tangent of 2^h 24^m 46^s is 9.864312 Ex. 3.—Required the secant of 9^h 45^m 36^s?

The cosecant of its excess above 6^h, or 3^h 45^m 36^s, gives 10.079396.

Required the sine of 20^h 44^m 56^s?

The cosine of 2 44 56 is 9.876236 being the sine of $20^{h} 44^{m} 56^{s}$.

PROBLEM III.—To find the Sine or Tangent of a small Arc, less than three Degrees.

1. To find the sine.

To the logarithm of the arc reduced to seconds, with the decimal annexed, add the constant quantity 4.685575, and from the sine subtract the third of the arithmetical complement of the log. cosine, or, which comes to the same thing, one third of the secant; the remainder will be the logarithmic sine of the given arc.

2. To find the tangent.

To the logarithm of the arc in seconds and constant quantity 4.685575, add two-thirds of the secant, the sum is the log. tangent of the given arc.

Ex. 1.—What is the log. sine of the sun's mean horizontal paral-

lax, supposed to be 8".68?

Logarithm of 8".68 is 0.938520 Constant . 4.685575 One-third of sec. 8".68 is 0.000000 Log. sin of 8".68 is 5.624095 Or, since in very small arcs the sine and tangent are each very nearly equal to the length of the arc, when it does not exceed 10', and the length of an arc of one second is 0.0000048481368; multiply the length of one second by the number of seconds and parts of a second making the index positive by the former rules, and the sine or tangent, will be obtained, thus,-

 $0.0000048481368 \times 8''.68 = 0.0000420818274$; the log. of this is

5.624094, the log. sine or tangent required.

Ex. 2.—Required the tangent of 1° 24′ 36″.46? To the constant logarithm . 4.685575 Add log. of 1° 24′ 36″.46=5076.46 3.705561 And $\frac{2}{3} \times 0.000132 =$

> Log. tang. of 1° 24′ 36″.46 8.391224

PROBLEM IV.—To find the Degrees, Minutes, and Seconds answering to any given log. Sine or Tangent.

RULE.—In its respective column find the nearest sine, tangent, &c. to that given; and take the degrees from the top or bottom of the page, according as the quantity is found in a column, with the proper title at the top or bottom; and the minute is found in the same horizontal line, in the left or right hand marginal columns, according as the quantity is found in a column titled at the top or at the bottom of the page.

Ex. 1.—Required the arc, or degrees and minutes corresponding

to the log. sine 9.584665?

This is found in a column marked sine at the top under 22 degrees, and opposite 36 minutes, or 1 hour, 30 minutes, and 24 seconds of time.

Ex. 2.—What is the arc in degrees or time answering to the log. tangent 10.358430, making use of the tables of proportional parts at the bottom of the page.

| Given log. tangent . 66° 20′ 0″ corresponds to | 10.358430 10.358253 |
|---|------------------------|
| And 0 0 30 to | 177 173 |
| Hence 66 20 30 is the arc required. Or, 4 ^h 25 ^m 20 ^s answer to | 10.358253 |
| And 2 to 173 or nearly | 177 |

Hence 4 25 22 is the time nearly.

Or to 177 add two ciphers, and divide by 572, the number under D. and opposite to 10.358253, or rather by 573, the number above it, as the form in which the tables are printed requires, and we have 66° 20′ 31" very nearly; and this method must be followed in all

PROBLEM V.—To find the Degrees, Minutes, and Seconds answering

to the Logarithmic Sine or Tangent of a very small Arc.

RULE.—To the given log. sine add the constant 5.314425 and onethird of the corresponding secant, the sum, rejecting 10 in the index, will be the logarithm of the number of seconds in the required arc.

To the given log. tangent add the constant 5.314425, and from the sum subtract two-thirds of the corresponding secant, rejecting 10 in the index, the result will be the logarithm of the seconds of the required arc.

Ex. 1.—Required the arc whose log. sine is 6.497655?

Constant 5.314425
Given log. sine 6.497655
3 of 0.000000 is 0.000000

Log. arc 64".8756 . 1.812080 Or 1' 4".8756

Ex. 2.—What is the arc whose log. tangent is 7.164440?

TABLE VI.—Natural Sines, Tangents, Secants, and versed Sines

to every Degree of the Quadrant.

The method of taking out the numbers required from this table will be readily comprehended from what has already been said relative to the preceding. When minutes or seconds occur, proportional parts must be taken by means of the differences found by actual subtraction.

Ex.—What is the natural sine of 5° 48' 56"?

Natural sine for 5° 48′ 56″ . 101324

TABLE VII.—Meridional Parts to every Degree of the Quadrant.
The degrees are found under the letter D, and the meridional parts under M. P., and when minutes and seconds occur, proportional parts of the difference must be taken in the manner shewn above.

Ex.—Required the meridional parts answering to 45° 36'?

Meridian parts to 45°

Prop. part of diff. 85.7 to 36' is

50.6

Meridian parts to 45° 36′ is 3080.5

TABLE VIII.—Traverse Table, or difference of Latitude and Departure.

This table contains the measures of the sides and angles of rightangled plane triangles, the distance being represented by the hypotenuse, and the difference of latitude and departure by the legs or sides about the right angle, and the course and its complement by the acute angles. Hence, if any two of these be known, except the two acute angles, the rest are found by inspection. The course is given in degrees or points in the two exterior marginal columns, the distance is found at the top or bottom of the page, according as the course is less or greater than four points or 45°; and the difference of latitude and departure is found in columns under or above these words respectively.

If there are minutes in the course, proportional parts may be taken where great accuracy is required, otherwise they may be omitted if less than 30', but, if more than 30', the degrees in the course must be increased by 1°. The distances 1, 2, 3, 4, &c. at the top and the bottom may be accounted 10, 20, 30, &c., or 100, 200, 300, &c. if the difference of latitude and departure be increased in the same proportion by removing the decimal point a corresponding number of places to the right. If the distance consist of several effective figures, the difference of latitude and departure must be found for each figure separately, and the sum of the results taken.

PROBLEM I.—The Course and Distance being given, to find the Dif-

ference of Latitude and Departure.

Find the course in right or left hand column, and in a line with it, under or above the given distance, the difference of latitude and departure will be obtained.

Ex. 1.—A ship sails N. N. E. 60 miles, what difference of latitude

and departure has she made?

Course. Dist. Diff. Lat. Departure. 2 points . 60 . 55.433 . 22.961

Ex. 2.—A ship sails S. E. b. S. $\frac{1}{2}$ S., or S. S. E. $\frac{1}{2}$ E. 244 miles, re-

quired her difference of latitude and departure?

244 . 215.1847 . 115.0216

Ex. 3.—A ship sails 300 miles S., 54° 30' W., what is her differ-

ence of latitude and departure?

Diff. Lat. Departure. Dist. Course. 54° 300 176.34 242.7155 300 172.07 245.75 244.23 Mean $54\frac{1}{9}$. 300 . 174.20

When several courses and distances are given, the results must be placed in a table, the sum of the several northings and southings, eastings and westings taken, and placing the less sums under the greater, the differences will shew how much the ship has, upon the whole, changed her situation, and in what direction she has moved.

TABLE IX.—Diurnal Logarithms.

This table, to which I have ventured to give the title of Diurnal Logarithms, is useful for making computations in which time is concerned, particularly for reducing the right ascension and declination, &c. of the sun or moon to any intermediate time between those times given in the Nautical Almanac, where the proportional parts to daily differences are required. It has two sets of arguments, the one answerto 12^h, since the moon's place is given in the Nautical Almanac for every noon and midnight; the other corresponding to 24^h for the sun.

Rule.—To the logarithm from this table corresponding to the Greenwich apparent time add the proportional logarithm (Table X.) of the variation on the given day for 24^h or 12^h, as the case may be, the sum will be the proportional logarithm of the part of it for the given time, which, added to or subtracted from the number corresponding to the preceding noon or midnight, according as it is increasing or decreasing, will give its value at the instant required.

Ex. 1.—Required the sun's right ascension March 20th, 1826, at $20^{\rm h}$ $46^{\rm m}$ $40^{\rm s}$ apparent Greenwich time.

Greenwich time 20^h 46^m 40^s D. L. 0.06262 Change of R. A. in 24^h 3 38.2 P. L. 1.69457

Prop. part for 20^h 46^m 40^s 3 9.0 1.75719 R. A. at preceding noon 23 57 42.0

R. A. at preceding noon $23 \ 57 \ 42.0$ R. A. at $20^{\text{h}} \ 46^{\text{m}} \ 40^{\text{s}}$ $0 \ 0 \ 51.0$

Ex. 2.—Required the moon's declination September the 15th, 1826, at 7^h 48^m 30^s P. M. apparent time on the meridian of Greenwich?

Moon's declination at noon . 2° 7′ 8″ S. at midnight 0 9 19 N.

Change in 7^h 48^m $30^s+1^{\circ}28$ 47 prop. log. 30692 Dec. at noon -2 7 8

Dec. at 7^h 48^m 30^s —0 38 21 S.

When the differences are very irregular, a correction on that account becomes necessary. This will be exemplified in the explanation of Table XXVII.

TABLE X.—Proportional Logarithms.

This table is chiefly useful for facilitating the method of finding the apparent time at Greenwich, answering to a given central distance between the moon and the sun, a fixed star or a planet, by the assistance of the Nautical Almanac. It is extended to three hours on account of the distances being given in various ephemerides to every three hours of time. As degrees and hours are similarly divided, it answers equally well for either, and is marked accordingly. To this table proportional parts have been added at the bottom of each page to every tenth of a second, which may be useful where great accuracy is required. The table is very useful in calculations where sexagesimal divisions are employed. The method of taking out the log, of any quantity will be readily understood from what has already been said.

TABLE XI.—Depression or Dip of the Horizon.

The dip of the horizon is an angle contained between a horizontal line passing through the eye of the observer, and a line from his eye to the visible horizon, when these lines are in the same vertical plane. This table contains the dip answering to a free unobstructed horizon, and the numbers corresponding to the height of the eye are to be subtracted from the observed altitude when taken by the fore observation, but added to it in the back observation.

TABLE XII.—The Dip at different Distances from the Observer. If the land is not sufficiently distant to afford a free horizon, it may be sometimes necesary to obtain an altitude referred to the surface of the sea at some known or estimated distance. Under such circumstances the dip may be taken from this table.

TABLE XIII.—Correction to be added to the observed Altitude of the Sun's lower Limb when taken by a fore Observation to find the true Altitude.

This table was computed by the author a good many years ago for the purpose of combining the usual corrections, namely, dip, refraction, parallax, and semidiameter. The variation of the sun's semidiamenter from 16'. is given at the bottom of the table, which, unless considerable accuracy be required, may be neglected. The arithmetical complement of the numbers from this table to 32', will be the correction to be *subtracted* when the upper limb is observed.

TABLE XIV .- Correction to be subtracted from the observed Al-

titude of a fixed Star to find the true.

This table is similar to the last, and contains the sum of the two corrections, dip and refraction, to be subtracted when the fore observation is employed.

TABLE XV.—This table, taken from the Nautical Almanac for 1826, will answer for most purposes for a considerable number of years to come. It contains the time of the sun's semidiameter passing the meridian, the sun's semidiameter, hourly motion in longitude, and the log. of the sun's distance from the earth, for every sixth day

in the year.

The time of the sun's passing the meridian is useful for reducing an observation of a passage of the preceding or subsequent limb over the meridian taken with a transit instrument, to that of the centre. The semidiameter of the sun is necessary to reduce an observation of the limb to that of the centre, whether in altitudes or angular distances. It is also useful for determining the index error of a sextant, or the exactness of the scale of micrometers.

The hourly motion is useful for computing eclipses. The log. of the sun's distance is requisite in the calculation of the places of the

planets and comets, and for some other purposes.

TABLE XVI.—The Sun's Parallax in Altitude and Zenith Dis-

tance.

The author computed this table from a mean of the determinations of Delambre from the observations of the transit of Venus over the sun's disk in June 1769. He found the mean horizontal parallax to be 8".68. It is hoped it will prove useful where great accuracy is required.

TABLE XVII.—Mean Refractions.

For the elements of this table the author is indebted to the liberality of Mr Ivory, the most distinguished mathematician in the British islands. On comparing it with that given in the Transactions of the Royal Society of London, it will be seen that it has been expanded considerably, so as to render its application more easy by giving the mean refraction, and its logarithm for every 10' from the zenith to the horizon, subjoining the differences of the logarithms for the purpose of computing proportional parts more readily.

TABLES XVIII, XIX, and XX.—These tables are employed to correct the preceding according to the state of the barometer and thermometer, as shown in the explanation at the bottom of page 89

of the tables. In the seventh line from the bottom of that page, after thermometer, there should have been added, "or 0.002083 for one degree of Fahrenheit," that used in the construction of the table.

Ex. 1.—Required the mean refraction for 21° 40' of zenith distance

or 68° 20' of altitude?

Opposite to 21° 40′ in table XVII., and under 30, will be found 0′ 23″.21, the refraction required when the barometer stands at 30 inches, and the thermometer at 50°, and this is sufficient for most purposes when great accuracy is not required.

Ex. 2.—Required the true refraction when the zenith distance is

70° 41'.7, the barometer 30.045, and thermometer 34°?

| Zenith distance 70° 40′ log. 80 Table XVII. | 2.21752 |
|--|---------|
| 1.7 | . 68 |
| Thermometer 34° Table XVIII. | 0.01472 |
| Barometer 30.0 Table XIX | 0.00000 |
| .045 | 6 |
| Thermometer 34 Table XX. | . 70 |
| 1 O/ 51// 95 171//95 | 0.02260 |
| Log. r . 2' 51".27 = 171"27 . Observed refraction 2 51 .50 | 2.23368 |
| Observed refraction 2 51 .50 | |
| | |

Error of the table — 0.23

Ex. 3.—Let $\theta = 87^{\circ} 42' 10''$, thermometer 35°, and barometer 29.5 inches, what is the true refraction?

| 0 = 87° | 40' 0" | log, de | - Than | No. | | 3.00466 |
|---------|--------|-------------------|------------|------|------|---------|
| | 2 10 | | 0.00 | 1030 | - | 390 |
| Ther. | 35° | CONTRACT NATIONAL | 000 = 01 = | | | 0.01379 |
| Bar. | 29.5 | | | | | 9.99270 |
| Ther. | 35 | 100 | 11 7 70 | 10- | -7.7 | 65 |

Log.
$$r'$$
 . 17' 16".81 = 1036".81 . 3.01570

$$\frac{-0.606 \times -15}{\frac{\partial d}{\partial p} \times (29.5 - 30.0)} = +9.09$$

$$\times 1.04 \times -0.5$$
 . = -0.52

| r = . | | 17 | 25 | .38 |
|----------|------------|----|----|-----|
| Observed | refraction | 17 | 26 | .50 |

| | | | | Example | es for | Exercise | | | |
|----|-----|-----|-------|---------|--------|----------|----|----------|---------|
| | Z. | D |). | Bar. | | | | bs. Ref. | Error. |
| | | | | In. | In. | Out. | | | |
| 1. | 70° | 46' | 30".0 | 29.686 | 469 | 44.17 | 2' | 44".83 | + 1".51 |
| 2. | 76 | 55 | 31 .2 | 29.686 | 40 | 37.10 | 4 | | + 1 .86 |
| 3. | 81 | 27 | 18 .6 | 29.924 | 61 | 58.19 | 6 | 1 .90 | + 1 .55 |
| 4. | 83 | 58 | 6 .7 | 29.810 | 36 | 29.95 | 8 | 48 .52 | + 0 .53 |
| 5. | 86 | 14 | 42 .0 | 29.174 | | 47.75 | | | + 0 .28 |
| 6. | 87 | 23 | 44 .0 | 30.000 | 60 | 56.08 | | | - 1 .15 |
| 7. | 88 | 39 | 32 .0 | 29.800 | 38 | 34.40 | 23 | 7 .94 | -15.70 |
| 8. | 89 | 26 | 51 .4 | 29 907 | 39 | 33.46 | 30 | | -39 .70 |

Hence at moderate zenith distances the error of the table is small, sometimes + and at other times -. From 70° to about 85°, the error is generally +, but from 85° to 90° it becomes -, and is considerable near the horizon. We may therefore infer that the horizontal refraction, 34' 17".5, given by the table in a mean state is, in general, too small, though, from the uncertainty and irregularity to which it is subject, it is very difficult to estimate accurately its true quantity. Perhaps from the irregularity of temperature in various parts of a line near the surface of the earth through which the ray of light must pass to reach the eye of the observer, it will be impossible ever to assign the true quantity of the horizontal refraction under given circumstances. In fact, no instrument, as yet, has been employed to ascertain the effects of aqueous vapour floating in the atmosphere, on the exact quantity of the horizontal refraction; and we suspect that the barometer and thermometer alone are inadequate to that purpose.

TABLE XXI.—Augmentation of the Moon's Semidiameter in Al-

titude and Zenith Distance.

The apparent magnitude of any object being in the inverse ratio of its distance, and as the moon is nearer the observer in the zenith than in the horizon, by the earth's radius her apparent semidiameter must be greater in the former situation than in the latter. This table contains that increase corresponding to six different values of the semidiameter, at different degrees of altitude. If the quantity is not found to the accuracy required by inspection, it may be determined by proportional parts in the usual manner.

TABLE XXII.—Reduction of the Moon's Parallax in the Spheroid.

As the earth differs somewhat considerably from a sphere, the eccentricity being about $\frac{1}{310}$, it follows that the equatorial parallax must be greater than that at the various intermediate latitudes from the equator to the pole. This table contains the quantity to be subtracted from the equatorial parallax given in the Nautical Almanac to reduce it to what it ought to be at any other latitude.

TABLE XXIII.—Logarithms of the Earth's Radii in each Parallel of Latitude; the Equatorial Radius being Unit, and Compression $\frac{1}{2400}$.

This table will be found useful in some nice observations in astronomy, where the spheroidal figure of the earth must be taken into account.

Example. To Greenwich in latitude 51° 28′ 38″ the radius is 9.9991121.

TABLE XXIV.—Angles which, the vertical to any point of the Earth's surface, makes with the Radius drawn from that point to the centre, or, as it is usually called, the Reduction of the Latitude to $\frac{1}{2}\frac{1}{12}\frac{1}{12}$ of compression.

This table is useful in several astronomical observations, such as

the computation of eclipses, occultations, &c.

Example.—The apparent latitude of Greenwich is 51° 28′ 38″.4, required that reduced to the centre?

Latitude . 51° 28′ 38″.4 Reduction . — 11′ 10 .8

Reduced latitude 51 17 27 .6

From this table the reduction of the altitude may be obtained by the

following rule:

To the secant of the azimuth reckoned from the meridian of an opposite name from the latitude, add the proportional logarithm of the reduction of latitude, the sum will be the reduction of the altitude, to be reckoned positive when the azimuth is less than 90°, and negative when greater.

Example.—Required the reduction of altitude corresponding to an

azimuth of 36° 42′ in the latitude Greenwich 51° 28′ 38″ N.

Latitude 51° 28′ 38″ Secant 0.20563

Reduction of alt. 11 10.8 Prop. log. 1.20683

Reduction of lat. 6 57.8 Prop. log. 1.41246

In computing time, &c., if the reduced latitude be used, the reduced altitude must be employed also; but, in general, unless absolutely necessary in such computations as that of time, it is easier not to employ either of these reductions.

TABLE XXV.—For determining the Latitude at any time by the Pole Star.

This table was computed by Mr Littrow of Vienna, and will be found very useful for determining the latitude of a place by the pole star. A full explanation is given at the bottom of the page immediate.

ately under the table.

Ex 1.—In latitude 56° N. nearly, the zenith distance (Z) of the pole-star, by an astronomical circle, was found to be 35° 20′ 50″, when its apparent polar distance (p) was 1° 36′.7, and the star just 14° 26° 56° from the time of upper culmination; required from these data the exact colatitude of the place of observation.

Now $14^{h} 26^{m} 56^{s}$ gives M = 3''.23, and $N = -0^{9} 0' 0''.48$ And $31''.23 \times -3'.3 \times 0.02 = -2''.06 = -3.3 \times .02 M$

1.6140=-0 0 41 .12

Cos. t. 14^h 26^m 56^s=9.9039 p 96'.7 log. 1.9854

-1.8893 = -77'.5 = -1 17 30 .00 -1 18 11 .60 Z 35 20 50 .00

Colatitude 34 2 38 .40 Latitude 55 57 21 .60

Edinburgh, 10th January, 1826.

On the Caltonhill, near the Observatory, with one of Troughton's reflecting circles on a stand, and an artificial horizon, the author, at about ten o'clock, r. m. observed the following double altitudes of the polar star, when the symplesometer stood at 29.86 inches, and

thermometer at 42° Fahrenheit; required the latitude of the place of observation.

| bservation. | |
|--|--|
| Siderial Time. | Double Altitudes |
| After Transit. | With Art. Horizon. |
| 4 ^h 22 ^m 30 ^s | 113° 10′ 50″ |
| 4 23 35 . | 113 10 55 |
| | The second secon |
| | |
| 4 25 40 . | 113 10 50 |
| 4 26 45 | 113 11 0 |
| 100 H | |
| Means 4 24 36 . | 113 10 54 |
| means 4 24 00 . | 110 10 01 |
| | F.O. OF OF |
| App. alt. or half | 56 35 27 |
| | 90 0 0 |
| | |
| App. zenith dist. or comp. | 33 24 33 |
| Man 1 Ashlas 17 10 10 and 00 | |
| Now by tables 17, 18, 19, and 20 | , compute the retraction. |
| Zenith dist.=33° 24′ 33″ log | |
| Thermometer 42° Fah. (18) | . 0.0073 |
| Barometer 29.86 inches (| |
| Thermometer 42° Fah. (20) | . 0.0003 |
| Thermometer 42 Fan. (20) | . 0.0000 |
| tana an | 2 7020 |
| Log. r=39".05 | 1.5916 |
| App. zenith distance | 33° 24′ 33″ |
| Refraction | + 0.39.05 |
| remaction . | . 1 0 00.00 |
| m t-1 11 - | 00 05 10 05 |
| True zenith distance . | . 33 25 12.05 |
| Now 4 ^h 24 ^m 36 ^s gives M=72".97 | 3, and $N = +0^{\circ} 0' 0''.57$ |
| Then $72''.973 \times -3'.3 \times 0.02 = -$ | $4.816 = 3'.3 \times .02 \text{ M}.$ |
| And 72".973-4".816=68".157 log | r 1.833510 |
| | |
| Cot. Z=33° 25′ 12″ | 0.180535 |
| and the second s | |
| Natural number . 103".29 | =2.014045=-0143.29 |
| Cos. $t=4^{\text{h}} 24^{\text{m}} 36^{\text{s}}$. 9 | .606751 |
| | .985426 |
| p 30 .7 log | .303420 |
| 27 2 2 20170 | ************************************** |
| Natural number . 39'.19=1 | .592177 = +0.3911.40 |
| | , |
| Sum | + 0 37 28.68 |
| Z | . 33 25 12.05 |
| | , 00 20 12.00 |
| , | 04 0 40 70 |
| ↓ or colatitude | 34 2 40.73 |
| Latitude | . 55 57 19.27 N. |
| From a trigonometrical measurer | nent he also found the latitude 55 |
| 7' 90' 7 N supposing with Canta | |

From a trigonometrical measurement he also found the latitude 55° 57′ 20″.7 N., supposing with Captain Kater the latitude of the flag-staff in Leith fort to be 55° 58′ 39″ N.

TABLE XXVI.—Delambre first calculated this Table for finding the augmentation of the semidiameter of the Moon in solar Eclipses and occultations, without computing the altitude. It is used as follows:

To the altitude of the nonagesimal in signs, add the distance of the moon from it, and from that altitude subtract the moon's distance from it; then take the equations from this table, Part I. answering to the sum and difference, and take the sum of these, regard being had to the signs. To this add the equations corresponding from Part II. If the observation be that of an occultation, the equation answering to

the true latitude and parallax in latitude of the moon is to be taken from Part III. In a solar eclipse this part vanishes. Then enter Part IV. with the sum of the former equations in the first vertical column, and the horizontal semidiameter at the top; and take out the corresponding number, which being applied to the former aggregate, according to its sign will give the augmentation of the moon's semidiameter.

Ex.—Let the altitude of the nonagesimal be 55° 18′, the apparent distance of the moon from it 14° 42′, the moon's true latitude 24′ 2″ S., the parallax in latitude 35′ 40″, and the horizontal semidiameter 15′ 30″; what is the augmented semidiameter?

Altitude of nonagesimal 1° 25° 18′ App. dist. of moon from it 0 14 42

| Sum | | 10 10 | | | | 7".70 - 5.33 |
|--------------------------------------|-------|----------|---------|-------------------|-----|-----------------|
| Moon's true lat. 24' 2" S., and par. | in la | at. 3 | 35′ 40″ | Part I Part II | I.+ | |
| Sum | d S | lum | 13″.08 | Part I | | 13.08 0.82 |
| Augmentation | | | | 4 | | 12.26 30.00 |
| Augmented semidiameter | 1 | | 1 ma | | 15 | 42.26 |

TABLE XXVII.—Equations of Second Differences for twelve Hours.

In computing the moon's place from the nautical almanac for any given time by proportion, a correction resulting from the moon's unequal motion must be applied to the proportional part of the moon's motion in longitude or latitude, answering to the given time after noon or midnight. This correction is contained in the table, the arguments of which are the mean of the two second differences of the moon's motion at the top, and the apparent time after noon or midnight in the respective side column. This equation must be added to, or SUBTRACTED from, the proportional part of the first difference of the moon's motion in twelve hours, according as that difference is decreasing or INCREASING.

Hence the correct change, corresponding to the given interval, will

be obtained.

. If the given second difference is not found in the table exactly, the sum of the equations answering to the several terms, which make up

the second difference collectively, is to be taken.

This table may be applied in the computation of the place of a planet. And as the sun's declination varies somewhat irregularly about the solstices, a column has been added to the lower half of the table on the right side for differences in twenty-four hours, to determine the exact declination for any given time where great accuracy is required.

Ex. 1.—Required the moon's declination on the 15th of September,

1826, at 7^h 48^m 30^s P. M. apparent time on the meridian of Green-

In the explanation of Table IX. this is found to be 0° 38′ 21″ S. by proportion; it is only now required to find the correction depending on second differences. For this purpose two declinations must be taken out preceding the given time, and two after it, from which the mean second difference must be found.

The Moon's declination,

First Diff. Sec. Diff. Sept. 14th at midnight is 4° 23′ 24″ S. 2° 16′ 16″ 15th at noon 2 7 8 S. 2° 16′ 16″ 15th at midnight 0 9 19 N. 2 16 17 16th at noon 2 24 27 N. 0' 1" 34" 1 9

If the first differences first increase and then decrease, or vice versa, half the difference of the two second differences is the mean, instead of half the sum, as would have been the case had the differences regularly increased or decreased.

In this case the equation must be added or subtracted, according as the first first difference is greater or less than the third first differ-

ence.

Now to 30" and 7h 481m the equation is 0 .4

3 .8 The whole equation is Which, according to the rule above, must be added to the proportional part formerly found under the explanation of Table IX.; that is, to I° 48' 47" we must add 4", and the true proportional part be-+ 1° 48′ 51″ N. comes

And declination at noon being

The true declination is Unless the declinations are all north or all south, it is almost unnecessary to use the equation of second differences.

Ex. 2.—Required the moon's right ascension on the 20th November, 1826, at 9h 36m 30s p. m.?

The Moon's right ascension,

1826 First Diff. Sec. Diff. Nov. 19th at midnight is 116° 20′ 7″ 6° 11′ 40″ 122 31 47 20th at noon 6 9 49 20th at midnight 128 41 36 1 18 8 31 21st at noon 134 50 7 App. time 9^h 36^m 30^s Diurnal log. .09653 Change of dec. 6° 9' 49" Prop. log. 1.46543 $Or \div by 60=6' 9''.82$ Prop. log.

Prop. part 4' 56'.12 Prop. log. 1.56196 4° 56′ 7″.2

In this example we have considered the degrees minutes, the minutes seconds, and the seconds have been converted into a decimal by dividing by 6, since the change of declination exceeds the limits of the table. This comes to the same thing as dividing by 60; but any other aliquot part might have been taken,—such as a half, a

third, &c. provided the proportional part be doubled, trebled, &c. as derived from this table.

Amount of the whole equation is 7.2

Which must be added to 4° 56′ 7″.2, because the first differences are decreasing, consequently the corrected proportional part is 4° 56′ 14.″4.

The true right ascension required is . . . 127 28 1 .4.

Ex. 3.—Required the sun's declination at noon, on the 20th of

June, 1826, at Otaheité, in longitude 9^h 58^m W.? Sun's declination at noon 23° 27′ 11″ N.

Time 9^h 58^m diurnal log. 0.38166 Var. 0' 25" prop. log. 2.63548

P. P. 0 10".4 . 3.01714 + 10 .4

First Diff. Second Diff. Mean.

Diff. for 19th 25 26 25 + 3 .0

21st 1 23 27 24.4

In this example the argument in time is found in the right-hand column in the lower half of the table. In lunar distances the approximate time found by proportion after the hour given in the nautical almanac must be quadrupled, which, being used as an argument, will give to the mean second difference the true equation, amounting, in some cases, to about 6" in distance, or 3' of longitude.

TABLE XXVIII.—Reduction to the Meridian, Parts I. and II.

In the course of the great trigonometrical survey lately performed in France, the repeating circle was much used in the determination of latitudes and other operations. Latitudes were determined by observing repeatedly, near noon, the altitudes or zenith distances of a celestial object, reducing those taken off the meridian by appropriate formulæ or tables to what they would have been on the meridian. This method may be successfully practised by smaller instruments,—such as Troughton's reflecting circle, or even a good sextant; and Dr Brinkley, with his large eight-feet circle in the observatory at Dublin, takes three or four observations each day as near noon as possible, which are afterwards reduced to noon.

To facilitate these operations, this table has been computed, Part

I. by Delambre, and Part II. by Schumacher.

Ex. 1.—Application of the preceding table to observations of the star Arcturus at the observatory of Dublin, on May 12th 1820, made with the eight-feet circle, having three microscopes, one on the right side of the instrument, one at the bottom, and one on the left.

The latitude of the observatory from numerous observations of Dr Brinkley, corrected by his own very accurate table of refractions,

| Time by Clock. | Left Micros. | Z. D. Bottom Microscope. | Right Micros. | | the three scopes. | Refraction. |
|----------------------|-----------------|---------------------------------|------------------|-------|-------------------|-------------|
| h. m. s. 13 56 28 | 49.7 | 3 19 50.5 E. | 4.3 | 33 19 | 54.83 | 37.82 |
| 14 0 28 | | 33 17 32.6 E. | 47.1 | | 37.13 | 37.77 |
| 14 9 51 | | 33 14 54.5 W. | 45.0 | 14 | | 37.74 |
| 14 14 52 | 38.0 3 | 33 16 41.0 W. | 31.7 | 16 | 36.90 | 37.77 |
| Barometer S | | nter. Ther. 52.5 ext. — 48.0 | Mean. | 33 17 | 14.72 | 37.775 |
| Time of Star's | Time of Obse | Difference. | | Redu | etion. | |
| Transit by Clock. | h. m. s | | Part | I. | Par | t II. |
| 14 7 3.3 | 13 56 2 | | 220" | .10 | 0" | .12 |
| 14 7 3.3 | 14 0 2 | 8 0 6 35.3 | 85 | .22 | 0 | .02 |
| 14 7 3.3 | 14 9 5 | 1 0 2 47.7 | 15 | .32 | 0 | .00 |
| 14 7 3.3 | 14 14 5 | 2 0 7 48.7 | 119 | .80 | 0 | .04 |
| , | | Sum's | 440 . | 44 | 0 | .18 |
| | | | 110 . | 11 | 0 | .045 |
| | | 1 | | | | |

Now, if the tabular quantity in Part I. be called m, and that in Part II. be called n, the latitude λ , the declination δ , the approximate zenith distance z, the declination and zenith distance being + if north, and - if south, and the true zenith distance Z;

then
$$Z = z - \frac{\cos \lambda \cos \delta}{\sin Z}$$
 $m + (\frac{\cos \lambda \cos \delta}{\sin Z})^2 \cot Z$ or $Z = z - \frac{\cos \lambda \cos \delta}{\sin Z} (m - \frac{\cos \lambda \cos \delta}{\sin Z}) \cot Z$ n nearly.

In the formula it is supposed that the latitude of the place and declination of the star, and consequently its zenith distance, are previously known; but in all cases where the latitude alone, or the declination alone, is known, z must be substituted for Z in the formula. and then the resulting reduction, which will not differ materially from the truth, when applied to z will give Z and a very nearly correct; after which, the operation pointed out by the formula, must be repeated with Z and \(\lambda\) as if they had been previously known. This repetition which, as appears by the following example, is easily performed, will give the reduction correct enough for all observations made near the meridian; but, if the horary distance be great, a second repetition may be necessary, though scarcely when the observations are kept within the extent of our table, and, unless from necessity, they should not be taken more distant, as in that case. a small error in the time will produce a considerable error in the zenith distance. On this account observations very distant from the meridian are not to be recommended, as they may tend to vitiate those made near it.

| λ 53° 23′ 13″ cos. λ 20 7 28 cos. z 33 17 15 cosec. | 9.775544 9.972541 0.260554 (a) cot. | 0.182722 |
|--|---|-------------------|
| m 110.11 log . | 0.008739 × 2 = . 2.041787 n 0.045 log. | 0.017478 8.653213 |
| pellit out | $38\ 2d$, cor. $+.0713$ | 8.853413 |
| 1st, Cor. — 112".35 (e) or — 1' 52 .35 2d, Cor. + 0 .071 | 2.050564 (c) 380 | 11 8 |
| 20, 001. + 0.0/1 | 134 | |
| z 33° 17 14 .720 | | (- C A |
| z' 33 15 22 .441 Ref. + 37 .775 | | |
| z" 33 16 0.216 (f) cosec. | 0.260794(b) | 0.00 |
| | 240 (b—a) | |
| -112.41 (d) . | $2.050804 \{c + (b - a)\}$ | |
| (de) | 766 | |

z"' 33 16 0 .156 $\{f-(d-e)\}$ 38 This result scarcely differs from Dr Brinkley's, which is 33° 15′ 0".17, to which the aggregate of precession, aberration, and nutation, amounting to -13".53, being applied, gives 33° 15′ 46".64 for the

mean zenith distance on January 1, 1820.

Ex. 2.—At Maranham, August 28, 1822, Captain Sabine took the following observations of the star & Lyræ with a repeating circle of six inches in diameter, the barometer being 29ⁱⁿ .95, the thermometer 80° Fahrenheit, the chronometer, No 423, fast 2^h 55^m 59^s; the star, whose right ascension was 18^h 30^m 57^s.4, was on the meridian, at 8^h 4^m 35^s mean time, and at 11^h 1^m 34^s by the chronometer.*

^{*} This example is extracted from Captain Sabine's work on the determination of the length of the seconds pendulum at various points of the earth's surface, lately published at the expense of the Board of Longitude. It is a work highly to be recommended, for perusal, to those likely to be employed in such experiments in future, as it contains valuable examples of all the requisite operations likely to occur in such researches.

| Chronometer Horary Redu Angles P. I. | P. II. Level. | Readings. | The boston |
|--|--|--|---|
| 10 55 44 3 50 28.88 11 0 49 0 45 1.10 | $\begin{array}{c ccccccccccccccccccccccccccccccccccc$ | First Vernier 1676 Second Third Fourth Mean 167 Second Third First Vernier 1366 Second Third Fourth Third Fourth | 11 30 12 10 11 40 11 47 .5 |
| Means 92.01 | 0.0425 | Mean . 136 Index + 192 Level — | 35 0 48 12 .5 16 .5 |
| # 41° 10′ 22″ log. & Ther. 80 F. Bar. 29.95 Ther. r 47″.84 | 9.97367 9.99367 9.99926 9.99870 1.67976 | r Cor. $+$ True Z D 41 | 22 56 10 22 47 .84 1 49 .01 9 20 .83 37 37 .60 |
| λ 29 31' 45" cos. λ 38 37 38 cos. z 41 10 22 cosec. | 9.999578 9.892776 0.181555 (a) cot | and the same of the same | 31 43 .23 |
| m 92".01 log. | $\begin{array}{c} 0.073909 \times 2 = \\ 1.063835 & n, 0.04 \end{array}$ | | |
| 1st cor.—109''.08 or — 1' 49 .08 2d cor. + 0 .07 — 1 49 .01 | 2.037744 0.06 426 318 | 8.834400 | |

It is unnecessary to repeat the operation in this case, as the difference in the result would only be 0".04, making the latitude 2° 31' 43."19

TABLE XXIX.—Reduction to either Solstice, the Obliquity of the

Ecliptic being 23° 27′ 40″.

The obliquity of the ecliptic is determined by a number of meridian altitudes, or zenith distances near either solstice. If the sun's longitude were three or nine signs exactly at noon, the operation would be very simple; but as that seldom happens, it is necessary to reduce the actual observations to which they would have been under these circumstances. To accomplish this object, this table has been constructed. In the table the obliquity is supposed to be 23° 27′ 40″, and the reduction is the difference between this quantity and the sun's declination at the several points of the ecliptic corresponding to the observed right ascensions. With the differences and variation for 100" change of obliquity the table may be adapted to any time within the limits of the table's variation of obliquity. Both quantities will thus be additive till the year 1835. The table is extended to 30^m, and consequently observations may be reduced by it for about seven days before and as many after the solstice.

Ex. 1. On the 15th of June, 1826, the sun's declination was observed to be 23° 18′ 51″.7, when the right ascension was 5^h 25^m 51°.4, and the obliquity 23° 27′ 39″, what was the reduction to the

solstice?

| Oh Om O | Tabular obliq Estimated obl | uity | 23° 27′ | 40' |
|--------------|--------------------------------|---------|---------|-----|
| 6h 0m 0s | Estimated ob | liquity | 23 27 | 39 |
| 5 32 51.4 | Excess | | 100 | 1 |
| | distance from t | | | |
| 27 0.0 giv | es | | 2".73 | |
| 8.6 giv | es · · | | 5 .564 | |
| 1".0 var | obl. gives | es. 4 | 0 .005 | |
| Reduction | 6a . II. | | 8 .299 | |
| Sun's declin | ation 23° | 28 5 | 1 .7 | |
| - m - 11: | 00 | 07 2 | 0000 | |

By operating in this way for several days near either solstice, the true obliquity may be obtained from a mean of a number of observations, and consequently likely very near the truth. It may be observed, however, that the sun's latitude from Delambre's tables, taken

in this manner.

Ex. 2.—I had commenced to determine the obliquity of the ecliptic from the totality of the Greenwich observations by Dr Maskelyne, and had proceeded so far when I was anticipated by Dr Brinkley. I used the French table of refractions, Delambre's table of reduction depending on the sun's longitude instead of the R. A., which, being rather more convenient in practice, is made the argument here. The longitude and latitude of the sun were computed from Delambre's Tables, and, as the methods are analogous, any one who can compute by the longitude can readily also use the right ascension, and the following example is given as an illustration of either.

with a contrary sign, should be applied to the obliquity determined

Th

-12

CALCULATION OF THE OBLIQUITY OF THE ECLIPTIC, JUNE 1765.

| | Dec. year. | 0.468 | | | .04 Motion in 24bs=57, 12,"96 | deur Service Personnis Personnis Personnis | | |
|-----|-------------|---|-----------|------------------|--|---|--|--------------------------|
| 10 | Z | 27 | 52 | | tion in | | | 11. |
| | 뚬, | 153 | 169 | 19. | .04 Moi | mid y pose | U 0 | |
| | 図 | 275 | 314 | 15' 45".67 | 2 23 8 | male = | 0.8 73 0.8 73 | |
| | D | 37 249 | 286 | eter | notion | , , , , , , , , , , , , , , , , , , , | 518 18 72 73 | |
| | 0 | 515 | 276 | O's semidiameter | Horary motion Hor. parallax | 76g | 90000 | . Y 2 |
| 90 | B | 281 468 | 749 | O's se | | un's Lor 16th 2° 2 19 2 2 | 25 25 25 25 25 25 25 25 25 25 25 25 25 2 | =Transport |
| | A | 294 789 | 83 | П | 94 | S. June J | | |
| . 0 | M | 425 206 | 631 | | CONTRACTOR OF THE CONTRACTOR O | onti agi | முன் சி. மே. மே. | FIR B |
| | Perigee | 0° 0° 0′ 0″ 9 8 52 56 29 | 9 8 53 25 | 2 29 54 38 | 5 21 1 13 or 5 21 1.2 Sun's mean anom. | Toyley (by | | |
| Y | Longitude O | 0° 0° 0′ 0″.3 9 11 21 50″.3 5 18 32 44 .4 | 3.1 | 2 29 54 38 .1 | 16 54 .2 1 .1 11 .8 | ++ 6.38 6.09 6.09 | 3 0 12 12 .2 + 5 .8 + 0 .0 | O's T. lon. 3 0 12 18 .3 |
| | Argum. | Sec. equa. 1765 June 21st | 1m 15s | Mean lon. | - L | M M M M M M M M M M M M M M M M M M M | Lun. nu. Sol. nu. Aberra. | ⊙'s T. lon. |

zenith distances, which amounts to +1".1. Mr. Thomas Henderson has found the latitude of Greenwich, by Ivory's Refractions, to be still less from Mr. Pond's late very accurate observations. If my estimation, 51° 28' 38".4, prove right, the obliquity would be 23° 28' 6".

| App. Obliquity. 23° 28' 16".9 17.2 11.6 11.8 13.5 15.2 | 23 28 15 .9 - 8 .8 - 8 .8 - 8 .8 - 8 .7 .1 - 0 .6 N. c. 5 28 7 .1 - 0 .6 N. c. 5 28 6 5. c. 5 28 6 5. c. 6 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 |
|---|--|
| Declination. 23° 23′ 33′.1 27 37 .6 28 3 .9 28 17 .2 27 55 .2 27 15. 9 26 8 .9 | In these examples the English barometer and Fahrenheit's thermometer have been reduced to the French measures. This might have been avoided by using proper factors now usually given with the French tables. In this computation we have made the latitude of Greenwich 51° 28′ 39″ N., or 1″ less too great by about 1″ or 1½′. The error of the line of collimation has been applied to the zenith distances, which amounts to 1″ 1″ Tr. |
| Par. Reduction. 4.43".8. 1.1 4'43".8. 39.6 1.1 7.7 1.1 0.2 1.1 1 0.2 1.1 2 8.2 | A A Commeter be been rehis might St. factors tables. If the latitude of (et agree nearly we error of the line error of the line of the lin |
| Befrac. 30%.29 300%.29 300%.29 300%.29 300%.29 300%.29 300%.29 300%.29 444444 | In these examples the English barometer and Fahrenheit's thermometer have been reduced to the French measures. This might have been avoided by using proper factors now usually given with the French tables. In this computation we have made the lattithan Dr Maskelyne, and in this we agree r too great by about 1" or 1½". The error of the senith distances, which amounts to ±1". |
| Metr. Cent. 7508 18.33 7627 17.22 7.7627 17.22 7.7627 17.60 7.7607 19.58 7.7585 17.77 7.7610 19.30 7.7594 19.16 | In these examp and Fahrenheit's duced to the Fre have been avoide now usually give In this comput than Dr Maskely, too great by abou zenith distances. |
| Thermometer. Out. In. Mean 68 62 65 654 604 63 69 62 65 702 64 67 71 622 64 71 622 663 69 64 663 | Distances. 22° 28"3 227 48 52 .0 28"3 28 16 21 .4 27 48 52 .0 28 15 54 .3 28 15 54 .4 .4 .4 .4 .4 .4 .4 .4 .4 .4 .4 .4 .4 |
| Day. Bar. June. Inches. 16 29.57 19 30.04 20 30.04 21 29.96 22 29.97 23 29.97 24 29.97 | Obs. Zenith June 16 { U. L. L. 19 { U. L. L. 20 [L. L. 21 { U. L. 22 [L. L. 23 { U. L. 24 { U. L. U. L. 25 { U. L. 26 [L. L. 27 { U. L. 28 { U. L. 29 { U. L. 20 { U. L. |

TABLE XXX.+To change Mean Solar into Sidereal Time.

As a clock regulated by sidereal time is indispensable in every observatory, it is necessary to convert solar into sidereal time in order to know by the clock when any phenomena, such as eclipses, occultations, &c., calculated in mean solar time should take place. This table is employed for that purpose, as will appear by the following example.

An immersion of θ Aquarii by the moon took place on January 5, 1824, at 3^h 46^m 50^s, apparent solar time by the meridian of Greenwich; what will be the time by a sidereal clock which shows 0 h0^m 0^s when the point Aries is on the meridian, and her error that

day 36s .54 fast?

In this case the clock would be a right-ascension clock; and if she went true would show the right ascension of the celestial bodies as they passed the meridian when observed by a transit instrument. Now on the 5th of January, 1824, the sun's right ascension at noon is 19^h 1^m 37^s.0, the same as would be shown by a clock truly regulated.

But as the clock was 36°.54 fast on that day this must be added to give the time shewn by the clock, that is, she shows 19^h 2^m 13°.54 at noon. As the immersion happened at 3^h 46^m 50° P. M. this must be converted into sidereal time, and added to the preceding to give the time shown by the clock, so that an astronomer may be prepared to observe it.

This operation may be accomplished by the table.

| Time. | Acceler | ation. |
|------------------------|--------------------------------------|-------------------------|
| 3h 0m 0s g | gives 0 ^m 29 ^s | .569 |
| 46 0 | | .557 |
| 50 | . 0 | .138 |
| | - | |
| 3 46 50 | | .264 |
| Hence to the time show | by the clock | 19h 2m 13s.54 |
| There must be added | | 0 0 37.26 3 46 50.00 |
| And | | 3 46 50 .00 |
| 日本共工工工 医自己病 | | |
| Whence the time shown | will be . | 22 49 40 .80 |

TABLE XXXI .- To change Sidereal into Mean Solar Time.

This table may be useful for finding the rate of a clock or chronometer. As the transit of a fixed star advances 3^m.55^s.908 daily on mean solar time, if the passage of a star be observed with a transit instrument each day for several successive days, or the disappearance of a star during several successive nights behind a fixed object, such as the vane of a steeple or the body of the steeple itself, nearly in the meridian, the position of the eye of the observer being also fixed, the rate of the clock becomes known on sidereal, and consequently, by this table, on mean solar time.

Required the retardation on 10d 5h 48m 56s of sidereal time?

| For 10 days we have | 0 ^h 39 ^m 19 ^s .080 |
|--|---|
| 0 ^d 5 ^h 0 ^m 0 ^s 48 0 | 49.147 7.864 |
| 56 | . 0.153 |
| Russian A Wester | 0.40.10044 |
| 1 5 48 56 | - 0 40 16.244 10d 5 48 56.000 |
| Total Carlotte and the second | - 10 0 10 00:000 |
| Mean solar time | 10 5 8 39.756 |

TABLE XXXII.—To convert Mean Time into Parts of the Equator.

This table may be useful for converting into degrees, &c. the hours, minutes, &c. shown by a clock or chronometer regulated according to mean time; and the method of using it will be readily understood from the examples to the two preceding tables, and that of Captain Kater's in the appendix.

TABLE XXXIII.—Lengths of circular Arcs.

The method of using this can be no difficulty to those acquainted with the preceding tables, as they are employed in a similar manner.

TABLES XXXIV., XXXV., XXXVI., XXXVII., XXXVIII., XXXIII., XXXIX., XL., XLI., and XLII. are abridged from a series of tables, by Mr Fallows, astronomer at the Cape of Good Hope, and were transmitted to the Admiralty, along with an approximate catalogue of stars which he had formed there, and are very convenient for finding at once the amount of the corrections for precession, aberration, and nutation for any given observation, both in right ascension and declination. In addition to these, however, another table must be computed annually. Since the tables are only given to every ten minutes of right ascension, proportional parts are added for every single minute as far as 6 indicated by the figure in the place of tens in the side column. If the odd minutes exceed 6, the proportional part must be taken at twice, or the complementary proportional part to the next minute of even tens, must be applied with a contrary sign when necessary.

To understand the method of applying these tables is premised

the following

PANCE

Synopsis: -Constants. Table XXXIV. = 1°.3362 sin. R. A. tan. dec. + 3°.0678 = a XXXV. = 1.3500 sin. R.A. = p, and $p \times \sec$ dec. = b XXXVI. = 1.2390 cos. R.A. = q, and $q \times sec. dec. <math>=$ c XXXVII. = + 0.6430 cos. R.A. = s, and $s \times \tan dec = d$ XXXVIII. = $-20.0436 \cos R.A. = \text{annual precession} = a'$ = $-20.2550 \cos R.A. = p'$, and $p' \times \sin dec. = b'$ XL. $= + 18.5800 \text{ sin. R.A.} = q', \text{ and } q' \times \sin \cdot d + r' = c'$ XLI. $= + 8.0659 \cos dec. =$ = 9.6480 sin. R.A. = s' sin. & sin. 2 O Annual Table, part 1st = $t - \frac{1}{3}$ 40 part 2d = 0.93046 (cos. \otimes - cos. 2 \otimes + $\frac{2}{31}$ cos. $2 \odot$)

where t is the time elapsed since the commencement of the year when the sun's mean R. A. is supposed to be $18^{\text{h}} 40^{\text{m}}$.

Table of sines of sun's longitude at the time of culmination = B Table of cosines of the same $\cdot \cdot \cdot =$ C Then the whole correction in R. A. = A a + B b + C c + D d (1)

in dec. = A a' + B b' + C c' + D d' (2)

Ex.—Required the corrections of Fomalhaut in right ascension and declination for July 20th, 1824, at the time of his passing the meridian of Greenwich, the R. A. of the star being 22^h 48^m, and declination 30° 33′ South.

The sun's longitude for this time is 118° 12', of which the natural sine is .881 = B, and the cosine is .473 = E. A and D must be taken from an annual table, or computed from the formulæ given

above for that purpose.

Then from table XXXIV., &c. take the proper numbers for the R. A. of the star, and complete the multiplications indicated by formula (1) the sum of the results will be the total correction in R. A., and those by formula (2) will be that in declination.

| Thus Table XXXIV414 590 | В | C | A | D |
|------------------------------|--------------------|-----------------|--------------------------------------|------------------------|
| $\frac{207}{37}$ | .881 | .473— 1.178— | .901+ 3.312+ | .112+ .616+ .061 |
| | .352 . 9 . 6 | 471 82 3 | 2.981 | 061 |
| Prec. in R. A. 3.312 | .367+ .556+ | 556+ | 2.984+ Tan. dec. | 068+ |
| Nat. sec. dec. | .923+ 1.161 | and Miles in | (fam) (mas an sh | 034 |
| The second of the second of | 923 92 55 | | AT THE ST CONTRACTOR LANGESTON | 040+ |
| | 1.071+ | _ x | 7128 | 2-15 |
| | 2.984+ 0.040+ | =y | - 7500 | - |
| rections in right ascension. | 4.095+ | =x+y+ | z=the sun | a of cor- |

Annual precession for 22^h 48^m, table XXXVIII. is = 19".062.

| - | В | C | C | A | D |
|--|-----------------------------|-----------------------|-----------------------|-----------------|------------------|
| bern control | .881 + 19.264— | .473— 6.945+ | .472 — 6.945 + | .901+ 19.02- | .112+ 2.981+ |
| 1 000 2 L | 15.411 1.541 .019 | 2.778 .486 .021 | 2.778 .486 .021 | 17.156 019 | 0.298 30 6 |
| The state of the s | 16.971— 2.716+ | 3.285— | 3.285— | 17.175— | .040+ |
| sin. dec. | 14.255 — .508 + | I I I I I I I I | | | |
| - A - 1 445 - | 7.127 .114 | 7 | 144 | | |
| 100 | 7.241— 3.285— 17.175— | =y' | 110 | For a | -100-1 |
| | 0.334+ | high | | | = 1 :N 1 :- |
| 1 | 27".366— | = sum of | correction | ns in decli | nation. |

And in this manner the total corrections for any number of stars may be readily computed.

TABLES XLIII., XLIV., XLV., XLVI., XLVII., and XLVIII. are general for the same purpose as those above. By the former are computed more readily the corrections of a number of stars near one another than by the present, though they are convenient and very accurate for computing the corrections for any single star.

Ex.—Required the true apparent right ascension and declination of a Aquilla on the 1st of January, 1828; the mean R. A. being 19^h 42^m 23^s.6 and declination 8^o 25′ 15″ N.?

1st, To find the Nutation in R. A. and Declination.

| R. A. of star . Lon. moon's node | | | | 241211 | | |
|-------------------------------------|--------------|-------|--------------------------|---------------|-------|----------------------|
| Remainder Sum | 2 23 4 27 | | tab. XLIII tab. XLIV. | | | |
| Declination 8° 2 | 5' tange | ent | Care from | + 0.12 | - | nut. in dec.+9 .41 |
| Product, or part Long. moon's not | | secon | | 0.018 9.14 | | the same of the same |
| Nutation in R. A | | | + | 9.158 | = 0°. | 61 |

To find the Aberration in R. A. and declination.

| R. A. of star 9° 25° 36′ Sun's lon. 9 10 8 |
|--|
| Remainder 0 15 28 Tab. XLVI. — 18".72 Sum 7 5 44 Tab. XLVII. — 0 .68 |
| Declination of star 8° 25' secant |
| Aberration in R.A. — $1^{\circ}.3 = -19^{\circ}.51$ log. 1.2925 Remainder + 3° = $3^{\circ}.15^{\circ}.28^{\circ}$ Tab. XLVI. +5".18 Sum + 3° = $10^{\circ}.5$ 44 Tab. XLVII. +0 .48 |
| Star's declination 8° 25' Sine +5 .56L.0.7528 9.1654 |
| Sun's longitude 9° 10 8 Part 1st +0".83 L. 9.9182 |
| Sum 9 18 33 Table XLVIII. -1 .28 Remainder 9 1 43 Table XLVIII. -0 .12 |
| Aberration in declination |
| True R. A. 19 42 22.91 True dec. 8 25 23 .8 |

TABLE XLIX. contains the mean obliquity of the ecliptic for the beginning of the year, which I have determined from all the most accurate observations I could obtain, together with the annual and monthly diminutions for the purpose of computing it at any other time.

TABLES L. and LI. give the necessary corrections to determine the apparent obliquity at any given time, which will be easily applied, and the mode of application is obvious.

TABLES LII. and LIII. contain the Lunar and Solar Equations of the Equinoxes in time, which are sometimes more convenient than in space.

TABLE LIV. contains the mean right ascensions and declinations of a few of the principal fixed stars for 1828, together with their annual variations for reducing them to any other time required.

TABLE LV.—Decimal Numbers for each Day in the year. It is useful wherever the fraction of the year is wanted, as in reducing the places of stars, &c. to any given day in the year. This is accomplished by multiplying the annual variation by the number of

years and decimal for the given day. The result applied with its proper sign will give its mean place after the given time to which the corrections for precession, nutation, and aberration, being also applied with their proper signs, will give the apparent place at that time.

TABLE LVI.—The Right Ascension of the Sun.

This table is adapted to leap year, particularly the year 1828, and is only intended to answer the purposes of instruction when no great degree of accuracy is required, and the Nautical Almanac not at hand.

In order to adapt it to common years, one-fourth of the difference between the given and preceding days is to be subtracted from the right ascension in the table for the first after leap year, one-half for the second after leap year, and three-fourths for the third; and in the months of January and February, the right ascension is to be taken for the day following that given.

This table may be employed in finding the apparent time by the altitude of a star, for finding the time of a star's transit when that is required, for obtaining the latitude by a meridian altitude, &c.

I. To find the Time of Transit.

Rule.—From the R. A. of the star, increased by 24° if necessary, subtract that of the sun; the remainder will be the approximate time of transit. To this time apply the longitude of the given place in time by addition or subtraction, according as it is nest or east; the result may be called the reduced time. To this reduced time compute the right ascension of the sun, which will be the sun's true R. A. at the time of transit. Now from the star's right ascension for the given time subtract the sun's true R. A.; the remainder will be the apparent time of transit.

II. To find the apparent time of rising and setting of a known star, the latitude and longitude of the place, and the year and day

of the month, being known.

Rule.—Find the apparent time of the transit of the star by the preceding rule; then find half the time of the continuance of the star above the horizon, by the method shown in Problem VI. of Spherical Trigonometry in the Introduction, page 72 and 73, which, being applied to the time of transit by subtraction and addition, will give the apparent times of the rising and setting of the star respectively.*

TABLE LVII.—Declination of the Sun.

This table contains the sun's declination for the noon of each day, on the meridian of Greenwich for the year 1828, or leap year. By this table the declination, sufficiently correct for many purposes, may be found for other years. For the first year after leap year, take one-fourth of the difference between the declinations for the given

Mr Thomas Lyan has given, in his extensive collection of Nautical Tables, the times of transits of 60 principal stars for every day in the year, which, in many calculations, are very useful.

and preceding days, which is to be added to the declination for the given day, if at that time the declination is decreasing, but subtracted if increasing. In the second after leap year take the half, in the third take three-fourths of the difference, and apply this correction in the same manner as before; the result will be the declination required. And in the months of January and February the declination is to be taken for the day following that given.

TABLE LVIII.—The Equation of Time.

This table contains the equation of time for 1828, or leap year; and is to be found for any other year in the same manner as the de-

clination above explained.

Time, deduced from observations of the sun, is called apparent time, to which the equation of time, being applied according to its title in the table, gives mean time. Since a clock or chronometer is constructed upon the supposition of a uniform motion, this table will be useful for ascertaining the rate and error on mean solar time. Also, if a clock be regulated to mean solar time, the instant when the sun's meridian altitude ought to be observed to find the latitude, is known by applying the equation of time to 12h, with a contrary sign to that in the table. These applications will be more readily understood by consulting the article on finding the longitude by chronometers in the introduction.

TABLE LIX.—Correction of the Longitude by Chronometers. This table is on the same principles as that given by Rossel in the third volume of Biot's Astronomie Physique, only substituting for the natural numbers their logarithms, as being more convenient in practice.

Ex.—At Tongatabou, on the 6th April, 1793, at 19^h 53^m 31^s .44, the daily rate of a chronometer was + 5°.24, with an original error of + 1^m 20°.93. The ship sailed from Tongatabou, and arrived at Ballade harbour, on the 22d of April, when, by observation, the daily rate was + 8°.56, and the error 1^h 24^m 23^s .71 fast for mean

| daily rate | was $+ 8^{\circ}.56$, | and the e | rror 1h 24m | 23°.71 fast | for mean |
|---------------|------------------------|------------|-------------|---------------|-------------------|
| time. | | | | | |
| | at Tongatabo | u . | | | + 5:.24 + 8.56 |
| | at Ballade | | | | +8.56 |
| | ~ | | | | 1 |
| | Sum | • | 100 | • | 13.80 |
| | TT 10 | 7.77 | | | 0.0 |
| | Half, or mea | | | | 6.9 |
| Differen | ce of longitu | de betweer | 1 Tongatabe | ou and Ball | ade by the |
| first daily 1 | ate of 5°.24 | | | . 20 | ° 24′ 34″ |
| Difference | of longitude | by the mea | n rate of 6 | s.9 20 | 17 55 |
| 1 1-01 | 17 00 00 10 | 1,000 | Wings. | L'ANDERSON DE | |

Difference easterly 6 39 E. because the difference of longitude ought to be diminished.

From these data, what is the correction of the observed longitude, on the 17th of April, at 7^h 34^m?

of the los

| Correction of the longitude of Dahade for 10 days | |
|---|---------|
| 6' 39"=399" log | 2.60097 |
| Log. for 16 days, Table LIX., ar. co. | 7.86646 |
| From 6th April to the 17th, or 11 days, log. Table LIX. | 1.81954 |

Correction $3' 14' = 194'' \log$. 2.28697

The correction of the longitude of the 17th gives the place of observation more easterly, because Ballade ought to be to the east of the position calculated by the daily rate determined at Tongatabou.

Since the first two logarithms are constant, the correction of the longitude for other days in the same run, is easily obtained by substituting for the last logarithm that from Table LIX. for the given number of days elapsed from the time at which the rate was originally determined, and in this manner ought all longitudes to be corrected in a long run, where the rate of the chronometer has experienced considerable alterations.

The same thing may be done without the table, as in the following example taken from Captain Hall's observations on the coast of

South America:-

" San Blas, West Coast of Mexico."

"Corrections to be applied to chronometrical measurements of

the longitude of places between Acapulco and San Blas."

"The rate of the chronometer, by which the differences of longitude was obtained, of places between Acapulco and San Blas, was

that determined at Acapulco, or ± 0°.0 per diem."

"On arriving at San Blas, however, after an interval of 18 days from Acapulco, the rate was found to be +2.6 per day. It became necessary, therefore, to make a proportional allowance at intermediate places for the increase of rate, which increase may be taken as uniform during the interval. This is effected by computing the whole difference of longitude by the mean of the two rates ±0.0 and 2.6, namely 1.3, and taking the difference between this determination and that by the first rate, whence are obtained 351" for the accumulated error in longitude in I8 days' interval."

"Now the sum of a series of 18 terms in Arithmetical progression, having 1" for the first term, and 1" for the common difference, is

171, consequently $\frac{351''}{171} = 2''.053$ nearly for the daily increase in

the error of longitude, and this multiplied by the sum of the terms in the series before designed, according to the number of the days elapsed since the rate was first determined, will give the respective corrections in longitude, to be applied to those deduced by chronometer, with the Acapulco rate. Whence we get 2' 15", for an interval of 11 days, to be deducted from the longitude of Colima, west of Acapulco; and the correction for an interval of 15½ days is 4' 21", to be taken from the longitude of Cape Corrientes, west of Acapulco.

TABLE LX.—Latitudes and Longitudes of Places.

This table contains the latitudes and longitudes of a few of the principal places in the world, given with all the accuracy in my power. It also contains the time of high water at the times of new and full moon, and the depth of the water at spring and neap tides, which are necessary to find the time of high water at any particular place on a given day, as well as the depth of the water of any tide, and at any hour of the tide, which may sometimes be necessary. The height of the neap tides is seldom given in tide tables, though for these purposes the one should be given as well as the other.

Indeed, it were to be wished that officers of the Royal Navy, as well as others, should carefully mark all these circumstances; so

that a complete tide table, embracing all the necessary data, might at last be formed.

TABLES LXI. and LXII. serve to convert space into time and conversely, and their use is so easy to those acquainted with many of the foregoing tables that any farther explanation is unnecessary.

TABLE LXIII. contains a selection of useful numbers frequently wanted in calculation, which have their logarithms and arithmetical complements subjoined.

TABLES LXIV. and LXV. are given for the purpose of computing the time and height of high water, as well as its height at any particular time of the tide, at such places where the heights at spring and neap tides are known, It is to be hoped that our navy officers will be enjoined to give, not only the time and height at new and full moon, but also at the quarters, to furnish data for these tables.

Ex.—Required the time and depth of high water at Leith, on the 12th of December, 1826; and also the depth 2^h before or after high water, or about 4^h from the nearest low water?

As the time of high water would be that on the following morning, half the sum of the transits on the preceding and given days must be taken, thus:—

| Moon's transit on the 11th | 10 ^h 3 ^m 10 50 |
|---|--------------------------------------|
| Mean | 10 27 + 1 |
| Reduced transit Time of high water at new and full moon Equation, Table LXIV. | 10 28 2 20 + 10 |
| True time | 12 58 |

Or 58^m, part noon of the 12th.

To transit 10^h 27^m and parallax 54' (Table LXV.) in which a is the height of the spring tide, and b that of the neap, the multipliers respectively are $0.676 \ a = 0.676 \times 16 = 10.816$ feet and $0.176 \ b = 0.176 \times 8 = 1.408$ feet

Total height in feet = 12.224

Now, with the time 2^h after the nearest high water, the multiplier in the right-hand part of the table is 0.779. This multiplied by 12.224 gives 9.5 feet at that time of the tide.

TABLES LXVI. and LXVII. contain the equation of third and fourth differences, which must be applied in order to obtain the moon's apparent place with great accuracy, especially in occultations, in determining the longitude by the moon's transit over the meridian, &c. They are used in the following manner:—Take out of the Nautical Almanac the three right ascensions, &c. preceding, and the three following the given time, and deduce their first, second, third, and fourth differences, also the mean of the two second differences standing on each side of the given time, and the mean of the two

fourth differences. Then to the proportional part of the middle first difference, corrected by the equation of mean second difference, by Table XXVII. apply the correction of the third difference from Table LXVII. answering to the middle third difference, and the correction in Table LXVII. answering to the mean fourth difference, and the result will be the correct moon's place. These corrections must be made according to the following rules.

If the third difference be positive and the time from noon or midnight less than six hours, the correction is positive; but if greater than six hours, the correction is negative. If the third difference be

negative the rule must be reversed.

The equation of fourth difference has the same sign as the fourth

difference itself.

These tables and rules were given by Mr Henderson in the 38th No. of the London Journal of Science; but we have not room to exemplify them here, though to those well acquainted with the application of the equation of second differences there will be little difficulty.

TABLE LXVIII. was drawn up by Captain Kater, and, being easy in its application, it will be found very convenient at sea, for which it is chiefly intended.

Ex.—On the 23d of June, 1826, in longitude 30° W., the following altitudes of the pole star were taken, the height of the eye be-

ing 20 feet; required the latitude?

| 61 - 3 · | 8h | | imes. 24 ^s 0 | Observed Altitudes. 50° 38′ 20′′ 50′ 40′ 20′ 50′ 22′ 10′ |
|--------------------------|------|-------------|-------------------------|---|
| Means Long. | - | 38 | 3 | 50 33 37 Dip to 20 ft. — 4 26 |
| M. T. G. Eq. T. | | | 3 37 | 50 29 11 Refraction — 48 |
| App. T. Sun's R.A. | 10 6 | 36 6 | 26 6 | T: alt. 50 28 23 tang. 0.0835. 1st cor. + 54 23 log. A" 1.7584 |
| R. A. mer. R. A. star | 16 | 42 58 | | 2d cor. + 1 10 log. 1.8419 |
| *'s M. D. | 15 | 43 | 48 | Latitude 51 23 56 N. |

the state of the second district and the state of the sta

APPENDIX.

On the Minute Corrections of Lunar Distances.

In lunar observations the corrections for the spheroidal figure of the earth have been applied according to the method of Professor Lax of Cambridge, Dr Inman of Portsmouth, Mr Riddle of Greenwich, &c. by diminishing the equatoreal horizontal parallax by the reduction for the latitude; but unless the latitude and altitudes are in like manner reduced, which leads to a complex calculation, the results are still inexact. The method here proposed is similar to that of Mendoza Rios, requiring only a small table to facilitate its application. The table has been computed by my ingenious friend,

Mr Thomas Henderson, for an ellipticity of $\frac{1}{300}$, which seems to

agree well with the latest measures, and to the mean horizontal parallax 57', which is sufficiently accurate for practical purposes, as the greatest error can hardly exceed 1", and at a mean not above half that quantity. This is within the limits of uncertainty arising

from an error in the ellipticity, which seems to vary between $\frac{1}{295}$ and

 $\frac{1}{305}$ even from the best measures, the mean between which, $\frac{1}{300}$,

has been here adopted. No doubt such refinements are unnecessary in the usual sea practice; but as the lunar method, which is still capable of improvement, can be practised with great success at land, it was thought necessary to correct an erroneous rule, which I believe has been generally acted upon. For illustration we shall give Example 4th, page 97 of the introduction, corrected in this manner as explained by Mr Henderson in the 40th No. of the London Journal of Science.

Rule.—When computing the parallax in altitude; to the logarithm of the earth's radius (Table XXIII.) add the secant of the moon's apparent altitude, and the proportional logarithm of the moon's equatoreal horizontal parallax, the sum of these will be the proportional logarithm of the moon's parallax in altitude to be employed in computing the true distance. Now from half the sum of the moon's polar distance, the sun's or star's polar distances, and the distance of the moon from the sun or star, subtract the moon's polar distance, and the distance from the sun or star respectively. Then to the con-

stant logarithm 0.30103, add the cosecant of the moon's distance from the sun or star, the sines of the two remainders, and the logarithm of the number from the table (I.) here given; the sum of these is the logarithm of the number of seconds to be always subtracted from the computed distance, while the number from the table itself is always to be added to it to give the true distance on

the hypothesis of the earth being a spheroid of $\frac{1}{300}$ of ellipticity.

| Ex. 1.—Latitude | 56° 12′ | 0" S. log. radius | . 9.99900 |
|---|--|--|---|
| Moon's alt. | | 0 secant | . 0.07190 |
| Hor. par. | 58 1 | 4 P. log. | . 0.49010 |
| and the second second | | make all more | |
| Par. in alt. | 49 2 | 8 P. L. | . 0.56100 |
| App. alt. of moon's cer | ntre | ment / m / m/ | 32° 15′ 35″ |
| Refraction . | T. Alle | | — 1 32 |
| Parallax in altitude | 11 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 | Name of Street, Street | + 49 28 |
| | | di modernite an | and the second second |
| Competed alakerda | | the same and table | 00 0.05 |
| Corrected altitude | 1000 | and the second section of the | 33 3 31 |
| | | And the State of Stat | |
| Observed distance | The state | one VI re- | 61 56 30 |
| Moon's aug. semidiame | eter | med full makes the said | + 16 1 |
| Correction for oblique | | | 0, |
| AE 74 (0) | | | |
| A | A SHOW MAN | Street Land | 61 10 01 |
| Apparent central dista | nce | | . 61 12 31 |
| tude and the moon's cusual, which, in this e which the corrections by the foregoing rule, | xample, w for the spl must be a | ill be found to b peroidal figure of | e 62° 26′ 17½″, to |
| Moon's polar dist. | 68° 59′ | Second to 1 and | AND TO TOUR DESIGNATION OF THE PARTY OF THE |
| Star's polar distance | 62 13 | 00000004 | 0.05000 |
| Apparent distance | 02 13 | cosecant | . 0.05320 |
| Sum . | 190 40 | const. log. | 0.30103 |
| THE PERSON NAMED IN | | FRANCISCO DESCRIPTION | THE RESIDENCE |
| Half . | 95 20 | THE PERSON NAMED IN | SOUTH PROPERTY. |
| First remainder | 26 21 | sine . | 9.64724 |
| Second remainder | 33 7 | sine . | 9.73747 |
| Number from Table I. | + 18".9 | log. | 1.27646 |
| The County and | - 10 .4 | log. | 1.01540 |
| and the same | | AND THE RESERVE | A Kennyalan |
| Sum - | + 8.5 o | r about 8½" to be | added. |
| Hence to 62° 26′ 17½″ is 92° 26′ 26″ | add $8\frac{1}{2}$ ", a | and the true dista | nce |

09 44' 15"

1 28 56

1h 29m 34s

P. L.

P L.

P. L.

0.60936

0.30621

0 30315

D. at 12h 63 10 41

15 61 41 45

| eyman tool (= 1) by I | 1 ¹ 12 | 29° | n' 34s |
|---------------------------------------|----------------------|---------|----------|
| Equation of sec. diff. | 13 | 29 | 34 11 |
| App. Greenwich time App. ship time | 13 7 | 29 1 | 23 6 |

Long. in time . 6 28 17 = 97° 4′ 15″ W.

The earth being a sphere, it is = 97 12 30

According to Lax's method = 97 13 30

So that the error on the spherical hypothesis, without allowing for the equation of second difference in three hours, is +8'15"

By Lax's method it is +9 15

Ex. 2.—On the 28th of August, 1823, on the east coast of Greenland, in latitude 74° 32′ 19″ N., longitude 18° 40′ W., Captain Sabine observed the distance of the sun and moon's limbs to be 100° 39′ 4″, the apparent altitude of the moon's centre 29° 54′ 48″, the sun's 19° 52′ 34″; the barometer 30.03; the thermometer 39°.4; and the apparent time at the place of observation 20^h 44^m 35s. Required the true longitude?

Calculating on the foregoing principles, Mr Henderson has found the apparent central distance to be 101° 15′ 5″, and the true distance came out to be 100° 47′ 25″

Captain Sabine makes it

The apparent time at Greenwich, corrected for the equation of second difference to the true distance 100° 47′ 25″ is 21h 59m 45s

Time at the place of observation,

20 44 35

If the true distance be calculated by diminishing the equatoreal horizontal parallax only, as directed by some authors, the true distance becomes 100° 47′ 29″, but allowing it to remain uncorrected for the latitude, the distance is 100° 47′ 24″. In general the correction of lunar distances for the earth's ellipticity, is small, seldom amounting to 10″ of distance or 5′ of longitude, in any case that can occur in practice; and in any place within the tropics, the results on the spherical hypothesis, may be considered almost perfectly correct.

On this subject Mr Henderson has remarked to me, that "the method prescribed by most authors, of allowing for the effects of the earth's spheroidal figure upon the lunar distances, by diminishing the equatoreal parallax, is not altogether exact, but leaves an error uncorrected, which, at its maximum under any particular latitude, is nearly one-sixtieth of the reduction of latitude, or angle of the vertical with the radius. The greatest error therefore which can possibly happen in any part of the globe, is under the parallel of 45°, where it may amount to 12". Under the equator and poles the error is nothing.

"If the equatoreal parallax be employed in the computation of the true distance; the result is liable to a greater error. The maximum error under any particular latitude, may be expressed by the hypothenuse of a right-angled plane triangle, in which one side is equal to the sixtieth part of the reduction of latitude, and the other to the correction of the equatorial parallax. Under the parallel of

London, the maximum error is 14".

When this work was nearly ready for publication, the author learned that Captain Kater, whose skill and experience as an able practical man command the utmost respect, was in the habit of using the direct method of obtaining the latitude by the pole star, as much shorter and simpler than by the use of tables, and upon application being made by a friend, who has interested himself in the success of this work, Captain Kater was so obliging as to forward to the author, the following example computed by the tables in this volume, which had been submitted to his inspection in their progress through the Captain Kater transmitted, at the same time, a small table containing the tangents and secants to every 10" of the polar distance of polaris, which will answer for some years to come, and will be found to save the computer some trouble.

The solution depends upon the following formulæ:-Tan. $u = \tan p \times \cos t$

Cos.
$$(\psi - u) = \frac{\cos u \times \cos z}{\cos p} = \cos u \times \cos z \times \sec p$$
. (B.)

"At York Gate, Regent's Park, London, on the 22d of February, 1826, at 7h 42m 49s, mean time, the altitude of the pole star was observed by Captain Kater to be 51° 58′ 11″; required the latitude?

First to find the mean solar time when the star was upon the meridian.

| *s App. R. A. O's R. A. at noon, | 0 ^h 58 ^m 15. ^s 2 App. alt. 51° 58′ 11″ 22 21 18.3 Refrac. — 45.4 |
|---|--|
| Difference from Table XXXI | 2 36 56.9 True alt. 51 57 25.6 - 25.7 z = 38 2 34.4 |
| Equation of time for noon, | 2 36 31.2 + 13 50.7 |
| * Upon the Meridian, . Time of Observation, . | 2 50 21.9 7 42 49.0 |
| Distance of Star from the Meridian in mean time, $p=1^{\circ}$ 36' 48". tan. $t=73$ 18 47. cos. | $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$ |
| u = 0 27 48.2 + tan | 7.907813 cosine 9.999986 8° 2′ 34.4″ cosine 9.896278 |
| $(\psi - u) = 38 0 58 \ .2$ | cosine . 9.896436 |
| ψ =38 28 46 .4 λ =51 31 13 .6 | |

⁺ Found by precept, page 10 of Explanation of the Tables."

Were the author permitted to add any thing to what Captain Kater approves, it would be to employ the constant log. 5.314425, the log. of an arc=R", Table LiXIII. and the sum of these logs, would be the log. u in seconds, which would save the trouble of finding the value of the log. tangent of small arcs.

To those not very familiar with such Computations it may be useful to show the Manner of Calculation.

As a rule in words at length might be serviceable in the solution of this problem, to those who are little conversant with formulæ, it has been added.

To the constant log. 5.314425, add the log. tangent of the star's polar distance p, and the log. cosine of the meridian distance t, in degrees, the sum of these will be the log. of the arc u in seconds. Now, to the log. secant p add the log. cosine u, and the cosine of the zenith distance s, the sum will be the cosine of $(\psi \pm u)$, an arc which, being increased or diminished by the arc u, will be the colatitude ψ , whence the latitude λ is readily obtained.

| وفعليم | Constant lo | garithm, | of the last | 5.314425 | Carpinal Control | Marine Sul |
|-------------------|---|----------------------------|-------------|------------------------|------------------|----------------------|
| 4.00 | $p = 1^{\circ} 36^{\circ}$ t = 73 18 | 48" tangent, 47 cosine, | | 8.449117 9.458097 | secant, | 0.000172 |
| | u= 0 27 | 48.2=1668".2 | - = ==38 | 3.222243 • 2' 34."4 | | 9.999986 9.896278 |
| (4 -1 | u)=38_0 & | 58.2 | 1672 14 | 10/0H 55 | cosine, | 9.896436 |
| λ | =38 28 4 =51 31 1 | | 41-2 | ***** | - | av lab |

In the application of u, attention must be paid to the sign of the arc t, according to its situation in the circle which the star describes round the pole, in its diurnal revolution. If t is in the first or fourth quadrant, it is additive; but if in the second or third, it is subtractive.

TABLE I.

Corrections for Mean Horizontal Parallax, to be added to the Lunar Distances on account of the Spheroidal Figure of the Earth, its Ellipticity being 300.

By MR HENDERSON.

| La t. | | Moon's Declination. | | | | | | | Moon's Declination. | | | | | | |
|----------|---------------|---------------------|------|------------|------------|------------|----------------|----------|---------------------|------|------|------|------|------|--------------|
| | ° 0 | 5 | 10 | 15 | 20 | 25 | 30 | | 0 | 5 | 10 | 15 | 20 | 25 | 30 |
| 00 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.4 | 00. | 469 | 16.4 | 163 | 16.1 | 15.8 | 15.4 | 14.0 | 14.9 |
| - 2 | 0.8 | | | | | 0.0 | | 48 | 16.9 | 16.9 | 16.7 | 16.4 | 15.9 | 15.4 | 14.7 |
| 4 | 1.6 | | | | | | 1.4 | 50 | | | | | | | 15.2 |
| 6 8 | 3.2 | | | 2.3 | 2.2 | | | 52 54 | | | | | | | 15.6 16.0 |
| 10 | 4.0 | | | | 3.7 | 3.6 | | 56 | | | | | | | 16.4 |
| 12 | 4.7 | 4.7 | | 4.6 | 4.4 | 4.3 | | 58 | | | | | 18.2 | | |
| 14 16 | 5.5 6.3 | | | | 5.2 5.9 | | | 60 | | | | | | | 17.1 17.5 |
| 18 | 7.0 | | | | | | | 64 | | | | | | | 17.8 |
| 20 | 7.8 | | | 7. | 7.3 | _ | 6.7 | 66 | | | - | | | | 18.1 |
| 22 | 8.5 | | | 8.2 | 8.0 | | 7.4 | 68 | | | | | | | 18.4 |
| 24 26 | $9.3 \\ 10.0$ | 0-10 | | 8.9 9.7 | 8.7 | 8.4 9.1 | 8.0 | 70 72 | | | | | | | 18.6 18.8 |
| 28 | 10.7 | 10.6 | 10.5 | 10.3 | 10.0 | 9.7 | 9.3 | 74 | 21.9 | 21.8 | 21.6 | 21.2 | 20.6 | 19.9 | 19.0 |
| 30 | 11.4 | - | | _ | | | | | - | | | | | | 19.2 |
| 32 34 | 12.1 | | | | | | $10.5 \\ 11.0$ | | | | | | | | 19.3 19.5 |
| 36 | | | | | | | 11.6 | | | | | | | | 19.5 |
| 38 | 14.0 | 14.0 | 13.8 | 13.6 | 13.2 | 12.7 | 12.2 | 84 | | | | | | | 19.6 |
| 40 | | | | | | | 12.7 | | | | | - | | _ | 19.7 |
| 42 | 15.8 | | | | | | 13.2 13.7 | 88 90 | | | | | | | 19.7 19.8 |
| | 12300 | 23.0 | 2500 | | 2 210 | | 20.11 | | - | | | | | | |

TABLE II.

For Finding the Latitude by the Pole Star.—By CAPTAIN KATER.

| Polar Distance. | Tangent. | + | Cosine Co. Ar. or Secant. | Polar Distance | Tangent- | P. P. + | Cosine Co. Ar. or Secant. |
|--------------------|----------|----------|---------------------------------|-------------------|----------|------------|---------------------------------|
| 10 33' 0" | 8.432315 | | 0.000159 | 1° 35′ 0″ | 8.441560 | | 0.000166 |
| 10 | 8.433093 | 1'' = 77 | 0.000159 | 10 | 8.442322 | 1'' = 75 | 0.000166 |
| 20 | 8.433870 | 2 = 154 | 0.000160 | 20 | 8.443082 | 2 = 151 | 0.000167 |
| 30 | 8.434645 | 3 = 231 | 0.000161 | 30 | 8.443841 | 2 = 226 | 0.000168 |
| 40 | 8.435419 | 4 = 308 | 0.000161 | 40 | 8.444599 | 4 = 302 | 0.000168 |
| 50 | 8.436191 | 5 = 385 | 0.000162 | 50 | 8.445355 | 5 = 377 | 0.000169 |
| 19 34 0" | 8.436962 | 6 = 462 | 0.000162 | 1° 36′ 0″ | 8.446110 | 6 = 453 | 0.000169 |
| 10 | 8.437732 | 7 = 539 | 0.000163 | 10 | 8.446864 | 7 = 528 | 0.000170 |
| 20 | 8.438500 | 8 = 616 | 0.000163 | 20 | 8.447616 | | 0.000170 |
| 30 | 8.439267 | 9 = 693 | 0.000164 | 30 | 8.448368 | 9 = 679 | 0.000171 |
| 40 | 8.440033 | | 0.000165 | 40 | 8.449117 | | 0.000172 |
| 50 | 8.440797 | | 0.000165 | 50 | 8.449866 | | 0.000172 |

ERRATA AND ADDITIONS.

INTRODUCTION.

Page

- 50 For H = 799.32 feet, read H = 801.16 feet. Defect, for 3.34 feet, read 1.50 feet.
- 53 Second line from the top, for his assistant, read an officer of the Griper who assisted him in making the observations.
- 84 For sum, read sun, in the fifth line from the top. For -3' 27".02, read -2' 27".02, in the third line from bottom.
- 85 For Dip section, read dip sector.
- 88 For 67° 12' 12", read 67° 18' 12", line 20.
- 102 Table IV. to var. 1° 38' and 2" of second difference, for 2.7, read 3.7.
- 116 For a Leonis, read A Leonis.
- 119 For z, from Parry's last Journal, I suspect n Geminorum must be read.
- 126 For sun's dec. 22° 35′ 40″, read 22° 35′ 45″, on account of having applied the equation of second difference with a wrong sign. Long. 9^m 55° W.
- 128 For 18° 1′ 0".0, read 18h 1m 0.0.
- 159 Ex. 2. Captain Hall reduced both his experiments to 68° F., and therefore my correction is erroneous; it may, however, serve as an example of the manner in which such a correction should be made.
- 160 For cos 2 L., read cos 2 L.

EXPLANATION.

- 17 Example for reduction of altitude is wrong, but may be easily corrected by the rule.
- 21 Line 11, for 4° 65' 14".4, read 4° 56' 14".4.
- 23 For 33° 15′ 0″.17, read 33° 16′ 0″.17, in 11th line from the bottom.
- 25 For 23° 28' 51".7, read 23° 18' 51".7.
 - In the tables not stereotyped there are two or three errors.

 1 Table XLIV., for R. A. Star—Lon, Moon's Node, read +
- Table XLIV., for R. A. Star—Lon. Moon's NodTable L., for Moon's true Long. read Sun's.
- 104 Declination Fomalhaut, for 30° 34' 24", read 30° 31' 54".
 - Appendix to Explanation of the Tables, page 39, line 3d from bottom, for 92° 26' 26", read 62° 26' 26".

MATHEMATICAL TABLES.

AND ANY OF A SHARLEST PARTY OF A SHARLEST PARTY AS

TABLE I.

THE MILES AND PARTS OF A MILE IN A DEGREE OF LONGITUDE AT EVERY DEGREE OF LATITUDE.

| D.L | Miles, | D.L. | Miles. |
|-----|--------|------|--------|------|--------|------|--------|------|--------|------|--------|
| 1 | 59.99 | 16 | 57.67 | 31 | 51.43 | 46 | 41.68 | 61 | 29.09 | 76 | 14.52 |
| 2 | 59.96 | 17 | 57.38 | 32 | 50.88 | 47 | 40.92 | 62 | 28.17 | 77 | 13.50 |
| 3 | 59.92 | 18 | 57.06 | 33 | 50.32 | 48 | 40.15 | 63 | 27.24 | 78 | 12.47 |
| 4 | 59.85 | 19 | 56.73 | 34 | 49.74 | 49 | 39.36 | 64 | 26.30 | 79 | 11.45 |
| 5 | 59.77 | 20 | 56.38 | 35 | 49.15 | 50 | 38.57 | 65 | 25.36 | 80 | 10.42 |
| 6 | 59.67 | 21 | 56.01 | 36 | 48.54 | 5l | 37.76 | 66 | 24.40 | 18 | 9.39 |
| 7 | 59.55 | 22 | 55.63 | 37 | 47.92 | 52 | 36.94 | 67 | 23.44 | 82 | 8.35 |
| 8 | 59.42 | 23 | 55.23 | 38 | 47.28 | 53 | 36.11 | 68 | 22.48 | 83 | 7.31 |
| 9 | 59.26 | 24 | 54.81 | 39 | 46.63 | 54 | 35.27 | 69 | 21.50 | 84 | 6.27 |
| 10 | 59.08 | 25 | 54.38 | 40 | 45.96 | 55 | 34.41 | 70 | 20.52 | 85 | 5.23 |
| 11 | 58.89 | 26 | 53.93 | 41 | 45.28 | 56 | 33.55 | 71 | 19.53 | 86 | 4.19 |
| 12 | 58.68 | 27 | 53.46 | 42 | 44.59 | 57 | 32.68 | 72 | 18.54 | 87 | 3.14 |
| 13 | 58.46 | 28 | 52.97 | 43 | 43.88 | 58 | 31.80 | 73 | 17.54 | 88 | 2.09 |
| 14 | 58.22 | 29 | 52.47 | 44 | 43.16 | 59 | 30.90 | 74 | 16.54 | 89 | 1.05 |
| 15 | 57.95 | 30 | 51.96 | 45 | 42.43 | 60 | 30.00 | 75 | 15.53 | 90 | 0.00 |

113

TABLE II.

LOGARITHMS OF NUMBERS.

| r | И. | No. 1- | | 100 | | Log. | 0.000 | 0002 | .00000 | 0 |
|----|-----|----------|-----|----------|-----|----------|-------|----------|--------|----------|
| 1 | No. | Log. | No. | Log. | No. | Log. | No. | Log. | No. | Log. |
| 1 | 1 | 0.000000 | 21 | 1.322219 | 41 | 1.612784 | 61 | 1.785330 | 81 | 1.908485 |
| П | 2 | 0.301030 | 22 | 1.342423 | 42 | 1.623249 | 62 | 1.792392 | 82 | 1.913814 |
| 1 | 3 | 0.477121 | 23 | 1.361728 | 43 | 1.633468 | 63 | 1.799341 | 83 | 1.919078 |
| н | 4 | 0.602060 | 24 | 1.380211 | 44 | 1.643453 | 64 | 1.806180 | 84 | 1.924279 |
| 1 | 5 | 0.698970 | 25 | 1.397940 | 45 | 1.653213 | 65 | 1.812913 | 85 | 1.929419 |
| | 6 | 0.778151 | 26 | 1.414973 | 46 | 1.662758 | 66 | 1.819544 | 86 | 1.934498 |
| н | 7 | 0.845098 | 27 | 1.431364 | 47 | 1.672098 | 67 | 1.826075 | 87 | 1.939519 |
| | 8 | 0.903090 | 28 | 1.447158 | 48 | 1.681241 | 68 | 1.832509 | 88 | 1.944483 |
| н | 9 | 0.954243 | 29 | 1.462398 | 49 | 1.690196 | 69 | 1.838849 | 89 | 1.949390 |
| 1 | 10 | 1.000000 | 30 | 1.477121 | 50 | 1.698970 | 70 | 1.845098 | 90 | 1.954243 |
| 1 | 11 | 1 041393 | 31 | 1.491362 | 51 | 1.707570 | 71 | 1.851258 | 91 | 1.959041 |
| Ŧ. | 12 | 1.079181 | 32 | 1.505150 | 52 | 1.716003 | 72 | 1.857332 | 92 | 1.963788 |
| 1 | 13 | 1.113943 | 33 | 1.518514 | 53 | 1.724276 | 73 | 1.863323 | 93 | 1.968483 |
| в | 14 | 1.146128 | 34 | 1.531479 | 54 | 1.732394 | 74 | 1.869232 | 94 | 1.973128 |
| н | 15 | 1.176091 | 35 | 1.544068 | 55 | 1.740363 | 75 | 1.875061 | 95 | 1.977724 |
| 1 | 16 | 1.204120 | 36 | 1.556303 | 56 | 1.748188 | 76 | 1.880814 | 96 | 1.982271 |
| ı | 17 | 1.230449 | 37 | 1.568202 | 57 | 1.755875 | 77 | 1.886491 | 97 | 1.986772 |
| - | 18 | 1.255273 | 38 | 1.579784 | 58 | 1.763428 | 78 | 1.892095 | 98 | 1.991226 |
| 1 | 19 | 1.278754 | 39 | 1.591065 | 59 | 1.770852 | 79 | 1.897627 | 99 | 1.995635 |
| L | 20 | 1.301030 | 40 | 1.602060 | 60 | 1.778151 | 80 | 1.903090 | 100 | 2.000000 |

| 192 | | | | A Table | of Log | garithm | s of Nu | mbers | from 1 | to 100, | 000. | | |
|--|-----|-----|--------|---------|--------|---------|---------|--------|-------------------------|---------|--------|--------------|-----|
| 14 | . 1 | N. | 0 | 1 | 2 | 3 . | 4 | 5 | 6 | 7 | 8 | 9 | D. |
| 182 | 11 | 00 | | | | | | | | | | | |
| 124 3 012837 013239 013600 014100 4521 4940 5366 5779 6197 6197 62036 0203 | | - | | 1 | | | | | | | | | |
| 166 | | | | | | | | | | | | | |
| Solidador Soli | | | | | | | | | | | | | |
| 247 6 5306 5715 6125 6533 6942 73.00 77.57 8164 8.571 8.28 8.79 894 9789 030195 03060 031040 031408 031819 032216 032819 0333 030 303424 033826 4227 4628 5029 5430 5380 6230 6629 77.00 14.00 1 | | | | | | | | | | | | | |
| 288 | | | | | | | | | | | | | |
| South Sout | | | | | | | | | | | | | |
| 10 9 1426 7825 8228 8620 9017 9414 9811 040207 040602 04050 04185 04187 042170 042969 043362 043755 044148 04448 04448 04451 044 | | | | | | | | | | | | | |
| 110 | | - 1 | | | | | 1 | 3 | | | | | |
| Section Sect | 1 | - | | | | | | | Complete on the last of | - | - | | |
| Total | 1. | - 1 | | | | | | | | | | | |
| 113 | | | | | | | | | | | | | |
| 150 | | | | | | | | | | | | | |
| 188 | | | | | | 1 | | | | | 1 | 1 | |
| 226 6 4 4456 4832 5206 5580 5958 6326 6699 7071 7443 77 263 7 8186 8557 8928 9298 9668 070038 070407 070776 071145 0715 301 8071882 072250 072617 072985 073352 3718 4085 4451 4816 51 338 9 5547 5912 6676 6640 7004 7368 7731 8094 8457 88 35 1082785 08314 083503 3661 4129 4576 4934 5221 5647 66 32 6360 6716 7071 7426 7781 8136 8490 8845 9198 95 104 3 9905 090286 090611 090963 091315 091667 092018 092370 092721 0936 38 4 093422 3772 4122 4471 4820 5169 5518 5666 6215 65 173 5 6910 7257 7604 7951 8298 8644 8990 9335 9681 1000 38 6 100371 100715 101059 101403 101747 102091 102434 102777 103119 34 24 7 3804 4146 4487 4828 5169 5510 5851 6191 6531 68 277 8 7210 7549 7888 8227 8565 8903 9241 9579 9916 1102 311 9 110590 110926 111263 111599 111934 112270 112605 112940 113275 36 64 2 120574 120903 121231 121360 121888 122216 122544 122871 123198 35 96 3 3852 4178 4504 4830 5166 7481 5500 51224 12231 121360 121888 122216 122544 122871 123198 35 96 3 3852 4178 4504 4830 5166 7481 5500 513250 132900 32 1 7 771 7603 7934 8265 8595 8926 9256 9586 9915 1202 257 6721 7037 7354 7671 7987 8303 8618 8934 9249 95 99 143015 3327 8339 3951 44054 4115078 115013 11594 112319 31393 132260 132580 132900 32 1 9 219 9527 9835 150142 150449 150756 151063 151370 151676 1519 60 2 152288 152594 152900 3205 3510 3815 4120 4424 4728 509 9136 1606 1940 15086 161667 161967 162266 162266 162264 162863 3161 3460 3756 400 99 3186 3478 3769 8989 8990 1800 3153 6640 8945 8965 9266 9567 9868 161068 160469 160769 1610 49 516186 161667 161967 162266 162266 162564 162863 3161 3460 3756 400 99 3186 3478 3769 8989 8980 9990 9980 9980 9980 9980 99 | | 5 | 060698 | | | | | | | 063333 | 063709 | 4083 | 376 |
| Solid Soli | | | | | | | | | | | | | |
| 138 | | 7 | 8186 | 8557 | 8928 | 9298 | 9668 | 070038 | 070407 | 070776 | 071145 | 071514 | 370 |
| 120 079181 079543 079904 080266 080626 080987 081347 081707 082067 08248 1082785 083144 083503 3861 4219 4576 4934 5291 5647 6699 2 6360 6716 7071 7426 7781 8136 8490 8845 9198 953 9905 9909288 099611 090963 091315 091667 092018 092370 092371 09308 10342 3772 4122 4471 4820 5169 5518 5866 6215 6518 5660 6215 6782 | | 8 | 071882 | 072250 | 072617 | 072985 | 073352 | 3718 | 4085 | 4451 | 4816 | 5182 | 366 |
| 35 | | 9 | 5547 | 5912 | 6276 | 6640 | 7004 | 7368 | 7731 | 8094 | 8457 | 8819 | 363 |
| Color | 12 | 50 | 079181 | 079543 | 079904 | 080266 | 080626 | 080987 | 081347 | 081707 | 082067 | 082426 | 360 |
| 104 | | 1 | 082785 | 083144 | 083503 | | | | | | | 6004 | 357 |
| 138 | | 2 | 6360 | 6716 | | | | | | | | | |
| 173 | | 3 | 9905 | 090258 | 090611 | 090963 | 091315 | 091667 | 092018 | 092370 | | 093071 | 352 |
| 208 6 100371 100715 101059 101403 101747 102091 102434 102777 103119 34 242 7 3804 4146 4487 7888 5169 5510 5851 691 6531 68 277 8 7210 7549 7888 8227 8565 8903 9241 9579 9916 1102 311 9110590 110926 111263 111599 111934 112270 112605 112940 113275 3661 21834 12231 121560 121888 122216 122544 122971 123198 35 128 4 7105 7429 7753 8076 8399 8729 9045 9368 9690 13090 193 6 3539 3858 4177 4496 4814 5133 5461 5769 6986 645 257 8 9579 140194 140508 140622 | | | | | 4122 | 4471 | | | | | | 6562 | |
| 242 7 3804 4146 4487 4828 5169 5510 5851 6191 6531 68 277 8 7210 7549 7888 8227 8565 8903 9241 9579 99161 11023 311 910590 110926 111263 111599 1112940 113275 36 130 113943 114277 114611 114944 115278 115611 115943 116276 116608 1169 64 2 120574 120903 121231 121560 121888 122216 122541 122871 123198 35 166 3 3852 4178 4504 4830 5156 5481 5806 6131 6456 67 160 5 130334 130655 130977 131298 131619 131939 132280 13280 13280 132900 32 193 6 3539 3858 4177 4496 4814 5133 5451 | | | | | | | | | | | | | |
| 105 | | | | | | | | | | | | 3462 | |
| 131 9 110590 110926 111263 111599 111934 112270 112605 112940 113275 36 113943 114277 114611 114944 115278 115611 115943 116276 116608 1169 | | | | | | | | | | | | 6871 | |
| 130 | | | | | | | | | | | | | |
| 32 1 7271 7603 7934 8265 8595 8926 9256 9586 9915 1202 120274 120903 121231 121560 121888 122216 122544 122571 123198 35 128 4 7105 7429 7753 8076 8399 8722 9045 9368 9690 130 160 5 130334 130655 130977 131298 131619 131939 132260 132580 132900 32 193 6 3539 3858 4177 74496 4814 5133 5461 5769 6086 64 257 8 9879 140194 140508 140822 141136 141450 147076 14785 5196 5507 58 30 1 9219 9527 9835 150142 150449 150756 151063 151370 151676 1519 30 1 9219 | - | | | - | | | | | | | | 3609 | - |
| 64 2 120574 120903 121231 121560 121888 122216 122544 122871 123198 35 96 3 3852 4178 4504 4830 5156 5481 5806 6131 6456 67 160 5 130334 130655 130977 131298 131619 131939 132580 132800 132800 132800 132800 132800 132800 132800 132800 132800 132800 132800 132800 132800 132800 132800 32080 32900 32800 32949 95 32949 95 4263 4814 5133 5451 5769 6086 64 64 881427 7671 7987 8303 8618 8934 9249 95 27 9835 140822 141136 141405 141763 142076 142389 14276 142389 14276 142894 148003 1489 142076 142889 14276 <td></td> | | | | | | | | | | | | | |
| 96 3 3852 4178 4504 4830 5156 5481 5806 6131 6456 67 128 4 7105 7429 7753 8076 8399 8722 9045 3368 9690 18300 193 6 3539 3858 4177 4496 4814 5133 5451 5769 6086 64 225 7 6721 7037 7354 7671 7987 8303 8618 9934 9249 95 257 8 9879 140194 140508 140822 14136 141450 141763 142076 142889 1427 289 9 143015 3327 3639 3951 4263 4574 4885 5196 5507 86 140 146128 146438 146748 147058 147367 147676 147985 148294 148003 1449 30 1 9219 9527 9835 150142 150449 150756 151063 151370 151676 1519 60 2 152288 152594 152990 3205 3510 3815 4120 4424 4728 50 3 3 5336 5640 5943 6246 6549 6852 7154 7457 7759 80 120 4 8362 8664 8965 9266 9567 9868 160168 160469 160769 1610 149 5 161368 161667 161967 162266 162564 162863 3161 3460 3758 40 179 6 4353 4650 4947 5244 5541 5838 6134 6430 6726 70 239 8 170262 170555 170848 171141 171434 171726 172019 172311 172603 1728 289 9 3186 3478 3769 4060 4351 4641 4932 5222 5512 58 1 8 8977 9264 9552 9839 180126 180413 180699 180986 181272 1815 28 1 18044 182129 182415 182700 2985 3270 3555 3839 18026 72 112 4 7521 7803 8084 8366 8647 8928 9209 9490 9771 1900 139 5 190332 190612 190892 191171 191451 191730 192010 192289 192567 28 18657 8932 9206 9481 9755 200029 200303 200577 200850 20115 2231 9201397 201670 201943 202216 202488 2761 3033 3305 3577 38 | | | | | | | | | | | | | |
| 128 4 7105 7429 7753 8076 8399 8722 9045 9368 9690 1300 160 5 130334 130655 130977 131298 131619 131999 132260 132500 32 225 7 6721 7037 7354 7671 7987 8303 8618 8934 9249 95 257 8 9879 140194 140508 140822 141136 141450 141763 142076 142389 1427 289 9 143015 3327 3639 3951 4263 4574 4885 5196 5507 58 30 1 9219 9527 9835 150142 150449 150756 151063 151370 167676 1676 60 2152288 152594 152900 3205 3510 3815 4120 4424 4728 50 966 9567 9868 160168 160469 | | | | | | | | | | | | 3525 | |
| 193 3838 130655 130977 131298 131619 131939 132260 132580 132900 32 193 6 3539 3858 4177 4496 4814 5133 5461 5769 6086 64 257 76721 7037 7354 7671 7987 8303 8618 8934 9249 95 257 8 9979 140194 140508 140822 141136 141450 141763 142076 142389 1427 289 9 143015 3327 3639 3951 4263 4574 4885 5196 5507 58 140 146128 146438 146748 147058 147367 147676 147985 148294 148003 1489 30 1 9219 9527 9835 150142 150449 150756 151063 151370 151676 1519 90 3 5336 5640 5943 6246 6549 6852 7154 74478 50 140 4 8362 8664 8965 9266 9567 9868 160168 160469 160769 1610 149 5 161366 161667 161967 162266 162564 162863 3161 3460 3758 40 179 6 4353 4650 4947 5244 5541 5838 6134 6430 67726 70 209 7 7317 7613 7908 8203 8497 8792 9086 9380 9674 99 239 8 170262 170555 170848 171141 171434 171726 172019 172311 172603 1728 28 9 3186 3478 3769 4060 4351 4641 4932 5222 5512 58 150 176091 176381 176670 176959 177248 177558 177825 178113 178401 1786 28 1 8977 9264 9552 9839 180166 180413 180699 180986 18127 1815 56 2 181844 182129 182415 182700 2985 3270 3555 3839 4123 44 84 3 4691 4975 5259 5542 5825 6108 6391 6674 6956 72 112 4 7521 7803 8084 8366 8647 8928 9209 9490 9771 1900 139 5 190332 190612 190892 191171 19145 191730 192010 192289 19567 28 8 8 8657 8932 9206 9481 9755 200029 200303 200577 200850 2011 223 8 8657 8932 9206 9481 9755 200029 200303 200577 200850 2011 251 9 201397 201670 201943 202216 202488 2761 3033 3305 3577 38 | | | | | | | | | | | | 6781 | |
| 193 6 3539 3858 4177 74496 4814 5133 5451 5769 6086 64 225 7 6721 7037 7354 7671 7987 8303 8618 8934 9249 95 289 9143015 3327 3639 3951 4263 4574 4885 5196 5507 58 30 1 9219 9527 9835 150142 150449 150756 151063 151370 151676 1519 30 1 9219 9527 9835 150142 150449 150756 151063 151370 151676 1519 60 2 152288 152594 152900 3205 3510 3815 4120 4424 4728 50 120 4 8362 8664 8965 9266 9567 9868 160168 160469 160769 1610 149 5 161368 | | | | | | | | | | | | | |
| 225 7 6721 7037 7354 7671 7987 8303 8618 8934 9249 95 289 9 143015 3327 3639 3951 4263 4574 4885 5196 5507 58 30 1 9219 9527 9835 140768 147058 147367 147676 147985 148294 148003 1489 30 1 9219 9527 9835 150142 150494 150766 151063 151370 151676 15196 60 2 152288 152594 152900 3205 3510 3815 4120 4424 4728 50 90 3 5336 5640 5945 6246 6549 6852 7154 7457 7759 80 120 4 8362 8664 8965 9266 9567 9868 160469 160769 167667 161967 162266 162564 162863 36161 3460 3758 <td< td=""><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td>3219 6403</td><td></td></td<> | | | | | | | | | | | | 3219 6403 | |
| 257 8 9879 140194 140508 140822 141136 141450 141763 142076 142389 1427 289 9 143015 3327 3639 3951 4263 4574 4885 5196 5507 58 140 146128 146438 146708 147058 147367 147676 147955 148294 148003 1489 30 1 9219 9527 9835 150142 150746 150756 151063 151370 151676 15196 60 2 152298 152990 3205 3510 3815 4120 4424 4728 50 90 3 5336 5640 5943 6246 6549 6852 7154 7457 7759 80 120 4 8362 8664 8965 9266 9567 9868 160168 160469 160769 16162266 162863 162863 3161 3460 </td <td></td> <td>9564</td> <td></td> | | | | | | | | | | | | 9564 | |
| 289 9 143015 3327 3639 3951 4263 4574 4885 5196 5507 58 30 1 9219 9527 9835 150142 150449 150756 151663 151370 151676 15199 90 3 5336 5640 5943 6246 6549 6852 7154 4478 50 120 4 8362 8664 8965 9266 9567 9868 160168 160469 160769 161049 149 5 161368 1616671 161967 162266 162564 162863 3161 3460 3758 40 179 6 4353 4650 4947 5244 5541 5838 6134 6430 3758 40 209 7 7317 7613 7908 8203 8497 8709 9086 9380 9674 99 239 8 170262 170555 < | | | | | | | | | | | | | |
| 140 | | - 1 | | | | | | | | | | 5818 | |
| 30 1 9219 9527 9835 150142 150449 150756 151063 151370 151676 1519 60 2 152288 152594 152900 3205 3510 3815 4120 4424 4728 50 120 4 8362 8664 8965 9266 9567 9868 16068 160469 160769 1611967 149 5 161368 161667 161967 162266 162564 162863 3161 3460 3758 40 179 6 4353 4650 4947 5244 5541 5838 6134 6430 3758 40 209 7 7317 7613 7908 8203 8497 8792 9086 9380 9674 99 239 8 170262 170555 170848 171141 17134 1717261 172311 172603 17281 269 3 186 3478 <t< td=""><td>_</td><td>-</td><td></td><td>-</td><td></td><td></td><td></td><td>-</td><td></td><td></td><td>-</td><td></td><td></td></t<> | _ | - | | - | | | | - | | | - | | |
| 66 2 152288 152594 152900 3205 3510 3815 4120 4424 4728 50 90 3 5336 5640 5943 6246 6549 6852 7154 7457 7759 80 120 4 8362 8664 8965 9266 9567 9868 160168 160469 160769 161049 161368 1616671 161967 162266 162564 162863 3161 3460 3758 40 179 6 4353 4650 4947 5244 5541 5838 6134 6430 6726 70 299 7 7317 7613 7908 8203 8497 8792 9086 9380 9674 99 9669 9380 9674 99 9669 9389 18014 1712019 172311 172603 1728 172019 172311 172603 1728 269 3186 3478 3769< | | - 1 | | | | | | | | | | | |
| 90 | | | | | | | | | | | | 5032 | |
| 120 | | | | | | | | | | | | 8061 | |
| 149 5 161368 161667 161967 162266 162264 162863 3161 3460 3758 40 179 6 4353 4650 4947 5244 5541 5838 6134 6430 6726 70 209 7 7317 7613 7908 8203 8497 8792 9086 9380 9674 99 239 8170262 170555 170848 171141 171344 171726 172019 172311 172603 17281 269 9 3186 3478 3769 4060 4351 4641 4932 5222 5512 58 150 176091 176381 176670 176959 177248 177536 177825 178113 178401 1786 28 J 8977 9264 9552 9839 180126 180413 180699 180986 181272 1812 44 4461 4975 5259 | | - 1 | | | | | | | | | | | |
| $\begin{array}{cccccccccccccccccccccccccccccccccccc$ | | | | | | | | | | | | 4055 | |
| 209 7 7317 7613 7908 8203 8497 8792 9086 9380 9674 99 239 8 170262 170555 170848 171141 1711434 171726 172019 172311 172603 1728 269 9 3186 3478 3769 4600 4351 4641 4932 5222 5512 58 150 176091 176381 176670 176959 177248 177536 177825 178113 178411 1786 56 2 181844 182129 182415 182700 2985 3270 3555 3839 4123 44 84 3 4691 4975 5259 5542 5825 6108 6391 6674 6956 72 112 4 7521 7803 8084 8366 8647 8928 9209 9490 9771 1906 139 5 190332 190612 | | | | | | | | | | | | 7022 | |
| 239 8 170262 170555 170848 171141 171434 171726 172019 172311 172603 17282 269 9 3186 3478 3769 4060 4351 4641 4932 5222 5512 58 1 150 176091 176691 1767959 177248 177536 177825 178113 174741 180699 180986 181272 1815 56 2181844 182129 182415 182700 2985 3270 3555 3839 4123 44 43 4691 4975 5259 5542 5825 6108 6391 6674 6956 72 112 47521 7803 8084 8366 8647 8928 9209 9490 9771 1900 19289 192567 28 19171 191451 191730 192010 192899 192567 28 19267 28 4514 4792 5669 5346 56 56 | | 7 | 7317 | 7613 | 7908 | | | | | 9380 | 9674 | 9968 | |
| 150 176091 176381 176670 176959 177248 177536 177825 178113 178401 17865 18977 9264 9552 9839 180126 180413 180699 180986 181272 1815 18144 182129 182415 182700 2985 3270 3555 3839 4123 44 3 4691 4975 5259 5542 5825 6108 6391 6674 6956 72 17803 190612 190892 191171 191451 191730 192010 192289 192567 28 167 6 3125 3403 3681 3959 4237 4514 4792 5069 5346 56 195 7 5900 6176 6453 6729 7005 7281 7556 7832 8107 83 223 8 8657 8932 9206 9481 9755 200029 200303 200577 200850 2011 251 9 201397 201670 201943 202216 202488 2761 3033 3305 3577 38 3577 38 3889 3889 3889 4123 44 4752 | | 8 | 170262 | | | | 171434 | 171726 | 172019 | 172311 | 172603 | 172895 | 293 |
| 28 J 8977 9964 9552 9839 180126 180413 180699 180986 181272 1815 56 2 181844 182129 182415 182700 2985 3270 3555 3839 4123 44 34 4691 4975 5259 5542 5825 6108 6391 6674 6956 72 112 4 7521 7803 8084 8366 8647 8928 9209 9490 9771 1900 1900 19171 191451 191730 192010 192289 192567 28 167 6 3125 3403 3681 3959 4237 4514 4792 5069 5346 56 195 7 5900 6176 6453 6729 7005 7281 7556 7832 8107 83 223 8 8657 8932 9206 9481 9755 200029 200303 200577 200850 2011 2 | | 9 | 3186 | 3478 | 3769 | 4060 | 4351 | 4641 | 4932 | 5222 | 5512 | 5802 | 291 |
| 28 J 8977 9264 9552 9839 180126 180413 180699 180986 181272 1815 56 2181844 182129 182415 182700 2985 3270 3555 3839 4123 44 84 3 4691 4975 5259 5542 5825 6108 6391 6674 6956 72 112 4 7521 7803 8084 8366 8647 8928 9209 9490 9771 1900 139 5 190332 190612 190892 191171 191451 191730 192010 192289 192567 28 167 6 3125 3403 3681 3959 4237 4514 4792 5069 5346 56 195 7 5900 6176 6453 6729 7005 7281 7556 7832 8107 83 223 8 8657 8932 | 15 | 0 | 176091 | 176381 | 176670 | 176959 | 177248 | 177536 | 177825 | 178113 | 178401 | 178689 | 289 |
| $\begin{array}{cccccccccccccccccccccccccccccccccccc$ | | | | 9264 | 9552 | 9839 | 180126 | 180413 | 180699 | 180986 | 181272 | 181558 | |
| $\begin{array}{cccccccccccccccccccccccccccccccccccc$ | | 2 | 181844 | 182129 | 182415 | 182700 | 2985 | 3270 | 3555 | | 4123 | 4407 | 285 |
| $\begin{array}{cccccccccccccccccccccccccccccccccccc$ | | | 4691 | | | 5542 | | | | 6674 | | | |
| $\begin{array}{cccccccccccccccccccccccccccccccccccc$ | | -1 | | | | | | | | | | | |
| 195 7 5900 6176 6453 6729 7005 7281 7556 7832 8107 83 223 8 8657 8932 9206 9481 9755 200029 200303 200577 200850 2011 251 9 201397 201670 201943 202216 202488 2761 3033 3305 3577 38 | | | | | | | | | 192010 | | | 2846 | |
| 223 8 8657 8932 9206 9481 9755 200029 200303 200577 200850 2011 251 9 201397 201670 201943 202216 202488 2761 3033 3305 3577 38 | | | | | | | | | | | | 5623 | |
| 251 9 201397 201670 201943 202216 202488 2761 3033 3305 3577 38 | | | | | | | | | | | | 8382 | |
| | | | | | | | | | | | | | |
| | - | 9 | 201397 | 201670 | 201943 | 202216 | 202488 | 2761 | 3033 | 3305 | 3577 | 3848 | 272 |
| P. P. N. 0 1 2 3 4 5 6 7 8 9 | N | 1. | 0 | 1 | 2 | 3 | 4 | 5 . | 6 | 7 | 8 | 9 | D. |

| | | A | Table | of Loga | rithms | of Nu | mbers f | rom 1 t | o 100,0 | 00. | | 3 |
|------------|------|----------------|----------------|----------------|--------------|----------------|--------------|----------------|--------------|----------------|------------------|------------|
| P. P | . N. | 0 | 1 | 2 | 3 | 4 | 5 . | 6 | 7 | 8 | 9 | D. |
| 11 | 160 | 204120 | | | 204934 | | | 205746 | | | | 271 |
| 26 | 1 | 6826 | 7096 | 7365 | 7634 | 7904 | 8173 | | 8710 | 8979 211654 | 9247 | 269 267 |
| 52 79 | 2 | | 212454 | 210051 2720 | 210319 | 210586 3252 | 3518 | 211121 3783 | 4049 | 4314 | 1 - | |
| 105 | | | 5109 | 5373 | 5638 | 5902 | 6166 | 6430 | 6694 | 6957 | 7221 | |
| 131 | 5 | | 7747 | 8010 | 8273 | 8536 | 8798 | 9060 | 9323 | 9585 | 9846 | |
| 157 | 6 | | 220370 | | | | | 221675 | | | | |
| 183 209 | 8 | | 2976 5568 | 3236 5826 | 3496 6084 | 3755 6342 | 4015 6600 | | 4533 7115 | 4792 7372 | 5051 7630 | |
| 236 | 9 | | 8144 | 8400 | 8657 | 8913 | 9170 | | 9682 | | 230193 | |
| | 170 | 230449 | 230704 | | 231215 | 231470 | 231724 | 231979 | 232234 | 232488 | 232742 | 254 |
| 25 | 1 | | 3250 | 3504 | 3757 | 4011 | 4264 | | 4770 | 5023 | | |
| 50 | 2 | 1 | | 6033 | 6285 | 6537 | 6789 | | 7292 | 7544 | | |
| 74 99 | 3 | | 8297 240799 | 8548 | 8799 | 9049 | 9299 | | | 2541 | 240300 2790 | |
| 124 | 1 | | | 3534 | 3782 | 4030 | 4277 | | | 5019 | | |
| 149 | 6 | | | 6006 | 6252 | 6499 | | | 7237 | 7482 | | |
| 174 | | | | 8464 | 8709 | 8954 | 9198 | | 9687 | | 250176 | |
| 198 | 9 | 1 | 250664 | | 251151 | | | 251881 | | 252368 | | |
| 223 | 180 | | 3096 | 3338 255755 | 3580 | 3822 256237 | 4064 | 4306 256718 | 4548 | 4790 | - | - |
| 23 | | 7679 | 255514 7918 | 8158 | 8398 | 8637 | 8877 | 9116 | | 9594 | 257439 9833 | |
| 47 | | | 260310 | | | | | | | | | |
| 70 | 3 | | 2688 | | 3162 | 3399 | | | | 4346 | | |
| 94 | | 1 | 5054 | 5290 | 5525 | 5761 | 5996 | | 6467 | 6702 | | |
| 117 | 5 | | | | 7875 | 8110 | 8344 | | 8812 | 9046 | | |
| 140 164 | | | 9746 272074 | | 2538 | 270146 | 3001 | 270912 3233 | | 3696 | | |
| 187 | | | | 4620 | | | 5311 | 5542 | 5772 | 6002 | | |
| 211 | 9 | | - | | 7151 | 7380 | 7609 | | 8067 | 8296 | | |
| 10 | 190 | 278754 | 278982 | 279211 | 279439 | 279667 | 279895 | 280123 | 280351 | 280578 | 280806 | 228 |
| 22 | | | 281261 | | | | | | 2622 | 2849 | | |
| 44 | | 1 | 3527 | 3753 | | | | | | 5107 | | |
| 67 89 | 1 | | 5782 8026 | | 6232 8473 | 6456 8696 | 6681 8920 | 6905 9143 | | 7354 9589 | | |
| 111 | 1 3 | | 290257 | | | | | 291369 | | | 292034 | |
| 133 | | 2256 | | | 2920 | 3141 | 3363 | | | 4025 | 4.246 | 221 |
| 155 | | 1 | 1 | 4907 | 5127 | 5347 | 5567 | | 6007 | 6226 | | |
| 178 200 | 8 | | 1 | | 7323 | 7542 | 7761 | 7979 | 8198 | 8416 | 1 | |
| 200 | _ | | 1 | 9289 | 9507 | 9725 | | 300161 | | | 300813 302980 | |
| 21 | 200 | 301030 3196 | 3412 | | | | | | 302547 | 4921 | 5136 | |
| 42 | | | 5566 | | 5996 | 6211 | 6425 | | | 7068 | | |
| 63 | | | 7710 | 7924 | 8137 | 8351 | 8564 | 8778 | 8991 | 9204 | 9417 | 213 |
| 84 | | | | 310056 | | | | | | | | |
| 105 127 | | | 311966 | | 2389 | | | | | | | |
| 148 | | | 1 | | | 4710 6809 | | | 5340 7436 | 5551 7646 | 5760 7854 | |
| 169 | | | 1 | | 8689 | 8898 | 9106 | | | 9730 | | 1000 |
| 190 | | 320146 | | | | | | 321391 | | | | |
| | | 322219 | | | 322839 | 323046 | 323252 | 323458 | | | 324077 | 206 |
| 20 | | | | | | | | | | | | |
| 40 61 | | | | | 1 | | | | 7767 | | | |
| 81 | 1 | 8380 330414 | 8583 330617 | 8787 330819 | 8991 | 9194 | 9398 | 9601 | 331839 | 2034 | 330211 2236 | |
| 101 | 1 2 | | 2640 | | | | | | | | 4253 | |
| 121 | 1 | 4454 | 4655 | 4856 | | | | | 5859 | 6059 | | |
| 141 | | 0 = 0 0 | | | | | | | | | | |
| 162 182 | | 8456 340444 | 8656 | 8855 | 9054 | 9253 | 9451 | 9650 | 9849 | | 310246 | |
| - | | | | | | | | | | 2028 | 2225 | |
| P. P | . N. | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 . | D. |

| 4 | | I | A Table | of Log | arithms | of Nu | mbers f | rom 1 t | o 100,0 | 00. | | |
|-------------|-----|--------------|--------------|--------|---------|--------|---------|---------|--------------|--------------|---------------------|-----|
| P. P. | N. | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | D. |
| | | 342423 | | 342817 | | 343212 | | | | | 344196 | 197 |
| 19 | 1 | 4392 | 4589 | 4785 | 4981 | 5178 | 5374 | | 5766 | 5962 | 6157 | |
| 39 | 2 | 6353 | 6549 | 6744 | 6939 | 7135 | 7330 | | 7720 | 7915 | 8110 | |
| 58 | 3 | 8305 | 8500 | 8694 | 8889 | 9083 | 9278 | 9472 | 9666 | 9860 | 350054 | |
| 77 | 5 | | 350442 | 2568 | 2761 | 2954 | 3147 | 3339 | | | 1989 | |
| 96 116 | 6 | 2183 | 2375 | 4493 | 4685 | 4876 | 5068 | | 3532 5452 | 3724 5643 | 3916 5834 | |
| 135 | 7 | 4108 6026 | 4301 6217 | 6408 | 6599 | 6790 | 6981 | 7172 | 7363 | 7554 | 7744 | |
| 154 | 8 | 7935 | 8125 | 8316 | 8506 | 8696 | 8886 | 9076 | 9266 | 9456 | 9646 | |
| 174 | 9 | | 360025 | | | | | 360972 | | | 361539 | |
| | | | 361917 | | | 362482 | | 362859 | | | | 188 |
| 18 | 1 | 3612 | 3800 | 3988 | 4176 | 4363 | 4551 | 4739 | 4926 | 5113 | 5301 | |
| 37 | 2 | 5488 | 5675 | 5862 | 6049 | 6236 | 6423 | | 6796 | 6983 | 7169 | 1 |
| 55 | 3 | 7356 | 7542 | 7729 | 7915 | 8101 | 8287 | 8473 | 8659 | 8845 | 9030 | |
| 74 | 4 | 9216 | 9401 | 9587 | 9772 | 9958 | | | 370513 | | 370883 | |
| 92 | 5 | | 371253 | 371437 | | | 1991 | 2175 | 2360 | 2544 | | |
| 110 | 6 | 2912 | 3096 | 3280 | 3464 | 3647 | 3831 | 4015 | 4198 | | 4565 | |
| 129 | 7 | 4748 | 4932 | 5115 | 5298 | 5481 | 5664 | 5846 | 6029 | 6212 | 6394 | |
| 147 | 8 | 6577 | 6759 | 6942 | 7124 | 7306 | 7488 | | 7852 | 8034 | | |
| 166 | 9 | 8398 | 8580 | 8761 | 8943 | 9124 | | | 9668 | | 380030 | |
| | 240 | 380211 | 380392 | 380573 | 380754 | 380934 | 381115 | 381296 | 381476 | 381656 | 381537 | 181 |
| 18 | 1 | 2017 | 2197 | 2377 | 2557 | 2737 | 2917 | | 3277 | 3456 | 3636 | |
| 35 | 2 | 3815 | 3995 | 4174 | 4353 | 4533 | 4712 | 4891 | 5070 | 5249 | 5428 | 179 |
| 53 | 3 | 5606 | 5785 | 5964 | 6142 | 6321 | 6499 | 6677 | 6856 | 7034 | 7212 | 178 |
| 71 | 4 | 7390 | 7568 | 7746 | 7924 | 8101 | 8279 | | | 8811 | 8989 | |
| 88 | 5 | 9166 | 9343 | 9520 | 9698 | | 390051 | | | | 390759 | 177 |
| 106 | | | 391112 | | | | 1817 | | | | 2521 | |
| 124 | 7 | 2697 | 2873 | 3048 | 3224 | 3400 | | | 3926 | | 4277 | 1 |
| 142 | 8 | 4452 | 4627 | 4802 | 4977 | 5152 | 5326 | | 5676 | | | |
| 159 | 9 | 6199 | 6374 | 6548 | 6722 | 6896 | 7071 | 7245 | 7419 | | | 174 |
| | 250 | | 398114 | | | | | 398981 | | | | 173 |
| 17 | 1 | 9674 | | | | | | | | | 401228 | |
| 34 | | | 401573 | 1745 | 1917 | 2089 | 2261 | 2433 | | | 2949 | |
| 51 | 3 | 3121 | 3892 | 3464 | 3635 | 3807 | 3978 | | | | | |
| 68 | 4 | 4834 | 5005 | 5176 | 5346 | 5517 | 5688 | | 6029 | | | |
| 85 | 5 | 6540 | 6710 | 6881 | 7051 | 7221 | 7391 | 7561 | 7731 | 7901 | 8070 | |
| 102 119 | 7 | 8240 | 8410 | 8579 | 8749 | 8918 | | 9257 | . 9426 | 9595 | | |
| 136 | | 411620 | 1788 | 1956 | 2124 | 2293 | | 2629 | 2796 | | 411451 | |
| 153 | 9 | 3300 | 3467 | 3635 | 3803 | 3970 | 4137 | 4305 | 4472 | 2964 4639 | | |
| - | | | | | | - | | | | | 4806 | |
| | | | | | | | | | | | 416474 | |
| 16 33 | 2 | 6641 | 6807 | 6973 | 7139 | 7306 | 7472 | 7638 | 7804 | 7970 | 8135 | |
| 49 | 3 | 8301 | 8467 | 8633 | 8798 | 8964 | 9129 | | 9460 | 9625 | 9791 421439 | 165 |
| 66 | 4 | 421604 | 1768 | 1933 | 2097 | 2261 | 2426 | | | | | |
| 82 | 5 | 3246 | 3410 | 3574 | 3737 | 3901 | 4065 | 4228 | 2754 4392 | 2918 4555 | 3082 4718 | |
| 98 | 6 | 4882 | 5045 | 5208 | 5371 | 5534 | 5697 | 5860 | 6023 | | 6349 | |
| 115 | 7 | 6511 | 6674 | 6836 | 6999 | 7161 | 7324 | 7486 | 7648 | 7811 | 7973 | |
| 131 | 8 | 8135 | 8297 | 8459 | 8621 | 8783 | 8944 | | 9268 | 9429 | 9591 | |
| 148 | 9 | 9752 | | | | | | | | | 431203 | |
| | 270 | | 431525 | | | | | | | | | _ |
| 16 | 1 | 2969 | 3130 | 3290 | 3450 | 3610 | | | | 432049 | 432809 | |
| 32 | 2 | 4569 | | | | | | | | | 6004 | |
| 47 | 3 | | | | | | | | | | | |
| 63 | 4 | | 7909 | | | | | | 8859 | | 9175 | |
| 79 | 5 | 9333 | | | | 9964 | 440122 | 440279 | 440437 | 440594 | 440752 | 159 |
| 95 | | | 441066 | | | 441538 | 1695 | | | | 2323 | |
| 111 | 7 | 2480 | | | | | | 3419 | 3576 | | 3889 | |
| 126 | 8 | | 10 17 12 0 | 4357 | 4513 | | | | 5137 | 5293 | 5449 | |
| 142 | 9 | 5604 | 5760 | | 6071 | 6226 | | 6537 | 6692 | 6848 | 7003 | |
| - | N. | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | - Contract Contract | D. |
| P. P. | 17 | | | | | | | | | | | |

| | | A | Table | of Logs | rithms | of Nur | nbers fi | rom 1 t | o 100,0 | 00. | | 5 |
|----------|-----|----------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|----------------|-----|
| P. P. | N. | 0 | 1 | 2 | 3 | 4 | ,5 | 6 | 7 | 8 | 9 | D. |
| 1.1 | 280 | 147158 | 447313 | 147468 | 447623 | 417778 | | 448088 | 448242 | 448397 | 448552 | 155 |
| 15 | 1 | 8706 | 8861 | 9015 | 9170 | 9324 | 9478 | 9633 | 9787 | | 450095 | |
| 30 | 2 | | 450403 | | 450711 | 450865 | | 451172 | | | 1633 | |
| 46 | 3 | 1786 | 1940 | 2093 | 2247 | 2400 | 2553 | 2706 | 2859 | 3012 | 3165 | |
| 61 | 4 5 | 3318 4845 | 3471 4997 | 3624 5150 | 3717 5302 | 3930 5454 | 4082 5606 | 4235 5758 | 4387 5910 | 4540 6062 | 4692 6214 | |
| 76 91 | 6 | 6366 | 6518 | 6670 | 6821 | 6973 | 7125 | 7276 | 7428 | 7579 | | |
| 106 | 7 | 7882 | 8033 | 8184 | 8336 | 8487 | 8638 | 8789 | 8940 | 9091 | 9242 | |
| 122 | 8 | 9392 | 9543 | 9694 | 9845 | | 460146 | 460296 | 460447 | 460597 | 460748 | |
| 137 | 9 | 460898 | 461048 | 461198 | 461348 | 461499 | 1649 | 1799 | 1948 | 2098 | 2248 | 150 |
| | 290 | 462398 | 462548 | 462697 | 462847 | 462997 | 463146 | 463296 | 463445 | 463594 | 463744 | 150 |
| 15 | 1 | 3893 | 4042 | 4191 | 4340 | 4490 | 4639 | 4788 | 4936 | 5085 | 5234 | |
| 29 | 2 | 5383 | 5532 | 5680 | 5829 | 5977 | 6126 | 6274 | 6423 | 6571 | 6719 | |
| 44 | 3 | 6868 | 7016 | 7164 | 7312 | 7460 | 7608 | 7756 | 7904 | 8052 | 8200 | |
| 59 | 4 | 8347 | 8495 | 8643 | 8790 | 8938 | 9085 | 9233 | 9380 | 9527 | 9675 | |
| 73 88 | 5 | 9822 471292 | | 1585 | 1732 | 1878 | 2025 | 2171 | 2318 | 2464 | 471145 2610 | |
| 103 | 7 | 2756 | 2903 | 3049 | 3195 | 3341 | 3487 | 3633 | 3779 | 3925 | | |
| 118 | 8 | 4216 | 4362 | 4508 | 4653 | 4799 | 4944 | 5090 | 5235 | 5381 | 5526 | |
| 132 | 9 | 5671 | 5816 | 5962 | 6107 | 6252 | 6397 | 6542 | 6687 | 6832 | | |
| - | 300 | 477121 | - | | 477555 | | 477844 | 477989 | | | 478422 | 143 |
| 14 | 1 | 8566 | 8711 | 8855 | 8999 | 9143 | 9287 | 9431 | 9575 | 9719 | 9863 | 144 |
| 28 | 2 | 480007 | 480151 | 480294 | 480438 | 480582 | | | 481012 | 481156 | 481299 | |
| 43 | 3 | 1443 | 1586 | 1729 | 1872 | 2016 | 2159 | 2302 | 2445 | 2588 | | |
| 57 | 4 | 2874 | 3016 | 3159 | 3302 | 3445 | 3587 | 3730 | 3872 | 4015 | | |
| 71 | 5 | 4300 | 4442 | 4585 | 4727 | 4869 | 5011 6430 | 5153 6572 | 5295 | 5437 | | |
| 85 99 | 6 | 5721 7138 | 5863 7280 | 6005 7421 | 6147 7563 | 6289 7704 | 7845 | 7986 | 6714 8127 | 6855 8269 | | |
| 114 | 8 | 8551 | 8692 | 8833 | 8974 | 9114 | 9255 | 9396 | 9537 | 9677 | | |
| 128 | 9 | | 490099 | | | 490520 | | | | | 491222 | |
| | 310 | | 491502 | | | | | | 492341 | 492481 | | - |
| 14 | 1 | 2760 | 2900 | 3040 | 3179 | 3319 | 3458 | 3597 | 3737 | 3876 | | |
| 28 | 2 | 4155 | 4294 | 4433 | 4572 | 4711 | 4850 | 4989 | 5128 | 5267 | | |
| 41 | 3 | 5544 | 5683 | 5822 | 5960 | 6099 | 6238 | 6376 | 6515 | 6653 | 6791 | 139 |
| 55 | _ 4 | 6930 | 7068 | 7206 | 7344 | 7483 | 7621 | 7759 | 7897 | 8035 | | |
| 69 | 5 | 8311 | 8448 | 8586 | 8724 | 8862 | 8999 | 9137 | 9275 | 9412 | | |
| 83 | 6 | 9687 | 9824 | | | | | | | | 500922 | |
| 97 | 7 | 501059 2427 | 501196 | | 1470 | 1607 2973 | 1744 3109 | 1880 3246 | 2017 | 2154 | | |
| 110 | 8 | 3791 | 2564 3927 | 2700 4063 | 2837 4199 | 4335 | 4471 | 4607 | 3382 4743 | 3518 4878 | | |
| - | | 505150 | 505286 | | | 505693 | | | 506099 | | | - |
| 13 | 320 | 6505 | 6640 | 6776 | 6911 | 7046 | 7181 | 7316 | 7451 | 7586 | | |
| 27 | 2 | 7856 | 7991 | 8126 | 8260 | 8395 | 8530 | 8664 | 8799 | 8934 | | |
| 40 | 3 | 9203 | 9337 | 9471 | 9606 | 9740 | | 510009 | | | 510411 | |
| 53 | 4 | | 510679 | 510813 | 510947 | 511081 | | 1349 | 1482 | 1616 | | |
| 66 | 5 | 1883 | 2017 | 2151 | 2284 | 2418 | 2551 | 2684 | 2818 | 2951 | | |
| 80 | 6 | 3218 | 3351 | 3484 | 3617 | 3750 | 3883 | 4016 | 4149 | 4282 | | |
| 93 | 7 | 4548 | 4681 | 4813 | 4946 | | 5211 | 5344 | 5476 | 5609 | | |
| 106 | 8 | 5874 7196 | 6006 7328 | 6139 | 6271 7592 | 6403 | 6535 | 6668 | 6800 | | | |
| 120 | 9 | | | | | 7724 | | 7987 | 8119 | | 8382 | |
| | | 9828 | 0050 | 590000 | 590991 | 590950 | 59040 | 519303 | 519434 | 590000 | 519697 | 13 |
| 13. | | | 521269 | 1400 | | | | | | | 521007 2314 | |
| 39 | 3 | | | | | | | | | | | |
| 52 | 4 | | | | | | | | | | | |
| 65 | 5 | | | | | | | | | | | |
| 78 | 6 | | 1000 | | | | | | | | | |
| 91 | 7 | | | | 8016 | 8145 | 8274 | | | 8660 | 8788 | 12 |
| 104 | 8 | | | | | | | | | | 530072 | |
| 117 | 9 | 530200 | 530328 | 530456 | 530584 | 530712 | 530840 | 530968 | 531096 | | 1351 | 12 |
| | N. | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | D. |

| 6 | | | A Table | of Log | arithms | s of Nu | mbers f | rom 1 t | 0 100,0 | 00. | | |
|----------|------|----------------|----------------|----------------|----------------|--------------|----------------|----------------|----------------|--------------|----------------|-----|
| P. P. | . N. | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | D. |
| | 340 | | | | 531862 | | | 532245 | | 532500 | 532627 | 128 |
| 13 | 2 | 2754 | | | | | | 3518 4787 | 3645 4914 | 3772 5041 | 3899 5167 | |
| 25 38 | 3 | | | | 1 . | | | | | 6306 | 6432 | |
| 50 | 4 | | | | 6937 | | | | | 7567 | 7693 | |
| 63 | 5 | 7819 | | | 8197 | 8322 | | | | 8825 | 8951 | 126 |
| 76 | 6 | | | | | | | | | | 540204 | |
| 88 | 8 | 540329 | | | | | 540955 2203 | 541080 | 541205 2452 | 1330 2576 | 1454 | |
| 113 | 9 | 1579 2825 | | 1 | | | | | 3696 | 3820 | 2701 3944 | |
| | 350 | | 1 | 544316 | | | | 544812 | | | | - |
| 12 | 1 | 5307 | 5431 | 5555 | | | | | | 6296 | 6419 | |
| 24 | 2 | 6543 | 6666 | 6789 | 6913 | 1 | 7159 | 7282 | | 7529 | 7652 | |
| 37 | 3 | | | | 8144 | | 8389 | | 8635 | 8758 | 8881 | |
| 49 | 4 | 9003 | | | 9371 | 9494 | 9616 | | 9861 | | 550106 | |
| 61 73 | 6 | 1450 | 1572 | | | | 2060 | 550962 2181 | 2303 | | 1328 2547 | |
| 85 | 7 | 2668 | | | 3033 | | | | | 3640 | | |
| 98 | 8 | 3883 | 1 | | | 4368 | 4489 | | | 4852 | 4973 | |
| 110 | 9 | 5094 | 5215 | | | 5578 | 5699 | 5820 | 5940 | 6061 | 6182 | 121 |
| | | | 556423 | | | 556785 | | 557026 | | | | 120 |
| 12 | 1 | 7507 | 7627 | 7748 | | | 1 | | | 8469 | 8589 | |
| 36 | 2 3 | 8709 | 8829 | 8948 | | 9188 | 9308 | | 9548 | 9667 | 9787 560982 | |
| 48 | 4 | 561101 | 1221 | 1340 | | | | | 1936 | 2055 | | |
| 59 | 5 | 2293 | | 2531 | 2650 | | 2887 | | 3125 | 3244 | 3362 | |
| 71 | 6 | 3481 | 3600 | 3718 | 3837 | 3955 | 4074 | | 4311 | 4429 | 4548 | 119 |
| 83 | 7 | 4666 | | 4903 | | 5139 | 5257 | | 5494 | 5612 | 5730 | |
| 95 | 8 9 | 5848 | 5966 | 6084 | 6202 | 6320 | 6437 7614 | 6555 | 6673 7849 | 6791 7967 | 6909 | |
| 107 | | 7026 | 7144 568319 | 7262 | 7379 568554 | | | 7732 | | | 8084 569257 | 117 |
| 12 | 1 | 568202 9374 | 9491 | 568436 9608 | 9725 | 9842 | | 568905 | | | 570426 | |
| 23 | 2 | | | | 570893 | | | 1243 | 1359 | 1476 | 1592 | |
| 35 | 3 | 1709 | 1825 | 1942 | 2058 | 2174 | 2291 | 2407 | 2523 | 2639 | 2755 | |
| 46 | 4 | 2872 | 2988 | 3104 | 3220 | 3336 | 3452 | 3568 | 3684 | 3800 | 3915 | |
| 58 70 | 5 | 4031 | 4147 | 4263 | 4379 | 4494 | 4610 | | 4841 | 4957 | 5072 | |
| 81 | 7 | 5188 6341 | 5303 6457 | 5419 6572 | 5534 6687 | 5650 6802 | 5765 6917 | 5880 7032 | 5996 7147 | 6111 7262 | 6226 | |
| 93 | 8 | 7492 | 7607 | 7722 | 7836 | 7951 | 8066 | 8181 | 8295 | 8410 | 8525 | |
| 104 | 9 | 8639 | 8754 | 8868 | 8983 | 9097 | 9212 | 9326 | 9441 | 9555 | 9669 | |
| | 380 | 579784 | 579898 | 580012 | 580126 | 580241 | 580355 | 580469 | 580583 | 580697 | 580811 | 114 |
| 11 | 1 | | 581039 | 1153 | 1267 | 1381 | 1495 | 1608 | 1722 | 1836 | 1950 | |
| 23 | 2 | 2063 | 2177 | 2291 | 2404 | 2518 | 2631 | 2745 | 2858 | 2972 | 3085 | |
| 34 45 | 3 4 | 3199 4331 | 3312 4444 | 3426 4557 | 3539 4670 | 3652 4783 | 3765 4896 | 3879 5009 | 3992 5122 | 4105 5235 | 4218 5348 | |
| 56 | 5 | 5461 | 5574 | 5686 | 5799 | 5912 | 6024 | 6137 | 6250 | 6362 | 6475 | |
| 68 | 6 | 6587 | 6700 | 6812 | 6925 | 7037 | 7149 | 7262 | 7374 | 7486 | 7599 | |
| 79 | 7 | 7711 | 7823 | 7935 | 8047 | 8160 | 8272 | 8384 | 8496 | 8608 | 8720 | 112 |
| 90 | 8 | 8832 | 8944 | 9056 | 9167 | 9279 | 9391 | 9503 | 9615 | 9726 | 0.00 | 112 |
| 102 | 9 | | - | | | _ | | | | | 590953 | |
| 11 | 390 | | | 591287 | 591399 | 591510 | 591621 | | 591843 | - | 592066 | |
| - 22 | 2 | 2177 3286 | 2288 3397 | 2399 3508 | 2510 3618 | 2621 3729 | 2732 3840 | 2843 3950 | 2954 4061 | 3064 4171 | 3175 4282 | |
| 33 | 3 | 4393 | 4503 | 4614 | | 4834 | 4945 | 5055 | 5165 | 5276 | 5386 | |
| 44 | 4 | 5496 | 5606 | 5717 | 5827 | 5937 | 6047 | 6157 | 6267 | 6377 | 6487 | 110 |
| 55 | 5 | 6597 | 6707 | 6817 | 6927 | 7037 | 7146 | 7256 | 7366 | 7476 | 7586 | |
| 66 | 6 | 7695 8791 | 7805 8900 | 7914 | 8024 9119 | 8134 | 8243 | 8353 | 8462 | 8572 | 8681 | |
| 88 | 8 | 9883 | | | | 9228 | 9337 600428 | 9446 | 9556 600646 | 9665 | 9774 600864 | |
| 99 | | 600973 | 601082 | 1191 | 1299 | 1408 | 1517 | 1625 | 1734 | 1843 | 1951 | |
| P. P. | | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | | | D. |
| - 4 - | | | - 1 | 2 | 3 1 | 4 | 0 | 0 1 | - | 8 | 3 ! | U. |

| | | A | Table | of Log | arithms | of Nu | mbers | from 1 t | o 100,0 | 000. | | 7 |
|----------|------|--------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|-----|
| P. P. | N. | 0 | 1 | 2. | 3 | 4 | 5 | 6 | 7 | 8 | 9 | D. |
| 5 | 400 | 605060 | | | | 602494 | 602603 | | | 602928 | | 108 |
| 11 | 1 | 3144 | 3253 | 3361 | 3469 | 3577 | 3686 | 3794 | 3902 | 4010 | 4118 | |
| 21 | 2 | 4226 | 4334 | 4442 | 4550 | 4658 | 4766 | 4874 | 4982 | 5089 | 5197 | |
| 32 43 | 3 | | 5413 6489 | 5521 6596 | 5628 6704 | 5736 6811 | 5844 6919 | 5951 7026 | 6059 7133 | 6166 7241 | 6274 7348 | |
| 53 | 5 | 7455 | 7562 | 7669 | 7777 | 7884 | 7991 | 8098 | 8205 | 8312 | 8419 | |
| 64 | 6 | 8526 | 8633 | 8740 | 8847 | 8954 | 9061 | 9167 | 9274 | 9381 | 9488 | |
| 75 | 7 | 9594 | 9701 | 9808 | | | | | | | 610554 | |
| 86 | 8 | | 610767 | | | 1086 | 1192 | 1298 | 1405 | 1511 | 1617 | |
| 96 | 9 | 1723 | 1829 | 1936 | 2042 | 2148 | 2254 | 2360 | 2466 | 2572 | 2678 | - |
| | 410 | 612784 | | 612996 | | | | | | | 613736 | |
| 10 | 1 | 3842 | 3947 | 4053 | 4159 | 4264 | 4370 | 4475 | 4581 | 4686 | 4792 | |
| 21 | 2 | 4897 | 5003 | 5108 | 5213 | 5319 | 5424 | 5529 | 5634 | 5740 | 5845 | |
| 31 42 | 3 | | 6055 7105 | 6160 7210 | 6265 7315 | 6370 7420 | | 6581 7629 | 6686 7734 | 6790 7839 | 6895 7943 | |
| 52 | 5 | | 8153 | 8257 | 8362 | 8466 | 8571 | 8676 | 8780 | 8884 | | |
| 63 | 6 | | 9198 | 9302 | 9406 | 9511 | 9615 | 9719 | 9824 | | 620032 | |
| 73 | 7 | | | | | | | | | | | |
| 84 | 8 | 1176 | 1280 | 1384 | 1488 | 1592 | | 1799 | 1903 | | 2110 | |
| 94 | 9 | 2214 | 2318 | 2421 | 2525 | 2628 | 2732 | 2835 | 2939 | 3042 | | 1 |
| | 420 | | | 623456 | | | | | | | | |
| 10 | 1 | 4282 | 4385 | 4488 | 4591 | 4695 | | | 5004 | | | |
| 20 | 2 | 5312 | 5415 | 5518 | 5621 | 5724 | | | 6032 | | | |
| 31 | 3 | | 6443 7468 | 6546 7571 | 6648 7673 | 6751 | | | | | 1 | |
| 51 | 5 | | 8491 | 8593 | 8695 | 8797 | | | 8082 9104 | | | |
| 61 | 6 | | 9512 | 9613 | 9715 | 9817 | | 630021 | | | 630326 | |
| 71 | 7 | | 630530 | | | | | | | | 1342 | |
| 82 | 8 | | 1545 | 1647 | 1748 | 1849 | | 2052 | | | | |
| 92 | 9 | 2457 | 2559 | 2660 | 2761 | 2862 | 2963 | 3064 | 3165 | 3266 | 3367 | 101 |
| | 430 | | | | | | | 634074 | | | | |
| 10 | 1 | | 4578 | 4679 | 4779 | 4880 | | | 5182 | | | |
| 20 | 2 | | | | | 5886 | | 1 | | | | |
| 30 | 3 | | 6588 7590 | 6688 7690 | 6789 7790 | 6889 7890 | | | | | | 100 |
| 50 | 5 | | 8589 | 8689 | 8789 | 8888 | | | | | | |
| 60 | 6 | | 9586 | | 9785 | 9885 | | | | | 640383 | |
| 70 | . 7 | | 640581 | | 640779 | | | | | | | |
| 80 | 8 | 1474 | 1573 | 1672 | 1771 | 1871 | 1970 | 2069 | 2168 | | | |
| 90 | 9 | | 2563 | 2662 | 2761 | 2860 | 2959 | 3058 | 3156 | 3255 | 3354 | 99 |
| | 440 | 643453 | | | 643749 | | | | | | 644340 | 98 |
| 10 | 1 | | | 4636 | | | | | | | | |
| 19 29 | 3 | | | 5619 | | 5815 | | 1 | 6110 | | | |
| 39 | 4 | 1 | | 6600 7579 | | | | | | | | |
| 48 | 5 | | | 8555 | | | | | | | | |
| 58 | 6 | | | | 9627 | | | | | | 650210 | |
| 68 | 2 | | 650405 | | | | | 650890 | 0987 | | | |
| 78 | 8 | 1278 | 1375 | .1472 | 1569 | | | | | 1 | | |
| 87 | 9 | | | | | | | | | | | |
| 1 | | 653213 | 653309 | 653405 | 653502 | | | | 653888 | 653984 | 654080 | |
| 9 | 1 | 4177 | 4273 | 4369 | 4465 | 4562 | 4658 | 4754 | 4850 | 4946 | 5042 | 96 |
| 19 | 2 | | | | | | | | | | | |
| 28 | 3 | | | | | | | | | | | |
| 47 | 2 | | | | | | | | | | | |
| 57 | 6 | | | | | | | | | | | |
| 66 | 7 | | 660011 | | 660201 | 660296 | 660391 | 660486 | 660581 | 660676 | 660771 | 95 |
| 76 | 1 8 | 660865 | 0960 | 1055 | 1150 | 1245 | | | | | | |
| 85 | 9 | 1813 | | 2002 | 2096 | 2191 | 2286 | 2380 | | | | |
| P. P | . N. | 0 | 1 | 2 | 3 | 4 | 5. | 6 | 17 | 8 | 9 | D. |

| 9 19 28 37 46 56 65 74 84 | 4600 1 2 3 4 5 6 7 8 9 9 4 70 1 2 3 4 4 5 6 7 8 | 3701 4642 5581 6518 7453 8386 9317 670246 1173 | 1 662852 3795 4736 5675 6612 7546 8479 9410 670339 1265 672190 3113 4034 4953 5870 6785 7698 | 3889 4830 5769 6705 7640 8572 9503 670431 1358 | 3983 4924 5862 6799 7733 8665 9596 670524 1451 | 4078 5018 5956 6892 7826 8759 9689 670617 1543 | 5 663230 4172 5112 6050 6986 7920 8852 9782 670710 1636 672560 3482 | 4266 5206 6143 7079 8013 8945 9875 670802 1728 672652 | 4360 5299 6237 7173 8106 9038 9967 | 8 663512 4454 5393 6331 7266 8199 9131 670060 0988 1913 672836 | 4548 5487 6424 7360 8293 9224 670153 1080 2005 | 94 93 93 93 93 93 |
|--|--|--|---|--|--|--|---|--|--|---|--|--|
| 9 19 28 37 46 56 65 74 84 9 18 27 36 45 55 | 1 2 3 4 4 5 6 7 8 9 4 7 0 1 2 3 4 4 5 6 7 8 | 3701 4642 5581 6518 7453 8386 9317 670246 1173 672098 3021 3942 4861 5778 6694 7607 | 3795 4736 5675 6612 7546 8479 9410 670339 1265 672190 3113 4034 4953 5870 6785 | 3889 4830 5769 6705 7640 8572 9503 670431 1358 672283 3205 4126 5045 | 3983 4924 5862 6799 7733 8665 9596 670524 1451 672375 3297 4218 | 4078 5018 5956 6892 7826 8759 9689 670617 1543 672467 3390 | 4172 5112 6050 6986 7920 8852 9782 670710 1636 672560 | 4266 5206 6143 7079 8013 8945 9875 670802 1728 672652 | 4360 5299 6237 7173 8106 9038 9967 670895 1821 | 4454 5393 6331 7266 8199 9131 670060 0988 1913 | 4548 5487 6424 7360 8293 9224 670153 1080 2005 | 94 94 94 93 93 93 93 |
| 19 28 37 46 56 65 74 84 9 18 27 36 45 55 | 2 3 4 5 6 7 8 9 470 1 2 3 4 5 6 7 8 | 4642 5581 6518 7453 8386 9317 670246 1173 672098 3021 3942 4861 5778 6694 7607 | 4736 5675 6612 7546 8479 9410 670339 1265 672190 3113 4034 4953 5870 6785 | 4830 5769 6705 7640 8572 9503 670431 1358 672283 3205 4126 5045 | 4924 5862 6799 7733 8665 9596 670524 1451 672375 3297 4218 | 5018 5956 6892 7826 8759 9689 670617 1543 672467 3390 | 5112 6050 6986 7920 8852 9782 670710 1636 672560 | 5206 6143 7079 8013 8945 9875 670802 1728 672652 | 5299 6237 7173 8106 9038 9967 670895 1821 | 5393 6331 7266 8199 9131 670060 0988 1913 | 5487 6424 7360 8293 9224 670153 1080 2005 | 94 94 94 93 93 93 93 |
| 28 37 46 56 65 74 84 9 18 27 36 45 55 | 3 4 5 6 7 8 9 4 70 1 2 3 4 4 5 6 6 7 8 | 5581 6518 7453 8386 9317 670246 1173 672098 3021 3942 4861 5778 6694 7607 | 5675 6612 7546 8479 9410 670339 1265 672190 3113 4034 4953 5870 6785 | 5769 6705 7640 8572 9503 670431 1358 672283 3205 4126 5045 | 5862 6799 7733 8665 9596 670524 1451 672375 3297 4218 | 5956 6892 7826 8759 9689 670617 1543 672467 3390 | 6050 6986 7920 8852 9782 670710 1636 672560 | 6143 7079 8013 8945 9875 670802 1728 672652 | 6237 7173 8106 9038 9967 670895 1821 | 6331 7266 8199 9131 670060 0988 1913 | 6424 7360 8293 9224 670153 1080 2005 | 94 94 93 93 93 93 93 |
| 37 46 56 65 74 84 9 18 27 36 45 55 | 4 5 6 7 8 9 4 5 6 6 7 8 | 6518 7453 8386 9317 670246 1173 672098 3021 3942 4861 5778 6694 7607 | 6612 7546 8479 9410 670339 1265 672190 3113 4034 4953 5870 6785 | 6705 7640 8572 9503 670431 1358 672283 3205 4126 5045 | 6799 7733 8665 9596 670524 1451 672375 3297 4218 | 6892 7826 8759 9689 670617 1543 672467 3390 | 6986 7920 8852 9782 670710 1636 672560 | 7079 8013 8945 9875 670802 1728 672652 | 7173 8106 9038 9967 670895 1821 | 7266 8199 9131 670060 0988 1913 | 7360 8293 9224 670153 1080 2005 | 94 93 93 93 93 93 |
| 46 56 65 74 84 9 18 27 36 45 55 | 5 6 7 8 9 4 70 1 2 3 4 4 5 6 7 8 | 7453 8386 9317 670246 1173 672098 3021 3942 4861 5778 6694 7607 | 7546 8479 9410 670339 1265 672190 3113 4034 4953 5870 6785 | 7640 8572 9503 670431 1358 672283 3205 4126 5045 | 7733 8665 9596 670524 1451 672375 3297 4218 | 7826 8759 9689 670617 1543 672467 3390 | 7920 8852 9782 670710 1636 672560 | 8013 8945 9875 670802 1728 672652 | 8106 9038 9967 670895 1821 | 8199 9131 670060 0988 1913 | 8293 9224 670153 1080 2005 | 93 93 93 93 93 |
| 56 65 74 84 9 18 27 36 45 55 | 6 7 8 9 470 1 2 3 4 5 6 7 8 | 8386 9317 670246 1173 672098 3021 3942 4861 5778 6694 7607 | 8479 9410 670339 1265 672190 3113 4034 4953 5870 6785 | 8572 9503 670431 1358 672283 3205 4126 5045 | 8665 9596 670524 1451 672375 3297 4218 | 8759 9689 670617 1543 672467 3390 | 8852 9782 670710 1636 672560 | 8945 9875 670802 1728 672652 | 9038 9967 670895 1821 | 9131 670060 0988 1913 | 9224 670153 1080 2005 | 93 93 93 93 |
| 74 84 9 18 27 36 45 55 | 8 9 470 1 2 3 4 5 6 7 | 670246 1173 672098 3021 3942 4861 5778 6694 7607 | 670339 1265 672190 3113 4034 4953 5870 6785 | 670431 1358 672283 3205 4126 5045 | 670524 1451 672375 3297 4218 | 670617 1543 672467 3390 | 670710 1636 672560 | 670802 1728 672652 | 670895 1821 | 0988 1913 | 1080 2005 | 93 93 |
| 9 18 27 36 45 55 | 9 470 1 2 3 4 5 6 7 | 1173 672098 3021 3942 4861 5778 6694 7607 | 1265 672190 3113 4034 4953 5870 6785 | 1358 672283 3205 4126 5045 | 1451 672375 3297 4218 | 1543 672467 3390 | 1636 672560 | $\frac{1728}{672652}$ | 1821 | 1913 | 2005 | 93 |
| 9 18 27 36 45 55 | 470 1 2 3 4 5 6 7 | 672098 3021 3942 4861 5778 6694 7607 | 672190 3113 4034 4953 5870 6785 | 672283 3205 4126 5045 | 672375 3297 4218 | 672467 3390 | 672560 | 672652 | | - | | - |
| 9 18 27 36 45 55 | 1 2 3 4 5 6 7 8 | 3021 3942 4861 5778 6694 7607 | 3113 4034 4953 5870 6785 | 3205 4126 5045 | 3297 4218 | 3390 | | | 672744 | 672836 | CTONON | |
| 18 27 36 45 55 | 2 3 4 5 6 7 8 | 3942 4861 5778 6694 7607 | 4034 4953 5870 6785 | 4126 5045 | 4218 | | 3482 | | 0000 | | | 92 |
| 27 36 45 55 | 3 4 5 6 7 8 | 4861 5778 6694 7607 | 4953 5870 6785 | 5045 | | 4010 | | 3574 | 3666 4586 | 3758 4677 | 3850 4769 | |
| 36 45 55 | 4 5 6 7 8 | 5778 6694 7607 | 5870 6785 | | 0101 | 5228 | 4402 5320 | 4494 5412 | 5503 | 5595 | 5687 | |
| 45 55 | 5 6 7 8 | 6694 7607 | 6785 | | 6053 | 6145 | 6236 | 6328 | 6419 | 6511 | 6602 | |
| | 7 8 | | 7608 | 6876 | 6968 | 7059 | 7151 | 7242 | 7333 | 7424 | 7516 | |
| 64 | 8 | 8518 | | 7789 | 7881 | 7972 | 8063 | 8154 | 8245 | 8336 | 8427 | |
| | | 0100 | 8609 | 8700 | 8791 | 8882 | 8973 | 9064 | 9155 | 9246 | 9337 | |
| 73 82 | | 9428 | 9519 | 9610 | 9700 | 9791 | 9882 | | | | 680245 | 91 |
| | - | | 680426 | | | | 680789 | | 0970 | 1060 | 1151 | - |
| 9 | 480 1 | 681241 2145 | 681332 2235 | 681422 2326 | 681513 2416 | 681603 2506 | 681693 2596 | 681784 2686 | 681874 2777 | 681964 2867 | 682055 2957 | |
| 18 | 2 | 3047 | 3137 | 3227 | 3317 | 3407 | 3497 | 3587 | 3677 | 3767 | 3857 | |
| 27 | 3 | 3947 | 4037 | 4127 | 4217 | 4307 | 4396 | 4486 | 4576 | 4666 | 4756 | |
| 36 | 4 | 4845 | 4935 | 5025 | 5114 | 5204 | | 5383 | 5473 | 5563 | 5652 | |
| 45 | 5 | 5742 | 5831 | 5921 | 6010 | 6100 | 6189 | 6279 | 6368 | 6458 | 6547 | |
| 54 | 6 | 6636 | | | 6904 | 6994 | 7083 | 7172 | 7261 | 7351 | 7440 | 1 |
| 63 | 7 | 7529 | 7618 | 7707 | 7796 | 7886 | 7975 | 8064 | 8153 | 8242 | 8331 | |
| 72 81 | 8 | 8420 9309 | 8509 9398 | 8598 9486 | 8687 9575 | 8776 9664 | 8865 9753 | 8953 9841 | 9042 | 9131 690019 | 9220 | |
| | - | | 690285 | | | | 690639 | | 690816 | | | - |
| 9 | 1 | 1081 | 1170 | 1258 | 1347 | 1435 | 1524 | 1612 | 1700 | 1789 | 1877 | |
| 18 | 2 | 1965 | 2053 | 2142 | 2230 | 2318 | 2406 | 2494 | 2583 | 2671 | 2759 | |
| 26 | 3 | 2847 | 2935 | 3023 | 3111 | 3199 | 3287 | 3375 | 3463 | 3551 | 3639 | |
| 35 | 4 | 3727 | 3815 | 3903 | 3991 | 4078 | 4166 | 4254 | 4342 | 4430 | 4517 | |
| 44 | 5 | 4605 | 4693 | 4781 | 4868 | 4956 | 5044 | 5131 | 5219 | 5307 | 5394 | |
| 53 62 | 6 | 5482 | 5569 6444 | 5657 | 5744 6618 | 5832 | 5919 | 6007 | 6094 6968 | 6182 7055 | 6269 | |
| 70 | 8 | 6356 7229 | 7317 | 6531 7404 | 7491 | 6706 7578 | 6793 7665 | 6880 7752 | 7839 | 7926 | 7142 8014 | |
| 79 | 9 | 8101 | 8188 | 8275 | 8362 | 9449 | 8535 | 8622 | 8709 | 8796 | 8883 | |
| | 500 | | 699057 | - | | | | | | 699664 | | 87 |
| 9 | 1 | 9838 | | 700011 | | | | | | | | |
| 17 | 2 | 700704 | 700790 | 0877 | 0963 | 1050 | 1136 | 1222 | 1309 | 1395 | 1482 | 86 |
| 26 | 3 | | | | 1827 | 1913 | | 2086 | 2172 | 2258 | 2344 | |
| 34 43 | 4 | | 2517 | 2603 | | | | 2947 | 3033 | 3119 | 3205 | |
| 52 | 5 | 3291 4151 | 3377 4236 | 3463 4322 | 3549 4408 | 3635 4494 | | 3807 4665 | 3893 4751 | 3979 4837 | 4065 | |
| 60 | 7 | 5008 | | | 5265 | | | | 5607 | 5693 | | |
| 69 | 8 | | 1 | 1 | 6120 | 1 | 1 | 6376 | 6462 | | 6632 | |
| 77 | 9 | | | | 6974 | | | | 7315 | 7400 | 7485 | |
| | 510 | 707570 | 707655 | 707740 | 707826 | 707911 | 707996 | 708081 | 708166 | 708251 | 708336 | 85 |
| 8 | 1 | 8421 | 8506 | | 8676 | | | 8931 | 9015 | 9100 | 9185 | 85 |
| 17 | 2 | | | | | | | | | | 710033 | |
| 25 34 | | | 710202 | | | | | | | | | |
| 42 | 5 | | | | | | | | | | | |
| 50 | 6 | | | | | | | | | | | |
| 59 | 1 | | | | | | | | - | | | |
| 67 | 8 | 4330 | 4414 | 4497 | | | | | | | | |
| 76 | 5 | 5167 | 5251 | 5335 | 5418 | 5502 | | 5669 | 5753 | 5836 | 5920 | 84 |
| P. P. | N. | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 . | D. |

| | | · A | Table | of Loga | rithms | of Nu | mbers f | rom 1 t | 0 100,0 | 00. | 0) | 9 |
|-------|--------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|----------|
| P. P. | N. | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | D. |
| | 520 | 716003 | 716087 | 716170 | 716254 | 716337 | 716421 | 716504 | 716588 | 716671 | 716754 | 83 |
| 8 | 1 | 6838 | 6921 | 7004 | 7088 | 7171 | 7254 | 7338 | 7421 | 7504 | | 83 |
| 17 | 2 | 7671 | 7754 | 7837 | 7920 | 8003 | 8086 | 8169 | 8253 | 8336 | 8419 | 83 |
| 25 | 3 | 8502 | 8585 | 8668 | 8751 | 8834 | 8917 | 9000 | 9083 | 9165 | | 83 |
| 33 | 4 | 9331 | 9414 | 9497 | 9580 | 9663 | 9745 | 9828 | 9911 | 9994 | | 83 |
| 41 | 5 | | 720212 | | | | | | | | | 83 |
| 50 | 6 | 0986 | 1068 | 1151 | 1233 | 1316 | 1398 | 1481 | 1563 | 1646 | | 82 |
| 58 | 7 | 1811 | 1893 | 1975 | 2058 | 2140 | 2222 | 2305 | 2387 | 2469 | | 82 |
| 66 | 8 | 2634 | 2716 | 2798 | 2881 | 2963 | 3045 | 3127 | 3209 | 3291 | | 82 |
| 75 | 9 | 3456 | 3538 | 3620 | 3702 | 3784 | 3866 | 3948 | 4030 | 4112 | | 82 |
| 11 | | 724276 | | | | | | | | | | 82 |
| 8 | 1 | 5095 | 5176 | 5258 | 5340 | 5422 | 5503 | 5585 | 5667 | 5748 | | 82 |
| 16 | 2 | 5912 | 5993 | 6075 | 6156 | 6238 | 6320 | 6401 | 6483 | | | 82 |
| 24 | 3 | 6727 | 6809 | 6890 | 6972 | 7053 | 7134 | 7216 | 7297 | 7379 | | 81 |
| 32 | 4 | 7541 | 7623 | 7704 | 7785 | 7866 | 7948 | 8029 | 8110 | | 8273 | 81 |
| 40 | 5 | 8354 | 8435 | 8516 | 8597 | 8678 | 8759 | 8841 | 8922 | 9003 | | 81 |
| 49 | 6 | 9165 | 9246 | 9327 | 9408 | 9489 | 9570 | 9651 | 9732 | 9813 | | 81 |
| 57 | 7 | | 730055 | | | | | | | | 730702 | 81 |
| 65 | 8 9 | 730782 | 0863 | 0944 | 1024 | 1105 | 1186 | 1266 2072 | 1347 2152 | 1428 2233 | 1508 2313 | 81 |
| 13 | | 1589 | 1669 | 1750 | 1830 | 1911 | 1991 | | | | | |
| | | | 732474 | | | | | 732876 | | | 733117 | 80 |
| 8 | 1 | 3197 | 3278 | 3358 | 3438 | 3518 | 3598 | 3679 | 3759 | | | 80 |
| 16 | 2 | 3999 | 4079 | 4160 | 4240 | 4320 | 4400 | | 4560 | | | 80 |
| 24 | 3 | 4800 | 4880 | 4960 | 5040 | | | | 5359 | | | 80 |
| 32 | 4 | 5599 | 5679 | 5759 6556 | 5838 | 5918 | 5998 | | 6157 | | | 80 |
| 40 | 6 | 6397 | 6476 | 7352 | 6635 | 6715 | 6795 | | | | | 80 |
| 56 | 7 | 7193 7987 | 7272 | 8146 | 7431 | 7511 | 7590 8384 | | 8543 | | | 79 79 |
| 64 | 8 | | 8067 | 8939 | 8225 9018 | 8305 9097 | 9177 | | 9335 | 1 | | 79 |
| 72 | 9 | | 8860 9651 | 9731 | 9810 | 9889 | | 740047 | | | 740284 | 79 |
| 10 | - | | | | | | | | | | I | _ |
| 0 | 550 | | | | | | 740757 | | | 740994 | | 79 |
| 8 | 1 2 | 1152 | 1230 | 1309 | 1388 | | | | 1703 2489 | | | 79 79 |
| 16 23 | 3 | | 2018 2804 | 2096 2882 | 2175 2961 | | | | | | | |
| 31 | 4 | | 3588 | 3667 | 3745 | | | | | | | 78 78 |
| 39 | 5 | | 4371 | 4449 | 4528 | | | | | 1 | | 78 |
| 47 | 6 | | 5153 | 5231 | 5309 | | | | | | | 78 |
| 55 | 7 | | 5933 | 6011 | 6089 | | | | | | | 78 |
| 63 | 8 | | 6712 | 6790 | 6868 | | | 1 | | | 1 | 78 |
| 70 | 9 | | 7489 | 7567 | 7645 | | | | | | | 78 |
| 1 | 560 | | 748266 | | 748421 | | 748576 | | 74873 | | 748885 | 77 |
| 8 | 1 | | 9040 | 9118 | 9195 | | | | | | | 77 |
| 15 | 2 | | 9814 | 9891 | | | | | | | 750431 | 77 |
| 23 | 3 | | 750586 | | | | | | | | | 77 |
| 31 | 4 | 1 | 1356 | | | | | | | | | 77 |
| 38 | 1 8 | | | | | | | | | | | 77 |
| 46 | 1 | | | | | | | | | | | 77 |
| 54 | 1 7 | | | | | | | | | | | 77 |
| 62 | 8 | | | | | | | | | | | 76 |
| 69 | 9 | | | | | | | | | | | 76 |
| | | | | | | | | | | | 756560 | |
| 7 | 1 | | 6712 | 6788 | 6864 | 6940 | 7016 | | 7168 | | 7320 | 76 |
| 15 | 9 | | | | | | | | | | | |
| 22 | 1 5 | | | | | | | | | | | |
| 30 | 1 4 | | | | | | | | | | | |
| 37 | 1 2 | | | | | | | | | | 760347 | |
| 45 | 1 | | 760498 | | | | | | 1 | | | |
| 52 | 1 | | | | | | | | | | | |
| 60 | 1 8 | | | | | | | | | | | |
| 67 | 1 | 2679 | 2754 | 2829 | 2904 | 2978 | 3053 | | | | | |
| P. 1 | N | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 1 8 | 9 | D. |
| 7 | -1 740 | , 0 | 1 | 1 6 | 1 0 | 1 19 | 1 0 | . 0 | | , 0 | 9 | 11. |

| 10 | | , | A Table | of Log | garithm | s of N | ımbers | from 1 | to 100 | ,000. | | |
|-------|----------|--------------|--------------|--------------|--------------|--------------|----------------|----------------|--------------|--------------|----------------|----------|
| P. F | . N. | 0 | 1 | 2 | 3 | 1 4 av | 1 5 | 6 | 7 : | 8 | 9 | D. |
| | 580 | 763428 | 763503 | 763578 | 763653 | 763727 | 763809 | 76387 | 763952 | 76402 | 764101 | 75 |
| 7 | 1 | | | 4326 | | | | | | | | |
| 15 | 2 | | | | | | | | | | | |
| 30 | 3 | | | | | | | | | | - | |
| 37 | 5 | | 1 | | | | | | | | | |
| 44 | 6 | | | | | | | | | | | |
| 52 | 7 | | | 1 | | | | | | | | |
| 59 | 8 | | | 9525 | 9599 | | | | | | 770042 | |
| 67 | 9 | 770115 | 770189 | 770263 | 770336 | 770410 | 770484 | 770557 | 770631 | 770703 | 0778 | 74 |
| | 590 | 770852 | 770926 | 770999 | 771073 | 771146 | 771220 | 771295 | 771367 | 771440 | 771514 | 74 |
| 7 | 1 | 1587 | | 1734 | 1808 | 1881 | 1955 | | | | | 73 |
| 15 | 2 | 2322 | | 2468 | 2542 | | | | | 1 | | 73 |
| 22 | 3 | 3055 | | 3201 | 3274 | | | | | | 1 | |
| 29 | 4 | 3786 | | | 4006 | | | | | | | |
| 36 | 6 | 4517 | - | 4663 | 4736 | | | 1 | | | | |
| 51 | 7 | 5246 5974 | | 5392 6120 | 5465 6193 | | | | 5756 6483 | | | |
| 58 | 8 | 6701 | 6774 | 6846 | 6919 | 6992 | | | 1 | | | |
| 66 | 9 | 7427 | 7499 | 7572 | 7644 | 7717 | 7789 | | | | | |
| - | - | 778151 | 778224 | 778296 | | 778441 | | | - Shi | | | 72 |
| 7 | 1 | 8874 | | 9019 | 9091 | 9163 | 1 | | | | | |
| 14 | 2 | 9596 | | 9741 | 9813 | 9885 | 9957 | | 780101 | | 780245 | |
| 22 | 3 | 780317 | | | 780533 | | | | | 0893 | 0965 | |
| 29 | 4 | 1037 | 1109 | 1181 | 1253 | 1324 | | | | | | 72 |
| 36 | 5 | 1755 | | 1899 | 1971 | 2042 | | | | 2329 | | 72 |
| 43 | 6 | 2473 | | 2616 | 2688 | 2759 | 2831 | 2902 | | 3046 | | |
| 50 | 7 | 3189 | | 3332 | 3403 | 3475 | 3546 | 1 | | 3761 | | |
| 58 | 8 9 | 3904 4617 | | 4046 | 4118 | 4189 | 4261 | 4332 | 4403 | 4475 5187 | 1 | |
| 65 | - | | 4689 | 4760 | 4831 | 4902 | 4974 | 5045 | 5116 | | 5259 | - |
| 7 | 610 | | 785401 | 785472 | | | 785686 6396 | 785757 6467 | 6538 | 6609 | 785970 6680 | 71 |
| 14 | 2 | 6041 6751 | 6112 6822 | 6183 6893 | 6254 6964 | 6325 7035 | 7106 | 7177 | 7248 | 7319 | 7390 | 71 |
| 21 | 3 | 7460 | 7531 | 7602 | 7673 | 7744 | 7815 | 7885 | 7956 | 8027 | 8098 | |
| 28 | 4 | 8168 | | 8310 | - 8381 | 8451 | 8522 | 8593 | 8663 | 8734 | 8804 | |
| 35 | - 5 | 8875 | 8946 | 9016 | 9087 | 9157 | 9228 | 9299 | 9369 | 9440 | 9510 | 71 |
| 43 | 6 | 9581 | 9651 | 9722 | 9792 | 9863 | | | 790074 | | 790215 | 70 |
| 50 | 7 | | 790356 | | | | | 0707 | 0778 | 0848 | 0918 | 70 |
| 57 | 8 | 0988 | 1059 | 1129 | 1199 | 1269 | 1340 | 1410 | 1480 | 1550 | 1620 | 70 |
| 64 | 9 | 1691 | 1761 | 1831 | 1901 | 1971 | 2041 | 2111 | 2181 | 2252 | 2322 | 70 |
| | 620 | | 792462 | | | | 792742 | | | | 793022 | 70 |
| 7 | 1 | 3092 | 3162 | 3231 | 3301 | 3371 | 3441 | 3511 | 3581 | 3651 | 3721 | 70 |
| 21 | a 2 3 | 3790 4488 | 3860 4558 | 3930 | 4000 | 4070 | 4139 4836 | 4209 4906 | 4279 4976 | 4349 5045 | 4418 | 70 |
| 58 | 4 | 5185 | 5254 | 4627 5324 | 4697 5393 | 5463 | 5532 | 5602 | 5672 | 5741 | 5811 | 70 |
| 35 | 5 | 5880 | 5949 | 6019 | 6088 | 6158 | 6227 | 6297 | 6366 | 6436 | 6505 | 69 |
| 42 | 6 | 6574 | 6644 | 6713 | 6782 | 6852 | 6921 | 6990 | 7060 | 7129 | 7198 | 69 |
| 49 | 7 | 7268 | 7337 | 7406 | 7475 | 7545 | 7614 | 7683 | 7752 | 7821 | 7890 | 69 |
| 56 | 8 | 7960 | 8029 | 8098 | 8167 | 8236 | 8305 | 8374 | 8443 | 8513 | 8582 | 69 |
| 63 | 9 | 8651 | 8720 | 8789 | 8858 | 8927 | 8996 | 9065 | 9134 | 9203 | 9272 | 69 |
| | | 799341 | 799409 | | | | | | 799823 | | | 69 |
| 7 | | | 800098 | | | | | | | | | 69 |
| 14 | 2 | 0717 | 0786 | 0854 | 0923 | 0992 | 1061 | 1129 | 1198 | 1266 | | |
| 20 27 | 3 | 1404 | 1472 | 1541 | 1609 | 1678 | 1747 | 1815 | 1884 | 1952 | 2021 | 69 |
| 34 | 5 | 2089 2774 | 2158 2842 | 2226 | 2295 | 2363 3047 | 2432 3116 | 2500 | 2568 | 2637 3321 | 2705 3389 | |
| 41 | 6 | 3457 | 3525 | 3594 | 2979 3662 | 3730 | 3798 | 3184 3867 | 3252 3935 | 4003 | 4071 | 68 |
| 48 | 7 | 4139 | 4208 | 4276 | 4344 | 4412 | 4480 | 4548 | 4616 | 4685 | 4753 | 68 68 |
| 54 | 8 | 4821 | 4889 | 4957 | 5025 | 5093 | 5161 | 5229 | 5297 | 5365 | | 68 |
| 61 | 9 | 5501 | 5569 | 5637 | 5705 | 5773 | 5841 | 5908 | 5976 | 6044 | | 68 |
| P. P. | N. | 0 | 1 | 2 | - 3 | 4 | 5 | 6 | 7 | 8 | 9 | D. |
| | 241 | - | 1 | - | 00 | 4 | 0 | 0 | | 0 | 9 | D. |

| | | | Table | | | | | | | | | 1 |
|----------|-----|----------------|----------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|-----|
| P. P. | N. | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | I |
| | 640 | 806180 | 806248 | 806316 | 806384 | 806451 | 806519 | 806587 | 806655 | 806723 | 806790 | |
| 7 | 1 | 6858 | 6926 | 6994 | | | | | | | | 1 |
| 13 | 2 | 7535 | | | | | | | 8008 | | | |
| 20 | 3 | 8211 | 8279 | 8346 | | | 8549 | | | | 8818 | |
| 27 | 4 | 8886 | 8953 | 9021 | 9088 | | 9223 | | | | | |
| 33 | 5 | 9560 | | 9694 | | | 9896 | | | | 810165 | |
| 40 | | | 810300 | | | | | | | | | 1 |
| 47 | 8 | 0904 | 0971 | 1039 | 1106 | 1173 | 1240 | 1307 | 1374 | | 1508 | |
| 60 | 9 | 1575 2245 | 1642 2312 | 1709 2379 | 1776 2445 | 1843 2512 | 1910 2579 | 1977 2646 | 2044 | | 2178 2847 | |
| | | | | | | | | | | | | - |
| | | | 812980 | | | | | | | 813448 | | 1 |
| 7 | 1 | 3581 | 3648 | 3714 | 3781 | 3848 | 3914 | 3981 | 4048 | | 1 | 1 |
| 13 | 3 | 4248 4913 | 4314 | 4381 | 4447 5113 | 4514 | 4581 | 4647 | 5378 | | | 1 |
| 20 26 | 4 | 5578 | 4980 5644 | 5046 5711 | 5777 | 5179 5843 | 5246 5910 | 5312 5976 | | | 5511 6175 | |
| 33 | 5 | 6241 | 6308 | 6374 | 6440 | | 6573 | 6639 | 6705 | | 6838 | 3 |
| 40 | 6 | 6904 | 6970 | 7036 | 7102 | | 7235 | 7301 | 7367 | 7433 | 7499 | 1 |
| 46 | 7 | 7565 | 7631 | 7698 | 7764 | | 7896 | | | | | |
| 53 | 8 | 8226 | 8292 | 8358 | 8424 | | 8556 | | 8688 | | 8820 | |
| 59 | 9 | 8885 | 8951 | 9017 | 9083 | 9149 | 9215 | 9281 | 9346 | | 9478 | |
| 00 | - | 819544 | | | | | | I | | 1 | 820136 | |
| 0 | | | | | | | | | | | | |
| 6 | 2 | 0858 | 820267 0924 | 0989 | | 1120 | | 1251 | 1317 | 0727 1382 | 0792 | |
| 19 | 3 | 1514 | 1579 | 1645 | 1055 1710 | 1775 | 1186 1841 | 1906 | | | 2103 | |
| 26 | 4 | 2168 | 2233 | 2299 | | | 2495 | | | | 2756 | 1 |
| 32 | 5 | 2822 | 2887 | 2952 | 2364 3018 | 3083 | | 2560 3213 | | | | |
| 39 | 6 | 3474 | 3539 | 3605 | 3670 | | 3800 | 3865 | | | - | |
| 45 | 7 | 4126 | 4191 | 4256 | 4321 | 4386 | 4451 | 4516 | | 4646 | 1 | 1 |
| 52 | 8 | 4776 | 4841 | 4906 | 4971 | 5036 | 5101 | 5166 | | 5296 | | |
| 58 | - 9 | 5426 | 5491 | 5556 | 5621 | 5686 | 5751 | 5815 | | | | |
| - | | | | | | | | | | | | 1 - |
| 0 | 670 | 826075 6723 | 6787 | 826204 | | | | | 826528 | 7240 | 826658 | 1 |
| 6 | 1 | 7369 | | 6852 | 6917 | 6981 | 7046 | | 7175 | 7886 | 7305 7951 | |
| 13 | 3 | | 7434 | 7499 | 7563 | | 7692 | | | | | 1 |
| 19 26 | 4 | 8015 8660 | 8080 8724 | 8144 | 8209 | | 8338 | 8402 9046 | | 8531 9175 | 8595 9239 | 1 |
| 32 | 5 | 9304 | 9368 | 8789 9432 | 8853 9497 | 9561 | 8982 9625 | 9690 | | | | |
| 38 | 6 | 9947 | | | | | | | | | 830525 | |
| 45 | 7 | 830589 | 0653 | 0717 | 0781 | 0845 | 0909 | 0973 | | 1102 | 1166 | |
| 51 | 8 | 1230 | 1294 | 1358 | 1422 | 1486 | 1550 | 1614 | 1678 | | 1806 | |
| 58 | 9 | 1870 | 1934 | 1998 | 2062 | 2126 | 2189 | 2253 | 2317 | 2381 | 2445 | |
| | - | | | | | | | | | | - | 1- |
| | 680 | 832509 | | | | | | | | | 833083 | |
| 6 | 1 | 3147 3784 | 3211 | 3275 | 3338 | | 3466 | 3530 | 3593 | | 3721 | ٧. |
| 13 19 | 3 | 4421 | 3848 4484 | 3912 | 3975 | 4039 4675 | 4103 | | 4230 4866 | 4294 4929 | | |
| 25 | 4 | 5056 | 5120 | 4548 5183 | 4611 5247 | 5310 | 4739 5373 | 4802 5437 | 5500 | | 4993 5627 | |
| 31 | 5 | 5691 | 5754 | 5817 | | 5944 | | | 6134 | 6197 | | |
| 38 | 6 | 6324 | 6387 | 6451 | 5881 6514 | | 6007 | 6704 | 6767 | 6830 | 6261 6894 | 1 |
| 44 | 7 | 6957 | 7020 | 7083 | 7146 | 7210 | 7273 | 7336 | 7399 | 7462 | 7525 | 1 |
| 50 | 8 | 7588 | 7652 | 7715 | 7778 | 7841 | 7904 | 7967 | 8030 | 8093 | 8156 | |
| 57 | 9 | 8219 | 8282 | 8345 | 8408 | 8471 | 8534 | 8597 | 8660 | 8723 | 8786 | |
| | | | | | | | | | | | | |
| 6 | 1 | 9478 | | | | | | | | | 839415 | |
| 13 | | | 9541 840169 | 9604 | 9667 | 9729 | 9792 | | 9918 | 9981 | 840043 | |
| 19 | 3 | | | | | | | | | | | |
| 25 | _ | 1359 | | | 1547 | | | | | | | |
| 31 | 4 | 1985 | | 1485 2110 | 2172 | | 1672 2297 | | | | | |
| 38 | 5 | 2609 | | 2734 | | | 2921 | | | 2484 3108 | | |
| 44 | 7 | 3233 | | | 3420 | | 3544 | | | | | |
| 50 | 8 | 3855 | | 3980 | | | 4166 | | | 4353 | 3793 | |
| 57 | 9 | 4477 | 4539 | 4601 | 4664 | 4726 | 4788 | | | 4974 | 4415 | |
| P. P. | | | | | | | | | | | 5036 | (|
| | | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | Ī |

| 12 | | 1 | A Table | of Log | arithms | s of Nu | mbers f | rom 1 t | o 100,0 | 000. | | |
|-------|--------|--------------|----------------|--------------|--------------|--------------|--------------|--------------|--------------|--------|--------------|---|
| P. P. | | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | D |
| 9.0 | 700 | 845098 | 845160 | 845222 | 845284 | 845346 | 845408 | 845470 | 845532 | 845594 | 845656 | 6 |
| 6 | 1 | 5718 | 5780 | 5842 | 5904 | 5966 | 6028 | 6090 | | 6213 | 6275 | |
| 12 | 2 | 6337 | 6399 | 6461 | 6523 | | | 6708 | 6770 | | 6894 | |
| 19 | 3 | 6955 | 7017 | 7079 | 7141 | 7202 | | | | 7449 | 7511 | |
| 25 31 | 4 | 7573 | 7634 | 7696 | 7758 | | | 7943 | | | 8128 | |
| 37 | 5 | 8189 | 8251 | 8312 | 8374 | 8435 | 8497 | 8559 | 8620 | | 8743 | |
| 43 | 7 | 8805 9419 | 8866 | 8928 | 8989 | 9051 | 9112 | 9174 | | | 9358 | |
| 50 | | | 9481 | 9542 | 9604 | | 9726 | 9788 | | | 9972 | |
| 56 | 9 | 0646 | 850095 0707 | 0769 | 0830 | | 0952 | 1014 | 1075 | 1136 | | |
| - | | | | | | | - | | | | | 1 |
| 6 | 1 | | 851320 | | | | | | | 851747 | | |
| 12 | 2 | 1870 | 1931 | 1992 | 2053 | | 2175 | 2236 | | 2358 | 2419 | |
| 18 | 3 | 2480 3090 | 2541 3150 | 2602 | 2663 | | | 2846 3455 | 2907 3516 | 2968 | 3029 | |
| 24 | 4 | | | 3211 | 3272 | 3333 | | 4063 | | | 3637 | |
| 30 | 5 | 3698 4306 | 3759 4367 | 3820 | 3881 | 3941 | 4002 | 4670 | | 4185 | 4245 | |
| 37 | 6 | 4913 | 4974 | 4428 | 4488 5095 | 4549 5156 | | | 5337 | 5398 | 4852 5459 | |
| 43 | 7 | 5519 | 5580 | 5034 | 5701 | 5761 | 5822 | 5882 | 5943 | 6003 | | |
| 49 | 8 | 6124 | 6185 | 5640 | 6306 | 6366 | 6427 | 6487 | 6548 | 6608 | | |
| 55 | 9 | 6729 | 6789 | 6245 6850 | 6910 | 6970 | 7031 | 7091 | 7152 | | 6668 7272 | |
| | | | | | | | | | | - | | 1 |
| 6 | 1 | | 857393 | | | | | | | | | |
| 12 | 2 | 7935 | 7995 | 8056 | 8116 | | | 8297 | 8357 | 8417 | 8477 | 6 |
| 18 | 3 | 8537 | 8597 | 8657 | 8718 | 8778 | 8838 | 8898 | 8958 | 9018 | 9078 | |
| 24 | 4 | 9138 9739 | 9198 | 9258 | 9318 | 9379 | 9439 | 9499 | 9559 | 9619 | 9679 | |
| 30 | . 5 | | 9799 | 9859 | 9918 | | | | | 860218 | | |
| 36 | 6 | 000335 | 860398 | | | | 0637 | 0697 | 0757 | 0817 | 0877 | |
| 42 | . 7 | 0937 1534 | 0996 | 1056 | 1116 | 1176 | 1236 | 1295 | 1355 1952 | 1415 | 1475 | |
| 48 | 8 | 2131 | 1594 2191 | 1654 | 1714 2310 | 1773 | 1833 2430 | 1893 2489 | 2549 | 2012 | 2072 | |
| 54 | 9 | 2728 | 2787 | 2251 | | 2370 | | 3085 | 3144 | 2608 | 2668 | |
| | | | | 2847 | 2906 | 2966 | 3025 | | | 3204 | | |
| 6 | 130 | 863323 | 863382 | | | | | | | | | |
| 12 | 1 2 | 3917 | 3977 | 4036 | 4096 | 4155 | -4214 | 4274 | 4333 | 4392 | 4452 | |
| 18 | 3 | 4511 | 4570 | 4630 | 4689 | 4748 | 4808 | 4867 | 4926 | 4985 | 5045 | |
| 24 | 4 | 5104 | 5163 | 5222 | 5282 | 5341 | 5400 | 5459 | 5519 | 5578 | 5637 | |
| 29 | 5 | 5696 6287 | 5755 | 5814 | 5874 | 5933 | 5992 | 6051 | 6110 | 6169 | 6228 | |
| 35 | 6 | 6878 | 6346 6937 | 6405 | 6465 | 6524 | 6583 | 6642 | 6701 | 6760 | 6819 | |
| 41 | 7 | 7467 | 7526 | 6996 | 7055 | 7114 | | 7232 7821 | 7291 7880 | 7350 | 7409 | |
| 47 | 8 | 8056 | 8115 | 7585 | 7644 | 7703 | 7762 | | 8468 | 7939 | 7998 | |
| 53 | 9 | 8644 | 8703 | 8174 | 8233 | 8292 | 8350 | 8409 | 9056 | 8527 | 8586 | |
| | _ | | | 8762 | 8821 | 8879 | 8938 | 8997 | | 9114 | 9173 | |
| 6 | | | 869290 | | | | | | | 869701 | | |
| 12 | 1 | 9818 | 9877 | 9935 | | | | | | 870287 | | |
| 17 | 2 | 870404 | 870462 | | 870579 | 0638 | 0696 | 0755 | 0813 | 0872 | 0930 | |
| 23 | 3 | 0989 | 1047 | 1106 | 1164 | | 1281 | 1339 | 1398 | 1456 | 1515 | |
| 29 | 4 | 1573 | 1631 | 1690 | 1748 | 1806 | 1865 | 1923 | 1981 | 2040 | 2098 | |
| 35 | 5 6 | 2156 | 2215 | 2273 | 2331 | 2389 | 2448 | 2506 | 2,564 | | 2681 | 5 |
| 41 | 7 | 2739 3321 | 2797 | 2855 | 2913 | 2972 | 3030 | 3088 | 3146 | 3204 | 3262 | |
| 46 | 8 | 3902 | 3379 | 3437 | 3495 | 3553 | 3611 | 3669 | 3727 | 3785 | 3844 | |
| 52 | 9 | 4482 | 3960 4540 | 4018 | 4076 | 4134 | 4192 | 4250 | 4308 | 4366 | 4424 | |
| | | | | 4598 | 4656 | 4714 | 4772 | 4830 | 4888 | 4945 | 5003 | |
| | | | 875119 | | | 875293 | | | | 875524 | | 5 |
| 6 | 1 | 5640 | 5698 | 5756 | 5813 | 5871 | 5929 | 5987 | 6045 | 6102 | 6160 | |
| 17 | 2 | 6218 | 6276 | 6333 | 6391 | 6449 | 6507 | 6564 | | 6680 | 6737 | |
| 23 | 3 | 6795 | 6853 | 6910 | 6968 | 7026 | 7083 | 7141 | 7199 | 7256 | 7314 | |
| 23 | 4 | 7371 | 7429 | 7487 | 7544 | 7602 | 7659 | 7717 | 7774 | 7832 | 7889 | |
| 34 | 5 | 7947 | 8004 | 8062 | 8119 | 8177 | 8234 | 8292 | 8349 | 8407 | 8464 | |
| 40 | 6 | 8522 | 8579 | 8637 | 8694 | 8752 | 8809 | 8866 | 8924 | 8981 | 9039 | 5 |
| 46 | 8 | 9096 | 9153 | 9211 | 9268 | 9325 | 9383 | 9440 | 9497 | 9555 | 9612 | 5 |
| 51 | 9 | 9669 | 9726 | 9784 | 9841 | 9898 | | 880013 | | | 880185 | 5 |
| | | 880242 | 880299 | 880356 | 880413 | 880471 | 880528 | 0585 | 0642 | 0699 | 0756 | 5 |
| P. | N. | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |

| - | e e | | A Table | of Logs | arithms | of Nu | mbers f | rom 1 t | 0 100,0 | 00. | | 13 |
|----------|-----|-----------------------|----------------|--------------|--------------|--------------|--------------|----------------|--------------|--------------|--------------|----------|
| P. P. | N. | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | D. |
| | 760 | 880814 | 880871 | 880928 | 880985 | 881042 | 881099 | 881156 | 881213 | 881271 | 881328 | 57 |
| 6 | 1 | 1385 | 1442 | 1499 | 1556 | 1613 | 1670 | 1727 | 1784 | 1841 | 1898 | 57 |
| 11 | 2 | 1955 | 2012 | 2069 | 2126 | 2183 | 2240 | 2297 | 2354 | 2411 | 2468 | 57 |
| 17 23 | 3 | 2525 3093 | 2581 3150 | 2638 3207 | 2695 3264 | 2752 3321 | 2809 3377 | 2866 3434 | 2923 3491 | 2980 3548 | 3037 | 57 |
| 28 | 5 | 3661 | 3718 | 3775 | 3832 | 3888 | 3945 | 4002 | 4059 | 4115 | 4172 | 57 |
| 34 | 6 | 4229 | 4285 | 4342 | 4399 | 4455 | 4512 | 4569 | 4625 | 4682 | 4739 | 57 |
| 40 | 7 | 4795 | 4852 | 4909 | 4965 | 5022 | 5078 | 5135 | 5192 | 5248 | 5305 | 57 |
| 46 51 | 8 | 5361 | 5418 | 5474 | 5531 | 5587 6152 | 5644 6209 | 5700 6265 | 5757 6321 | 5813 | 5870 6434 | 57 56 |
| - 31 | | $\frac{5926}{886491}$ | 5983 | 6039 | 6096 | | | 886829 | | 6378 | | 56 |
| 6 | 1 | 7054 | 7111 | 7167 | 7223 | 7280 | 7336 | 7392 | 7449 | 7505 | 7561 | 56 |
| 11 | 2 | 7617 | 7674 | 7730 | 7786 | 7842 | 7898 | | 8011 | 8067 | 8123 | 56 |
| 17 | 3 | 8179 | 8236 | 8292 | 8348 | 8404 | 8460 | 8516 | 8573 | 8629 | 8685 | 56 |
| 22 | 4 | 8741 | 8797 | 8853 | 8909 | 8965 | 9021 | 9077 | 9134 | 9190 | 9246 | |
| 28 34 | 5 | 9302 | 9358 | 9414 | 9470 | 9526 | 9582 | 9638 890197 | 9694 | 9750 | 9806 | 56 56 |
| 39 | | 890421 | 9918 890477 | | 0589 | 0645 | 0700 | | 0812 | 0868 | 0924 | 56 |
| 45 | 8 | 0980 | 1035 | 1091 | 1147 | 1203 | 1259 | 1314 | 1370 | 1426 | 1482 | 56 |
| 50 | 9 | 1537 | 1593 | 1649 | 1705 | 1760 | 1816 | 1872 | 1928 | 1983 | 2039 | 56 |
| | 780 | | 892150 | | | | | | | | | 56 |
| 6 | 1 | 2651 | 2707 | 2762 | 2818 | 2873 | 2929 | 2985 | 3040 | 3096 | 3151 | 56 |
| 11 16 | 2 3 | 3207 3762 | 3262 | 3318 3873 | 3373 3928 | 3429 3984 | 3484 4039 | 3540 4094 | 3595 4150 | 3651 4205 | 3706 4261 | 56 55 |
| 22 | 4 | 4316 | | 4427 | 4482 | 4538 | 4593 | | 4704 | | 4814 | |
| 27 | 5 | 4870 | | 4980 | 5036 | 5091 | 5146 | 5201 | 5257 | 5312 | 5367 | |
| 33 | 6 | 5423 | 5478 | 5533 | 5588 | 5644 | 5699 | 5754 | 5809 | 5864 | 5920 | 55 |
| 38 | 7 | 5975 | | 6085 | 6140 | -6195 | 6251 | 6306 | 6361 | 6416 | 6471 | 55 |
| 44 | 8 9 | 6526 | 6581 | 6636 | 6692 7242 | 6747 7297 | 6802 7352 | 6857 7407 | 6912 7462 | 6967 7517 | 7022 | |
| | | 7077 | 7132 | 7187 | | | | | | | - | |
| 5 | 790 | 8176 | | 8286 | 8341 | 8396 | 8451 | 8506 | 8561 | 8615 | 8670 | |
| 11 | 2 | 8725 | | | 8890 | 8944 | 8999 | 9054 | 9109 | 9164 | 9218 | |
| 16 | . 3 | 9273 | 9328 | 9383 | 9437 | 9492 | 9547 | 9602 | 9656 | 9711 | 9766 | |
| 22 | 4 | | 9875 | 9930 | | | | 900149 | | | | |
| 27 33 | 6 | | 900422 | 1022 | 1077 | 0586 1131 | 0640 | | 0749 1295 | | 0859 1404 | |
| 38 | 7 | 1458 | | 1567 | 1622 | 1676 | 1731 | 1785 | 1840 | | 1948 | |
| 44 | 8 | 2003 | | 2112 | 2166 | 2221 | 2275 | | 2384 | 2438 | 2492 | |
| 49 | 9 | 2547 | 2601 | 2655 | 2710 | 2764 | 2818 | 2873 | 2927 | 2981 | 3036 | 54 |
| | 800 | | 903144 | | | | | | | | 903578 | 1 |
| 11 | 1 | 3633 | | 3741 | 3795 | 3849 | | | 4012 | 4066 | 4120 | |
| 16 | 3 | | 1 | 4283 4824 | | 4391 4932 | 4445 | | 4553 5094 | | 4661 5202 | 54 54 |
| 22 | 4 | | 1 | 5364 | | 5472 | | | 5634 | | 5742 | |
| 27 | 5 | 5796 | 5850 | 5904 | 5958 | 6012 | 6066 | 6119 | 6173 | 6227 | 6281 | 54 |
| 32 | 6 | | 1 | | | 6551 | 6604 | | 6712 | | | |
| 38 | 7 | 6874 | | 6981 | 7035 | - | 1 | | | | | |
| 49 | 8 9 | | | 1 | 1 | | | | 7787 8324 | | 7895 8431 | 54 54 |
| | - | | 908539 | | | | - | | | | | 54 |
| 5 | 1 | 9021 | | | | | | | | | | |
| 11 | 2 | 9556 | 9610 | 9663 | 9716 | 9770 | 9823 | 9877 | 9930 | 9984 | 910037 | 53 |
| 16 | | 1 | 9:0144 | | | | | | | | | |
| 21 26 | 4 | | | | | | | | | | 1104 1637 | |
| 32 | 6 | | | | | | | | | | | |
| 37 | 7 | | | | | | | 1 | 2594 | | | |
| 42 | 8 | 2753 | | 2859 | 2913 | 2966 | 3019 | 3072 | 3125 | 3178 | 3231 | 53 |
| 48 | 9 | 3284 | 3337 | 3390 | 3443 | 3496 | 3549 | 3602 | | 3708 | 3761 | 53 |
| P. P. | N. | 1 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | D. |

| | | | | | | | | | to 100, | | | |
|-------------------|-----|--------------|--------------|--------------|----------------|--------------|--------------|--------------|--------------|--------------|--------------|----|
| P. P. | N. | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | D |
| | 830 | 913814 | 913867 | 913920 | | | | | | 914237 | 914290 | 5 |
| 5 | 1 | 4343 | 4396 | 4449 | 4502 | | 1 | | | 4766 | 4819 | 5 |
| 11 | 2 | 4872 | 4925 | 4977 | 5030 | | 5136 | | | 5294 | 5347 | |
| 16 | 3 | 5400 | 5453 | 5505 | 5558 | 5611 | 5664 | | | 5822 | 5875 | |
| 21 | 4 | 5927 | 5980 | 6033 | | 6138 | 6191 | 6243 | | 6349 | 6401 | 5 |
| 26 | 5 | 6454 | 6507 | 6559 | | 6664 | 6717 | 6770 | | 6875 | 6927 | |
| 32 | 6 | 6980 | 7033 | 7085 | 7138 | 7190 | 7243 | | | 7400 | 7453 | |
| 37 | 8 | 7506 8030 | 7558 8083 | 7611 8135 | 7663 8188 | 7716 8240 | 7768 8293 | 7820 8345 | | 7925 8450 | | |
| 48 | 9 | 8555 | 8607 | 8659 | 8712 | 8764 | 8816 | 8869 | 8921 | 8973 | 8502 9026 | |
| 4.7 | | | | | | | | | - | | | _ |
| | | | 919130 | 919183 | 919235 9758 | 9810 | 9862 | 919392 | | 919490 | | 5 |
| 5 | 2 | 9601 | | | 920280 | | | | | 0541 | 0593 | 5 |
| 16 | . 3 | 0645 | 0697 | 0749 | 0801 | 0853 | 0906 | 0958 | 1010 | 1062 | 1114 | |
| 21 | 4 | 1166 | 1218 | 1270 | 1322 | 1374 | 1426 | 1478 | 1530 | | 1634 | |
| 26 | 5 | 1686 | 1738 | 1790 | 1842 | 1894 | 1946 | 1998 | 2050 | 2102 | 2154 | 5 |
| 31 | 6 | 2306 | 2258 | 2310 | 2362 | 2414 | 2466 | 2518 | 2570 | 2622 | 2674 | |
| 36 | 7 | 2725 | 2777 | 2829 | 2881 | 2933 | 2985 | 3037 | 3089 | 3140 | | |
| 42 | 8 | 3244 | 3296 | 3348 | 3399 | 3451 | 3503 | 3555 | 3607 | 3658 | 3710 | |
| 47 | 9 | 3762 | 3814 | 3865 | 3917 | 3969 | 4021 | 4072 | 4124 | 4176 | 4228 | |
| | 840 | 924279 | 924331 | 924383 | 924434 | 924486 | 924538 | 924589 | 924641 | 924693 | 924744 | 5 |
| 5 | 1 | 4796 | 4848 | 4899 | 4951 | 5003 | 5054 | 5106 | 5157 | 5209 | 5261 | 5 |
| 10 | 2 | 5312 | 5364 | 5415 | 5467 | 5518 | 5570 | 5621 | 5673 | 5725 | 5776 | |
| 15 | 3 | 5828 | 5879 | 5931 | 5982 | 6034 | 6085 | 6137 | 6188 | 6240 | 6291 | 5 |
| 20 | 4 | 6342 | 6394 | 6445 | 6497 | 6548 | 6600 | 6651 | 6702 | 6754 | 6805 | 5 |
| 25 | 5 | 6857 | 6908 | 6959 | 7011 | 7062 | 7114 | 7165 | 7216 | 7268 | 7319 | 5 |
| 31 | 6 | 7370 | 7422 | 7473 | 7524 | 7576 | 7627 | 7678 | 7730 | 7781 | 7832 | 5 |
| 36 | 7 | 7883 | 7935 | 7986 | 8037 | 8088 | | 8191 | 8242 | 8293 | 8345 | 1 |
| 4.1 | 8 | 8396 | 8147 | 8498 | 8549 | 8601 | 8652 | 8703 | 8754 | 8805 | 8857 | 5 |
| 46 | 9 | 8908 | 8959 | 9010 | 9061 | 9112 | 9163 | 9215 | 9266 | 9317 | 9368 | 5 |
| | 850 | | 929470 | | | | | | | 929827 | | 5 |
| 5 | 1 | 9930 | | | 930083 | | | | | | | 5. |
| 10 | | 930410 | | 0542 | 0592 | 0643 | 0694 | 0745 | 0796 | 0847 | 0898 | - |
| 15 | 3 | 0949 | 1000 | 1051 | 1102 | 1153 | 1204 | 1254 | 1305 | 1356 | 1407 | 5 |
| 20 | 4 | 1458 | 1509 | 1560 | 1610 | 1661 | 1712 2220 | 1763 | 1814 | 1865 | 1915 | |
| 25 | 5 | 1966 2474 | 2017 2524 | 2068 2575 | 2118 2626 | 2169 2677 | 2727 | 2271 2778 | 2322 2829 | 2372 2879 | 2423 2930 | 5 |
| 36 | 7 | 2981 | 3031 | 3082 | 3133 | 3183 | 3234 | 3285 | 3335 | 3386 | 3437 | 5 |
| 41 | 8 | 3487 | 3538 | 3589 | 3639 | 3690 | 3740 | 3791 | 3841 | 3892 | 3943 | 5. |
| 46 | 9 | 3993 | 4044 | 4094 | 4145 | 4195 | 4246 | 4296 | 4347 | 4397 | 4448 | 5 |
| | | | | | 934650 | | | | | | | _ |
| 5 | | 5003 | | | 5154 | 5205 | 5255 | 5306 | 5356 | 5406 | 5457 | 50 |
| 10 | 1 2 | 5507 | 5054 5558 | 5104 5608 | 5658 | 5709 | 5759 | 5809 | 5860 | 5910 | 5960 | |
| 15 | 3 | 6011 | 6061 | 6111 | 6162 | 6212 | 6262 | 6313 | 6363 | 6413 | 6463 | |
| 20 | 4 | 6514 | 6564 | 6614 | 6665 | 6715 | 6765 | 6815 | 6865 | 6916 | 6966 | |
| 25 | 5 | 7016 | 7066 | 7117 | 7167 | 7217 | 7267 | 7317 | 7367 | 7418 | 7468 | 50 |
| 30 | 6 | 7518 | 7568 | 7618 | 7668 | 7718 | 7769 | 7819 | 7869 | 7919 | 7969 | 50 |
| 35 | 7 | 8019 | 8069 | 8119 | 8169 | 8219 | 8269 | 8320 | 8370 | 8420 | 8470 | 5 |
| 40 | 8 | 8520 | 8570 | 8620 | 8670 | 8720 | 8770 | 8820 | 8870 | 8920 | 8970 | 5 |
| 45 | 9 | 9020 | 9070 | 9120 | 9170 | 9220 | 9270 | 9320 | 9369 | 9419 | 9469 | 5 |
| | 870 | 939519 | 939569 | 939619 | 939669 | 939719 | 939769 | 939819 | 939869 | 939918 | 939968 | 50 |
| 5 | | | | | 940168 | 940218 | | | | | | 5 |
| 10 | 2 | 0516 | 0566 | 0616 | 0666 | | 0765 | 0815 | 0865 | 0915 | 0964 | 5 |
| 15 | 3 | 1014 | 1064 | 1114 | | | 1263 | | 1362 | 1412 | 1462 | 5 |
| 20 | 4 | 1511 | 1561 | 1611 | 1660 | 1710 | 1760 | | 1859 | 1909 | 1958 | 5 |
| 25 | 5 | 2008 | 2058 | 2107 | 2157 | 2207 | 2256 | 2306 | 2355 | 2405 | 2455 | |
| 30 | 6 | 2504 | 2554 | 2603 | | 2702 | 2752 | 2801 | 2851 | 2901 | 2950 | |
| 35 | 7 | 3000 | 3049 | 3099 | 3148 | 3198 | 3247 | 3297 | 3346 | 3396 | 3445 | |
| | 8 | 3495 | 3544 | 3593 | 3643 | 3692 | 3742 | 3791 | 3841 | 3890 | 3939 | |
| 40 | | 9000 | 1000 | 1000 | | | | | | | | |
| 45 45 P. P. | 9 | 3989 | 4038 | 4088 | 4137 | 4186 | 4236 5 | 4285 | 4335 | 4384 | 4433 | 4 |

| | | 1 | A Table | of Log | garithm | s of Nu | mbers | from 1 | to 100,0 | 000. | | 15 |
|----------|-----|----------------|----------------|--------------|--------------|----------------|----------------|--------------|--------------|----------------|----------------|-----|
| P. P. | N. | 0 | 1 . | 2 | 3 . | 4 | 5 | 6 | 7 . | 8 | 9 | D |
| | 880 | 944483 | | 944581 | | 944680 | | | | | | |
| 10 | 2 | 4976 5469 | 5025 5518 | 5074 5567 | 5124 5616 | | | | | 5370 5862 | | |
| 15 | 3 | 5961 | 6010 | 6059 | | | | | | | | |
| 20 | 4 | 6452 | 6501 | 6551 | 6600 | 6649 | 6698 | | 6796 | | | |
| 24 | 5 | 6943 7434 | 6992 | 7041 | 7090 | | | | | | | |
| 29 | 7 | 7924 | 7483 7973 | 7532 8022 | 7581 8070 | 7630 8119 | 7679 8168 | | 7777 8266 | | | |
| 39 | 8 | 8413 | 8462 | 8511 | 8560 | | | | 1 | | | 1 . |
| 44 | 9 | 8902 | 8951 | 8999 | 9048 | 9097 | 9146 | 9195 | 9244 | 9292 | 9341 | 49 |
| | | | | | 949536 | | | | | | 949829 | |
| 5 | 1 | 9878 | 9926 | | 950024 | | | | | | 950316 | |
| 10 15 | 3 | 950365 0851 | 950414 | 0949 | 0511 0997 | 0560 1046 | | | 0706 1192 | | | |
| 20 | 4 | 1338 | 1386 | 1435 | 1483 | | 1580 | | | 1726 | | |
| 24 | 5 | 1823 | 1872 | 1920 | 1969 | 2017 | 2066 | | | | 2260 | |
| 29 | 6 | 2308 | 2356 | 2405 | 2453 | 2502 | | | 2647 | 2696 | | |
| 34 | 8 | 2792 | 2841 | 2889 | 2938 | 2986 | 3034 | 1 | | 3180 | | |
| 39 | 9 | 3276 3760 | 3325 3808 | 3373 3856 | 3421 3905 | 3470 3953 | 3518 4001 | 3566 4049 | 3615 4098 | 3663 4146 | 3711 | 48 |
| | | 954243 | | | | | | 954532 | - | 954628 | - | 48 |
| 5 | 1 | 4725 | 4773 | 4821 | 4869 | 4918 | 4966 | | 5062 | 5110 | | |
| 10 | 2 | 5207 | 5255 | 5303 | 5351 | 5399 | 5447 | 5495 | 5543 | | | |
| 14 | 3 | 5688 | 5736 | 5784 | 5832 | 5880 | 5928 | | 6024 | | 6120 | |
| 19 | 4 5 | 6168 | 6216 | 6265 | 6313 | 6361 | 6409 | | 6505 | 6553 | | 1 |
| 24 29 | 6 | 6649 7128 | 6697 7176 | 6745 7224 | 6793 7272 | 6840 7320 | 6888 7368 | | 6984 7464 | 7032 | 7080 7559 | |
| 34 | 7 | 7607 | 7655 | 7703 | 7751 | 7799 | 7847 | 7894 | 7942 | 7990 | 8038 | 1 |
| 38 | 8 | 8086 | 8134 | 8181 | 8229 | 8277 | 8325 | 8373 | 8421 | 8468 | 8516 | |
| 43 | 9 | 8564 | 8612 | 8659 | 8707 | 8755 | 8803 | 8850 | 8898 | 8946 | 8994 | 48 |
| | | | 959089 | | | 959232 | | | | | | 48 |
| 5 9 | 1 2 | 9518 | 9566 960042 | 9614 | 9661 | 9709 | 9757 | 9804 | 9852 | 9900 | 9947 960423 | |
| 14 | | 960471 | 0518 | 0566 | 0613 | 0661 | 0709 | | 0804 | | 0899 | |
| 19 | 4 | 0946 | 0994 | 1041 | 1089 | 1136 | | | 1279 | | 1374 | |
| 23 | 5 | 1421 | 1469 | 1516 | 1563 | 1611 | 1658 | 1706 | 1753 | 1801 | 1848 | |
| 28 | 6 | 1895 | 1943 | 1990 | 2038 | 2085 | 2132 | 2180 | 2227 | 2275 | 2322 | |
| 33 38 | 7 8 | 2369 2843 | 2417 2890 | 2464 | 2511 2985 | 2559 3032 | 2606 3079 | 2653 3126 | 2701 3174 | 2748 3221 | 2795 3268 | |
| 42 | 9 | 3316 | 3363 | 3410 | 3457 | 3504 | 3552 | 3599 | 3646 | 3693 | 3741 | 47 |
| | 920 | | 963835 | | | | | | 964118 | | - | - |
| 5 | 1 | 4260 | 4307 | 4354 | 4401 | 4448 | 4195 | | 4590 | 4637 | 4684 | |
| 9 | 2 | 4731 | 4778 | 4825 | 4872 | 4919 | 4966 | 5013 | 5061 | 5108 | 5155 | |
| 14 | 3 | 5202 5672 | 5249 5719 | 5296 5766 | 5343 5813 | 5390 | 5437 5907 | 5484 5954 | 5531 | 5578 | 5625 | |
| 23 | 5 | 6142 | 6189 | 6236 | 6283 | 5860 6329 | 6376 | 6423 | 6001 6470 | 6048 6517 | 6095 6564 | |
| 28 | 6 | 6611 | 6658 | 6705 | 6752 | 6799 | 6845 | 6892 | 6939 | 6986 | 7033 | 4.7 |
| 33 | 7 | 7080 | 7127 | 7173 | 7220 | 7267 | 7314 | 7361 | 7408 | 7454 | 7501 | 47 |
| 38 | 8 | 7548 | 7595 | 7642 | 7688 | 7735 | 7782 | 7829 | 7875 | 7922 | 7969 | 47 |
| 42 | 9 | 8016 | 8062 | 8109 | 8156 | 8203 | 8249 | 8296 | 8343 | 8390 | 8436 | 47 |
| 5 | 930 | 968483 8950 | 968530 8996 | 968576 | 968623 | 968670 9136 | 968716 9183 | | | 968856 9323 | 968903 9369 | |
| 9 | 2 | 9416 | 9463 | 9509 | 9556 | 9602 | 9649 | | 9276 9742 | 9323 | 9309 | |
| 14 | 3 | 9882 | 9928 | | 970021 | 970068 | 970114 | 970161 | 970207 | 970254 | 970300 | 47 |
| 18 | | 970347 | 970393 | 970440 | 0486 | 0533 | 0379 | 0626 | 0672 | 0719 | 0765 | 46 |
| 23 | 5 | 0812 | 0858 | 0904 | 0951 | 0997 | 1044 | 1090 | 1137 | 1183 | 1229 | |
| 28 32 | 6 | 1276 1740 | 1322 1786 | 1369 1832 | 1415 1879 | 1461 1925 | 1508 | 1554 2018 | 1601 2064 | 1647 | 1693 | |
| 37 | 8 | 2203 | 2249 | 2295 | 2342 | 2388 | 1971 2434 | 2481 | 2527 | 2110 2573 | 2157 2619 | |
| 41 | 9 | 2666 | 2712 | 2758 | 2804 | 2851 | 2897 | 2943 | 2989 | 3035 | 3082 | |
| . P. | - | 0 | === | 2 , | 3 | 4 | 5 | 6 | 7 | 8 | 9 | D. |

| 16 | | I | A Table | of Log | arithms | of Nu | nbers f | rom 1 t | 0 100,0 | 00. | | |
|----------|-----------------|----------------|----------------|--------------|----------------|--------------|--------------|--------------|--------------|--------------|--------------|----------|
| P. P. | N. | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 3 | 8 , | 9 | D. |
| 11 | 940 | | | 973220 | | | | 973405 | | 973497 | | 46 |
| 5 | 1 | 3590 | 3636 | 3682 | 3728 | 3774 | 3820 | 3866 | 3913 | 3959 | 4005 | 46 |
| 9 14 | 3 | 4051 4512 | 4097 4558 | 4143 4604 | 4189 4650 | 4235 4696 | 4281 4742 | 4327 4788 | 4374 4834 | 4420 4880 | 4466 4926 | 46 46 |
| 18 | 4 | 4972 | 5018 | 5064 | 5110 | 5156 | 5202 | 5248 | 5294 | 5340 | 5386 | 46 |
| 23 | 5 | 5432 | 5478 | 5524 | 5570 | 5616 | 5662 | 5707 | 5753 | 5799 | 5845 | 46 |
| 28 | 6 | 5891 | 5937 | 5933 | 6029 | 6075 | 6121 | 6167 | 6212 | 6258 | 6304 | 46 |
| 32 | 7 | 6350 | 6396 | 6442 | 6488 | 6533 | 6579 | 6625 | 6671 | 6717 | 6763 | 46 |
| 37 | 8 | 6808 7266 | 6854 | 6900 | 6946 7403 | 6992 7449 | 7037 7495 | 7083 7541 | 7129 7586 | 7175 7632 | 7220 7678 | 46 |
| 71 | $\frac{3}{950}$ | | 7312 | 7358 | 977861 | 977906 | | 977998 | | | - | 46 |
| 4 | 1 | 977724 8181 | 8226 | 8272 | 8317 | 8363 | 8409 | 8454 | 8500 | 8546 | 8591 | 46 |
| 9 | 2 | 8637 | 8683 | 8728 | 8774 | 8819 | 8865 | 8911 | 8956 | 9002 | 9047 | 46 |
| 13 | 3 | 9093 | 9138 | 9184 | 9230 | 9275 | 9321 | 9366 | 9412 | 9457 | 9503 | 46 |
| 18 | 4 | 9548 | 9594 | 9639 | 9685 | 9730 | 9776 | 9821 | 9867 | 9912 | 9958 | 46 |
| 22 | | | 980049 | | | | | | | | | 45 |
| 27 31 | 6 | 0458 | 0503 | 0549 | 0594 1048 | 0640 1093 | 0685 1139 | 0730 1184 | 0776 1229 | 0821 1275 | 0867 | 45 |
| 36 | 8 | 0912 | 0957 1411 | 1003 1456 | 1501 | 1547 | 1592 | 1637 | 1683 | 1728 | 1773 | |
| 40 | 9 | 1819 | 1864 | 1909 | 1954 | 2000 | 2045 | 2090 | 2135 | 2181 | 2226 | |
| | 960 | | 982316 | | | 982452 | 982497 | 982543 | | | 982678 | 45 |
| 4 | 1 | 2723 | | 2814 | 2859 | 2904 | 2949 | 2994 | 3040 | 3085 | 3130 | |
| 9 | 2 | 3175 | | | 3310 | 3356 | 3401 | 3446 | 3491 | 3536 | 3581 | 45 |
| 13 | 3 | 3626 | | 3716 | 3762 | 3807 | 3852 | 3897 | 3942 | | 4032 | |
| 18 | 5 | 4077 | 4122 | 4167 | 4212 | | 4302 4752 | 4347 4797 | 4392 4842 | 4437 | 4482 4932 | |
| 22 27 | 6 | 4527 4977 | 4572 5022 | 4617 | 4662 5112 | 4707 5157 | 5202 | 5247 | 5292 | | 5382 | |
| 31 | 7 | 5426 | | 5516 | 5561 | 5606 | 5651 | 5696 | 5741 | 5786 | | |
| 36 | 8 | 5875 | | 5965 | 6010 | 6055 | 6100 | 6144 | | 6234 | | |
| 4.0 | 9 | 6324 | 6369 | 6413 | 6458 | 6503 | 6548 | 6593 | 6637 | 6682 | 6727 | 45 |
| | 970 | | 986817 | | | | | 987040 | | | 987175 | 45 |
| 4 | 1 | 7219 | 7264 | 7309 | 7353 | | 7443 | 7488 | | | 7622 | |
| 9 | 2 | 7666 | | 7756 | 7800 | 7845 | 7890 8336 | | 7979 8425 | | | |
| 13 18 | 3 | 8113 8559 | | 8202 8648 | 8247 8693 | 8291 8737 | 8782 | 8826 | | 8470 8916 | | |
| 22 | 5 | 9005 | | | 9138 | 9183 | 9227 | 9272 | 9316 | | 9405 | |
| 27 | 6 | 9450 | | 9539 | 9583 | 9628 | 9672 | 9717 | 9761 | 9806 | | 44 |
| 31 | 7 | 9895 | | | | | | | | | 990294 | |
| 36 | 8 | | 990383 | | 0472 | 0516 | 0561 | 0605 | | | | |
| 40 | 9 | 0783 | | 0871 | 0916 | 0960 | 1004 | 1049 | 1093 | | 1182 | |
| 4 | | 991226 | 991270 1713 | | 991359 1802 | | 1890 | 1935 | 1979 | | | |
| 9 | 1 2 | 2111 | 2156 | | 2244 | | 2333 | | 2421 | 2465 | | |
| 13 | 3 | | | | 2686 | | | | 2863 | | | |
| 18 | 4 | | | | | 3172 | 3216 | 3260 | | 3348 | 3392 | 44 |
| 22 | 5 | | | | | | | | 3745 | | | |
| 26 | 6 | | | 3965 | | | | | 4185 | 1 | | |
| 31 35 | 8 | | | 4405 | 4449 | | | | 4625 5065 | | | |
| 40 | 9 | | | | | | 5416 | | 5504 | | | 44 |
| - | | | 995679 | | | | - | - | | | 996030 | |
| 4 | 1 | 6074 | | | | | | | 6380 | | | |
| 9 | 2 | | | | | 6687 | 6731 | 6774 | 6818 | 6862 | 6906 | 44 |
| 13 | 3 | | 6993 | 7037 | | | | | | | | |
| 18 | 4 | | | | | | | | | | | |
| 22 26 | 6 | | | | | | | | | | | |
| 31 | 1 7 | | | | | | | | | | | |
| 35 | 8 | | | | | | | | | 0000 | | |
| 40 | 1 | | | | | | 1 | | _ | | | |
| P. P. | N. | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | D. |
| - | - | | - | - | | - | | | | 1 | | |

TABLE III.

THE ANGLES WHICH EVERY POINT AND QUARTER POINT OF THE COMPASS MAKES WITH THE MERIDIAN.

| No | rth | Points. | 0 / 1/ | Points. | Sou | ith. |
|------------|-----------------|---|---|---|------------|------------|
| N. b. E. | N. b. W. | 0 4 0 0 0 1 1 1 1 1 1 1 2 3 1 3 1 3 1 3 1 3 1 3 1 | 2 48 45 5 37 30 8 26 15 11 15 0 14 3 45 16 52 30 | 0 4 0 2 0 2 1 1 4 1 2 34 | S. b. E. | S. b. W. |
| N.N.E. | N.N.W. | 1 3 2 2 2 2 1 | 19 41 15 22 30 0 25 18 45 | 2 | S.S.E. | s.s.w. |
| N.E. b. N. | N.W. b. N. | 2 1419 34 1419 34 | 28 7 30 30 56 15 33 45 0 36 33 45 39 22 30 | 22234 14-1224 | S.E. b. S. | S.W. b. S. |
| N.E. | N.W. | 4 | 42 11 15 45 0 0 47 48 45 | 4 1 | S.E. | s.w. |
| N.E. b. E. | N.W. b. W. | 4 3 5 5 4 5 5 | 50 37 30 53 26 15 56 15 0 59 3 45 61 52 30 | | S.E. b. E. | S.W. b. W. |
| E.N.E. | w. n.w.° | 5 ½ 6 6 ½ | 64 41 15 67 30 0 70 18 45 73 7 30 | 5 \$\frac{3}{4}\$ 6 \$\frac{1}{4}\$ 6 \$\frac{1}{2}\$ 6 \$\frac{3}{4}\$ | E.S.E. | w.s.w |
| E. b. N. | W. b. N. | 6 1 3 5 4 7 1 4 1 3 5 4 7 5 5 4 7 5 5 4 | 75 56 15 78 45 0 81 33 45 84 22 30 | 6 \$4 7 14 7 14 7 29 7 34 | E. b. S. | W. b. S. |
| East. | West. | 7 3 4 8 | 87 11 15 90 0 0 | 7 3/4 | East. | West. |

TABLE IV.

LOGARITHMIC SINES, TANGENTS, AND SECANTS, TO EVERY POINT AND QUARTER POINT OF THE COMPASS.

| Points. | Sine. | Cosine. | Tangent. | Cotang. | Secant. | Cosec. | Points. |
|---------|----------------------|-----------|----------------------|-----------|-----------|-----------|---------|
| . 0 | 0.000000 | 10.000000 | 0.000000 | Infinite. | 10.000000 | Infinite. | 8 |
| 0 ‡ | 8.690796 | 9.999477 | 8.691319 | 11.308681 | 10.000523 | 11.309204 | 7 3 |
| 0 4 | 8.991302 9.166520 | 9.997904 | 8.993398 9.171247 | 11.006602 | 10.002096 | 11.008698 | 7 1 |
| 1 | 9.290236 | 9.991574 | 9.298662 | 10.701338 | 10.004126 | 10.709764 | 7 |
| 111 | 9.290230 | 9.986786 | 9.298002 | 10.701338 | 10.008426 | 10.709764 | 6 3 |
| l i i | 9.462824 | 9.980885 | 9.481939 | 10.518061 | 10.019115 | 10.537176 | 6 1 |
| 1 3 | 9.527488 | 9.973841 | 9.553647 | 10.446353 | 10.026159 | 10.472512 | 6 1 |
| 2 | 9.582840 | 9.965615 | 9.617224 | 10.382776 | 10.034385 | 10.417160 | 6 |
| 2 1 | 9.630992 | 9.956163 | 9.674829 | 10.325171 | 10.043837 | 10.369008 | 5 3 |
| 2 1 | 9.673387 | 9.945430 | 9.727957 | 10.272043 | 10.054570 | 10.326613 | 5 1/2 |
| 2 3 | 9.711050 | | 9.777700 | 10.222300 | 10.066650 | 10.288950 | 5 1/4 |
| 3 | 9.744739 | 9.919846 | 9.824893 | 10.175107 | 10.080154 | 10.255261 | 5 |
| 3 1/4 | 9.775027 | 9.904828 | 9.870199 | 10.129801 | 10.095172 | 10.224973 | 4 2 |
| 3 3 | 9.802359 9.827084 | 9.888185 | 9.914173 9.957295 | 10.085827 | 10.111815 | 10.197641 | 4 4 |
| 4 | 9.849485 | 9.849485 | | | 10.150515 | | 4 |
| -8 | | | 10.000000 | 10.000000 | | 10.150515 | 4 |
| | Cosine. | Sine. | Cotang. | Tangent. | Cosec. | Secant. | 111111 |

| r | - | _ | - | m | | | 7 11 | | 11 000 | | | | | - | - | _ |
|---|----|----------|----------|--------------------|----------------|---------------------------|----------------------|----------------|------------------------|---------|------|-----------|--------------------|-----|-------|----------|
| 1 | 12 | 3 | | TABLE | | | Logarit | | nes, Tang | ents, | | 0.5 | | | | |
| 1 | | | 4 | 0 Ho | | Cosec. | Tang. | D. S. T. | Cotang. | Sécant | | 0 L D. | Degree. Cosine. | 111 | 777 | - |
| E | n. | 8. | = | | = | | | 17. 5. 1. | | | | | | = | m. | s. () |
| 1 | 0 | 0 | 0 | | | finite. 536274 | 0.000000 6.463726 | 501717 | Infinite. 13.536274 | 10.0000 | | 00 | 000000 | | 0() | 56 |
| ı | | 8 | 2 | 764756 | | 235244 | | 293484 | 235244 | 0000 | | 00 | 000000 | | П | 52 |
| ı | | 12 | 3 | 940847 | | 059153 | 940847 | 208231 | 059153 | | | 00 | 000000 | 57 | 117 | 48 |
| ł | | 16 | 4 | | | | 7.065786 | | 12.934214 | | | 00 | 000000 | | | 44 |
| ı | | 20 | 5 | 162696 | | 837304 758123 | | 131969 | 837304 | | | 00 | 000000 | _ | | 40 |
| ı | | 24 28 | 7 | 241877 308824 | | 691176 | 308825 | | 758122 691175 | | | 01 | 9.999999 999999 | | | 36 32 |
| ı | | 32 | 8 | 366816 | | 633184 | 366817 | 85254 | 633183 | | | 01 | 999999 | | | 28 |
| ı | | 36 | 9 | 417968 | | 582032 | 417970 | 76263 | 582030 | | | 01 | 999999 | | | 24 |
| ı | | 40 | | 463725 | | 536275 | 463727 | 68988 | 536273 | 0000 | - | 01 | 999998 | | | 20 |
| ı | | | 11 12 | 505118 542906 | | 494882 457094 | 505120 542909 | 62981 57934 | 494880 457091 | 0000 | | 01 | 999998 999997 | | | 16 12 |
| ı | | 52 | | 577668 | | 422332 | 577672 | 53642 | 422328 | 0000 | | 01 | 999997 | | | 8 |
| L | | 56 | | 609853 | | 390147 | 609857 | 49939 | 390143 | 0000 | | 01 | 999996 | | | 4 |
| - | 1 | 0 | 15 | 7.639816 | 12. | 360184 | 7.639820 | 46715 | 12.360180 | 10.0000 | 04 (| 01 | 9.999996 | 45 | 59 | 0 |
| ı | | | 16 | 667845 | | 332156 | 667849 | 43882 | 332151 | 0000 | | 01 | 999995 | | | 56 |
| ı | | | 17 | 694173 | | 305827 | 694179 | 41373 | 305821 | 0000 | | 01 | 999995 | | | 52 |
| | | 12 16 | | 718997 742477 | | 281003 257523 | 719003 742434 | 39136 37128 | 280997 257516 | 0000 | | 01 | 999994 999993 | | | 48 |
| ı | | 20 | | 764754 | | 235246 | 764761 | 35136 | 235239 | 0000 | | oi | 999993 | | | 40 |
| ı | | | 21 | 785943 | | 214057 | 785951 | 33673 | 214049 | 0000 | | 01 | 999992 | | | 36 |
| ı | | | 22 | 806146 | | 193854 | 806155 | 32176 | 193845 | , 0000 | . 1 | 01 | 999991 | | | 32 |
| ١ | | 32 36 | 24 | 825451 843934 | | 1 7454 9 156066 | 825460 843944 | 30806 29548 | 174540 156056 | 0000 | | 01 | 999990 999989 | 1 - | н | 28 |
| ı | | 40 | | 861662 | | 138338 | 861674 | 28389 | 138326 | | | 02 | 999988 | | | 20 |
| ı | | | 26 | 878695 | | 121305 | 878708 | 27318 | 121292 | 0000 | | 02 | 999988 | 34 | + | 16 |
| ı | | | 27 | 895085 | | 104915 | 895099 | 26324 | 104901 | 0000 | | 02 | 999987 | | | 12 |
| ı | | 52 | | 910879 926119 | | 089121 073881 | 910894 926134 | 25400 24539 | 089106 073866 | 0000 | | 02 | 999986 999985 | | | 8 |
| ŀ | _ | 56 | | 7.940842 | - | 059158 | 7.940858 | 23734 | 12.059142 | | | 05 | 9.999983 | | 20 | 0 |
| ı | 2 | | 31 | 955082 | | 044918 | 955100 | 22981 | 044900 | 0000 | | 02 | 9.999983 | | 38 | 56 |
| ı | | | 32 | 968870 | | 031130 | 968889 | 22274 | 031111 | 0000 | . 1 | 02 | 999981 | | 1 | 52 |
| ı | | 12 | 33 | 982233 | | 017767 | 982253 | 21609 | 017747 | 0000 | |)2 | 999980 | 27 | 1 | 48 |
| ı | | 16 | | 995198 | | 004802 | 995219 | 20982 | 004781 | 0000 | | 02 | 999979 | | | 44 |
| ı | | 20 24 | | 8.007787 020021 | | 992213 979979 | 8.007809 020045 | 20391 19832 | 11.992191 979955 | 0000 | | 02 | 999977 999976 | | | 40 36 |
| ı | | 28 | | 031919 | | 968081 | 031945 | 19304 | 968055 | 0000 | | 12 | 999975 | | | 32 |
| ı | | 32 | | 043501 | 1 | 956499 | 043527 | 18802 | 956473 | 0000 | | 30 | 999973 | | | 28 |
| ı | | 36 | | 054781 | | 945219 | 054809 | 18326 | 945191 | 0000 | | 02 | 999972 | | | 24 |
| ı | | | 40 | 065776 | | 934224 923500 | 065806 076531 | 17873 17443 | 934194 923469 | 0000 | - 1 | 02 | 999971 999969 | | | 20 |
| ı | | 44 48 | 41 | 076500 086965 | | 913035 | 086997 | 17033 | 913003 | 0000 | | 2 | 999968 | _ | 11 | 16 12 |
| ı | | 52 | | 097183 | | 902817 | 097217 | 16640 | 902783 | 0000 | | 02 | 999966 | | | 8 |
| L | | 56 | 44 | 107167 | | 892833 | 107202 | 16267 | 892797 | 0000 | 36 0 | 03 | 999964 | 16 | | 4 |
| ľ | 3 | | | 8.116926 | | | 8.116963 | 15909 | 11.883037 | | | 03 | 9.999963 | | 57 | 0 |
| l | | | 46 | 126471 | | 873529 | 126510 | 15567 | 873490 | 0000 | | 03 | 999961 | | | 56 |
| ı | | 8 12 | 47 48 | 135810 144953 | | $864190 \\ 855047$ | 135851 144996 | 15240 14926 | 864149 855004 | 0000 | | 03 | 999959 999958 | _ | | 52 48 |
| ı | | | 49 | 153907 | | 846093 | 153952 | 14624 | 846048 | 0000 | | 03 | 999956 | | | 44 |
| ı | | 20 | | 162681 | | 837319 | 162727 | 14334 | | | | 03 | 999954 | | | 40 |
| ı | | 24 | 51 | 171280 | | 828720 | | | | | | | 999952 | | | 36 |
| l | | 28 | | | | 820287 812015 | | | | | | | 999950 | _ | | 32 |
| I | | 32 36 | | | 1 | 803898 | | | | | | | 999948 999946 | | | 21 |
| ۱ | | 40 | | | | 795930 | | | | | | | 999944 | 5 | | 20 |
| 1 | | 44 | 56 | 211895 | | 788105 | | | .788047 | 0000 | 58 0 |)4 | 999942 | | | 16 |
| 1 | | 48 | | | | 780419 | | | | | | | 999940 | | | 12 |
| 1 | | | 58 59 | | | 772866 765443 | | | | | | | 999938 999936 | | | 8 |
| 1 | 4 | | 60 | | | 758145 | | 11965 | 758079 | | |)4 | 999934 | _ | 56 | 0 |
| 1 | n. | 8. | = | Cosine. | - | ecant. | Cotang. | | Tang. | Cosec. | | = | Sine. | | m. | F. |
| F | | - 04 | - | 5 Ho | A. Contraction | | cottang. | or | | Cosec. | - | D | egrees. | | EXI- | |
| t | D | D | - | | 5" | 3560 | 1s | 15" | 3560 | 18 | | 5" | 0 | | - | |
| 1 | | P. or | | 2 3 | 0 | 7120 | 2 | 30 | 7120 | 2 | . 30 | | 0 | | P. or | |
| 1 | 3 | dI. | | 3 4 | 5 | 10680 | 3 | 4.5 | 10681 | 3 | 4. | 5 | 1 | 5 | or | |

| Note | 1 | - | BLE V. | В | TA | | -Y | eants. | and Sec | And o'T. | -100 | - | | - | - | - |
|---|-------|----|----------|-----|------|------|----------|-----------|---------|----------|----------|-----|----------|----|----|----|
| No. | | | | | | | | | | | | 011 | 0 Ho | | | |
| 4 0 0 S.241855 1.758145 S.24192 11965 1.758079 1.000066 04 9.99993 50 4 1 249033 750967 249102 11770 750998 000061 04 9.99925 58 8 2 860944 743905 256165 11592 743855 000071 04 999925 58 12 3 263042 736955 263115 11400 736885 000073 04 999925 58 12 3 263042 736955 263115 11400 736885 000073 04 999925 58 20 5 276614 723386 276691 11052 723309 000075 04 999925 58 22 6 283943 716757 283323 30885 716677 000005 04 999925 58 23 8 296207 703793 286929 10568 703708 000055 04 999915 52 36 6 3 302546 697454 302684 10246 697366 000087 04 999915 52 36 6 3 302546 697454 302684 10268 691116 000000 04 999915 52 36 6 3 302546 697454 302684 10268 691116 000000 04 999915 52 36 6 3 302546 697454 303684 10268 691116 000000 04 999915 52 36 1 3 327016 672984 327114 9849 672866 000087 04 999917 40 48 12 321027 678973 321122 9984 678876 000093 04 999902 40 48 12 321027 678973 32719 9849 672866 000098 04 99902 40 46 13 34504 655496 344610 9463 656390 000106 05 999994 40 46 14 344504 655496 344610 9463 655390 000106 05 999981 12 18 355783 644217 358856 5958 1166144 10000103 05 999987 40 42 11 371171 637389 372692 9726 641723 838856 5983 633105 000112 05 999885 41 40 23 33101 606899 303293 633105 000112 05 999879 30 40 23 33101 606899 303234 8467 606766 000130 05 999871 30 41 22 387462 612038 386805 86787 00012 05 999871 30 41 22 387462 612038 386805 86787 000144 05 999885 35 22 447469 575858 427618 74858 74 | ′ m. | 1 | | | | | Secont | Cotong | | Tana | | Ju. | | / | 01 | 20 |
| 4 249033 750967 249102 11770 750805 000065 04 99928 58 2 86094 74809 256165 11589 74835 000073 04 99929 58 12 3 263042 736058 263115 11400 73885 000073 04 99929 56 12 3 263614 723386 276691 11032 723309 000078 04 99922 56 20 5 276614 723386 276691 11032 723309 000078 04 99922 56 20 5 276614 723386 276691 11032 723309 000078 04 99922 56 26 276614 723386 276691 11032 723309 000078 04 99922 56 276614 723386 276691 11032 723309 000078 04 999928 26 276614 723386 276691 11032 723309 000078 04 999918 33 36 302546 69744 302634 10146 697366 000087 04 999915 34 04 01 036794 691206 308884 10268 691116 000090 04 999918 04 04 036794 691206 308884 10268 691116 000090 04 999918 04 04 036794 691206 308884 10268 691116 000090 04 999918 04 04 036794 04 04 04 04 04 04 04 | | = | | = | | | | | | | | - | | _ | | _ |
| S | | | | 9 | _ | | | | | | | | | | | 4 |
| 12 3 263042 736958 263115 11400 736855 000075 04 999925 56 20 5 276614 723356 276601 11052 723300 000075 04 999925 56 22 6 28873 716737 710227 28955 10724 710144 000062 04 999915 33 32 296207 703793 296292 10568 703708 000055 04 999915 33 36 3 02546 697454 302034 10416 697356 000057 04 999915 33 36 3 02546 697454 302034 10416 697356 000057 04 999915 34 04 01 036794 691206 30884 10466 697356 000057 04 999915 34 04 01 036794 691206 30884 10466 697356 000057 04 999915 34 04 01 036794 691206 30884 10466 697356 000057 04 999915 34 04 01 036794 691206 338854 06776 038854 10668 691116 000090 04 999915 04 04 04 04 04 04 04 0 | | | | 1 | | | | | | | | | | | | |
| Texas | | | | 1 | | | | | | | | | | | | |
| 20 5 276614 729386 276691 11052 723309 000076 04 999928 53 24 6 288243 716757 283323 10885 716677 000080 04 999918 53 32 8 2962077 703793 296292 10568 703708 000085 04 999918 53 36 9 302546 697404 302684 10416 697366 000087 04 999918 53 40 10 306794 691206 308884 10268 691116 000090 04 999918 54 411 141934 658046 315046 10124 681951 000093 04 999918 54 52 13 321016 7678973 321122 9984 678878 000093 04 99990749 48 12 321037 678973 321122 9984 678878 000093 04 9999074 56 14 332924 667076 333025 9716 666975 000101 05 999902 47 56 14 332924 667076 333025 9716 666975 000101 05 999991 56 14 34504 65546 344610 9463 653390 00010 05 9999994 44 11 34504 65546 344610 9463 653390 00010 05 9999914 12 12 18 355783 644217 35595 922 644105 000112 05 999981 16 19 361315 63865 361430 9106 638570 000112 05 999888 12 16 19 361315 63865 361430 9106 638570 000112 05 999888 12 16 19 361315 63865 361430 9106 638570 000112 05 999887 13 20 20 366777 633223 368895 8993 633105 000118 05 999888 12 22 377499 622301 377622 8775 622378 000124 05 999879 33 36 24 387962 6172788 332898 9670 617111 000127 05 999879 33 36 24 387962 6172788 332898 9670 617111 000127 05 999878 33 62 4 387962 6172788 332898 9670 617111 000127 05 999878 33 62 4 387962 6172788 332898 9670 617111 000127 05 999878 33 63 64 34 34 34 34 34 34 34 34 34 34 34 34 34 | | 1 | | 1 | | - 6 | | | | | | | | | | |
| 28 7 289773 710227 289586 10724 710144 000080 04 999918 33 38 296207 703793 296592 10568 703705 000085 04 999918 33 36 9 302546 69744 302634 10416 697366 000087 04 999918 31 4010 306794 691206 308884 10268 691116 000090 04 999910 30 44 11 314954 635046 315046 10124 684954 000093 04 999910 30 50 50 50 50 50 50 50 50 50 50 50 50 50 | | | | ŀ | | | | | | | | | | | | |
| 28 1 289773 710227 289856 10724 710144 000062 04 999915 32 36 9 302546 697454 302634 10416 697366 000087 04 999915 32 4010 305794 691206 308884 10416 697366 000087 04 999913 30 40 10 305794 691206 308884 10416 684951 000093 04 999907 49 48112 314954 653046 315046 10124 684951 000093 04 999907 49 48112 321016 672944 327114 9849 678878 000095 04 999907 49 5213 327016 676973 321122 9984 678878 000095 04 999907 49 5614 332924 667070 333025 9716 666975 000101 05 999902 47 416 344504 655466 344610 9463 655390 000106 05 999997 44 15 1218 355783 642417 35595 9222 44105 000112 05 999981 44 15 1218 355783 642417 35595 9222 44105 000112 05 999988 16 19 361315 63865 361430 9106 635570 000112 05 999988 12 118 355783 642417 35595 9222 44105 000112 05 999988 12 16 19 361315 63865 361430 9106 635570 000112 05 999988 12 16 19 361315 63865 361430 9106 635570 000112 05 999885 12 12 18 355783 64217 35595 9998 983 627702 000112 05 999885 12 12 12 12 12 12 12 12 12 12 12 12 12 | | | | l | | | | | | | | | | | | |
| 30 302446 6697454 302634 10416 697366 000087 04 999915 51 40 10 305794 6691206 308884 10268 691116 000090 04 999910 50 44 11 314954 685046 315046 10124 684954 000093 04 999905 18 48 12 321027 678973 321122 9984 678878 000095 04 999905 18 52 13 327016 6702984 327114 9849 672886 000095 04 999905 18 56 14 332924 667076 333025 9716 666975 000101 05 999999 18 5 15 3338753 11.661247 8338855 9588 11.661144 10.000103 05 999999 18 5 16 344504 655496 344610 9463 655390 000106 05 999999 18 6 17 350181 649819 350289 9340 649711 000109 05 999891 18 12 18 355783 644217 35895 9222 644105 000112 05 999885 10 20 20 366777 633223 366895 8993 633105 000115 05 999885 10 20 20 366777 633223 366895 8993 633105 000112 05 999878 18 22 32 3238762 612038 388092 8567 617111 001127 05 999875 38 32 23 382762 612038 388092 8567 617111 001127 05 999875 38 44 26 398179 601821 398815 8369 601685 000136 05 999870 36 44 26 398179 601821 398815 8369 601685 000136 05 999861 33 52 28 40161 591899 408304 8180 591696 000142 05 999887 36 4 32 427462 572558 427618 7826 572382 000166 06 999844 28 23 447649 534059 446110 7502 533890 000169 06 999881 30 4 4 4 67985 532015 468172 7132 531828 000160 06 999881 12 44640 549560 54069 549431 7425 549887 000160 06 999881 12 44640 549560 54069 549431 7425 549887 000160 06 999881 12 5237 440440 549560 54069 549431 7425 549887 000160 06 999881 12 5237 440440 549560 54069 54969 54969 54969 54969 54969 54969 54969 54969 54969 54969 54969 54969 54969 54969 | | | | | | | | | | | | | | 7 | | |
| 40 10 305794 661206 305884 10268 691116 000090 04 999910 50 44 11 314954 655046 315046 10124 684954 000093 04 9999074 88 12 321027 678973 321122 9984 678878 000095 04 999902 47 56 14 329294 667076 33202 9716 666975 000101 05 999809 14 56 14 329294 667076 33202 9716 666975 000101 05 999899 16 50 015 8.338753 11.661247 8.338856 9588 11.661144 10.000103 05 999899 18 4 16 344504 655496 344610 9463 655390 000106 05 999899 18 12 18 355783 644217 355895 9222 644105 000112 05 999888 12 12 18 355783 644217 355895 9222 644105 000112 05 999888 12 20 20 366777 633223 366895 8993 633105 000118 05 999887 18 20 20 366777 633223 366895 8993 633105 000118 05 999878 12 21 22 374499 622501 377622 8773 622378 000124 05 999878 18 22 3738906 610238 388989 8670 617111 000127 05 999878 18 23 22 378499 622501 377622 8773 622378 000124 05 999878 18 24 26 387962 610238 388989 25670 611908 000130 05 999878 18 24 26 387962 610238 388989 25676 611908 000130 05 999878 18 24 27 403199 596801 403339 8274 596662 000139 05 999876 18 25 28 403161 591889 408304 8180 591696 000142 05 999887 35 25 28 403161 591889 408304 8180 591696 000142 05 999887 35 26 29 413068 586932 413213 8099 56662 000139 05 999861 32 28 32 374494 59560 403339 8274 596662 000139 05 999861 32 28 32 347462 572558 427618 7826 572892 000164 06 999884 12 28 32 34564 567844 432315 7743 567685 000164 06 999884 12 28 33 432156 567844 432315 7743 567685 000169 06 999884 12 28 33 4364 44594 554099 44610 7502 533990 000169 06 999881 22 28 33 44594 554099 44610 7502 533990 000169 06 999831 22 28 34 36 445941 554099 44610 7502 533990 000169 06 999881 22 28 35 44594 545609 44610 7502 533990 000169 06 999831 22 28 36 44594 545609 44610 7502 533990 000169 06 999881 27 28 36 44594 545609 44610 7502 533990 000169 06 999881 27 28 37 440440 549560 450613 7425 549387 000169 06 999881 27 28 36 44594 545609 54610 7500 53399 000169 06 999881 27 28 37 440440 549560 56860 56860 55860 000169 06 999881 27 28 36 44594 545609 54660 56860 55860 000169 06 999881 20 29 55 54434 44698 55560 6686 468610 55260 | 52 | 59 | 999915 | | 04 | 085 | 00008 | 703708 | 10568 | 296292 | 703793 | 7 | 296207 | 8 | 32 | |
| 48 12 321027 678973 321122 9984 678878 000093 04 99990749 48 12 321027 678973 321122 9984 678878 000095 04 99990749 56 14 332924 667076 333025 9716 666975 000101 05 998990 64 5 0 15 8338753 11.661247 8338855 9588 16661144 1000103 05 999899 66 617 37618 649819 350289 9340 649711 000109 05 999891 43 12 18 355783 644217 355895 9222 644105 000112 05 999891 43 12 18 355783 644217 355895 9222 644105 000112 05 999889 14 16 19 361315 638685 361430 9106 638570 000115 05 999885 14 16 19 361315 638685 361430 9106 638570 000115 05 999885 14 12 18 3523 382762 617238 382889 867708 000121 05 999879 39 12 18 12 372171 627829 372292 883 627708 000121 05 999879 39 12 18 12 372171 627829 372292 883 627708 000121 05 999879 39 12 18 18 35685 6992 8567 611908 000130 05 999870 38 12 18 387962 612038 388092 8567 611908 000130 05 999870 38 14 26 398179 601821 398315 8369 601685 000138 05 999870 36 14 26 398179 601821 398315 8369 601685 000138 05 999870 36 14 26 398179 601821 398315 8369 601685 000138 05 999864 34 18 27 403199 506801 403338 8274 596662 000139 05 999861 33 12 28 427462 572858 413213 8089 866787 000144 05 999885 38 15 23 427462 572858 427618 7826 572882 000169 06 999848 29 12 33 427462 572858 427618 7826 572882 000169 06 999844 28 12 33 44460 5440 549560 43061 7728 58660 41610 7502 553890 000169 06 999841 21 12 33 436800 563200 436862 7660 553036 000169 06 999841 21 12 33 44469 5440 549560 43061 7428 549897 000177 06 999887 23 12 33 44469 5440 549560 43061 7428 549897 000179 06 99980 16 12 32 34 44464 54985 532015 44817 7732 534897 000179 06 99980 16 12 44 46 488963 511037 489170 7739 544980 000160 06 99980 16 12 44 46 488963 511037 489170 7739 544980 000160 06 99980 16 12 44 5441 554059 44610 7502 553890 000169 06 99980 16 12 44 5441 554059 44610 7502 553890 000169 06 99980 16 12 45 445041 554059 44610 7502 553890 000169 06 99980 16 12 45 45 445041 554059 44610 7502 553890 000169 06 99980 16 12 45 45 445041 554059 44610 7502 553890 000169 06 99980 16 12 45 45 45 45 45 45 45 45 45 45 45 45 45 | | | | | | | | | | | | | | | | |
| 48 12 321027 678973 321122 9984 678878 000095 04 999905 48 52 13 327016 672984 327114 9849 672886 000098 04 999905 47 56 14 338924 667070 333025 9716 666975 000101 05 999899 47 56 14 338924 667070 330025 9716 666975 000101 05 999899 48 49 416 344504 655496 344610 9463 655390 000106 05 999899 44 416 344504 655496 344610 9463 655390 000106 05 999899 44 416 344504 655496 344610 9463 655390 000109 05 999899 44 416 34504 50180 40181 | | | | 1 | | | | | | | | | | | | |
| \$\frac{5}{5}\frac{14}{3}\frac{32}{2}\frac{6}{6}\frac{6}{7}\frac{6}{6}\frac{14}{3}\frac{32}{2}\frac{6}{6}\frac{6}{7}\frac{7}{6}\frac{33}{3}\frac{32}{2}\frac{5}{6}\frac{14}{6}\frac{32}{3}\frac{22}{2}\frac{6}{6}\frac{6}{7}\frac{7}{6}\frac{6}{6}\ | | | | | | | | | | | | - 1 | | | | |
| 50 14 332924 667070 333925 9716 666975 000101 05 999899 45 10 15 3338753 11.661247 8.338856 9588 11.661144 10.000103 05 9998991 45 11 619 344504 655390 000106 05 999894 48 12 18 355783 644217 355895 9222 644105 000112 05 999881 43 12 18 355783 644217 355895 9222 644105 000112 05 999881 43 12 18 355783 644217 355895 9222 644105 000112 05 999885 41 20 20 366777 633223 366895 8993 633105 000116 05 999885 41 24 21 372171 627829 37229 8833 627708 000121 05 999879 39 28 22 377499 622501 377622 8775 622378 000121 05 999879 39 28 22 377499 622501 377622 8775 622378 000124 05 999873 39 32 23 382762 617238 38289 8670 617111 000127 05 999873 39 40 25 393101 606899 393234 8467 606766 000133 05 999870 36 40 25 393101 606899 393234 8467 606766 000133 05 999870 36 42 42 63 398179 601821 398815 8369 601685 000136 05 999864 34 42 63 398179 506801 403339 8274 596662 000139 05 999861 33 52 28 408161 591839 408304 8180 591696 000142 05 999851 36 52 28 408161 591839 408304 8180 591696 000142 05 999851 36 52 28 408161 591839 408304 8180 591696 000142 05 999851 36 6 030 8.417919 11.582031 8.418068 586932 413213 8089 866787 000146 05 999854 36 12 33 428156 567844 432815 7743 567685 000166 06 999844 27 10 34 436800 563200 436962 7660 563038 000169 06 999844 27 10 34 436800 563200 436962 7660 563038 000169 06 999844 27 10 34 436800 563200 436962 7660 563038 000169 06 999844 27 10 34 446800 563200 436962 7660 563038 000169 06 999844 27 10 34 448690 563200 436992 54981 770 570837 44998 523502 476693 59995 51080 000109 06 999801 12 44 42 467985 523502 476693 6995 525440 000169 06 999801 12 44 44 44 467985 523502 476693 6995 523507 00019 06 999801 12 44 44 44 44 467985 523502 476693 6995 525440 000169 06 999801 12 44 44 44 44 44 44 44 44 44 44 44 44 44 | | | | | | | | | | | | | | | | |
| The color of the | | | | 1 | | | | | | | | | | | | |
| 4 16 344504 655496 344610 9463 655390 000106 05 999894 44 817 3×0181 649819 350289 9340 649711 000109 05 999891 43 12 18 355783 644217 355895 922 644105 000112 05 999885 42 16 19 361315 638685 361430 9106 638570 000113 05 999885 42 20 20 366777 633223 366895 8993 633105 000118 05 999882 40 24 21 372171 627829 372292 8883 627708 000121 05 999879 38 32 23 382762 617238 382895 8670 617111 000127 05 999870 38 32 23 382762 617238 382895 8670 617111 000127 05 999873 37 36 24 387962 612036 388092 8567 611906 000130 05 999870 38 44 26 398179 601821 398315 8369 601685 000136 05 999867 35 44 26 398179 601821 398315 8369 601685 000136 05 999867 35 42 80 40 25 393101 606899 393234 8467 606766 000133 05 999867 35 22 8 408161 591839 408504 8180 591696 000142 05 999854 31 52 8 408161 591839 408504 8180 591696 000142 05 999854 31 52 8 408161 591839 408504 8180 591696 000142 05 999854 31 56 29 413068 586932 413213 8089 58675 000146 05 999854 31 56 29 413068 586932 413213 8089 58675 000146 05 999854 31 56 29 413048 58696 44386 591696 000142 06 999854 31 56 29 413048 58696 44386 591696 000142 06 999854 31 56 29 413048 58696 441806 563200 436962 5660 563035 000166 06 999844 28 12 33 432156 567844 432315 7743 567685 000159 06 999844 28 12 33 432156 567844 432815 7743 567685 000159 06 999843 25 43 64 4494 54969 54960 450613 7425 549387 000173 06 999887 33 28 454893 545107 455070 7349 544930 000160 06 999834 25 44364 449846 53605 445941 54969 54941 776 540519 000180 06 99980 18 54494 440 549565 53035 48690 5735 5300 000169 06 99983 26 544 440 549560 450613 7425 54059 000169 06 99983 25 5444 440 549560 450613 7425 54059 000169 06 99983 25 5444 440 549560 450613 7425 54059 000169 06 99983 25 5443 446498 523502 476693 6995 523507 000173 06 999887 33 23 44640 54998 54941 776 540519 000180 06 99980 16 55444 440 549560 54060 54 | | - | | - | | - | | | | | | | | - | _ | _ |
| Sel 17 3-50 18 649e15 3-50989 9340 649711 000103 05 999881 13 12 18 355783 644217 355895 9222 644105 000112 05 999885 14 12 18 355783 644217 355895 9222 644105 000112 05 999885 14 12 12 12 12 12 12 12 | | | | 1 | | | | | | | | | | | | 5 |
| 12 18 355783 644217 355895 9222 644105 000115 05 999885 12 16 19 361315 638685 361430 9106 638570 000115 05 999885 12 12 17 627829 372292 8833 633105 000115 05 999885 12 12 17 627829 372292 8833 633105 000115 05 999876 38 32 37499 622501 377622 8775 622378 000124 05 999876 38 32 23 382762 617238 382898 8670 611711 000127 05 999873 36 24 387962 612038 388092 8567 611905 00130 05 999873 37 44 26 398179 601821 398315 8369 601685 000136 05 999867 38 42 27 403199 596801 403338 8274 596662 000139 05 999867 38 52 28 408161 591839 408804 8180 591660 000142 05 999854 31 55 629 413068 586932 413213 3089 566787 000146 05 999854 32 56 29 413068 586932 413213 3089 566787 000146 05 999854 32 431434 4346800 663200 436962 660 563038 000162 06 999844 28 29 23 445800 663200 436962 660 563038 000162 06 999848 29 29 34 445800 563200 445692 45060 530338 000162 06 999834 28 28 34 454893 545107 455070 7349 544930 000177 06 999832 28 446498 528502 476693 53045 48110 7502 533890 000160 06 999831 24 44 467985 532015 468172 7132 531828 000180 06 999812 19 5243 476498 523502 476693 6935 523307 000190 06 999801 15 4842 4842 487078 503924 47693 56355 52434 476498 523502 476693 6935 523307 000190 06 999801 15 4842 4842 48400 50306 489802 501288 6612 48702 000218 07 999793 16 4842 | | | | | | | | | | | | | | | | |
| 16 | | | | | | | | | | | | | | | | |
| 20 20 366777 633223 366895 8993 633105 000118 05 999879 39 24 21 372171 627829 372292 8883 627708 000121 05 999879 39 28 22 377499 622501 377622 8775 622378 000124 05 999876 38 36 24 387962 612038 388092 8567 611908 000130 05 999870 36 40 25 393101 606899 393234 8467 606766 000133 05 999867 35 44 26 399179 601821 399315 8369 601685 000136 05 999867 35 44 26 399179 506801 403338 8274 596662 000139 05 999867 35 48 27 403199 506801 403338 8274 596662 000139 05 999867 35 413068 586932 413213 8089 586787 000142 05 999858 32 413048 431 422717 577283 422869 7912 577131 000152 06 999848 29 832 427462 572538 427618 7826 572382 000160 06 999848 29 832 427462 572538 427618 7826 572382 000160 06 999848 20 20 35 441394 558606 441560 7560 558440 000160 06 999831 24 28 45940 540590 450613 7425 549387 000173 06 999823 22 23 4454893 544007 455070 7349 544930 000170 06 999823 24 24 44 467985 532737 474945 7705 545890 000160 06 999812 24 24 24 26 352737 474945 52436 476498 523502 476693 69985 51908 000180 06 999810 24 44 467985 532701 46892 6928 519108 000190 06 999801 25 24 36 44 480903 511937 48092 6928 519108 000190 06 999801 26 24 24 24 24 24 24 24 | | | | | 1 - | | | | | | | | | | | |
| 24 21 372171 627829 372292 8835 627705 000121 05 999876 38 28 22 377499 622501 377622 8775 622378 000124 05 999876 38 32 23 382762 617238 382899 8670 617111 000127 05 999876 38 36 24 387962 612038 388099 8567 611905 000130 05 999876 38 40 25 393101 606899 393234 8467 606766 000133 05 999867 38 44 26 393179 601821 398315 8369 601685 000136 05 999867 35 42 40 3199 506801 403338 8274 596662 000139 05 999861 35 52 28 408161 591839 408304 8180 591696 000142 05 999858 36 56 29 413068 586932 413213 8089 586787 000146 05 999858 36 56 29 413068 586932 413213 8089 586787 000146 05 999854 31 6 0 30 8.417919 11.582081 8.418068 8000 11.581932 10.000149 06 9.999854 31 2 33 432156 567844 432315 7743 567685 000159 06 999844 28 12 33 432156 567844 432315 7743 567685 000159 06 999844 28 2 0 35 441394 558606 441560 7580 558440 000160 06 999834 28 2 4 36 445941 554059 446110 7502 553890 000169 06 999831 24 2 8 37 450440 549560 450613 7425 549387 000170 06 999831 24 3 2 3 454893 545107 455070 7439 544930 000177 06 999823 23 3 2 454693 545107 455070 7439 544930 000177 06 999823 23 3 2 47649 853502 476699 6998 523307 000169 06 999801 24 4 441 467985 532015 468172 7132 531828 000168 06 999801 24 4 442 467985 532015 468172 7132 531828 000168 06 999801 25 5 24 34 476498 523502 476693 6995 523307 000199 06 999801 12 4 44 479304 506960 493250 6735 56767 000019 06 999801 12 4 44 93040 506960 493250 6735 506767 000019 06 999901 12 4 45 497078 502922 497293 6673 502707 000218 07 999797 15 4 45 501080 498920 501298 6612 498702 000218 07 999798 11 4 45 497078 502922 497293 6673 502707 000218 07 999798 11 4 45 501080 488920 501298 6612 498702 000218 07 999798 12 2 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 | | | | - | | | | | | | | | | | | |
| 28 22 377499 622501 377622 8775 622378 000124 05 999876 38 32 23 382762 617238 382889 8670 617111 000127 05 999873 37 36 24 387962 612038 388092 8567 611908 000130 05 999870 36 40 25 393101 606899 393234 8467 606766 000133 05 999867 35 44 26 398179 601821 398315 8369 601685 000136 05 999867 35 42 42 403199 566801 403338 8274 596662 000139 05 999861 33 52 28 408161 591839 408304 8180 591696 000142 05 999858 35 52 28 413018 586932 413213 8089 586787 000146 05 999858 36 52 24 413068 586932 413213 8089 586787 000146 05 999858 32 427462 572538 427618 7826 572382 000166 06 999844 27 13 436800 563200 436962 7660 563303 000162 06 999834 21 23 432156 567844 432315 7743 567685 000169 06 999834 22 23 44394 554659 44150 7502 553890 000169 06 999834 22 23 445494 554059 44610 7502 553890 000169 06 999834 22 23 454893 545107 455070 7349 544930 000177 06 999823 23 23 454893 545107 455070 7349 544930 000177 06 999820 23 43 448690 553354 468172 7132 531828 000189 06 999812 19 44842 472263 527374 474545 7063 527546 000199 06 999810 16 4444 467985 523502 476693 6998 523307 000199 06 999801 16 4444 48963 511937 480892 6928 519108 000199 06 999801 16 444 48963 511937 480892 6928 519108 000199 06 999801 16 444 48963 511937 480892 6928 519108 000199 06 999801 16 444 467985 523502 476693 6998 523307 000199 06 999801 16 444 467985 532502 476693 6998 523307 000199 06 999801 16 444 445 | | | | | | | | | | | | | | | | |
| 32 23 382762 617238 382899 8670 617111 000127 05 999873 37 62 43 87962 612038 388092 8567 611908 000130 05 999873 37 64 25 393101 606899 393234 8407 606766 000133 05 999867 35 44 26 398179 601821 308315 8369 601685 000136 05 999867 35 52 28 408161 591839 408304 8180 591696 001142 05 999865 32 52 28 408161 591839 408304 8180 591696 001142 05 999858 32 413068 586932 413213 8089 586787 000146 05 999854 31 431 422177 577283 422869 7912 577131 000152 06 999844 28 32 427462 572538 427618 7826 572382 000156 06 999844 28 12 33 432156 567844 432315 7743 567685 000159 06 999844 28 12 33 432156 567844 432315 7743 567685 000169 06 999884 28 20 35 441394 558606 441560 7580 558440 00166 06 99983 28 28 37 450440 549560 450613 7425 549387 000173 06 999827 33 23 8 454893 545107 455070 7349 544930 000177 06 999827 33 23 8 454893 545107 455070 7349 544930 000170 06 999827 33 23 8 476498 53605 45613 7425 549387 000173 06 999827 33 24 476498 523502 476693 5695 523307 000189 06 999812 19 40 40 463665 536335 468849 7203 536151 000184 06 999827 33 24 476498 523502 476693 6995 523307 000199 06 999812 19 4441 467985 532015 468172 7132 531828 000189 06 999812 19 4441 467985 532015 468172 7132 531828 000189 06 999812 19 5243 476498 523502 476693 6995 523307 000199 06 999812 19 5243 476498 523502 476693 6995 523307 000199 06 999801 16 44 46 468665 546335 54784 47493040 506990 493250 6735 566750 000191 06 999809 16 20 50 505454 49955 505267 6552 494733 000220 70 999797 15 24 51 508974 491026 509200 6493 490800 000226 07 999774 16 44 55 524343 475657 524586 6266 475414 000243 07 999769 12 48 57 13828 468172 532898 6612 498702 000218 07 999769 12 52 53 512867 487133 513098 6435 486902 000231 07 999769 12 52 53 54561 500024 77 999778 16 52 52 53 55267 487133 513098 6435 486902 000231 07 999769 12 52 53 55267 531867 487133 513098 6435 486902 000231 07 999769 12 52 53 55267 531867 548749 55059 550567 6552 494733 000222 07 999778 18 52 52 53 55267 487133 513098 6435 486902 000231 07 999769 12 52 53 5524343 475657 524586 6266 475414 000243 07 9997 | | | | | | | | | | | | | | | | |
| 36 24 987962 612038 388092 8567 611908 000130 05 999870 36 40 25 393101 606899 393234 8467 606766 000133 05 999864 34 42 398179 601821 398315 8369 601685 000136 05 999864 34 827 403199 596801 403338 8274 596662 000139 05 999861 35 25 408161 591839 408304 8180 591696 000142 05 999855 35 629 413068 586932 413213 8089 586787 000146 05 999854 31 422717 577283 422869 7912 577131 000152 06 999854 31 83 4227462 572538 427618 7826 572382 000105 06 999844 25 23 432315 567844 432315 7743 567685 000159 06 999844 27 16 34 436800 563200 436962 7660 563038 000162 06 999838 26 24 36 445941 554059 446110 7502 553890 000169 06 999831 24 28 37 450440 549560 450613 7425 549387 000173 06 999827 33 33 454593 545107 455070 7349 544501 000180 06 999820 24 44 467985 532015 468172 7132 531828 000189 06 999816 20 40 40 463665 536335 463849 7203 536151 000184 06 999816 20 44 447263 527737 472454 77663 527364 000191 06 999809 16 52434 476498 523502 476693 6995 523307 000195 06 999809 16 52434 476498 523502 476693 6995 523307 000195 06 999801 16 49 501080 498925 511988 000199 06 999801 12 48 497078 502922 497293 6673 502707 000214 07 999790 12 48 497078 502922 497293 6673 502707 000214 07 999778 16 49 501080 498925 501298 6612 498702 000235 07 999778 16 49 501080 498925 501298 6612 498702 000247 07 999778 16 49 501080 49825 50267 6552 494733 000220 07 999778 17 18 15 18 18 18 18 18 18 | | | | - | | | | | | | | | | | | |
| 40 25 393101 606899 393234 8467 606766 000133 05 999867 35 44 26 393179 601821 398315 8369 601685 000136 05 999861 33 52 28 408161 591839 408304 8180 591696 000142 05 999858 32 52 84 408161 591839 408304 8180 591696 000142 05 999858 32 42 42 42 42 42 42 42 42 42 42 42 42 42 | | | | _ | | | | | | | | | | | | |
| 44 26 398179 601821 398315 8369 601685 000136 05 999864 34 48 27 403199 566801 403338 8274 596662 000139 05 999861 33 52 28 408161 591839 408304 8180 591696 000142 05 999851 32 56 29 413068 586932 413213 8089 586787 000146 05 999851 30 4 31 422717 577283 422869 7912 577131 000152 06 999851 30 8 32 427462 572535 427618 7826 572382 000156 06 999844 27 8 32 427462 572535 427618 7826 572382 000156 06 999844 27 16 34 436800 563200 436962 7660 563038 000162 06 999834 22 20 35 441394 558606 441560 7580 558440 000169 06 999834 22 24 36 445941 554059 446110 7502 553890 000169 06 999831 24 28 37 450440 549560 450613 7425 549387 000173 06 999827 23 32 38 454893 545107 455070 7349 544930 000177 06 999827 23 32 38 454893 545107 455070 7349 544930 000180 06 999828 24 44 44 467985 532015 468172 7132 531828 000184 06 999812 19 48 42 472263 527737 472454 7063 527546 000191 06 999812 19 48 42 472263 527737 472454 7063 527546 000191 06 999801 16 56 44 489663 519307 480892 6928 519108 000199 06 999801 16 46 488963 519307 480892 6928 519108 000199 06 999801 16 47 0 45 8 484848 11.516152 8 485050 6798 510830 000207 07 999790 13 48 47 493040 506960 493250 6735 506750 000210 07 999790 13 48 49 49076 50292 497293 6673 502707 000214 07 999790 13 48 47 493040 506960 493250 6735 506750 000210 07 999790 13 48 47 493040 506960 493250 6735 506750 000210 07 999790 13 48 47 493040 506960 493250 6735 506750 000210 07 999790 13 48 47 493040 506960 493250 6735 506750 000210 07 999778 12 48 49 5076 502922 497293 6673 502707 000214 07 999760 12 50 50 505045 494955 505267 6552 494733 000222 07 999778 12 50 50 505045 494955 505267 6552 494733 000222 07 999778 12 50 50 505045 494955 505267 6552 494733 000222 07 999778 12 50 50 505045 494955 505267 6552 494733 000222 07 999778 12 50 50 505045 494955 505267 6552 494733 000222 07 999778 12 50 50 505045 494955 505267 6552 494733 000222 07 999778 12 50 50 505045 494955 505267 6552 494733 000222 07 999774 12 50 50 505045 494955 505267 6552 494733 000222 07 999774 12 50 50 505045 494955 505267 6552 494733 00 | | | | | | | | | | | | | | | | |
| 48 27 | | | | - 2 | | | | | | | | 9 | 398179 | | | |
| 52 28 | | | | | | | | | | | | | | 27 | 48 | |
| 6 0 30 8.417919 11.582081 8.418068 8000 11.581932 10.000149 06 9.999818 30 431 422717 577283 422869 7912 577131 000152 06 999848 29 8 32 427462 572538 427618 7826 572382 000156 06 999848 29 12 33 432156 567844 432315 7743 567685 000159 06 999841 27 16 34 436800 563200 436962 7660 553038 000162 06 999838 26 20 35 441394 558606 441560 7580 558440 000166 06 999834 25 28 37 450440 549560 450613 7425 549387 000173 06 999827 23 32 38 454893 545107 455070 7349 544930 000177 06 999823 22 36 39 459301 540699 459481 7276 540519 000180 06 999820 21 40 40 463665 536335 463849 7203 536151 000184 06 999812 19 48 42 472263 527737 472454 7063 527546 000191 06 99980 18 52 43 476498 523502 476693 6995 523307 000195 06 99980 18 52 43 476498 523502 476693 6995 523307 000195 06 99980 18 52 43 476498 523502 476693 6995 523307 000195 06 99980 18 52 43 476498 523502 476693 6995 523307 000195 06 99980 18 52 43 476498 523502 476693 6995 523307 000195 06 99980 18 52 43 476498 523502 476693 6995 523307 000195 06 99980 18 52 43 476498 523502 476693 6995 523307 000195 06 99980 18 52 43 476498 523502 476693 6995 523307 000195 06 99980 18 52 43 476498 523502 476693 6995 523307 000195 06 99980 18 52 43 476498 523502 476693 6995 523307 000195 06 99980 18 52 43 476498 523502 476693 6995 523307 000195 06 99980 18 52 43 476498 523502 476693 6995 523307 000195 06 99980 18 52 43 476498 523502 476693 6995 523307 000195 06 99980 18 52 43 476498 523502 476693 6995 523307 000195 06 99980 18 52 43 476498 523502 476693 6995 523307 000195 06 99980 18 52 43 476498 523502 476693 6995 523307 000195 06 99980 18 52 43 476498 523502 476693 6995 523307 000195 06 99980 18 52 43 476498 523502 476693 6995 523307 000195 06 99980 18 52 43 476498 523502 4776693 6995 523307 000195 06 99980 18 52 43 476498 523502 4776693 6995 523307 000195 06 99980 18 52 43 476498 523502 4776693 6995 523307 000195 06 99980 18 52 43 476498 523502 4776693 6995 52350 00000000000000000000000000000000 | | | | | | | | | | | | | | 28 | 52 | |
| 8 32 427462 572538 427618 7826 572838 000152 06 999848 29 8 32 427462 572538 427618 7826 572838 000156 06 999844 27 16 34 436800 563200 436962 7660 563038 000162 06 999838 26 20 35 441394 558606 441560 7580 558440 000166 06 999834 25 28 37 456440 549560 450613 7425 533890 000173 06 999827 33 32 38 454893 545107 455070 7349 544930 000177 06 999827 33 32 38 454893 545107 455070 7349 544930 000177 06 999827 32 32 38 454893 545107 455070 7349 544930 000177 06 999827 32 32 38 454893 545107 455070 7349 544930 000177 06 999820 21 40 40 463665 533015 468172 7132 551828 000188 06 999812 19 48 42 472263 527737 472454 7063 527546 000191 06 999801 18 52 43 476498 523502 476693 6995 523307 000195 06 999801 17 56 44 486963 511937 480892 6928 519108 000199 06 999801 17 56 44 486963 511037 489170 6798 510830 000203 07 999797 15 4 46 488963 511037 489170 6798 510830 000200 07 999799 18 6 47 493040 506960 493250 6735 506750 000210 07 999799 18 6 47 493040 506960 493250 6735 506750 000210 07 999799 18 6 47 493040 506960 493250 6735 506750 000210 07 999799 18 6 49 501080 498920 501298 6612 498702 000218 07 999781 12 6 49 501080 498920 501298 6673 502707 000214 07 999780 12 6 52 512867 487133 513098 6673 502707 000214 07 999781 12 6 52 512867 487133 513098 6435 466902 000231 07 999778 12 6 52 512867 487133 513098 6435 466902 000231 07 999765 13 6 54 520551 479449 520790 6323 479210 000239 07 999761 63 6 54 520551 479449 520790 6323 479210 000239 07 999761 63 6 52 512867 487133 513098 6435 466902 000231 07 999765 13 6 54 520551 479449 520790 6323 479210 000239 07 999761 63 6 54 520551 479449 520790 6323 479210 000239 07 999761 63 6 54 520551 479449 520790 6323 479210 000239 07 999761 63 6 54 520551 479449 520790 6323 4761651 000247 07 999783 12 6 54 520551 479449 520790 6323 479210 000239 07 999761 63 6 54 520551 479449 520790 6323 479210 000239 07 999761 63 6 54 520551 479449 520790 6323 479210 000239 07 999765 63 6 54 520551 479449 520790 6323 479210 000225 07 999788 12 6 54 520551 479449 52056 6668 475414 000243 07 999785 12 6 59 | 31 | 13 | 999854 | 1 | 05 | 146 | 00014 | 586787 | 8089 | 413213 | 586932 | 8 | 413068 | 29 | 56 | |
| 8 32 427462 572538 427618 7826 572838 000152 06 999848 29 8 32 427462 572538 427618 7826 572838 000156 06 999844 27 16 34 436800 563200 436962 7660 563038 000162 06 999838 26 20 35 441394 558606 441560 7580 558440 000166 06 999834 25 28 37 456440 549560 450613 7425 533890 000173 06 999827 33 32 38 454893 545107 455070 7349 544930 000177 06 999827 33 32 38 454893 545107 455070 7349 544930 000177 06 999827 32 32 38 454893 545107 455070 7349 544930 000177 06 999827 32 32 38 454893 545107 455070 7349 544930 000177 06 999820 21 40 40 463665 533015 468172 7132 551828 000188 06 999812 19 48 42 472263 527737 472454 7063 527546 000191 06 999801 18 52 43 476498 523502 476693 6995 523307 000195 06 999801 17 56 44 486963 511937 480892 6928 519108 000199 06 999801 17 56 44 486963 511037 489170 6798 510830 000203 07 999797 15 4 46 488963 511037 489170 6798 510830 000200 07 999799 18 6 47 493040 506960 493250 6735 506750 000210 07 999799 18 6 47 493040 506960 493250 6735 506750 000210 07 999799 18 6 47 493040 506960 493250 6735 506750 000210 07 999799 18 6 49 501080 498920 501298 6612 498702 000218 07 999781 12 6 49 501080 498920 501298 6673 502707 000214 07 999780 12 6 52 512867 487133 513098 6673 502707 000214 07 999781 12 6 52 512867 487133 513098 6435 466902 000231 07 999778 12 6 52 512867 487133 513098 6435 466902 000231 07 999765 13 6 54 520551 479449 520790 6323 479210 000239 07 999761 63 6 54 520551 479449 520790 6323 479210 000239 07 999761 63 6 52 512867 487133 513098 6435 466902 000231 07 999765 13 6 54 520551 479449 520790 6323 479210 000239 07 999761 63 6 54 520551 479449 520790 6323 479210 000239 07 999761 63 6 54 520551 479449 520790 6323 479210 000239 07 999761 63 6 54 520551 479449 520790 6323 4761651 000247 07 999783 12 6 54 520551 479449 520790 6323 479210 000239 07 999761 63 6 54 520551 479449 520790 6323 479210 000239 07 999761 63 6 54 520551 479449 520790 6323 479210 000239 07 999765 63 6 54 520551 479449 520790 6323 479210 000225 07 999788 12 6 54 520551 479449 52056 6668 475414 000243 07 999785 12 6 59 | 30 54 | 13 | 9.999851 | - | 06 | 14.9 | 10,00014 | 11.581932 | 8000 | 8.418068 | 1.582081 | 9 | 8.417919 | 30 | 0 | 6 |
| 8 32 | | | | - | | | | | | | | | | | | |
| 16 34 | 28 | 12 | 999844 | | | | | | | | | 2 | 427462 | 32 | 8 | |
| 20 35 441394 558606 441560 7580 558440 000166 06 999834 25 24 36 445941 554059 446110 7502 553890 000169 06 999831 25 28 37 450440 549560 450613 7425 549387 000173 06 999827 23 23 23 454893 545107 455070 7349 544930 000177 06 999829 22 36 39 459301 540699 459481 7276 540519 000180 06 999829 21 40 40 463665 536335 463849 7203 536151 000184 06 999816 20 44 41 467985 532015 468172 7132 531828 000188 06 999816 20 48 42 472263 527737 472454 7063 527546 000191 06 999809 18 52 43 476498 523502 476693 6995 523307 000195 06 999801 16 56 44 480693 519307 480892 6928 519108 000199 06 999801 16 7 0 45 8.484848 11.515152 8.485050 6862 11.514950 10.000203 07 9.999797 15 4 46 488963 511037 489170 6798 510830 000207 07 9.999797 15 4 46 488963 511037 489170 6798 510830 000207 07 9.99799 11 12 48 497078 502922 497293 6673 502707 000214 07 9.99780 11 12 48 497078 502922 497293 6673 502707 000214 07 9.99786 12 49 49050 501298 6612 498702 000218 07 9.99778 16 49 501080 498920 501298 6612 498702 000218 07 9.99778 16 49 501080 498920 501298 6612 498702 000218 07 9.99778 16 49 501080 498920 501298 6612 498702 000218 07 9.99778 16 49 501080 498920 501298 6612 498702 000218 07 9.99778 16 49 501680 498320 6735 506750 000210 07 9.99778 16 49 501080 498920 501298 6612 498702 000218 07 9.99778 16 49 501680 498920 501298 6612 498702 000218 07 9.99778 16 49 501680 498920 501298 6612 498702 000218 07 9.99778 16 40 55 524343 475657 524586 6268 475414 000243 07 9.99778 17 40 50000000000000000000000000000000000 | 27 | 12 | 999841 | 1 | 06 | 159 | 00013 | 567685 | 7743 | 432315 | 567844 | 6 | 432156 | 33 | 12 | |
| 24 36 445941 554059 446110 7502 553890 000169 06 999831 24 28 37 450440 549560 450613 7425 549387 000173 06 999827 23 32 38 454893 545107 455070 7349 544930 000177 06 999827 23 36 39 459301 540699 459481 7276 540519 000180 06 999820 21 40 40 463665 536335 463849 7203 536151 000184 06 999816 20 41 41 467985 532015 468172 7132 531828 000188 06 999812 18 48 42 472263 527737 472454 7063 527546 000191 06 999801 16 52 43 476498 523502 476693 6995 523307 000195 06 999801 16 56 44 480693 519307 480892 6928 519108 000199 06 999801 16 46 488963 511037 489170 6798 510830 000207 07 999790 13 12 48 497078 502922 497293 6673 502707 000214 07 999790 12 12 48 497078 502922 497293 6673 502707 000214 07 999780 12 45 15 080874 491026 509200 6493 498702 000218 07 999786 12 20 50 505045 494955 505267 6552 494733 000222 07 999778 12 45 15 080874 491026 509200 6493 498000 000226 07 999778 12 24 51 508974 491026 509200 6493 498000 000226 07 999778 12 24 51 508974 491026 509200 6493 498000 000226 07 999778 12 25 512867 487133 513098 6435 486902 000231 07 999769 12 25 52 512867 487133 513098 6435 486902 000231 07 999769 12 25 52 512867 487133 513098 6435 486902 000231 07 999769 12 25 53 516726 483274 516961 6379 483039 000225 07 999778 12 45 525 512867 487133 513098 6435 486902 000231 07 999769 12 25 53 516726 483274 516961 6379 483039 000235 07 999769 12 25 53 516726 483274 516961 6379 483039 000235 07 999765 12 45 52 54343 475657 524586 6268 475414 000243 07 999769 12 52 58 535523 464477 535779 6110 464221 000256 07 999735 12 48 57 531828 468172 532080 6162 467920 000252 07 999735 12 48 57 531828 468172 532080 6162 467920 000252 07 999735 12 48 57 531828 468172 532080 6162 467920 000255 07 999735 12 48 57 531828 468172 532080 6162 467920 000255 07 999735 12 48 57 531828 468172 532080 6162 467920 000255 07 999735 12 48 57 531828 468172 532080 6162 467920 000255 07 999735 12 48 57 531828 468172 532080 6162 467920 000255 07 999735 12 48 57 531828 468172 532080 6162 467920 000255 07 999735 12 48 57 531828 468172 532080 6162 467920 000255 | 26 | 32 | 999838 | | | | | | 7660 | 436962 | 563200 | | | | | |
| 28 37 450440 549560 450613 7425 549387 000173 06 999827 23 32 38 454893 545107 455070 7349 544930 000177 06 999828 22 36 39 459301 540699 459481 7276 540519 000180 06 999828 22 47693 536151 000184 06 999816 20 44 41 467985 532015 468172 7132 531828 000188 06 999812 19 48 42 472263 527737 472454 7063 527546 000191 06 999809 18 52 43 476498 523502 476693 6995 523307 000195 06 999805 17 56 44 480693 519307 480892 6928 519108 000199 06 999801 16 40 463665 519307 480892 6928 519108 000199 06 999805 17 40 45 8.484848 11.515152 8.485050 6862 11.514950 10.000203 07 9.999797 15 40 46 488963 511037 489170 6798 510830 000207 07 999790 12 12 48 497073 502992 497293 6673 506750 000210 07 999796 12 12 48 497073 502992 497293 6673 502707 000214 07 999786 12 20 50 505045 494955 505267 6552 494733 000222 07 999786 12 20 50 505045 494955 505267 6552 494733 000222 07 999786 12 20 50 505045 494955 505267 6552 494733 000222 07 999786 12 20 50 505045 494955 505267 6552 494733 000222 07 999786 12 20 50 505045 494955 505267 6552 494733 000222 07 999786 12 20 50 505045 494955 505267 6552 494733 000222 07 999786 12 20 50 505045 494955 505267 6552 494733 000222 07 999786 12 20 50 505045 494955 505267 6552 494733 000222 07 999786 12 20 50 505045 494955 505267 6552 494733 000222 07 999786 12 20 50 505045 494955 505267 6552 494733 000222 07 999786 12 20 50 505045 494955 505267 6552 494733 000222 07 999786 12 20 50 505045 494955 505267 6552 494733 000222 07 999786 12 20 50 505045 494955 505267 6552 494733 000222 07 999786 12 20 50 505045 494955 505267 6552 494733 000222 07 999786 12 20 50 505045 494955 505267 6552 494733 000222 07 999786 12 20 50 505045 494955 505267 6552 494733 000222 07 999786 12 20 50 505045 494955 505267 6552 494733 000222 07 999786 12 20 50 505045 494955 505267 6552 494733 000222 07 999786 12 20 50 505045 494955 505267 6552 494733 000222 07 999786 12 20 50 505045 494955 505267 6552 494733 000225 07 999786 12 20 50 505045 494955 505267 6552 494733 000225 07 999786 12 20 50 505045 494955 505267 6552 494733 000225 07 99978 | | | | | | | | 558440 | | | | | | | | |
| 32 38 | | | | - 4 | | | | | | | | | | | | |
| 36 39 | | | | - 1 | | | | | | | | | | | | |
| 40 40 463665 536335 463849 7203 536151 000184 06 999816 20 44 41 467985 532015 468172 7132 531828 000188 06 999812 19 52 44 472263 527737 472454 7063 527356 000191 06 999801 19 52 43 476498 523302 476693 6995 523307 000195 06 999805 17 56 44 480693 519307 480892 6928 519108 000199 06 999801 16 44 46 488963 511037 489170 6798 510830 000207 07 999797 15 4 46 488963 511037 489170 6798 510830 000207 07 999790 12 48 497078 50292 497293 6673 502707 000214 07 999780 12 48 497078 50292 497293 6673 502707 000214 07 999780 12 48 497078 50292 497293 6673 502707 000214 07 999780 12 44 505 505045 494955 505267 6552 494733 000222 07 999786 12 20 50 505045 494955 505267 6552 494733 000222 07 999778 12 451 508974 491026 509200 6493 490800 000226 07 999778 12 25 512867 487133 513098 6435 486902 000231 07 999769 12 25 52 512867 487133 513098 6435 486902 000231 07 999769 12 25 52 512867 487133 513098 6435 486902 000231 07 999769 12 25 52 512867 487133 513098 6435 486902 000231 07 999769 12 25 52 512867 487133 513098 6435 486902 000231 07 999769 12 25 52 512867 487133 513098 6435 486902 000231 07 999769 12 25 52 512867 487133 513098 6435 486902 000231 07 999769 12 25 52 512867 487133 513098 6435 486902 000231 07 999769 12 25 52 512867 487133 513098 6435 486902 000231 07 999769 12 25 52 512867 487133 513098 6435 486902 000231 07 999769 12 25 52 52 52 53 516726 483274 516961 6379 483039 000235 07 999761 12 45 52 58 535523 464477 535779 6110 464221 000256 07 999745 12 52 58 535523 464477 535779 6110 464221 000256 07 999735 12 52 58 535523 464477 535779 6110 464221 000256 07 999735 12 52 58 535523 464477 535779 6110 464221 000256 07 999735 12 52 58 535523 464477 535779 6110 464221 000256 07 999735 12 52 58 535523 464477 535779 6110 464221 000256 07 999735 12 52 58 535523 464477 535779 6110 464221 000256 07 999735 12 52 58 535523 464477 535779 6110 464221 000256 07 999735 12 52 58 535523 464477 535779 6110 464221 000256 07 999735 12 52 58 535523 464477 535779 6110 464221 000256 07 999735 12 52 58 535523 464477 535779 6110 464221 000256 | | | | - 1 | | | | | | | | | | | | |
| 44 41 467985 532015 468172 7132 531828 000188 06 999812 19 48 42 472263 527737 472454 7063 527346 000191 06 999809 18 52 43 476498 523502 476693 6995 523307 000195 06 999805 17 56 44 480693 519307 480892 6928 519108 000199 06 999801 16 7 0 45 8.484848 11.515152 8.485050 6862 11.514950 10.000203 07 9.999797 15 4 46 488963 511037 489170 6798 510830 000207 07 999793 14 8 47 493040 506960 493250 6735 506750 000210 07 999790 13 12 48 497078 502992 497293 6673 502707 000214 07 999796 12 20 50 505045 494955 505267 6552 494733 000222 07 999786 12 20 50 505045 494955 505267 6552 494733 000222 07 999786 12 20 50 505045 494955 505267 6552 494733 000222 07 999778 12 22 512867 487133 513098 6435 486902 000231 07 999769 12 28 52 512867 487133 513098 6435 486902 000231 07 999769 13 32 53 516726 483274 516961 6379 483039 000235 07 999769 13 40 55 524343 475657 524556 6268 475414 000243 07 999761 14 40 55 524343 475657 524556 6268 475414 000243 07 999765 13 44 56 528102 471898 528349 6215 471651 000247 07 999753 14 48 57 531828 468172 532080 6162 467920 000235 07 999744 18 56 59 539186 460814 539447 6059 460553 000260 07 999740 15 58 6 6 542819 457181 543084 6008 456916 000265 07 999745 15 6 7 | | | | - 4 | | | | | | | | | | | | |
| 48 42 472263 527737 472454 7063 527546 000191 06 999809 18 52 43 476498 523502 476693 6995 523307 000195 06 999805 17 56 44 480693 519307 480892 6928 519108 000199 06 999801 17 045 8.48448 11.515152 8.485050 6862 11.514950 10.000203 07 9.999797 18 446 488963 511037 489170 6798 510830 000207 07 999793 14 8 47 493040 506960 493250 6735 506750 000210 07 999790 13 12 48 497078 502992 497293 6673 502707 000214 07 999786 12 20 50 505045 494955 505267 6552 494733 000222 07 999786 12 24 51 508974 491026 509200 6493 490800 000226 07 999778 12 24 51 508974 491026 509200 6493 490800 000226 07 999778 12 25 52 512867 487133 513098 6435 486902 000231 07 999769 8 32 53 516726 483274 516961 6379 483039 000235 07 999761 14 55 524343 475657 524566 6268 475414 000243 07 999763 14 55 5284343 475657 524566 6268 475414 000243 07 999763 14 56 528102 471898 528349 6215 471651 000247 07 999734 15 52 58 535523 464477 535779 6110 464221 000256 07 999744 18 66 59 539186 460814 539447 6059 460553 000260 07 999744 18 06 542819 457181 543084 6008 456916 000265 07 999735 | | | | - 1 | | | | | | | | | | 1 | | |
| 52 43 476498 523502 476693 6995 523307 000195 06 999805 17 56 44 480693 519307 480892 6928 519108 000199 06 999801 16 446 488963 511037 489170 6798 510830 000207 07 999793 14 46 48963 511037 489170 6798 510830 000207 07 999793 14 48 497078 502922 497293 6673 502707 000214 07 999786 12 12 48 497078 502922 497293 6673 502707 000214 07 999786 12 20 50 505045 494955 505267 6552 494733 000222 07 999782 14 24 51 508974 491026 509200 6493 490800 000226 07 999774 52 25 512867 487133 513098 6435 486902 000231 07 999765 23 25 512867 487133 513098 6435 486902 000231 07 999765 23 25 512867 487133 513098 6435 486902 000231 07 999765 23 25 512867 487133 513098 6435 486902 000235 07 999765 24 45 52 524343 475657 524596 628 475414 000243 07 999765 24 45 52 524343 475657 524596 628 475414 000243 07 999765 24 45 52 5212867 487135 524596 628 475414 000243 07 999765 24 52 52 512867 487135 513098 6435 486902 000235 07 999761 64 55 524343 475657 524596 628 475414 000243 07 999765 24 52 52 512867 487135 513098 6435 486902 000235 07 999761 64 55 524343 475657 524596 628 475414 000243 07 999767 52 52 52 52 52 52 52 52 52 52 52 52 52 | | | | - 1 | | | | | 1 | | | | | | | |
| 56 44 480693 519307 480892 6928 519108 000199 06 999801 16 7 | | | | - 1 | | | | | | | | | | | | |
| 7 0 45 8.484848 11.515152 8.485050 6862 11.514950 10.000203 07 9.999797 15 4 46 488963 511037 489170 6798 510830 000207 07 9.999791 15 8 47 493040 506960 493250 6735 506750 000210 07 9.99790 13 12 48 497078 502992 497293 6673 502707 000214 07 9.99786 12 16 49 501080 498920 501298 6612 498702 000218 07 9.99786 12 20 50 505045 4.94955 505267 6552 4.94733 000222 07 9.99778 10 22 15 508974 4.91026 50.9200 64.93 4.90800 000226 07 9.99778 10 22 15 508974 4.91026 50.9200 64.93 4.90800 000226 07 9.99778 10 22 15 508974 4.91026 50.9200 64.93 4.90800 000226 07 9.99776 12 25 512867 487133 513098 6435 4.86902 000231 07 9.99769 13 25 53 516726 483274 516.961 6379 483039 000235 07 9.99769 13 36 54 520551 47.9449 520790 6323 47.9210 000239 07 9.99761 14 0.55 524343 47.5657 524586 6268 47.5414 000243 07 9.99757 12 44.56 528102 47.1898 528349 6215 47.1651 000247 07 9.99753 48 57 531828 468172 532080 6162 46.7920 000252 07 9.99740 12 52 58 535523 464477 535779 6110 464221 000256 07 9.99740 12 56 59 53.9186 46.0814 53.9447 60.59 46.0553 000260 07 9.99740 12 56 5.9 53.9186 46.0814 53.9447 60.59 46.0553 000260 07 9.99740 12 56 5.9 53.9186 46.0814 53.9447 60.59 46.0553 000260 07 9.99740 12 56 5.9 53.9186 46.0814 53.9447 60.59 46.0553 000260 07 9.99740 12 56 5.9 53.9186 46.0814 53.9447 60.59 46.0553 000260 07 9.99740 12 56 5.9 53.9186 46.0814 53.9447 60.59 46.0553 000260 07 9.99740 12 56 5.9 53.9186 46.0814 53.9447 60.59 46.0553 000260 07 9.99740 12 56 5.9 53.9186 46.0814 53.9447 60.59 46.0553 000260 07 9.99740 12 56 5.9 53.9186 46.0814 53.9447 60.59 46.0553 000260 07 9.99740 12 56 5.9 53.9186 46.0814 53.9447 60.59 46.0553 000260 07 9.99740 12 56 5.9 53.9186 46.0814 53.9447 60.59 46.0553 000260 07 9.99740 12 56 5.9 53.9 58 50.00260 07 9.99740 12 56 5.9 53.9 58 50.00260 07 9.99740 12 56 5.9 53.9 58 50.00260 07 9.99740 12 56 5.9 50.00260 07 9.99740 12 56 5.9 50.00260 07 9.99740 12 56 5.9 50.00260 07 9.99740 12 56 5.9 50.00260 07 9.99740 12 56 5.9 50.00260 07 9.99740 12 56 50.00260 07 9.99740 12 56 50.00260 07 9.99740 12 56 50.00260 07 | | | | | | | | | | | | | | | | |
| 4 46 488963 511037 489170 6798 510830 000207 07 999793 14 8 477 493040 506960 493250 6735 506750 000210 07 999790 13 12 48 497078 502992 497293 6673 502707 000214 07 999786 12 16 49 501080 498920 501298 6612 498702 000218 07 999786 12 20 50 505045 494955 505267 6552 494733 000222 07 999778 10 24 51 508974 491026 509200 6493 490800 000226 07 999778 10 24 51 508974 491026 509200 6493 490800 000226 07 999778 10 25 52 512867 487133 513098 6435 486902 000231 07 999769 12 25 53 512867 487133 513098 6435 486902 000231 07 999769 12 25 53 516726 483274 516961 6379 483039 000235 07 999769 12 36 54 520551 479449 520790 6323 479210 000239 07 999761 12 40 55 524343 475657 524586 6268 475414 000243 07 999757 12 40 55 524343 475657 524586 6268 475414 000243 07 999753 48 57 531828 468172 532080 6162 467920 000252 07 999740 12 52 58 535523 464477 535779 6110 464221 000256 07 999740 12 56 59 539186 460814 539447 6059 460553 000260 07 999740 12 56 59 539186 460814 539447 6059 460553 000260 07 999740 12 56 59 539186 450814 539447 6059 460553 000260 07 999740 12 56 59 539186 450814 539447 6059 460553 000260 07 999740 12 56 59 539186 450814 539447 6059 460553 000260 07 999740 12 56 59 539186 450814 539447 6059 460553 000260 07 999740 12 56 59 539186 450814 539447 6059 460553 000260 07 999740 12 56 59 539186 450814 539447 6059 460553 000260 07 999740 12 56 59 539186 450814 539447 6059 460553 000260 07 999740 12 56 59 539186 450814 539447 6059 460553 000260 07 999740 12 56 59 539186 450814 539447 6059 460553 000260 07 999740 12 56 59 539186 450814 539447 6059 460553 000260 07 999740 12 56 59 539186 450814 539447 6059 460553 000260 07 999740 12 56 59 539186 450814 539447 6059 460553 000260 07 999735 00 | - | - | | | - | | - | - | | | | | | - | | 7 |
| 8 47 493040 506960 493250 6735 506750 000210 07 999780 12 48 497078 502922 497293 6673 502707 000214 07 999786 12 1649 501080 498920 501298 6612 498702 000218 07 999786 12 20 50 505045 494955 505267 6552 494733 000222 07 999778 10 22 50 505045 491026 509200 6493 490800 000226 07 999774 12 28 52 512867 487133 513098 6435 486902 000231 07 999769 12 28 52 512867 487133 513098 6435 486902 000231 07 999769 12 28 52 512867 487133 513098 6435 486902 000231 07 999769 12 28 52 512867 487133 513098 6435 486902 000231 07 999769 12 28 52 512867 487133 513098 6435 486902 000231 07 999769 12 28 52 512867 487133 513098 6435 486902 000231 07 999769 12 28 52 512867 487133 513098 6435 486902 000231 07 999769 12 28 52 512867 487133 513098 6435 486902 000231 07 999769 12 28 52 512867 487133 513098 6435 486902 000235 07 999761 12 40 55 524343 475657 524556 6268 475414 000243 07 999761 12 40 55 524343 475657 524556 6268 475414 000243 07 999761 12 48 57 531828 468172 532080 6162 467920 000252 07 999748 12 52 58 535523 464477 535779 6110 464221 000256 07 999740 12 52 58 535523 464477 535779 6110 464221 000256 07 999740 12 56 59 539186 460814 539447 6059 460553 000260 07 999740 12 8 060 542819 457181 543084 6008 456916 000265 07 999740 12 8 060 542819 457181 543084 6008 456916 000265 07 999735 07 12 12 12 12 12 12 12 12 12 12 12 12 12 | | | | _ | | | | | | | | | | | | |
| 12 48 497078 502922 497293 6673 502707 000214 07 999786 12 16 49 501080 498920 501298 6612 498702 000218 07 999782 11 20 50 505045 494955 505267 6552 494733 000222 07 999778 11 20 50 505045 491955 505267 6552 494733 000222 07 999774 12 28 52 512867 487133 513098 6435 486902 000231 07 999765 12 28 52 512867 487133 513098 6435 486902 000231 07 999765 12 28 53 516726 483274 516961 6379 483039 000235 07 999765 12 28 52 512867 479449 520790 6323 479210 000239 07 999761 12 40 55 524343 475657 524586 6268 475414 000243 07 999767 12 44 56 528102 471898 528349 6215 471651 0000247 07 999757 12 48 57 331828 468172 532080 6162 467920 000252 07 999748 12 52 58 535523 464477 535779 6110 464221 000256 07 999740 12 56 59 539186 460814 539447 6059 460553 000260 07 999740 12 56 59 539186 460814 539447 6059 460553 000260 07 999740 12 56 59 539186 460814 539447 6059 460553 000260 07 999740 12 56 59 539186 460814 539447 6059 460553 000260 07 999740 12 56 59 539186 450814 539447 6059 460553 000260 07 999740 12 56 59 539186 450814 539447 6059 460553 000260 07 999740 12 56 59 539186 450814 539447 6059 450553 000260 07 999740 12 56 59 539186 450814 539447 6059 450553 000260 07 999740 12 56 59 539186 450814 539447 6059 450553 000260 07 999740 12 56 59 539186 450814 539447 6059 450553 000260 07 999740 12 56 59 539186 450814 539447 6059 450553 000260 07 999740 12 56 59 539186 450814 539447 6059 450553 000260 07 999740 12 56 59 539186 450814 539447 6059 450553 000260 07 999740 12 56 59 539186 450814 539447 6059 450553 000260 07 999740 12 56 59 539186 450814 539447 6059 450553 000260 07 999740 12 56 59 539186 450814 539447 6059 450553 000260 07 999740 12 56 59 539186 450814 539447 6059 450553 000260 07 999740 12 56 59 539186 12 54008 12 54008 12 56 59 539186 12 54008 12 54008 12 56 59 539186 12 54008 12 56 59 539186 12 54008 12 56 59 539186 12 54008 12 56 59 539186 12 54008 12 56 59 539186 12 54008 12 56 59 539186 12 56 59 539186 12 56 59 539186 12 56 59 539186 12 56 59 539186 12 56 59 539186 12 56 59 539186 12 56 59 539186 12 56 59 539186 | | | | | | | | | | | | - | | | | |
| 16 49 501080 | | | | | | | | | | | | | | | | 1 |
| 20 50 505045 494955 505267 6552 494733 000222 07 999778 10 24 51 508974 491026 509200 6493 490800 000226 07 999774 9 28 52 512867 487133 513098 6435 486902 000231 07 999765 13 25 3 516726 483274 516961 6379 483039 000235 07 999765 13 65 4 520551 479449 520790 6323 479210 000239 07 999765 14 0 55 524343 475657 524586 6268 475414 000243 07 999765 14 15 528102 471898 528349 6215 471651 000247 07 999753 14 15 531828 468172 532080 6162 467920 000252 07 999748 15 15 15 15 15 15 15 15 15 15 15 15 15 | | | | - | | | | | | | | | | | | |
| 24 51 508974 491026 509200 6493 490800 000226 07 999774 28 52 512867 487133 513098 6435 486902 000231 07 999765 799765 32 53 516726 483274 516961 6379 483039 000235 07 999765 7997765 7997765 7997765 7997765 7997765 7997765 7997765 7997765 7997765 7997765 7997765 7997765 7997765 7997765 7997765 7997765 7997745 7997765 7997745 7997745 7997745 7997745 7997745 7997745 7997745 <td></td> | | | | | | | | | | | | | | | | |
| 28 52 512867 487133 513098 6435 486902 000231 07 999769 8 22 53 516726 483274 516961 6379 483039 000235 07 999765 7 36 54 520551 479449 520790 6323 479210 000239 07 999761 7 40 55 524343 475657 524596 6268 475414 000243 07 999757 8 44 56 528102 471898 528349 6215 471651 000247 07 999753 4 48 57 331828 468172 532080 6162 467920 000252 07 999748 8 52 58 535523 464477 535779 6110 464221 000256 07 999740 8 56 59 539186 460814 539447 6059 460553 000260 07 999740 8 8 0 60 542819 457181 543084 6008 456916 000265 07 999730 0 m. s. ' Cosine. Secunt. Cotang. Tang. Cosec. Sine. ' P. P. to 1 | | | | | | | | | | | | | | | | |
| 32 53 516726 483274 516961 6379 483039 000235 07 999765 7 36 54 520551 479449 520790 6323 479210 000239 07 999761 6 40 55 524343 475657 524586 6268 475414 000243 07 999757 5 44 56 528102 471898 528349 6215 471651 000247 07 999753 4 48 57 331828 468172 532080 6162 467920 000252 07 999748 5 52 58 535523 464477 535779 6110 464221 000256 07 999744 5 56 59 539186 460814 539447 6059 460553 000260 07 999744 5 56 59 539186 460814 539447 6059 460553 000260 07 999745 5 56 59 539186 860814 539447 6059 460553 000260 07 999745 5 56 59 539186 860814 539447 6059 460553 000260 07 999745 5 56 59 539186 500260 07 999745 5 56 59 539186 500260 07 999745 5 56 59 539186 500260 07 999745 5 56 59 539186 500260 07 999745 5 56 59 539186 500260 07 999745 5 56 59 539186 500260 07 999745 5 56 59 539186 500260 07 999745 5 56 59 539186 500260 07 999745 5 56 59 539186 500260 07 999745 5 56 59 539186 500260 07 999745 5 56 59 539186 500260 07 999745 5 56 59 539186 500260 07 999745 5 56 59 539186 500260 07 999745 5 57 5002 000260 07 999745 5 58 5002 000260 07 999745 | | | | | | | | | | | | | | | | |
| 36 54 520551 479449 520790 6323 479210 000239 07 999761 64 65 524343 475657 524586 6268 475414 000243 07 999757 44 56 528102 471598 528349 6215 471651 000247 07 999753 48 57 531828 468172 532080 6162 467920 000252 07 999748 52 58 535523 464477 535779 6110 464221 000256 07 999744 56 59 539186 460814 539447 6059 460553 000260 07 999740 56 59 539186 457181 543084 6008 456916 000265 07 999735 0 m. s. / Cosine. Secant. Cotang. Tang. Cosec. Sine. / P. P. to 1s 15" 1200 1s 15" 1200 1s 15" 1 p 5 or " 2 30 2400 2 30 2400 2 30 2400 2 30 2 | | | | | | | | | | | | | | | | |
| 44 56 528102 471898 528349 6215 471651 000247 07 999753 4 48 57 531828 468172 532080 6162 467920 000252 07 999748 5 52 58 535523 464477 535779 6110 464221 000256 07 999740 8 6 0 60 542819 457181 543084 6008 456916 000265 07 999740 8 6 0 60 542819 545181 543084 6008 456916 000265 07 999740 | | 1 | 999761 | 7 | 0 07 | 0239 | | | 6323 | 520790 | 479449 | 1 | 52055 | 54 | 36 | |
| 44.56 528102 471898 528349 6215 471651 000247 07 999753 4 48.57 531828 468172 532080 6162 467920 000252 07 999748 5 52.58 535523 464477 535779 6110 464221 000256 07 999748 5 56.59 539186 460814 539447 6059 460553 000266 07 999740 1 8 0.60 542819 457181 543084 6008 456916 000265 07 999735 0 m. s. ' Cosine. Secant. Cotang. Tang. Cosec. Sine. / | | | | | | | | | 6268 | 524586 | | | | | | |
| 52.58 535523 464477 535779 6110 464221 000256 07 999744 2 5659 539186 460814 539447 6059 460553 000260 07 999740 1 8 0 60 542819 457181 543084 6008 456916 000265 07 999735 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 | | | | 7 | 7 07 | 0247 | 0002 | | 6215 | | | | | | | |
| 56 59 539186 460814 539447 6059 460553 000260 07 999740 1 8 0 60 542819 457181 543084 6008 456916 000265 07 999735 0 m. s. / Cosine. Secant. Cotang. Tang. Cosec. Sine. / b Hours, or 88 Degrees. P. P. to 1s 15" 1200 1s 15" 1200 2400 1s 15" 15" 15" 15" 1200 2400 2 30 2400 | | | | | | | | | | | | | | | | |
| 8 0 60 542819 457181 543084 6008 456916 000265 07 999735 0 m. s. ' Cosine. Secant. Cotang. Tang. Cosec. Sine. ' 5 Hours, or 88 Degrees. P. P. to 2 30 2400 2 30 2400 2 30 2 | | - | | | | | | | | | | | | | | |
| Tang. Cosec. Sine. | | | | | | | | | | | | - | | | | - |
| S Hours, Or S8 Degrees. P. P. to 1s 15" 1200 1s 15" 1200 1s 15" 1 P S or 2 30 2400 2 30 2 P | 0 52 | 5 | 999735 | 1 | 5 07 | 0265 | 0002 | 456916 | 6008 | 543084 | 457181 | 9 | | - | | 2 |
| 5 Hours, or 88 Degrees. P. P. to 1 ^s 15" 1200 1 ^s 15" 1 1200 1 ^s 15" 1 P 1 1 1 1 1 1 1 1 | / m. | - | Sine. | - | | ec. | Cosec. | Tang. | | Cotang. | Secant. | | Cosine. | 11 | S | m |
| P. P. to 2 30 2400 2 30 2400 2 30 2 30 2 | 1 | - | | e | 8 D | - | | | - | | | | | | | |
| s or " 2 30 2400 2 30 2400 2 30 2 | 1 | 1 | 0 | - | | | 1 18 1 | | | 1 15 | | | | 1 | n | F |
| SUL | P. P. | | | | | 1 | | | | | | | | | | |
| 3 45 3600 3 45 3600 3 45 3 | sor | 1 | 3 | | | | 3 | | | 3 | | | | | Ur | |

| ~ | 0 | | TABL | | Lo | garithmi | | es, Tanger | its, | | | - | |
|-----|----------|----------|------------------|------|------------------|----------|------------|------------------|----------|-----------|------------------|-----|------|
| , | | 1 4 | 0 He | | 1 Coses | Tena | or D. | Cotono | I Samuel | | grees. | 1/1 | 200 |
| m. | S. | | Sine. | D. | Cosec. | Tang. | _ | Cotang. | Secant. | _ | Cosine. | = | m. |
| 8 | 0 | | | | 11.457181 | | | | | | | | 52 |
| | 8 | | | | | | | | | | 999731 | | |
| | 12 | | | | | 55381 | | 446183 | | | | | |
| | 16 | | 557054 | | 442946 | | | 442664 | | | 999717 | | 7 |
| | 20 | 5 | 560540 | 4 . | 439460 | | | | | | | | |
| | 24 | 6 | 563999 | | 436001 | 56429 | | 435709 | | | | | |
| | 28 | 7 | 567431 | 5674 | 432569 | 56772 | 7 5682 | 432273 | 0002 | 96 08 | | | 51 |
| | 32 | 8 | 570836 | 5630 | 429164 | 57113 | 7 5638 | 428863 | 0003 | 01 08 | 999699 | | 5. |
| | 36 | 9 | 574214 | | 425786 | | | | | | | | 1 |
| | 40 | | 577566 | | 422434 | | | 422123 | | | 999689 | | |
| | 44 | | 580892 | | 419108 | | 1 1 | 418792 | | | 999685 | | |
| | 48 | | 584193 | | 415807 | 58451 | | 415486 | | | 999680 | | |
| | | 13 14 | 587469 | | 412531 | 58779 | | 412205 | | | 999675 | | |
| _ | | | 590721 | | 409279 | 59105 | | 408949 | | | 999670 | - | |
| 9 | | 15 | | | 11.406052 | | | | | | | | 51 |
| | 4 | 16 | 597152 | | 402848 | 597499 | | 402508 | | | | | |
| | 12 | 17 | 600332 | | 399668 | | | 399323 | | | | | |
| | 16 | | 603489 606623 | | 396511 393377 | 603839 | | 396161 393022 | 0003 | | 999650 999645 | | |
| | 20 | | 609734 | | 390266 | | | 389906 | | | 999640 | | |
| | 24 | | 612823 | | 387177 | 61318 | | 386811 | 0003 | | 999635 | | |
| | 28 | | 615891 | | 384109 | 61626 | | 383738 | 0003 | | 999629 | | |
| | 32 | | 618937 | | 381063 | | | 380687 | 0003 | | 999624 | | |
| | 36 | | 621962 | 5006 | 378038 | 622343 | | 377657 | 00038 | | 999619 | 36 | 25 |
| | 40 | 25 | 624965 | 4972 | 375035 | 625353 | 4981 | 374648 | 00038 | 36 09 | 999614 | 35 | |
| | 44 | | 627948 | 4938 | 372052 | 628340 | 1947 | 371660 | 00039 | 02 09 | 999608 | 34 | |
| | 48 | | 630911 | | 369089 | 631308 | | 368692 | 00039 | | 999603 | | |
| | 52 | | 633854 | 1 | 366146 | 634256 | | 365744 | 00040 | | 999597 | | |
| | 56 | - | 636776 | _ | 363224 | 637184 | | 362816 | 00040 | | 999592 | - | |
| 0 | | | | | 11.360320 | | | | | | 9.999586 | | 50 |
| | | 31 | 642563 | | 357437 | 642985 | | 357018 | | | 999581 | | |
| | | 32 | 645428 | | 354572 | 645853 | | 354147 | 00043 | | 999575 | | |
| | 12 | | 648274 | | 351726 | 648704 | | 351296 | 00043 | | 999570 | | |
| | 16 | | 651102 | | 348898 | 651537 | | 348463 345648 | | | 999564 | | |
| | 20 24 | | 653911 656702 | | 346089 343298 | 654352 | | 342851 | 00044 | | 999553 | | |
| | 28 | | 659475 | | 340525 | 659928 | | 340072 | 0004 | | 999547 | | |
| | 32 | | 662230 | | 337770 | 662689 | | 337311 | 00048 | | 999541 | | |
| | 36 | | 664968 | | 335032 | 665433 | | 334567 | 00046 | | 999535 | | |
| | 40 | | 667689 | | 332311 | 668160 | | 331840 | | | 999529 | | |
| | 44 | | 670393 | | 329607 | 670870 | | 329130 | 00047 | 6 10 | 999524 | 19 | |
| | 48 | 42 | 673080 | 4451 | 326920 | 673563 | 3 4461 | 326437 | 00048 | 2 10 | 999518 | 18 | |
| | 52 | 43 | 675751 | 4424 | 324249 | .676239 | 4434 | 323761 | 00048 | | 999512 | | |
| | 56 | 44 | 678405 | 4397 | 321595 | 678900 | 4417 | 321100 | 00049 | 10 | 999506 | 16 | - |
| 1 | | 45 | 8.681043 | | 11.318957 | 8.681544 | 4380 | | | | 9.999500 | | 49 |
| | | 46 | 683665 | | 316335 | 684172 | | 315828 | | | 999493 | | |
| | | 47 | 686272 | | 313728 | 686784 | | 313216 | 00051 | | 999487 | | |
| | 12 | 100 | 688863 | | 311137 | .689381 | | 310619 | 00051 | | 999481 | | |
| | 16 | | 691438 | | 308562 | 691963 | | 308037 | 00052 | | 999475 | | |
| | 20 | | 693998 | | 306002 | 694529 | | 305471 | 00053 | | 999469 | | |
| | 24 28 | | 696543 699073 | | 303457 | | | 302919 | | | | | |
| | 32 | | 701589 | | 300927 | 699617 | | | _ | | 999456 | | |
| | 36 | | 701389 | | 298411 295910 | | | | | | 999430 | | |
| | 40 | | | | 293423 | | | | | | 999437 | | |
| | | 56 | 709049 | | 290951 | 709618 | | 290382 | | | 999431 | | |
| | 48 | | 711507 | | 288493 | | | 287917 | 00057 | | 999424 | | |
| | | 58 | | | 286048 | 714534 | | | | | 999418 | | |
| | | 59 | 716383 | | 283617 | 716972 | | 283028 | | | 999411 | 1 | |
| 2 | 0 | 60 | | | 281200 | 719396 | | 280604 | | | 999404 | 0 | 48 |
| n. | 8. | = | Cosine. | | - | Cotang. | | | | | Sine. | | m. |
| -10 | - 00 | | 5 Ho | 1170 | Secant. | Cotang. | 1 | Tang. | Cosec. | 87 De | | - | ILI. |
| - | - | | 15 | 15" | 1 701 | 1- 1 | or | 1 ,000 | | | 0 | | |
| | P. | | 2 | 30 | 721 | 15 | 15" | 722 | 15 | 15" 30 | 1 2 | | P. 1 |
| | or | 41 | 3 | 45 | 2163 | 2 3 | 30 45 | 1445 2167 | 2 3 | 45 | 3 | S | or ' |

| | - | - | | | | and | Seca | nte | | Т. | BLE V. | - | 21 |
|----|----------|-----------------|------------------|------|-------------------|------------------|----------|---------------------|-----------|-----|--------------------|------|------|
| | | | 0 Но | | | and | or | mirs. | , | | grees. | | 21 |
| 20 | 0 | // | Sine. | D. | Cosec. | Tang. | D. | Cotang. | Secant. | D. | Cosine. | / jx | n |
| n. | 8. | | | | | 0 | | | | - | | | |
| 12 | 0 | | | | | | | 11.280604 | | | 9.999404 999398 | | 18 |
| | 4 | 1 | 721204 723595 | | 278796 276405 | 721806 724204 | | 278194 275796 | 000602 | | 999398 | | |
| | 8 12 | 2 | 725972 | | 274028 | 726588 | | 273412 | 000616 | | 999384 | | - |
| | 16 | 4 | 728337 | | 271663 | 728959 | | 271041 | 000622 | | 999378 | | |
| ũ. | 20 | 5 | 730688 | | 269312 | 731317 | | 268683 | 000629 | | 999371 | | |
| | 24 | 6 | 733027 | | 266973 | 733663 | | 266337 | 000636 | | 999364 | | . : |
| | 28 | 7 | 735354 | | 264646 | 735996 | | 264004 | 000643 | 12 | 999357 | 53 | |
| 1 | 32 | 8 | 737667 | | 262333 | 738317 | | 261683 | 000650 | 12 | 999350 | | 1 |
| | 36 | 9 | 739969 | | 260031 | 740626 | | 259374 | 000657 | 1 | 999343 | | 19 |
| | 40 | | 742259 | | 257741 | 742922 | | 257078 | 000664 | | 999336 | | . : |
| | | 11 | 744536 | | 255464 | 745207 | | 254793 | 000671 | | 999329 999322 | | |
| | 48 52 | | 746802 749055 | | 253198 | 747479 749740 | | 252521 250260 | 000678 | | 999315 | | |
| ш | | 14 | 751297 | | 250945 248703 | 751989 | | 248011 | 000692 | | 999308 | | |
| 0 | | _ | | | | | | | | | 9.999301 | | 4.77 |
| 3 | | | | | 244253 | | | 11.245773 243547 | 000706 | | 999294 | | ¥1 |
| | | $\frac{16}{17}$ | 755747 757955 | | 244253 | 756453 758668 | | | 000714 | | 999286 | | |
| | 12 | | 760151 | | 239849 | 760872 | | | 000721 | | 999279 | | |
| | 16 | | 762337 | | 237663 | 763065 | | | 000728 | | 999272 | | |
| V | 20 | | 764511 | | 235489 | 765246 | | A COLUMN TO SERVICE | 000735 | | 999265 | | |
| 1 | 24 | 21 | 766675 | 3588 | 233325 | 767417 | 3600 | 232583 | 000743 | 12 | 999257 | 39 | |
| | 28 | | 768828 | | 231172 | 769578 | | | 000750 | | 999250 | | |
| | 32 | | 770970 | | 229030 | 771727 | | | 000758 | - | 999242 | | |
| | 36 | | 773101 | | 226899 | 773866 | | 226134 | 000765 | | 999235 | | |
| Н | 40 | | 775223 | | 224777 | 775995 | | 224005 | 000773 | | 999227 | | |
| | 44 | | 777333 | | 222667 | 778114 | | | 000780 | 200 | 999220 | | |
| | 48 | | 779434 781524 | | 220566 | 780222 782320 | 1 1 1 | 219778 217680 | 000788 | | 999205 | | |
| | 52 56 | | 783605 | | 218476 216395 | 784408 | | 215592 | 000803 | 1 | 999197 | | |
| 4 | - | _ | 8.785675 | | made and a second | | 2 2 40 3 | and it was | 10.000811 | | 9.999189 | 1 | 10 |
| 4 | | 31 | 787736 | | 212264 | 788554 | | | | | 999181 | | 40 |
| | | 32 | 789787 | | 210213 | | | | 000826 | | 999174 | | |
| | 12 | | 791828 | | 208172 | 792662 | | | 000834 | | 999166 | | |
| | 16 | | 793859 | | 206141 | 794701 | | | 000842 | | 999158 | | |
| | 20 | | 795881 | | 204119 | | | | 000850 | | 999150 | 25 | |
| | 24 | | 797894 | 3339 | 202106 | | 3352 | 201248 | 900858 | 13 | 999142 | | |
| | 28 | | 799897 | | 200103 | 800763 | | 199237 | 000866 | | 999134 | | |
| | 32 | | 801892 | | 198108 | 802765 | | | 000874 | | 999126 | | |
| | 36 | | 803876 | | 196124 | 804758 | | 195242 | 000882 | | 999118 | | |
| | 40 | | 805852 | | 194148 | 806742 | | 193258 | 000890 | | 999110 | | |
| | 44 | | 807819 | | 192181 | 808717 | | | 000898 | | 999102 | | |
| | 48 52 | | 809777 811726 | | 190223 | 810683 812641 | | | 000906 | | 999094 | | |
| | 56 | | 811720 | | 188274 186333 | 814589 | | | 000914 | | 999077 | | |
| 5 | | - | | | | | | 11.183471 | | - | 9.999069 | | 1.E |
| U | | 46 | 817522 | | 182478 | 818461 | | | 000939 | | 9.999061 | | ±0 |
| | _ | 47 | 819436 | | 180564 | 820384 | | 179616 | 000933 | | 999053 | | |
| | 12 | | 821343 | | | 822298 | | | 000956 | | 999044 | | |
| | 16 | | 823240 | | 176760 | | | | | | 999036 | | |
| | 20 | 50 | 825130 | 3135 | 174870 | 826103 | 3150 | 173897 | 000973 | 14 | 999027 | 10 | 1 |
| | 24 | | 827011 | | 172989 | 827992 | 3136 | 172008 | 000981 | 14 | 999019 | 9 | |
| | 28 | | 828884 | | | | | | | | 999010 | | |
| | 32 | | | | | | | | | | 999002 | | |
| | 36 | | | | | | | | | | | | |
| | 40 | | 834456 | | | | | | | | | | |
| | 44 | | | | | | | | | | 998976 | | |
| | 48 52 | | 838130 839956 | | | | | | 001033 | | 998958 | | |
| | 56 | | 841774 | | 158226 | _ | | | | | 998950 | | |
| 6 | | 60 | 843585 | | | | | | | | 998941 | | 1.4. |
| | | = | | 3003 | | | 3019 | | | 10 | | | |
| 2. | S. | 1 | Cosine. | | Secant. | Cotang. | 1 | Tang. | Cosec. | 1 1 | Sine. | 1 | m. |
| | | | 5 Ho | | 1 | | or | 19 1 | | | grees. | | |
| P. | P. 1 | to | 18 | 15" | 515 | 18 | 15" | 517 | 18 | 15" | 2 | P | P. 1 |
| | or | | 2 | 30 | 1030 | 2 3 | 30 | 1034 | 2 | 30 | 4 | S | or ' |
| | | 100 | 3 | 45 | 1544 | 3 | 45 | 1551 | 3 | 45 | 6 | | |

| | | - | | A-10.00 | (2) | | | - | The same of | | | | | |
|------|---------|--|------------|--------------------|-----------|------------------|------------------|----------|------------------|-----------|------------------|------------------|-------|----------|
| ı | | 22 TABLE V. Logarithmic Sines, Tangents, | | | | | | | | | | | | |
| á | 1 | | | 0 Hour, | | | · or | | - VI | - V I - 4 | | Degrees. | | |
| | m. s. / | | Sine. D. | | Cosec. | Tang. D. | | Cotang. | Secant. D. | | Cosine. | 1 / lx | n. s. | |
| | | | = | | | | | | | | | | === | - |
| | 16 | 0 | | 8.843583 845387 | | 11.156415 | 84645 | | | | 059 15 068 15 | 9.998941 998932 | | 56 |
| | 150 | 8 | 2 | 847189 | | 154613 152817 | 848260 | | 153545 151740 | | 100 | 998932 | | 52 |
| 1 | * | 12 | 3 | | | 151029 | | | 149943 | | 086 15 | 998914 | | 48 |
| | | 16 | 4 | 850751 | | 149249 | | | 148154 | | 95 15 | 998905 | | 41 |
| ı | | 20 | 5 | | | 147475 | | | 146372 | | | 998896 | | 40 |
| ı | | 21 | 6 | | | 145709 | | | 144597 | 0011 | | 998887 | | 36 |
| J | | 28 | 7 | 856049 | | 143951 | 85717 | | 142829 | | 22 15 | 998878 | | 32 |
| H | | 32 | 8 | 857801 | | 142199 | | | 141068 | | | 998869 | | 28 |
| ı | | 36 | 9 | 859546 | 2896 | 140454 | 86068 | 2911 | 139314 | 0011 | 40 15 | 998860 | | 24 |
| l | | 40 | 10 | 861283 | | 138717 | 862433 | | 137567 | | | 998851 | 50 | 20 |
| ı | | 44 | 11 | 863014 | | 136986 | | | 135827 | | | 998841 | | 16 |
| ı | | 48 | | 864738 | 1 | 135262 | 86590 | | 134094 | | | 998832 | | 12 |
| ı | | 52 | | 866455 | | 133545 | 867632 | | 132368 | | | 998823 | | 8 |
| ı | | 56 | 190 | 868165 | | 131835 | 86935 | | 130649 | 0011 | | 998813 | - | 4 |
| B | 17 | - | | | | | | | 11.128936 | | | 9.998804 | | |
| H | | 4 | 16 | 871565 | | 128435 | 872770 | | 127230 | | | 998795 | | 56 |
| | | | 17 | 873255 | | 126745 | 874469 | | 125531 | | 215 16 | 998785 | | 52 |
| 1 | 1 | 12 16 | | 874938 | | 125062 | 876169 877849 | | 123838 122151 | 0013 | 224 16 234 16 | 998776 | | 48 44 |
| | 14 . | 20 | | 876615 878285 | | 123385 121715 | 877848 | | 122151 | 0012 | | 998766 | | 40 |
| 1 | | 24 | | 879949 | | 121715 | 88120 | | 118798 | | | 998747 | | 36 |
| ı | | 28 | | 881607 | | 118393 | 882869 | | 117131 | 0012 | | 998738 | | 32 |
| l | | 32 | | 883258 | | 116742 | 884530 | | 115470 | | | 998728 | | 28 |
| ۱ | | 36 | | 884903 | | 115097 | 88618 | | 113815 | | The second | 998718 | | 24 |
| ı | ч | 40 | | 886542 | | 113458 | 887833 | | 112167 | - 0012 | | 998708 | | 20 |
| ı | 7 | 44 | 26 | 888174 | | 111826 | 889476 | | 110524 | 0013 | 301 16 | 998699 | 34 | 16 |
| ı | | 48 | | 889801 | 2700 | 110199 | 891112 | 2717 | 108888 | 0013 | 311 16 | 998689 | 33 | 12 |
| ı | | 52 | | 891421 | | 108579 | 892743 | | 107258 | 0013 | | 998679 | | 8 |
| ı | U | 56 | | 893035 | | 106965 | 894366 | 2697 | 105634 | 0013 | 331 17 | 998669 | 31 | 4 |
| ı | 18 | , 0 | 30 | 8.894643 | 2670 | 11.105357 | 8.895984 | 2687 | 11.104016 | 10.0013 | 341 17 | 9.998659 | 30 | 12 0 |
| ı | | 4 | 31 | 896246 | | 103754 | 897596 | | 102404 | 0013 | 351 17 | 998649 | 29 | 56 |
| ı | | | 32 | 897842 | 2651 | 102158 | 899203 | 2667 | 100797 | 0013 | 361 17 | 998639 | 28 | 52 |
| ľ | | 12 | | 899432 | | 100568 | 900803 | | 099197 | 0013 | | 998629 | | 48 |
| ŀ | | | 34 | 901017 | | 098983 | 902398 | | 097602 | 0013 | | 998619 | | 44 |
| ı | | 20 | | 902596 | | 097404 | 903987 | | 096013 | | | 998609 | | 40 |
| ı | | 24 28 | | 904169 | | 095831 | 905570 | | 094430 | | | 998599 | | 36 |
| ľ | | 32 | | 907297 | | 094264 092703 | 90714 | | 092853 091281 | 0014 | | 998589 998578 | | 28 |
| ı | ы | 36 | | 908853 | | 092703 | 910283 | | 089715 | | 32 17 | 998568 | | 24 |
| ı | | 40 | | 910404 | | 089596 | 911846 | | 088154 | | | 998558 | | 20 |
| ı | . , | | 41 | 911949 | | 088051 | 913401 | | 086599 | 0014 | | 998548 | | 16 |
| ı | | | 42 | 913488 | | 086512 | 914951 | | 085049 | 0014 | | 998537 | | 12 |
| ı | | 52 | 43 | 915022 | | 084978 | 916498 | | 083505 | 0014 | | 998527 | | 8 |
| | 1 | | 44 | 916550 | | 083450 | 918034 | | 081966 | 0014 | | 998516 | | 4 |
| 1 | 19 | 0 | 15 | 8.918073 | 2529 | | | | 11.080432 | | | 9.998506 | | |
| 1 | | | 46 | 919591 | 2520 | 080409 | 921096 | | 078904 | 0013 | | 998495 | | 56 |
| 1 | | 8 | 47 | 921103 | | 078897 | 922619 | | 077381 | 0013 | | 998485 | 13 | 52 |
| 1 | | 12 | | 922610 | | 077390 | 924136 | | 075864 | | | 998474 | | 48 |
| 1 | | 16 | | 924112 | | 075888 | 925649 | | 074351 | 0013 | | 998464 | | 44 |
| 1 | | 20 | | 925609 | 2486 | 074391 | 927156 | | 072844 | | | 998453 | | 40 |
| 1 | | 24 | | 927100 | 2477 | 072900 | 928658 | | 071342 | | 558 18 | 998442 | | 36 |
| | | 28 | | 928587 | | 071413 | | | | | 69 18 | 998431 | | 32 |
| 1 | 13 | 32 | | | | 069932 | | | | | 79 18 | 998421 | | 28 |
| | | 36 | | | | 068456 | | | | | 90 18 | 998410 | | 24 |
| | | 40 | | | | 066985 065519 | | | 065384 | | 01 18 12 18 | 998399 998388 | | 20 16 |
| | | 48 | | | | 064058 | | | 063907 062435 | | 23 18 | 998377 | | 12 |
| | | | 58 | | | 062602 | | | 060968 | | 34 18 | 998366 | | 8 |
| | | | 59 | | | 061150 | | | | | 45 18 | 998355 | | 4 |
| | 20 | | 60 | | | 059704 | | | 058048 | | 56 18 | 998344 | | |
| | m. | S. | = | Cosine. | | | | | | | | | | |
| 1 | -240 | 3+ | | | 22200 | Secant. | Cotang. | | Tang. | Cosec | | Sine. | 1 11 | n. s. |
| | | - | - | 5 H | | 1 407 | 1 | or | 1 100 | | 85 De | | - | - |
| J | P. | P. | to | 18 | 15" | 401 | Is | 15" | 403 | Is o | 15" | 3 | P. | P. to |
| | S | or | " | 3 | 30 4.5 | 801 1202 | 2 3 | 30 45 | 806 1209 | 2 3 | 30 45 | 5,8 | S | or " |
| e di | - | | | | | 1 2000 | | 217 | 1 1200 | 3 () | 70 | 1 0 | | - |

| - | | _ | | - | | | | | | m | | | | |
|-----|----------|----------|-------------------|------|------------------|------------------|--------|------------------|------------------|------|--------------------|-----|------|-----|
| | - | _ | 0.11 | | 7 | and | l Seca | ints. | | | BLE V. | | - 5 | 23 |
| - | | 1 | O H | D. | Corre | F m | or | | | 5 De | cosine. | 1 | lana | _ |
| m. | | = | | | | Tang. | D. | Cotang. | Secant. | = | | | m. | - |
| 20 | | | | | 11.059704 | | | | 10.001656 | | 9.998344 998333 | | | 5 |
| п | 8 | | | | | | | | | | 998322 | | | 5 |
| 0 | 12 | | | | | | | | | | 998311 | | | 4 |
| 2 | 16 | | 0 -000 | | 053966 | 947734 | 2390 | 052266 | | | 998300 | | | 4 |
| | 20 | | The second second | | | | | | 001711 | | 998289 | | | 4 |
| | 24 | | | | | | | | 001723 001734 | | 998277 998266 | | | 3 |
| di | 32 | | | | | | | | 001745 | | 998255 | | | 2 |
| | 36 | 1 | | | | | | 045144 | 001757 | | 998243 | | 1 | 2 |
| | 40 | | | | 045501 | 956267 | | | 001768 | | 998232 | | | 2 |
| | 44 | | 955894 | | | | | | 001780 | | 998220 | | | 1 |
| | 48 | 12 | | | | | | | 001791 | 1 | 998209 998197 | | | -1 |
| | | 14 | 960052 | | | | | 039321 | 001814 | 1 | 998186 | | | 1 |
| 21 | . 0 | | | | | | | 11.036745 | | | 9.998174 | - | - | |
| V | 4 | 16 | 962801 | | | | 2300 | 035361 | 001837 | 19 | 998163 | | | 5 |
| | 8 | 17 | 964170 | | | | | | 001849 | | 998151 | 43 | | 5 |
| | | 18 | 965534 | | | | | | 001861 | | 998139 | | | 4 |
| | | 19 | 966893 968249 | | | | | 031234 | 001872 001884 | | 998128 | | T | 4. |
| | 24 | | 969600 | | | | | 029867 028504 | 001896 | 1 | 998116 998104 | | | 3 |
| 4 | | 55 | 970947 | | | | | 027145 | 001908 | | 998092 | | 1 | 3 |
| | | 23 | 972289 | 2231 | 027711 | | 2251 | 025791 | 001920 | 20 | 998080 | 37 | | 2 |
| | | 24 | 973628 | | | | | 024440 | 001932 | | 998068 | | | 2 |
| 4 | | 25 26 | 974962 | | 025038 | | | 023094 | 001944 | | 998056 | | 34 | 20 |
| | 44 | | 976293 977619 | | | 978248 979586 | | 021752 020414 | 001956 001968 | | 998044 998032 | | | 1: |
| | | 28 | 978941 | | | | | 019079 | 001980 | | 998020 | | | - 8 |
| | 56 | 29 | 980259 | | | 982251 | | 017749 | 001992 | 20 | 998008 | | | 4 |
| 22 | - 0 | 30 | 8.981573 | 2183 | 11.018427 | 8.983577 | 2204 | 11.016423 | 10.002004 | 20 | 9.997996 | | 38 | (|
| | 4 | 31 | 982883 | 2177 | 017117 | 984899 | | 015101 | 002016 | | 997984 | | | 56 |
| | | 32 | 984189 | | | 986217 | | 013783 | 002028 | | 997972 | | | 5 |
| | 16 | 33 | 985491 986789 | | 014509 013211 | 987532 988842 | | 012468 011158 | 002041 | 20 | 997959 997947 | | 17 | 48 |
| - | 20 | | 988083 | | | 990149 | | 009851 | 002065 | | 997935 | | | 4(|
| | 24 | 36 | 989374 | | | | | 008549 | 002078 | | 997922 | | | 30 |
| | 28 | | 990660 | | 009340 | | | 007250 | 002090 | | 997910 | 23 | | 32 |
| , | 32 | | 991943 | | 008057 | 994045 | | 005955 | 002103 | | 997897 | | | 28 |
| | 36 40 | | 993222 994497 | | 006778 005503 | 995337 996624 | | 004663 003376 | 002115 002128 | | 997885 997872 | | | 21 |
| 9 | 44 | | 995768 | | 003303 | 997908 | | 003310 | 002140 | | 997860 | | | 10 |
| | 48 | 42 | 997036 | | 002964 | 999188 | | 000812 | 002153 | | 997847 | | | 12 |
| | 52 | | 998299 | | | | | 10.999535 | 002165 | 21 | 997835 | | | 8 |
| - | 56 | | 999560 | | 000441 | 001738 | | 998262 | 002178 | 21 | 997822 | - | | 4 |
| 23 | | | | | | | | 10.996993 | | | 9.997809 | | 37 | (|
| | | 46 47 | 002069 003318 | | 997931 996682 | 004272 005534 | | 995728 994466 | 002203 002216 | | 997797 997784 | | | 56 |
| | 12 | | 004563 | | 995437 | 006792 | | 993208 | 002229 | | 997771 | | | 48 |
| | 16 | 49 | 005805 | | | 008047 | | 991953 | 002242 | | 997758 | 11 | | 44 |
| | 20 | | | | | | | 990702 | 002255 | | 997745 | | 4 | 40 |
| | 24 28 | | 008278 | | | 010546 | | 989454 | 002268 | | 997732 | | | 36 |
| | 32 | 53 | 009510 010737 | | | 011790 | | 988210 986969 | 002281 | | 997719 997706 | 8 | | 32 |
| | 36 | | 011962 | | | | | 985732 | 002307 | | 997693 | | | 21 |
| | 40 | | 013182 | | | | | 984498 | 002320 | | 997680 | | 0 | 20 |
| | 44 | | 014400 | 2023 | 985600 | | | 983268 | 002333 | | 997667 | | | 16 |
| | 48 | | 015613 | | 984387 | 017959 | | 982041 | 002346 | | 997654 | | | 12 |
| | 52 56 | | 016824 018031 | | 983176 981969 | 019183 020403 | | 980817 979597 | 002359 | | 997641 997628 | 2 | | 4 |
| 1 | | 60 | 019235 | | 980765 | 021620 | | 978380 | 002312 | | 997614 | 0 | 36 | 0 |
| n. | | - | Cosine. | = | | Cotang. | | Tang. | Cosec. | | Sine. | = | - | - |
| 110 | S. | | 5 Ho | ire | Secant. | Cotang. | or | rang. | | Dec | rees. | 1 | m. | S. |
| - | _ | 1 | ls | 15" | 327 | 18 | 15" | 330 | | 5" | 3 1 | - | | - |
| | P. 1 | | 2 | 30 | 655 | 2 | 30 | 661 | | 30 | 6 | | P. | |
| 5 | or | | 3 | 45 | 982 | 3 | 45 | 992 | | -5 | 9 | , 3 | or ' | |
| - | - | | - | - | - | - | - | | THE RESERVE | - | - | - | - | - |

| 2 | 24 | | TAB | LE V. | Lo | garithm | ic Sine | s, Tangen | ts, | -, | | | |
|-----|----------|----------|------------------|------------------|------------------|----------|--------------------|------------------|----------|--------|------------------|--------|-------|
| | | _ | 0 H | Iour, | | | or | | | 6 D | egrees. | | |
| m | . s | . 1 | Sine. | D. | Cosec. | Tang | . D. | Cotang. | Secant | 1 | | 11 | m. |
| 24 | . (| | 9.01923 | 35 2000 | 10.98076 | 9.0216 | 20 2023 | 10.978380 | 10.0023 | 86 22 | 9.997614 | 60 | 36 |
| | 4 | | | 5 1995 | | | 34 2017 | | | | 997601 | | |
| P | 8 | | | 2 1989 | | | 44 2011 | 975956 | | | 997588 | 58 | |
| | 12 | | | 5 1984 | 977175 | | 51 2006 | | | 26 22 | 997574 | | |
| | 16 | | | 6 1978 | 975984 | | 55 2000 | | | | 99756 | | |
| | 20 24 | | | $\frac{1973}{6}$ | 974797 973614 | | 55 1995 52 1990 | | | | 997547 | | |
| | 28 | | | 7 1962 | 972433 | | 46 1985 | 971148 969954 | | | 997534 | | |
| | 32 | | | 4 1957 | 971256 | | 37 1979 | 968763 | | | 997507 | | |
| | 36 | 9 | | 8 1951 | 970082 | | 25 1974 | 967575 | | | 997493 | | 2 |
| | 40 | | | 9 1947 | 968911 | | 09 1969 | 966391 | 0025 | .1 | 997480 | | 2 |
| ij. | 44 | | | 7 1941 | 967743 | | 1 1964 | | | | 997466 | | |
| | 48 52 | | | 1 1936 | 966579 | | 59 1958 | 964031 | 0025 | | 997452 | | |
| | | 14 | | 2 1930 1 1925 | 965418 964259 | | 44 1953 6 1948 | 962856 961684 | 0025 | | 997439 | | |
| 25 | | | 9.03689 | | | | | 10.960515 | | | 9.99741 | | _ |
| 60 | 4 | | | 8 1915 | 961952 | | 1938 | 959349 | 0026 | | 997397 | | 5 |
| | | 17 | | 7 1910 | 960803 | | 3 1933 | 958187 | 0026 | | 997383 | | |
| | 12 | | | 2 1905 | 959658 | | 3 1928 | 957027 | 00263 | 4.1 | 997369 | | |
| | 16 | | | 5 1899 | 958515 | | 30 1923 | 955870 | 00264 | | 997355 | | 4 |
| | 20 | | 04262 | 5 1895 | 957375 | 04528 | 34 1918 | 954716 | 0026 | | 997341 | | 4 |
| | 24 | | | 2 1889 | 956238 | | 34 1913 | 953566 | 0026 | | 997327 | | 3 |
| | 28 | | | 5 1884 | 955105 | | 1908 | 952418 | 00268 | | 997313 | | 3 |
| | 32 36 | | | 6 1879 | 953974 | | 1903 | 951273 | 00270 | | 997299 | | 2 |
| | 40 | | | 4 1875 9 1870 | 952846 951721 | | 69 1898 08 1893 | 950131 948992 | 0027 | | 997285 | | 2 2 |
| H. | 44 | | | 0 1865 | 950600 | | 4 1889 | 947856 | 00274 | | 997257 | | 1 |
| H | 48 | | | 9 1860 | 949481 | | 7 1884 | 946723 | 0027 | | 997248 | | |
| 1 | 52 | | | 5 1855 | 948365 | | 7 1879 | 945593 | 00277 | | 997228 | | |
| -0 | 56 | 59 | 05274 | 9 1850 | 947251 | 05553 | 35 1874 | 944465 | 00278 | 36 24 | 997214 | 31 | |
| 26 | 0 | 30 | 9.05385 | 9 1845 | 10.946141 | 9.05665 | 9 1870 | 10.943341 | 10.00280 | 1 24 | 9.997199 | 30 | 34 |
| | 4 | 31 | 05496 | | 945034 | | 1 1865 | 942219 | 00281 | | 997185 | 29 | 5 |
| | | 32 | 05607 | | 943929 | | 00 1860 | 941100 | 00283 | | 997170 | | 5 |
| | 12 | 33 | 05717 | | 942828 | | 6 1855 | 939984 | 00284 | | 997156 | | 1 4 |
| ķ. | 16 20 | | | 1 1827 | 941729 | | 0 1851 | 938870 | 00288 | | 997141 | | 4 |
| | 24 | | 05936 06046 | | 940633 939540 | | 0 1846 8 1842 | 937760 936652 | 00287 | | 997127 | | 4 3 |
| | 28 | | 06155 | | 938449 | | 3 1837 | 935547 | 00290 | | 997098 | | 3 |
| | 32 | | 06263 | | 937361 | | 6 1833 | 934444 | 00291 | | 997083 | | 2 |
| | 36 | | 06372 | | 936276 | | 5 1828 | 933345 | 00293 | 2 25 | 997068 | | 2 |
| | 40 | 40 | 06480 | 6 1799 | 935194 | 06775 | 2 1824 | 932248 | 00294 | | 997053 | 20 | 2 |
| | 44 | | 06588 | | 934115 | | 6 1819 | 931154 | 00296 | | 997039 | | . 1 |
| | 48 | | 066965 | | 933038 | | 8 1815 | 930062 | 00297 | | 997024 | | 1 |
| | 52 | 43 | 068030 | | 931964 | | 7 1810 | 928973 | 00299 | | 997009 | | 5 |
| 100 | - | _ | 06910 | _ | 930893 | | 3 1806 | 927887 | 00300 | _ | 996994 | - | 012 |
| 27 | | 45 46 | 9.070170 | | | | | 10.926803 | | | 9.996979 | PRINT. | - |
| | 8 | | 071242 | | 928758 927694 | | 8 1797 6 1793 | 925722 924644 | 00303 | | 996964 996949 | | 5 |
| | 12 | | 073366 | | 926634 | | 2 1789 | 923568 | 00306 | | 996934 | | 4.5 |
| | 16 | | 074424 | | 925576 | | 5 1784 | 922495 | 00308 | - 1 | 996919 | | 4. |
| | 20 | | 075480 | | 924520 | | 6 1780 | 921424 | 00309 | | 996904 | | 40 |
| | 24 | | 076533 | 3 1750 | 923467 | 07964 | 4 1776 | 920356 | 00311 | | 996889 | 9 | . 3 |
| | 28 | | 077583 | | 922417 | | 0 1772 | 919290 | 00312 | | 996874 | | 32 |
| | 32 | | 078631 | | 921369 | | 3 1767 | 918227 | 00314 | | 996858 | _ | 28 |
| | 36 | | 079676 | | 920324 | | 3 1763 | 917167 | 00315 | | 996843 | | 24 |
| | 40 | | 080719 081759 | | 919281 918241 | | 1 1759 7 1755 | 916109 915053 | 00317 | | 996828 996812 | | 20 |
| | 48 | | 082797 | | 917203 | | 0 1751 | 914000 | 00318 | | 996797 | | 12 |
| | 52 | | 083832 | | 916168 | | 0 1747 | 912950 | 00320 | | 996782 | | . 8 |
| | 56 | | 084864 | 1 | 915136 | | 8 1743 | 911902 | 00323 | | 996766 | | 4 |
| 8 | 0 | | 085894 | | 914106 | 08914 | | 910856 | 00324 | | 996751 | | |
| 7. | S. | 7 | Cosine. | | Secant. | Cotang. | ===== | Tang. | Cosec. | | Sine. | 7 1 | |
| | | i | 5 Ho | ours. | Decide . | Journey. | or | rang. | | 33 Deg | | - 1 | ., 5 |
| - | | 1 | 18 | 15" | 277 | 1s | 15" | 280 | 18 | 15" | 3 | | |
| P. | P. t | | 2 | 30 | 554 | 2 | 30 | 561 | 2 | 30 | 7 | | P. to |
| | or ' | | 3 | 45 | 831 | 3 | 45 | 841 | 3 | 45 | 11 | Q | or " |

| - | - | - | | - | - | and | Seca | nts. | | TA | BLE V. | | | 25 |
|-----|----------|----------|--------------------|-----------|---------------------|------------------|-----------|------------------|------------------|----------|------------------|----|-----|-------------------|
| H | | _ | 0 H | ONE | | | or | | | | egrees. | _ | _ | 20 |
| n | 1. \$ | 1/ | Sine. | D. | Cosec. | Tang. | D. | Cotang. | Secant. | D. | | 11 | km. | . 8 |
| 2 | | | | | | | | | | | 9.996751 | - | - | - |
| 1 | 8 (| | | | | | | | | | 996735 | | 34 | 5 |
| Ю | 8 | | | | | | | | | | 996720 | 58 | | 59 |
| н | - 19 | | | | | | | 907734 | 003296 | | 996704 | | | 48 |
| н | 16 | | | | | | | 906698 | 003312 | | 996688 | | 12 | 44 |
| | 20 | | | | | | | 905664 904633 | 003327 003343 | | 996673 | | 1 | 36 |
| н | 28 | | | | | | | 903605 | 003359 | | 996641 | | 13 | 32 |
| | 32 | | | | | 097422 | 1707 | 902578 | 003375 | 26 | 996625 | | | 28 |
| | 36 | | | | | | | 901554 | 003390 | | 996610 | | E | 2 |
| ь | 40 | 11 | | | | | 7 | 900532 899513 | 003406 | | 996594 | | 10 | 20 |
| н | 48 | 1 | | | | | | 898496 | 003422 | | 996562 | | | 16 |
| | | 13 | | | 900938 | | | 897481 | 003454 | | 996546 | | 10 | - 8 |
| П | 56 | 14 | | | 899938 | 103532 | 1684 | 896468 | 003470 | 27 | 996530 | | 10 | 4 |
| 29 | 0 | | | 1653 | 10.898944 | | | | 10.003486 | | 9.996514 | 45 | 31 | |
| 1 | . 4 | | | | | | | 894450 | 003502 | | 996498 | | | 56 |
| - 3 | | 17 | | | 896963 | | | 893444 | 003518 | | 996482 | | | 52 |
| | | 18 19 | | | 895975 894990 | | | 892441 891440 | 003535 003551 | | 996465 | | ·I | 4.4 |
| | | 20 | 105993 | | 894008 | | | 890441 | 003567 | | 996433 | | AL | 4(|
| 1 | 24 | 21 | 106973 | 1630 | 893027 | 110556 | 1658 | 889444 | 003583 | 27 | 996417 | | 1 | 36 |
| E | | 22 | 107951 | | 892049 | | | 888449 | 003600 | | 996400 | | 11 | 32 |
| | 36 | 23 | 108927 | | 891073 890099 | | | 887457 886467 | 003616 003632 | | 996384 996368 | | 1 | 28 |
| | 40 | | 110873 | | 889127 | | | 885479 | 003649 | | 996351 | | 1 | 20 |
| | | 26 | 111842 | | 888158 | | | 884493 | 003665 | | 996335 | | 4 | 16 |
| | 48 | | 112809 | | 887191 | | | 883509 | 003682 | | 996318 | 33 | ii. | 12 |
| | | 28 | 113774 | | 886226 | | | 882528 | 003698 | | 996302 | | | 8 |
| - | | 29 | 114737 | | 885263 | | | 881548 | 003715 | - | 996285 | | - | 4 |
| 30 | | 1 | 9.115698 116656 | | 10.884302 883344 | | | | 10.003731 | 28 | 9.996269 | | 30 | |
| ю | 4. | 32 | 117613 | | 882387 | | | 879596 878623 | 003748 003765 | | 996252 996235 | | | 56 |
| 0.5 | | 33 | 118567 | | 881433 | | | 877652 | 003781 | 28 | 996219 | | | 48 |
| Е | | 34 | 119519 | | 880481 | 123317 | | 876683 | 003798 | | 996202 | | | 4.4 |
| 10 | | 35 | 120469 | | 879531 | 124284 | | 875716 | 003815 | | 996185 | | | 40 |
| 1 | 24 28 | | 121417 122362 | | 878583 877638 | 125249 126211 | | 874751 873789 | 003832 003849 | | 996168 | | U | 38 |
| | 32 | | 123306 | | 876694 | | | 872828 | 003866 | | 996134 | | 0 | 28 |
| 6 | 36 | | 124248 | | 875752 | 128130 | | 871870 | 003883 | | 996117 | | O. | 24 |
| 15 | 40 | | 125187 | | 874813 | 129087 | | 870913 | 003900 | | 996100 | | | 20 |
| 11 | 44 | | 126125 | | 873875 | 130041 | | 869959 | 003917 | 29 | 996083 | | ď. | 16 |
| ш | 48 52 | | 127060 127993 | | 872940 872007 | 130994 131944 | | 869006 868056 | 003934 003951 | 29 29 | 996066 996049 | | ű, | 12 |
| г | 56 | - | 128925 | | 871075 | 132893 | | 867107 | 003968 | 29 | 996032 | | ä, | 4 |
| 31 | | 45 | | | 10.870146 | | | | 10.003985 | | 9.996015 | | 29 | 0 |
| 1 | 4 | 46 | 130781 | 1542 | 869219 | 134784 | 1571 | 865216 | 004002 | 29 | 995998 | | | 56 |
| | | 47 | 131706 | | 868294 | 135726 | | 864274 | 004020 | | 995980 | 13 | | 52 |
| | 12 | - | 132630 133551 | | 867370 | 136667 | | 863333 | 004037 | 29 | 995963 | | | 48 |
| 1 | 16 20 | | 134470 | | 866449 865530 | 137605 138542 | | 862395 861458 | 004054 | 29 29 | 995946 995928 | | | 44 |
| | 24 | 51 | 135387 | | 864613 | 139476 | | 860524 | 004012 | | 995911 | 9 | | 36 |
| | 28 | | 136303 | 1522 | 863697 | 140409 | 1551 | 859591 | 004106 | | 995894 | 8 | 8 | 32 |
| | 32 | | 137216 | | 862784 | 141340 | | 858660 | 004124 | | 995876 | 7 | | 28 |
| | 36 40 | | 138128 139037 | | 861872 860963 | 142269 143196 | | 857731 856804 | 004141 | 29 | 995859 995841 | 6 | | 24 |
| 1 | 44 | | 139944 | | 860056 | 143190 | | 855879 | 004177 | 29 | 995841 | 4 | | 16 |
| | 48 | 57 | 140850 | 1506 | 859150 | 145044 | | 854956 | 004194 | | 995806 | 3 | 1 | |
| | 52 | | 141754 | | 858246 | 145966 | 1532 | 854034 | 004212 | 29 | 995788 | 2 | | 12 8 4 0 |
| 20 | 56 | | 142655 | | 857345 | 146885 | | 853115 | 004229 | | 995771 | 1 | 20 | 4 |
| 32 | = | 60 == | 143555 | 1496 | 856445 | 147803 | 1526 | 852197 | 004247 | 29 | 995753 | 0 | _ | 0 |
| m. | S. | 1 | Cosine. | | Secant. | Cotang. | | Tang. | Cosec. | | Sine. | 1 | m. | S. |
| - | | - | 5 Hor | | 1 010 | 4. | or | 1 0// | | | grees. | | - | |
| | P. 1 | | 1s 2 | 15" 30 | 240 479 | 1 ^s 2 | 15" 30 | 244 | | 5" | 4 | P. | P. | to |
| S | or ' | ' | 3 | 45 | 719 | 3 | 45 | 731 | | 5 | 8 | S | or | " |
| - | - | - | | - | | | - | | - | | | - | | - |

| 0 | 6 | - | TAR | LE V. | To | garithm | ic Sin | es, Tanger | nts. | | | _ | _ | - |
|------|----------|----------|---------|------------------------------|---------------------|--|-----------------------------------|---------------------|---------|---|--------------------------|---------|-------|----------|
| - | | | | Hour, | 3.70 | Parrellilli | or | co, ranger | 100, | Q T | egrees. | | | |
| m. | · S. | 11 | Sine. | D. | Cosec. | Tang. | D. | Cotang. | Secan | | | 1/ | m. | 8. |
| 32 | | - | | | 10.856445 | | _ | | | | | GO | | - |
| | 4 | | | 53 1493 | | | 8 1523 | | | 265 30 | | | 20 | 56 |
| li. | 8 | | | 19 1490 | | | 2 1520 | 850368 | 004 | | | | 1 | 52 |
| 1, | 12 | | | 13 1487 | 853757 | The state of the s | 4 1517 | 849456 | 004 | 1 | W . | | =0 | 48 |
| 11. | 16 20 | | 14/13 | 36 1484 26 1481 | 852864 851974 | | 4 1514 3 1511 | 848546 847637 | | $ \begin{array}{c c} 319 & 30 \\ 336 & 30 \end{array} $ | | | | 44 |
| | 24 | 6 | | 15 1478 | 851085 | | 9 1508 | 846731 | | 354 30 | | | | 36 |
| 100 | 28 | 7 | .14980 | 2 1475 | | | 4 1505 | 845826 | | 372 30 | | | | 32 |
| | 32 | 8 | | 36 1472 | 849314 | | 7 1502 | 844923 | | 390 30 | | A COURT | 1 | 28 |
| 71 | 36 40 | 9 | | 59 1469 51 1466 | 848431 847549 | | 8 1499 7 1496 | 844022 843123 | 004 | 110 | | | | 24 |
| O.E. | 44 | 11 | | 30 1463 | | | 5 1493 | 842225 | 004 | | | | | 16 |
| 2 | 48 | 12 | 1,1 | 08 1460 | 845792 | 15867 | 1 1480 | 841329 | 004 | 463 30 | 995537 | 100 | | 12 |
| | 52 | | | 33 1457 | 844917 | | 5 1487 | 840435 | 004 | 10. | | | The | 8 |
| 20 | - | 14 | - | 1454 | 844043 | | 7 1484 | 839543 | 004 | - | | | - | 4 |
| 33 | 0 | | | 00 1448 | 10.843170 842300 | | $\frac{7}{6}$ $\frac{1481}{1478}$ | 10.838653 837764 | 10.004 | 1 | | | | 56 |
| | 8 | 17 | | 9 1445 | 841431 | | 3.1475 | 836877 | 004 | | | | 1 | 52 |
| ů. | | 18 | | 35 1442 | 840565 | | 8 1473 | 835992 | 004 | | | | | 48 |
| ű. | | 19 | | 1 1439 | 839699 | | 2 1470 | 835108 | 004 | | | | | 44 |
| 1 | 20 | 20 21 | | 1436 1433 | 838836 837975 | | 4 1467 4 1464 | 834226 833346 | 004 | 1 | | | | 36 |
| Е | | 22 | | 35,1430 | 837115 | | 2 1461 | 832468 | 004 | | | | 1 | 32 |
| 5 | 32 | | | 3 1427 | 836257 | | 9 1458 | 831591 | 004 | 1 | | | 1 | 28 |
| E | | 24 | | 00 1424 | 835400 | | 4 1455 | 830716 | 004 | | | | | 24 |
| 1 | 40 | | | 1422 | 834546 | | 7 1453 9 1450 | 829843 828971 | 004 | | | | | 20 |
| j. | 44 | 27 | | $\frac{07}{1419}$ | 833693 832841 | | 9 1447 | 828101 | 004 | | | | | 12 |
| E. | | 28 | | 8 1413 | 831992 | | 7 1444 | 827233 | 004 | | | | | 8 |
| | 56 | 29 | 16885 | 66 1410 | 831144 | 17363 | 4 1442 | 826366 | 004 | 778 32 | 995228 | 31 | | 4 |
| 34 | 0 | | 9.16970 | | 10.830298 | | | 10.825501 | 10.004 | | | | 26 | 0 |
| 3 | 4 | 31 32 | | 7 1405 | 829453 | | | 824638 | 004 | | | | | 56 |
| | | 33 | | 39 140 2 30 1399 | 828611 827770 | 17708 | 4 1433 | 823776 822916 | 004 | | | | 1 | 52 48 |
| 10 | 16 | | | 0 1396 | 826930 | 17794 | | 822058 | 004 | | The second second second | | | 44 |
| 100 | 20 | | | 8 1394 | 826092 | 17879 | | 821201 | 004 | | | | | 40 |
| 12 | 24 28 | | | 4 1391 8 1388 | 825256 | 17965 | | 820345 | 004 | | | | | 36 |
| 111 | 32 | | | 1 1386 | 824422 823589 | 18050 18136 | | 819492 818640 | 004 | | | | | 32 |
| 100 | 36 | | | 2 1383 | 822758 | 18221 | | 817789 | 004 | | | | - | 24 |
| 1 | 40 | | | 2 1380 | 821928 | 18305 | | 816941 | 004 | | | | | 20 |
| 12 | 44 | 41 | | 0 1377 | 821100 | 18390 | | 816093 | 0050 | | | | | 16 |
| 8 | 48 52 | | | 6 1374 1 1372 | 820274 819449 | 18475 18559 | | 815248 814403 | 0050 | | 1 | | | 12 |
| | 56 | | | 4 1369 | 818626 | 18643 | | 813561 | 0050 | | | | | 4 |
| 35 | 0 | 45 | 9.18219 | 6 1367 | 10.817804 | 9.18728 | 0 1399 | 10.812720 | 10.0050 | 084 33 | 9.994916 | 15 | 25 | (1 |
| , | 4 | 46 | | 6 1364 | 816984 | 188120 | | 811880 | 005 | | | | | 56 |
| | 12 | 47 | | 4 1361 | 816166 | 188958 18979 | | 811042 | 005 | | | | | 52 48 |
| | | 49 | | 1 1359 6 1356 | 815349 814534 | 19062 | | 810206 809371 | 005 | | | | | 44 |
| 66 | 20 | | | 0 1353 | 813720 | 19146 | | 808538 | 005 | | | | | 40 |
| | 24 | | | 2 1351 | 812908 | | | 807706 | | 202 33 | | | | 36 |
| | 28 | | | 3 1348 | 812097 | 193124 | | 806876 | | 221 33 | | | | 32 |
| m | 32 | | | 2 1346 9 1343 | 811288 810481 | 193953 194780 | | 806047 805220 | 0052 | 241 33 261 33 | | | | 28 |
| 6 | 40 | | 19032 | 5 1341 | 809675 | 195606 | | 804394 | 0052 | | | | | 20 |
| ii. | 44 | | 19113 | 0 1338 | 808870 | | | 803570 | 0053 | 300 33 | | | | 16 |
| | 48 52 | | | 3 1336 | 808067 | 197253 | | 802747 | | 320 33 | | | | 12 |
| 2 | 56 | | | 4 1333 4 1330 | 807266 806466 | 198074 198894 | | 801926 801106 | | 340 33 360 33 | | | | 8 |
| 36 | | 60 | | 2 1328 | 805668 | 199713 | | 800287 | | 880 33 | | | 24 | 0 |
| m. | S. | - | Cosine. | | Secant. | Cotang. | | Tang. | Cosec | - | Sine. | 7 | m. | S. |
| | | | | ours, | December | cottang. | or | z unig. | COSCC | | grees. | | | |
| P | P. 1 | 10 | 18 | 15" | 211 | 15 | 15" | 216 | 18 | 15" | 5 | P | P | +0 |
| | or | | 2 | 30 | 422 | 2 | 30 | 432 | 2 | 30 | 10 | | P. or | |
| | | | 3 | 45 | 633 | 3 | 45 | 648 | 3 | 4.5 | 14 | 0 | OF | - |

| | | | - | 1000 | | | | I. | 7.0 | 100 | 77 | 1 |
|-----|----------------|------------------|-----------|------------------|-------------------------|-----------|---|--------------|----------------|------------------|------|------|
| | | | -A 10 | | and | d Seca | nts. | | TA | BLE V. | | 27 |
| | and the | . 0 Но | ur, | | Lame J. | or' | 1000 | | | grees. | H | |
| m. | S. / | Sine. | D. | Cosec. | Tang. | D. | Cotang. | Secant | D. | Cosine. | | |
| 36 | | 9.194332 | | | 9.199713 | | 10.800287 | | | 9.994620 | | |
| in. | 4 1 8 2 | 195129 195925 | | 804871 804075 | 200529 201345 | | 799471 798655 | 00540 | 1000 | 994600 994580 | | 56 |
| й | 12 3 | | | 803281 | 202159 | | 797841 | 0054 | | 994560 | | 48 |
| М | 16 4 | | | 802489 | 202971 | | 797029 | 00540 | | 994540 | | 44 |
| | 20 5 24 6 | 198302 199091 | | 801698 800909 | 203783 | | 796218 795408 | 00548 | | 994519 994499 | | 30 |
| | 28 7 | 199879 | | 800121 | 205400 | | 794600 | 0055 | | 994479 | 53 | 35 |
| П | 32 8 | 200666 | | 799334 | 206207 | | 793793 | 0055 | | 994459 | | 2: |
| ě | 36 9 40 10 | 201451 202234 | | 798549 797766 | 207013 207813 | | 792987 792183 | 0055 | | 994438 994418 | | 2 |
| K. | 44 11 | 203017 | | 796983 | 208619 | | 791381 | 0056 | 02 34 | 994398 | 19 | 1 |
| | 48 12 | 203797 | | 796203 | 209420 | | 790580 | 0056 | | 994377 | | 1 |
| - | 52 13 56 14 | | | 795423 794646 | 210220 | | 789780 788982 | 0056 | | 994357 994336 | | -3 |
| 37 | | | 1 | 10.793869 | | | | | - | 9.994316 | - | |
| 4. | 4 16 | 206906 | 1289 | 793094 | 21261 | | 787389 | 0057 | 05 34 | 994295 | 44 | . 5 |
| 10 | 8 17 | | | 792321 | 21340 | | 786595 | 0057 | | 994274 | | 5 |
| Ģ. | 16 19 | 208452 209222 | | 791548 790778 | | | 785802 785011 | 0057 | | 994254 | | 4 |
| of: | 20 20 | | | 790008 | | | 784220 | 0057 | | 994212 | 40 | 4 |
| 7. | 24 21 | 210760 | | 789240 | 216568 | | | 0058 | | 994191 | | . 3 |
| | 28 22 32 23 | 211526 212291 | | 788474 787709 | 217350 218145 | 1 | 782644 781858 | 0058 0058 | THE RESERVE | 994171 | | 3000 |
| è | 36 24 | | | 786945 | | | 100000000000000000000000000000000000000 | | | 994129 | | 64 |
| £ | 40 25 | | | 786182 | | | | | | 994108 | | 2 |
| ji) | 44 26 48 27 | | | 785421 784662 | 22049 | | 779508 778728 | 0059 0059 | | 994087 | | 1 |
| Ľ | 52 28 | | | 783903 | | | 777948 | 0059 | 100 | 994043 | | |
| | 56,29 | 216854 | 1259 | 783146 | | | 777170 | 0059 | 76 35 | 994024 | - | 3 |
| 38 | | | | | | | 10.776393 | | | 9.994003 | | |
| | 4 31 8 32 | | | 781637 780884 | 22438 2 2 515 | | | | | 993982 | | 1 2 |
| | 1233 | | | 780132 | | | | 0060 | 100 | 993939 | | 1 |
| - | 16 34 | | | 779382 | | | | | | 993918 | | , 4 |
| | 20 35 24 36 | | | 778633 777885 | | | | 0061 | | 993897 | | 4 |
| | 28 37 | | | 777139 | | | | | | 993854 | | |
| | 32 38 | | | 776394 | | | | 0061 | | 993832 | | |
| | 36 39 | 4 - | | 775651 774908 | | | 769461 768698 | 0061 0062 | | 993811 | | |
| | 44.41 | 225833 | | 774167 | | | | | | 993768 | 19 | |
| | 48 42 | 226573 | 1231 | 773427 | 23282 | 6 1267 | 767174 | | | 993746 | | Ž. |
| | 52 43 56 44 | | | 772689 771952 | | | | | 00 | 993728 | | 3 |
| 39 | - | | | 10.771216 | | | | - | _ | 9.99368 | | |
| | 446 | 229518 | 1222 | 770482 | 23585 | 9 1258 | 764141 | 0063 | | 993660 | | 1 2 |
| | 8 47 | | | 769748 | | | | | 0. | 993638 | | i |
| | 12 48 16 49 | | | 769016 768286 | | | | | | 993616 | | |
| | 20,50 | | | | | | | 0064 | 28 37 | 993578 | | 3 |
| | 24 51 | | | | | | | 0064 | 50 37 | 993550 | | |
| | 28 52 32 53 | | | | | | | 0064 | 72 37 94 37 | 993528 | | |
| | 36 54 | | | | | | | | 16 37 | | | |
| | 40 55 | | | | | | | | | | | |
| | 44 56 | | | 763205 762485 | | | | | 60 37 82 37 | | | |
| | 52 58 | 238235 | | | | | | 0066 | 04 37 | 993396 | | |
| 10 | 56 59 | 238953 | 1195 | 761047 | 24557 | 9 1233 | 754421 | 0066 | 26 37 | | 1 | |
| 40 | | | 1193 | | 1 | 9 1230 | | | 49 37 | | | |
| m. | S. / | | | Secant. | Cotang. | | Tang. | Cosec | | Sine. | / m | 1. |
| | | 5 Ho | _ | 1 100 | 1 10 | or | 1 104 | 1 20 | | egrees. | | |
| | P. to | 18 | 15" 30 | 189 | 1s 2 | 15" 30 | 194 388 | 1s 2 | 15" 30 | 10 | P. F | |
| 8 | or " | 3 | 45 | 566 | 3 | 45 | 581 | 3 | 45 | 16 | S o | r " |
| _ | | | | | | | | | | | | |

| _ | 1. | _ | | - | | 1,2 | C. | m | | _ | | _ | | - |
|-----|----------|----------|------------------|-----------|------------------|---|----------|------------------|------------------|----------|---------------------------|----|-----|----------|
| 2 | 8 | | TABLE | | Log | garithmi | | s, Tangen | - | | | _ | | |
| 1 | | 1 . | 0 Ho | | 1 () | I Than | or | I Coton | | | grees. | | | _ |
| m. | S. | - | Sine. | D. | Cosec. | Tang. | D. | Cotang. | Secant. | D. | | - | m. | 8. |
| 40 | 0 | 1 3 | | | 10.760330 | | | | 10.006649 | | 9.993351 | | 20 | . 0 |
| 8 | 8 | | | | 759614 758899 | | | 752943 752206 | 006671 006693 | 37 | 993329 993307 | | 2 | 56 |
| | 12 | | | 1 | 758186 | 100000000000000000000000000000000000000 | 10000 | 751470 | 006715 | | 993285 | | | 48 |
| | 16 | 4 | 242526 | | | | | 750736 | | | 993262 | | | 44 |
| 6 | 20 | | | | | | | 750002 | 006760 | | 993240 | | | 40 |
| 3% | 24 | 6 | | | 756053 | | | 749270 | 006783 | | 993217 | | - 1 | 36 |
| , | 28 32 | 8 | 244656 245363 | | 755344 754637 | | | 748539 747809 | 006805 006828 | - | 993195 993172 | | | 32 |
| | 36 | 9 | 246069 | | 753931 | | | 747080 | 006851 | | 993149 | | | 24 |
| В | | 10 | | | | | | 746352 | 006873 | | 993127 | | | 20 |
| 100 | 44 | | 247478 | | 752522 | | | 745626 | 006896 | | 993104 | | | 16 |
| 1 | | 12 13 | 248181 | | 751819 | | | 744900 | 006919 | | 993081 | | | 12 |
| | 56 | | 248883 249583 | | 751117 750417 | 255824 25654 | | 744176 743453 | 006941 006964 | | 993059 993036 | | | 8 |
| 41 | 0 | | | | | | | 10.742731 | | | 9.993013 | = | 10 | 0 |
| - | 4 | _ | 250980 | | 749020 | | | 742010 | 007010 | | 992990 | | -0 | 56 |
| | 8 | 17 | 251677 | 1159 | 748323 | | | 741290 | 007033 | 38 | 992967 | 43 | | 52 |
| -31 | 12 | | 252373 | | 747627 | 25942 | | 740571 | 007056 | | 992944 | | | 48 |
| e | 16 | | 253067 253761 | | 746933 | | | 739854 | 007079 | | 992921 | | = | 44 |
| 15 | 24 | | 254453 | | 746239 745547 | 260863 261578 | | 739137 738422 | 007102 007125 | | 992875 | _ | | 36 |
| | 28 | | 255144 | | 744856 | | | 737708 | 007148 | | 992852 | | | 32 |
| | 32 | | 255834 | | 744166 | | | 736995 | 007171 | 1 | 992829 | | | 28 |
| | 36 | | 256523 | | 743477 | 26371 | | 736283 | 007194 | | 992806 | | | 24 |
| 15 | 40 | | 257211 257898 | | 742789 742102 | | | 735572 734862 | 007217 007241 | | 992783 9927 <i>5</i> 9 | | | 20 16 |
| 15 | 48 | | 258583 | | 741417 | 26584 | | 734153 | 007264 | | 992736 | | | 12 |
| 10. | 52 | | 259268 | | 740732 | | | 733445 | 007287 | | 992713 | | | 8 |
| | 56 | 29 | 259951 | 1137 | 740049 | 26726. | 1176 | 732739 | 007310 | 39 | 992690 | 31 | | 4 |
| 42 | | | 9.260633 | | | | | | | | 9.992666 | | 18 | 0 |
| 0.5 | | 31 | 261314 | | 738686 | | | 731329 | 007357 | | 992643 | | 0 | 56 52 |
| 44 | 12 | 32 | 261994 262673 | | 738006 737327 | 269373 27007 | | 730625 729923 | 007381 007404 | | 992619 992596 | | | 48 |
| 19 | 16 | | 263351 | | 736649 | | | 729221 | 007428 | | 992572 | | | 44 |
| | 20 | 35 | 264027 | 1126 | 735973 | | | 728521 | 007451 | | 992549 | 25 | 83 | 40 |
| 10 | 24 | | 264703 | | 735297 | 272179 | | 727822 | 007475 | | 992525 | | | 36 |
| | 28 32 | | 265377 266051 | | 734623 733949 | | | 727124 726427 | 007499 007522 | | 992501 992478 | | - | 32 |
| | 36 | | 266723 | | 733277 | 27426 | | 725731 | 007546 | | 992454 | | | 24 |
| | 40 | _ | 267395 | | 732605 | | | 725036 | 007570 | | 992430 | | | 20 |
| | 44 | | 268065 | | 731935 | | | 724342 | 007594 | | 992406 | | | 16 |
| 100 | 48 | | 268734 | | 731266 | | | 723649 | 007618 007641 | | 992382 992359 | | | 12 |
| 17 | 52 56 | | 269402 270069 | | 730598 729931 | 277043 27773 | | 722957 722266 | 007665 | | 992335 | | | 8 |
| 43 | | 45 | | | | | | 10.721576 | | 1 | 9.992311 | _ | 17 | 0 |
| | | 46 | 271400 | | 728600 | | | 720887 | 007713 | 40 | 992287 | 14 | - | 56 |
| - | 8 | 47 | 272064 | 1105 | 727936 | 27980 | 11145 | 720199 | 007737 | 40 | 992263 | 13 | | 52 |
| 70 | 12 | | 272726 | | 727274 | | | 719512 | 007761 | | 992239 | | | 4.8 |
| | 16 20 | | 273388 274049 | | 726612 725951 | | | 718826 718142 | 007786 | | 992214 | | | 44 |
| 1 | 24 | | 274708 | | | | | 717458 | 007810 | | 992166 | | | 36 |
| | 28 | | 275367 | | | | | | 007858 | 40 | 992142 | | | 32 |
| | 32 | | | | | | | 716093 | 007882 | 41 | 992118 | | | 28 |
| | 36 | | | | | | | | 007907 | | 992093 | | | 24 |
| | 40 | 56 | | | | | | 714732 714053 | | | 992069 992044 | | | 20 16 |
| | | 57 | | | | | | | 007980 | | 992020 | | | 12 |
| 13 | 52 | 58 | 279297 | 1086 | 720703 | 28730 | | 712699 | 008004 | 41 | 991996 | 2 | | 8 |
| | | 59 | | | | | | 712023 | 008029 | | 991971 | | 10 | 4 |
| 44 | - | 60 | | 1082 | 719401 | 28865 | 1123 | 711348 | 008053 | 41 | 991947 | =0 | 16 | 0 |
| m. | S. | 1 | Cosine. | | Secant. | Cotang. | 1 | Tang. | Cosec. | VIT | Sine. | 1 | m. | S |
| | - | | 5 Ho | - | | | or | | | | grees. | | | |
| | P. | | 18 2 | 15" 30 | 170 | 15 | 15" | 176 | | 15" | 6 | P. | P. | to |
| S | or | " | 3 | 45 | 340 511 | 2 3 | 30 45 | 352 528 | | 30 45 | 12 | | or | |
| - | - | | - | - | | | 20 | 020 | | | 10 | - | - | |

| No. Color | - | | - | | • | | and | Seca | nts. | 20 | TA | BLE V. | | 2 | 9 |
|--|-----|-----|----|----------|------|-----------|----------|------|--|---|----------|----------|-----|------|-----------------|
| S | | | - | 0 Hc | our. | | | or | | 1 | De | grees. | - | _ | - |
| ## 0 0 0.2805.99 10.82 10.719401 9.2856.52 12.3 10.71134s 10.008053 \$1 9.9194.4 \$1 1 2.8124s 10.811 71870.2 89.932c 11.22 71.0074 70.00810 \$1 9.9189.5 12.3 2.8254s 10.77 71.714.66 2.90671 11.8 70.9329 0.081.27 \$1 9.9184.5 10.008053 \$1 9.9184.5 | m. | S. | 1 | | | Cosec. | Tang. | | Cotang. | | _ | | 1 | m. | 8 |
| A | - | - | = | | | | | | | | 4.1 | | - | - | - |
| 8 2 921849 1079 718103 289999 1120 710001 008103 41 991892 12 9 298244 1077 717456 990671 117 709399 008127 41 991872 166 4 283190 1076 716810 291342 1117 708658 008127 41 991872 12 6 283480 1072 715350 292868 1114 707318 008201 41 991872 12 6 283480 1072 715350 292868 1114 707318 008201 41 991872 12 6 28356 1069 714234 293350 1112 706650 008226 42 991743 12 991744 12 991872 12 12 706650 008226 42 991743 12 991744 12 991872 12 706650 008226 42 991744 12 991749 12 706650 008261 42 991744 12 991749 12 706650 008261 42 991744 12 991749 12 706650 008261 42 991744 12 991749 12 706650 008261 42 991744 12 991749 12 706650 008261 42 991744 12 991749 12 706650 008261 42 991744 12 991749 12 70660 12 70 | ** | | | | | | | | | | 1 | | | 10 | 56 |
| 12 3 282541 1077 717456 290671 1118 709329 008127 41 991874 106 4 283190 1076 716810 292132 1117 709658 008152 41 991874 24 6 284180 1072 715520 292689 114 707318 008201 41 991875 28 7 285124 1071 714876 293350 1112 706650 008226 42 991774 32 8 285766 1069 714234 294017 1111 705893 008251 42 991744 40 10 287048 1066 712952 295349 1107 704651 008301 42 991694 40 10 287048 1066 712952 295349 1107 704651 008301 42 991694 41 12 288326 1063 711674 296677 1104 703323 008351 42 991674 45 12 288326 1053 711674 296677 1104 703323 008351 42 991674 45 12 2880964 1051 711036 297339 1103 702661 008376 42 991634 45 15 2998070 1056 709130 299322 1098 700678 008451 42 991574 416 299870 1056 709130 299322 1098 700678 008452 42 991574 416 299870 1056 709130 299382 1098 700678 008502 42 99157 416 299876 1051 707232 301295 1093 699705 008502 42 99157 42 12 12 12 291291 1053 707663 301951 1092 698049 008502 42 991494 42 12 294029 1048 705971 302607 1090 697393 008578 42 991444 42 291594 42 42 294029 1048 705971 302607 1090 697393 008578 42 991448 42 297164 1040 702336 300549 1081 693481 008705 43 991324 44 42 297164 1040 702336 300549 1081 693481 008705 43 991324 44 42 297164 1040 702336 300549 1081 693481 008707 43 991324 44 42 297164 1040 702336 300549 1081 693481 008707 43 991324 44 42 297164 1040 702336 300549 1086 695433 008678 43 991324 44 42 297164 1040 702336 300549 1081 693481 008707 43 991324 44 42 297164 1040 702336 300569 1083 694703 008670 43 991324 44 42 297164 1040 702336 300569 1083 | | | | | | | | | | | | 991897 | | | 59 |
| 20 5 283836 1074 716164 292013 1115 707987 008177 41 99182 24 6 94480 1072 715520 992688 1114 707318 008201 41 991795 28 7 285124 1071 714876 293350 1112 706650 008226 42 991774 32 8 7 285124 1071 714876 293350 1112 706650 008226 42 991774 32 8 7 285124 1071 714876 293350 1112 706650 00826 42 991794 32 91744 1112 707318 008276 42 991794 32 91744 1112 705881 008276 42 991794 32 91744 1112 705881 008276 42 991794 32 91744 1112 705881 008276 42 991694 34 112 286826 1063 711674 296677 1104 703323 008351 42 991694 34 112 288326 1063 711674 296677 1104 703323 008351 42 991694 35 13 288964 1061 711036 297339 1103 702661 008376 42 991694 45 0159.990236 1058 10.7097649.995662 1100 10.701339 10.008426 42 991594 45 0159.990236 1058 10.7097649 299980 1067 700670 008401 42 991594 45 0159.990236 1058 10.7097649 299980 1096 700678 008451 42 991594 416 299137 1033 707863 300633 1095 699362 00850 4991594 112 18 29137 1033 707863 300633 1095 699362 008502 42 991494 112 18 29137 1033 707863 300633 1095 699362 008502 42 991494 12 12 294029 1048 705971 302607 1090 697393 008578 42 991444 12 294029 1048 705971 302607 1090 697393 008578 42 991444 12 12 294029 1048 705971 302607 1090 697393 008563 42 991494 12 294029 1048 705971 302607 1090 697393 008563 42 991494 12 295931 1043 704087 304567 1086 69543 008664 43 991342 42 6 297164 1040 702836 305869 1083 694705 008628 43 991342 42 6 297164 1040 702836 305869 1083 694705 008628 43 991342 44 26 297164 1040 702836 305869 1083 694705 008628 43 991344 42 6 297164 1040 702836 305869 1083 694313 008664 43 991344 42 6 297164 1040 702836 305869 1083 694705 008628 43 991344 42 6 297164 1040 702836 305869 1083 694705 008628 43 991344 42 6 297164 1040 702836 305869 1083 694705 008628 43 991344 44 26 297164 1040 702836 305869 1083 694705 008628 43 991344 44 26 297164 1040 608628 43 305861 1089 696739 008603 43 99134 44 26 297164 1040 608628 43 305861 1070 60863 44 99134 1444 46 299164 44 906828 44 906828 44 906828 44 906828 44 906828 44 906828 44 906828 44 906828 44 906828 44 906828 44 906828 44 | | | 3 | 282544 | | | | | | | | 991873 | | 73,0 | 48 |
| 28 | | | | | 1076 | | | | | | | 991848 | | | 44 |
| 28 7 28.5124 1071 714876 293350 1112 706650 008226 42 991742 32 8 38.5766 1050 714234 394017 1117 705933 008251 42 991743 36 9 286408 1067 713592 294684 1109 705316 008276 42 991743 40 10 287049 1066 712952 293349 1107 704651 008301 42 991694 44 11 287687 1064 712313 296073 1106 703997 008326 42 991674 45 12 288326 1063 711674 296677 1104 703323 008351 42 991687 45 12 288326 1063 711674 296677 1104 703323 008351 42 991687 56 14 289600 1059 710400 298001 1101 701999 008401 42 991594 45 0 15 9.290236 1058 10.709764 9.299662 1100 10.701338 10.008426 42 991544 4 16 290870 1056 709130 299322 1098 700678 008451 42 991544 5 0 16 9.29237 1053 707863 300638 1095 699362 008502 42 991594 6 17 291504 1054 708496 299980 1096 700020 008476 42 991549 6 19 292768 1051 707323 301295 1093 699705 008502 42 991495 16 19 292768 1051 707323 301295 1093 699705 008502 42 991495 16 19 292768 1051 707323 301295 1093 699705 008557 42 991482 20 20 293399 1030 706660 1301951 1092 698049 008502 42 991449 21 294029 1048 705971 302607 1090 697393 008503 42 991492 28 22 294658 1046 705342 303261 1089 697639 008603 42 991393 36 24 295913 1043 704067 304567 1086 695433 008654 43 991349 44 26 297164 1040 702356 305569 1083 699705 008628 43 991349 44 26 297164 1040 702356 305569 1083 694543 008654 43 991349 44 26 297164 1040 702356 305569 1083 694543 008654 43 991349 44 26 297164 1040 702356 305569 1086 693481 008705 43 991249 52 28 298419 1037 701588 307168 1080 699832 008568 43 991144 54 26 297164 1040 702356 305590 1086 693481 008705 43 991249 54 29 299034 1036 700666 307815 1078 699690 008853 43 991161 54 30 30364 1025 696636 312927 1068 689602 008858 43 991134 54 26 297164 1040 698569 30073 689602 008858 43 991134 54 26 297164 1040 698569 30073 689602 008858 43 991134 54 26 297164 1040 688608 30073 689602 008858 43 991134 54 26 297164 1040 688608 30073 689602 008858 43 991134 54 26 30 30364 1025 696636 312927 1068 687673 008902 43 991092 52 33 301514 1099 69486 31098 1075 68939 009074 44 990694 54 46 300874 1010 690868 31189 1066 688381 0090 | | | | | | | | | | | | 991823 | | 100 | 40 |
| 36 9 286408 1067 713592 294684 1109 705316 0008376 42 991748 40 10 287048 1066 712952 2953349 1107 704651 0008301 42 991695 44 11 287687 1064 712313 296013 1106 705387 0068326 42 991674 45 12 288326 1063 711674 296677 1104 703323 008351 42 991685 56 14 290600 1059 710400 298001 101 701999 008401 42 991595 45 0 15 9.290236 1058 10.709764 9.298662 1100 10.701338 10.008426 42 991544 41 41 290870 1056 709130 299382 1098 700678 700678 5 17 291504 1054 708496 299980 1096 700020 7008451 42 991549 12 18 292137 1053 707863 3006381 1095 699362 006802 42 991495 16 19 29768 1051 707323 301295 1092 698049 008552 42 991448 20 20 293399 1050 706601 301951 1092 698049 008552 42 991438 25 22 294658 1044 705342 303261 1089 696739 008603 42 991393 32 23 295286 1045 704714 303914 1087 696086 008602 43 99137 36 24 295913 1043 704087 304567 1086 695439 008603 43 99137 44 26 297164 1040 702836 305869 1083 694782 008673 43 99124 45 29 29034 1036 700966 307815 1078 692815 00873 43 99124 46 23 290934 1036 700966 307815 1078 692815 008763 43 99124 46 309, 299655 1034 10,700345 9.308463 1077 10,691537 10,008074 43 99124 46 303, 299655 1034 0,700345 9.308463 1077 10,691537 10,008074 43 99127 47 48 49 49 49 49 49 49 49 | | | | | | 1 | | | | | | | | | 30 |
| 36 9 286408 1067 713592 294684 1109 703516 008376 42 991692 44 111 287687 1064 712313 296013 1106 703387 008326 42 991674 44 111 287687 1064 712313 296013 1106 703387 008326 42 991674 2513 288326 1063 711674 296687 1104 703323 008351 42 991682 5213 288964 1061 711036 297339 1103 703661 008376 42 991684 52 13 289600 1059 710400 298001 1101 701999 008401 42 991595 45 10 10 10 10 10 10 10 10 10 10 10 10 10 | | | | | | | | | | | 100.00 | | | | 38 |
| 40 10 287048 1066 | | | | | | | | | | | 200 00 0 | | | 16 | 24 |
| 44 11 | | | | | 1 | | | | | | | | | 100 | 20 |
| 48 12 28836 1063 711674 296677 1104 703323 008351 42 991645 52 13 288964 1061 711036 297339 1103 702661 008376 42 991636 56 14 289600 1059 710400 298001 1101 701999 008401 42 991536 44 105 290870 1056 709130 299322 1088 700676 008451 42 991546 416 291544 1054 708496 299980 1096 700020 008476 42 991522 1218 292137 1053 707823 201295 1093 698705 008451 42 991542 20129 293399 1050 707863 300638 1095 699362 008502 42 991495 2020 293399 1050 706601 301951 1092 698049 008524 42 991442 2914029 1048 705971 302607 1090 697393 008574 42 991437 42 42 42 42 42 42 42 4 | | | | | | | | | | | | 991674 | | | 16 |
| Sec. 14 289600 1059 710400 298001 1101 701999 008401 42 991895 | | 48 | 12 | | | | | | 703323 | 008351 | 42 | 991649 | 48 | | 12 |
| 45 0 15 9.290236 1058 10.709764 9.298662 1100 10.701338 10.008426 42 9.991574 4 16 299870 1056 709130 299322 1098 700078 008451 42 991544 12 12 12 12 15040 1054 708496 299980 1096 700070 008476 42 991546 12 12 18 292137 1053 707863 300638 1095 699362 008502 42 991495 16 19 292768 1051 707232 301295 1093 698705 008527 42 991495 20 20 203339 1050 706601 301951 1092 698049 008552 42 991448 22 22 24658 1046 705342 303361 1099 696739 008563 42 991495 32 22 24658 1046 705342 303361 1099 696739 008503 42 991393 32 23 295286 1045 704714 303914 1087 696086 008628 43 991393 32 23 295286 1045 704714 303914 1087 696086 008628 43 991393 44 26 297164 1040 702836 308569 1089 696739 008503 42 991394 42 62 297164 1040 702836 305869 1089 696742 0086769 43 991391 44 26 297164 1040 702836 305869 1083 694131 008703 43 991295 44 26 297164 1040 702836 305869 1083 694131 008703 43 991295 44 26 297164 1040 702836 305869 1083 694131 008703 43 991295 44 27 39461 1037 701588 307168 1080 692852 008756 43 99124 56 29 299934 1036 700966 307815 1078 692185 008762 43 991214 12 33 301514 1029 698468 310398 1073 699283 008636 43 991121 12 33 301514 1029 698468 310398 1073 699691 008833 43 991161 12 33 301514 1029 698468 310398 1073 689602 008859 43 991141 12 33 301514 1029 698468 310398 1073 689602 008856 43 991141 12 33 301514 1029 698468 310398 1073 689602 008856 43 991104 12 33 304593 1022 699507 315608 1073 689602 008856 43 991104 12 33 304593 1022 699507 315608 1078 686703 008962 43 991092 44 44 41 306430 1017 693570 315523 1068 687673 008962 43 991092 44 44 46 303914 1016 692350 316350 1056 686392 00914 43 990980 44 44 1064 306430 1017 693570 315523 1068 687673 009964 44 990968 44 44 1064 306430 1017 693570 315523 1068 687673 009962 43 991092 44 990061 12 46 310685 1006 68871 314957 1006 68871 314957 1006 68871 314957 1006 68871 314957 1006 68871 314957 1006 68871 314957 1006 68871 314957 1006 68871 314957 1006 68903 314957 1007 68903 32479 1015 68003 314997 1001 686903 32479 1056 68304 32496 00940 44 990581 44 6006 317879 998 685703 32185 | | | | 288964 | 1061 | 711036 | 297339 | 1103 | | | 100 | 991624 | | | 8 |
| 4 16 290870 1036 709130 299322 1098 700678 008451 42 991545 8 17 291504 1054 708496 299980 1096 700020 0084676 42 991495 12 18 292137 1033 707863 300638 1095 699362 008502 42 991495 20 20 293399 1050 706601 301951 1092 698049 008552 42 991474 20 20 293399 1050 706601 301951 1092 698049 008552 42 991474 22 21 294029 1048 705971 303607 1090 697393 008578 42 991472 28 22 294658 1046 705342 303261 1089 696739 008603 42 991397 32 23 295286 1045 704714 303914 1087 6996086 008628 43 991347 36 24 295913 1043 704087 304567 1086 695433 008664 43 991347 40 25 296539 1042 703461 303218 1084 694782 008679 43 991324 44 26 297164 1040 702836 305869 1083 694131 008705 43 991297 48 27 297788 1039 702212 305519 1081 693481 008730 43 991297 52 28 2994121037 701588 307168 1080 692832 008756 43 991247 45 300276 1032 699724 309109 1075 699281 008736 43 991214 45 300276 1032 699724 309109 1075 690891 008883 43 991161 28 301514 1029 698486 310398 1073 690891 008883 43 991161 28 301514 1029 698486 310398 1073 690890 008853 43 991161 30 30 30354 1025 696636 312937 1068 687673 008968 43 99104 24 36 303364 1025 696636 312937 1068 687673 008968 43 99104 24 36 303364 1025 696636 312937 1068 687673 008968 43 99104 24 36 303364 1025 696636 312937 1068 687673 008968 43 99104 24 36 303364 1025 696636 312937 1068 687673 008968 43 99104 24 36 303364 1025 696636 312937 1068 687673 008968 43 99104 24 36 30354 1025 696636 312937 1068 687673 008968 43 99104 24 36 30364 1025 696636 312937 1068 687673 008964 49 99093 24 36 30368 1006 68871 314987 1068 688715 009064 44 990934 24 46 309474 1010 69256 31659 1066 688747 009927 44 990692 24 36 307650 1014 609350 31659 1066 688747 009927 44 990906 25 33 31698 1009 68680 313991 1053 680671 009260 44 990934 25 33 316598 1009 68680 313991 1053 680671 009260 44 990936 25 33 31698 1009 68680 331804 1055 10.681936 10.009197 44 990892 25 33 31898 1004 688107 321222 1048 67878 009328 44 990671 25 50 31899 1001 686903 321891 1055 67879 009452 44 990675 | | 56 | | | | | 298001 | 1101 | | | - | 991599 | 46 | | 4 |
| S | 45 | 0 | | 9.290236 | 1058 | 10.709764 | 9.298662 | 1100 | 1 | | | 9.991574 | | | (|
| 12 18 | | | | | | | | | | | | 991549 | | | 56 |
| 16 19 2927 c8 1051 707232 301295 1093 698049 008552 42 991445 24 21 294029 1048 705971 302607 1090 697393 008507 42 991445 28 22 294658 1046 705342 303261 1089 696739 008603 42 991332 32 23 295286 1045 704714 303914 1087 696666 606686 43 991343 40 25 296539 1042 703461 305218 1084 694782 008679 43 991344 44 26 297164 1040 702836 305869 1083 694181 008705 43 991297 48 27 297788 1039 702212 306519 1081 693481 008705 43 991297 48 27 299034 1036 700966 307815 1078 692832 008756 43 99127 46 0 30 9.299655 1034 10.700345 9.308463 1077 10.691537 10.008807 43 991214 46 0 30 9.299655 1034 10.700345 9.308463 1077 10.691537 10.008807 43 991114 47 0 43 300276 1032 699724 309109 1075 699246 0088539 43 991114 48 13 300276 1032 699724 309109 1075 699024 008853 43 991114 49 30 303364 1025 696636 311042 1071 688958 008910 43 991104 40 40 303364 1025 696636 312327 1068 687673 008962 43 99103 28 37 303979 1026 694789 311287 1066 687834 009914 43 990986 36 39 305207 1020 694789 311287 1066 68324 00914 44 41 306430 1017 693570 315523 1061 684477 009092 44 990984 40 40 305815 1019 694181 314885 1062 683205 009144 44 990882 41 44 45 307650 1014 692959 31659 1066 683245 009145 44 990984 42 43 307650 1014 692959 31659 1066 683245 009145 44 990984 44 45 315485 906 688711 320552 1050 679408 009303 44 990977 44 45 31289 1006 688711 320552 1050 679408 009303 44 990673 32 31 31698 1006 688711 320552 1050 679408 009305 44 990673 32 31 31 31 31 31 31 31 | | | | | | | | | | | | | | | 52 |
| 20 20 293399 1050 706601 301951 1092 698049 008552 42 991442 28 22 294658 1046 705342 3032601 1099 697393 008503 42 991432 28 22 294658 1046 705342 303261 1089 696739 008603 42 991392 32 32 294658 1045 704714 303914 1087 696686 008628 43 991374 40 25 296539 1042 703461 305218 1084 694782 008679 43 991342 44 266 297164 1040 702836 305869 1083 694131 008705 43 991297 44 266 297164 1040 702836 305869 1083 694131 008705 43 991297 52 28 298412 1037 701588 307168 1080 692832 008756 43 991297 52 28 2994058 1037 701588 307168 1080 692832 008756 43 991297 52 28 2994058 1034 10.700345 9.308463 1077 10.691537 10.008807 43 991214 43 10.00870 10.008807 43 991214 12 33 301514 1029 698486 310398 1073 689602 008885 43 991116 12 33 301514 1029 698486 310398 1073 689602 008885 43 991116 16 34 302132 1028 697868 311042 1071 688958 008910 43 99109 2036 303644 1027 697252 311685 1070 688315 008936 43 99109 28 37 303979 1023 696021 312907 1067 687033 008968 43 991042 28 37 303979 1023 696021 312907 1067 687033 008968 43 99109 28 37 303979 1023 696021 312907 1067 687033 008968 43 99109 28 37 303979 1023 696021 312907 1067 687033 008968 43 99109 28 37 303979 1023 696021 312907 1067 687033 008968 43 99109 44 41 306430 1017 693570 315523 1068 6687673 008962 43 99103 305207 1009 694181 314885 1062 685715 009060 44 990934 44 41 306430 1017 693570 315523 1061 684477 009092 44 990934 44 64 309474 1010 690526 318697 1054 681303 009223 44 990777 84 84 310685 1007 689315 319991 1054 681303 009223 44 990777 84 84 310685 1007 689315 319991 1054 681303 009223 44 990777 84 1248 310685 1007 689315 319991 1054 681303 009223 44 990777 84 1248 310685 1007 689315 319991 1054 681303 009223 44 990777 84 1248 310685 1007 689315 319991 1054 68304 009354 44 990934 44 990832 32 33 313699 1001 686903 323479 1055 679408 009303 44 990934 44 990555 44 314997 999 685104 324358 1044 676894 009409 44 990595 44 590565 44 514997 999 685104 324358 1044 676894 009409 44 990595 45 5050 311893 1006 688701 323331 1044 676894 009409 44 990595 44 5050 31899 1096 68350 31040 | | | 1 | | | | | | | | | | | 1 | 48 |
| 24 21 | | | | | | | | | | | 100 | | | | 4(|
| 28 22 29468 1045 705342 30326 1089 696739 008603 42 991337 36 24 295913 1043 704087 304567 1086 695483 008663 43 991347 40 25 296539 1042 703461 303218 1084 694782 008679 43 991324 44 26 297164 1040 702836 303869 1083 694131 008705 43 991287 48 27 297788 1039 702212 306519 1081 693481 008705 43 991287 52 28 298412 1037 701588 307168 1080 692832 008756 43 991287 44 26 299034 1036 700966 307815 1078 692185 008782 43 991218 46 0309 299655 1034 10.700345 3.038646 1077 10.691537 10.008807 43 991218 43 300276 1032 699724 309109 1075 690891 008833 43 991167 43 301514 1029 698468 310398 1073 689602 008885 43 99114 12 33 301514 1029 698468 310398 1073 689602 008885 43 99114 16 34 302132 1028 697868 311042 1071 688958 008910 43 991082 24 36 303364 1025 696636 312327 1068 6887673 008968 43 991082 28 37 303379 1023 696021 312967 1067 687033 008968 43 991082 28 37 303379 1023 696021 312967 1067 687033 008968 43 99104 44 1306430 1017 693570 315523 1061 684477 009092 44 990985 44 44 306430 1017 693570 315523 1061 684477 009092 44 990985 44 44 306430 1017 693570 315523 1061 684477 009092 44 990985 44 44 306430 1017 693570 315523 1061 684477 009092 44 990985 44 44 306430 1017 693570 315523 1061 684477 009092 44 990985 45 45 45 45 45 45 45 | | | | | | | | | The state of the s | | 1000 | | | | 36 |
| 36 24 295913 1043 704087 304567 1086 695433 008654 43 991342 44 26 297164 1040 702936 305869 1083 694131 008705 43 991329 48 27 297788 1039 702212 306519 1081 693481 008730 43 991297 52 28 298412 1037 701588 307168 1080 692832 008756 43 991249 56 29 299034 1036 700966 307815 1078 692185 008782 43 991214 146 0 30 9.299655 1034 10.700345 9.308463 1077 10.691537 10.008807 43 991214 12 33 301514 1029 693486 310398 1073 689602 008855 43 991116 12 33 301514 1029 693486 310398 1073 689602 008855 43 991116 16 34 302132 1028 69786 311042 1071 68958 008910 43 991090 20 35 302748 1027 697252 311685 1070 68815 008963 43 991116 24 36 303364 1025 696636 312327 1068 687673 008963 43 99103 28 37 303979 1023 696021 312967 1067 687033 008985 43 99103 28 37 303979 1023 696021 312967 1067 687033 008985 43 99103 28 37 303979 1023 696021 312967 1067 687033 008985 43 99103 28 37 303979 1023 696021 312967 1067 687033 008985 43 99103 28 37 303979 1023 696021 312967 1067 687033 008985 43 99103 28 37 303979 1023 696021 312967 1067 687033 008985 43 99103 28 37 303979 1023 696021 312967 1067 687033 008985 43 99103 28 37 303979 1023 696021 312967 1067 687033 008985 43 99103 28 37 303979 1023 696021 312967 1067 687033 008985 43 99103 28 37 303979 1023 696021 312967 1067 687033 008985 43 99103 28 37 303979 1023 696021 312967 1067 687033 008985 43 99103 40 40 305819 1019 694181 314885 1062 685115 009066 44 990934 44 41 306430 1017 693570 315523 1061 684477 009092 44 990934 44 42 307041 101 692959 316159 1066 68341 009118 49 990852 43 307650 1014 692959 316159 1066 68341 009118 49 990852 43 307650 1014 692959 316159 1066 68341 009118 49 990852 44 990770 45 316891 10910 688711 305029 1050 687678 009127 44 990934 44 41 104 104 104 104 104 104 104 104 | | | | | | | | | | | | 991397 | | | 32 |
| 40 25 296539 1042 703461 305218 1084 694782 008679 43 991321 44 26 297164 1040 702353 305869 1083 694131 008730 43 991321 48 27 297788 1039 702212 306519 1081 693481 008730 43 991275 52 28 298412 1037 701588 307168 1080 692832 008756 43 991245 66 29 299034 1036 700966 307815 1078 692818 008782 43 991218 43 13 3002761 1032 699724 309109 1075 690891 008833 43 991162 832 300895 1031 699105 309754 1074 690246 008859 43 991161 12 33 301514 1029 698486 310398 1073 689602 008885 43 991141 16 34 302132 1028 697868 311042 1071 688958 008910 43 991006 2035 302748 1027 697252 311685 1070 688315 008936 43 991064 28 37 303979 1023 696021 312967 1067 688315 008936 43 991064 28 37 303979 1023 696021 312967 1067 687033 008985 43 991012 32 33 304503 1022 695407 313608 1065 686392 009014 43 990996 40 40 305819 1019 694181 314885 1062 685115 009064 49 990994 44 41 306430 1017 693570 315523 1061 684477 009092 44 990998 44 41 306430 1017 693570 315523 1061 684477 009092 44 990998 44 44 1 306430 1017 693570 315523 1061 684477 009092 44 990998 44 44 309041 692550 316795 1058 683205 009145 44 990985 52 43 307650 1014 6922550 316159 1060 683841 009118 44 990852 52 43 307650 1014 6922550 316159 1060 683841 009118 44 990885 52 43 307650 1014 6922550 316159 1060 683841 009118 44 99085 52 43 307650 1014 6922550 316159 1060 683841 009119 44 990852 52 43 307650 1014 692350 316795 1058 683205 009145 44 990750 124 11899 1006 688711 320592 1050 679408 009303 44 990767 124 131289 1006 688711 320592 1050 679408 009303 44 990767 124 131289 1006 688711 320592 1050 679408 009303 44 990671 124 131289 1006 688703 32333 1043 676267 009435 44 990750 44 55 314897 997 685104 324358 1040 675017 009489 45 990611 3250 316991 1051 680039 009276 44 990750 44 55 314897 997 685104 324358 1040 675017 009489 45 990681 3255 313698 1000 686302 323166 1044 676894 009409 44 990505 316991 1006 688716 326851 1007 67521 009455 44 990750 44 55 314897 997 685104 324358 1040 675017 009489 45 990641 44 990551 44 55 314897 997 685104 324358 1040 675017 009489 45 990645 52 58 | | | | | | 704714 | 303914 | 1087 | | | | 991372 | | - | 28 |
| 44 26 297164 1040 702836 303869 1083 694131 008705 43 991292 48 27 297788 1039 702212 306519 1081 693481 008730 43 991276 52 28 298412 1037 701588 307168 1080 692832 008736 43 991276 56 29 299034 1036 700966 307815 1078 692185 008782 43 991218 693481 0086807 43 991218 693481 0086807 43 991218 693481 0086807 43 991218 693481 0086807 43 991218 693481 0086807 43 991218 693481 0086807 693481 008807 43 991118 12 33 301514 1029 698486 310398 1073 689602 008885 43 991118 12 33 301514 1029 698486 310398 1073 689602 008885 43 991118 16 34 302132 1028 697868 311042 1071 688958 008910 43 991090 20 35 302748 1027 697525 311685 1070 688315 008936 43 991008 24 36 303364 1025 696636 312327 1068 687673 008962 43 991038 28 37 303979 1023 696621 312967 1067 687033 008985 43 991012 32 38 304593 1022 695407 313608 1065 686392 009014 43 990968 44 44 41 306430 1017 693570 315523 1061 684477 009092 44 990934 44 41 306430 1017 693570 315523 1061 684477 009092 44 990998 52 43 307041 1016 692959 316159 1056 683841 009118 44 990982 52 43 307650 1014 692350 316795 1058 683205 00914 43 990986 52 43 30741 1016 692559 316159 1056 683841 009118 44 990882 52 43 307650 1014 692350 316795 1058 683205 00914 43 990986 52 43 30741 1016 692526 318697 1054 681303 009223 44 990777 847 31080 1008 688920 319329 1053 680671 009250 44 990750 12 48 310685 1007 689315 319961 1055 680309 009274 44 990829 44 99077 847 31080 1008 688920 319329 1053 680671 009250 44 990750 12 48 310685 1007 689315 319961 1051 680039 009276 44 990750 12 48 310685 1007 689315 319961 1051 680039 009276 44 990750 12 48 310685 1007 689315 319961 1051 680039 009276 44 990750 12 48 310685 1007 689315 319961 1051 680039 009276 44 990750 12 48 310685 1007 689315 319961 1051 680039 009276 44 990531 32451 1047 673149 009356 44 990644 32 53 313097 1001 686903 322479 1045 673789 009356 44 990671 24 51 312495 1006 688711 320522 1050 679408 009303 44 990671 24 51 312495 1006 688711 326521 1007 673769 009452 45 990458 44 56 315495 996 684505 324981 1040 675017 009489 45 990511 48 060 317879 99 | | | | | | | | | 1,000 | 1.02 | | 991346 | | | 24 |
| ## 48 27 297788 1039 702212 306519 1081 693481 008730 43 991270 5228 298412 1037 701588 307168 1080 692832 008756 43 991244 56 29 299034 1036 700966 307815 1078 692185 008758 43 991244 56 29 299034 1036 700966 307815 1078 692185 008758 43 991244 56 309 299655 1034 10.700345 3.088463 1077 10.691537 10.008807 43 9.991195 43 300276 1032 699724 309109 1075 690891 008833 43 991167 690891 1283 301514 1029 698466 310398 1073 689602 008855 43 99114 1634 302132 1028 697868 311042 1071 688958 008910 43 991082 20 35 302748 1027 697252 311685 1070 688315 008936 43 991084 24 36 303364 1025 696636 312327 1068 687673 008962 43 991082 28 37 303979 1023 696021 312967 1067 687033 008968 43 991038 305207 1020 694793 314247 1064 685753 0099040 43 990960 40 40 305819 1019 694181 314885 1065 686392 009014 43 990986 44 41 306430 1017 693570 315523 1061 684477 009092 44 990988 44 42 307041 1016 699259 316159 1066 683841 009118 44 990882 43 307650 1014 692350 316795 1058 683205 009145 44 990882 45 46 309474 1010 690526 318697 1054 681303 009223 44 990777 847 310080 1008 689920 319329 1053 680671 009250 44 990777 44 45 310685 1007 689315 319961 1051 680039 009276 44 990774 44 45 311289 1006 688711 320592 1050 679408 009303 44 990671 2451 312495 1003 687505 321851 1047 678149 009305 44 990671 2451 312495 1003 687505 321851 1047 678549 009455 44 990671 2451 312495 1003 687505 321851 1047 678649 009455 44 990671 2451 312495 1003 687505 321851 1047 678649 009455 44 990671 2451 312495 1003 687505 321851 1047 678525 009961 45 99 | | | | | | | | | | the second second | August . | | | | 20 |
| Second Part 1037 701588 307168 1080 692832 008756 43 991244 60 30 929965 1034 10.700345 9.308463 1077 10.691537 10.008807 43 9.991185 431 300276 1032 699724 309109 1075 699891 008853 43 991145 1233 301514 1029 698466 310398 1073 689802 008855 43 991145 1634 302132 1028 697868 311042 1071 689862 008855 43 991145 1634 302132 1028 697868 311042 1071 689858 008910 43 991062 20 35 302748 1027 697252 311685 1070 688315 008936 43 991082 24 36 303364 1025 696636 312327 1068 687673 008962 43 991082 23 304593 1022 695407 313608 1065 686392 009014 43 990986 36 305207 1020 694793 314247 1064 685753 009040 43 990996 44 41 306430 1017 693570 315523 1061 684477 009092 44 909094 44 41 306430 1017 693570 315523 1061 684477 009092 44 990985 5644 308259 1013 691741 317430 1057 682570 009117 44 990882 47 045 9.308867 1011 10.691133 9.318064 1055 10.681936 10.009197 44 9.99865 103 691741 317430 1057 682570 009171 44 990824 1248 310685 1007 689315 319961 1051 680393 009223 44 990777 847 310280 1008 688920 319329 1053 680671 009250 44 990730 2451 312495 1003 687505 321851 1047 678149 009356 44 990742 1248 31685 1007 689315 319961 1051 680939 009276 44 990750 311893 1004 688107 321222 1048 67878 009303 44 990671 2451 312495 1003 687505 321851 1047 678149 009356 44 990644 8252 3133097 1001 686903 322479 1045 678525 0099409 44 990651 3655 314897 997 685104 324358 1041 675642 009435 44 990665 44 456 315495 996 684505 322851 1047 678149 009356 44 990665 44 456 315495 996 684505 322851 1047 678149 009456 44 990665 44 990665 44 900665 | в | | | | | | | | The second second | | | | | | 16 |
| Seco Second Sec | | | | | | | | | | | | | | | 12 |
| 46 0 30 9.299655 1034 10.700345 9.308463 1077 10.691537 10.008807 43 9.991195 431 300276 1032 699724 309109 1075 690891 008833 43 991167 832 300695 1031 699105 309754 1074 690246 008859 43 991145 12 33 301514 1029 698486 310398 1073 689602 008885 43 991145 16 34 302132 1028 697868 311042 1071 688958 008910 43 991195 20 35 302748 1027 697252 311685 1070 688315 008936 43 991064 24 36 303364 1025 696636 312327 1068 687673 008962 43 991032 28 37 303979 1023 696021 312967 1067 687033 008968 43 991012 32 38 304593 1022 695407 313608 1065 686392 009014 43 990986 44 41 306430 1017 693570 315523 1061 684477 009092 44 990984 44 13 306430 1017 693570 315523 1061 684477 009092 44 990986 52 43 307650 1014 692350 316795 1058 68320 009114 54 990882 52 313080 1008 689920 319329 1053 680671 009118 44 990882 52 43 307650 1014 692350 316795 1058 683205 009145 44 990882 52 43 307650 1014 692350 316795 1058 683205 009145 44 990882 52 43 307650 1014 692350 316795 1058 683205 009145 44 990882 52 43 307650 1014 692350 316795 1058 683205 009145 44 990882 52 43 307650 1014 692350 316795 1058 683205 009145 44 990882 52 43 307650 1014 692350 316795 1058 683205 009145 44 990882 52 43 307650 1014 692350 316795 1058 683205 009145 44 990882 52 3133991 103 68771 320592 1050 679408 009303 44 990671 2451 312495 1003 687505 321851 1047 678149 009356 44 990750 321899 1006 688711 320592 1050 679408 009303 44 990671 2451 312495 1003 687505 321851 1047 678149 009356 44 990644 2852 3138097 1001 686903 322479 1045 677521 009382 44 990671 2451 312495 1003 687505 321851 1047 678149 009356 44 990644 2852 318698 1000 686302 323166 1044 676694 009409 44 990697 44 56 314897 997 685104 324358 1040 67507 009489 45 990671 2451 312495 1003 687505 321851 1047 678149 009356 44 990658 45 52 31899 1096 684505 324893 1040 67507 009489 45 990671 2451 312495 1003 687505 321851 1047 678149 009356 44 990697 3253 318698 1000 686302 323166 1044 676994 009409 44 990697 3253 318598 1000 686903 322479 1045 677520 009356 44 990658 45 900458 45 900458 45 900458 45 900458 45 900 | 1 | | | | | | | | | | | | | | 4 |
| ## ## ## ## ## ## ## ## ## ## ## ## ## | 16 | | | | | | | | | | - | | _ | 14 | 0 |
| 8 32 300895 1031 699105 309754 1074 690246 008859 43 991141 12 33 301514 1029 698486 310398 1073 689602 008885 43 991114 16 34 302132 1028 697868 311042 1071 688958 008910 43 991090 20 35 302748 1027 697252 311685 1070 688315 008936 43 991064 24 36 303364 1025 696636 312327 1068 687673 008962 43 991038 28 37 303979 1023 696021 312967 1067 687033 008988 43 991013 32 38 304593 1022 695407 313608 1065 686392 009014 43 990986 40 40 305819 1019 694181 314885 1062 685115 009066 44 990934 44 41 306430 1017 693570 315523 1061 684477 009092 44 990998 44 41 306430 1017 693570 315523 1061 684477 009092 44 990986 52 43 307650 1014 692350 316795 1058 683205 009145 44 990882 52 43 307650 1014 692350 316795 1058 683205 009145 44 990882 52 43 307650 1014 692350 316795 1058 683205 009147 44 990829 44 46 309474 1010 690526 318697 1054 681303 009223 44 990775 87 310080 1008 689920 319329 1053 680671 009250 44 990724 16 49 311289 1006 688711 320592 1050 679408 009303 44 9907724 16 49 311289 1006 688711 320592 1050 679408 009303 44 990724 16 49 311289 1006 688711 320592 1050 679408 009303 44 990671 24 51 312495 1003 687505 321851 1047 678149 009326 44 990671 24 51 312495 1003 687505 321851 1047 678149 009326 44 990671 24 51 312495 1003 687505 321851 1047 678149 009326 44 990671 24 51 312495 1003 687505 321851 1047 678149 009326 44 990651 3253 313698 1000 686302 3231061 1044 676894 009409 44 990585 44 56 315495 996 684505 324388 1041 675642 009462 44 990585 5258 316689 993 683111 326231 1037 673769 009452 45 990458 5258 316689 993 683113 326231 1037 673769 009452 45 990458 5258 316689 993 683113 326231 1037 673769 009542 45 990458 5258 316689 993 683113 326231 1037 673769 009542 45 990458 5258 316689 993 683113 326231 1037 673769 009542 45 990458 5258 316689 993 683113 32623 | FU | | | | | | | | | | | | | 13 | 56 |
| 12 33 301514 1029 698486 310398 1073 689602 008885 43 991118 1634 302132 1023 697868 311042 1071 688958 008910 43 991064 391064 391064 36303748 1027 697252 311685 1070 688315 008962 43 991064 301064 301064 | | | | | | | | | | | | 991141 | | | 52 |
| 20 35 302748 1027 697252 311685 1070 688315 008936 43 991064 24 36 303364 1025 696636 312327 1068 687673 008962 43 991036 28 37 303979 1023 696021 312967 1067 687033 008968 43 991018 3238 304593 1022 695407 313608 1065 686392 009014 43 990966 36 39 305207 1020 694793 314247 1064 685753 009040 43 990966 40 40 305819 1019 694181 314885 1062 685115 009066 44 990934 44 41 306430 1017 693570 315523 1061 684477 009092 44 990998 48 42 307041 1016 692959 316159 1060 683841 009118 44 990882 52 43 307650 1014 692350 316795 1058 683205 009145 44 990882 52 43 307650 1014 692350 316795 1058 683205 009145 44 990882 564 308259 1013 691741 317430 1057 682570 009171 44 990829 44 63 309474 1010 690526 318697 1054 681303 009223 44 990778 847 310080 1008 689920 319329 1053 680671 009250 44 990724 16 49 311239 1006 688711 320592 1050 679408 009303 44 990724 16 49 311239 1006 688107 321222 1048 678778 009329 44 990677 24 51 312495 1003 687505 321851 1047 678149 009356 44 990671 24 51 312495 1003 687505 321851 1047 678149 009356 44 990671 24 51 312495 1003 687505 321851 1047 678149 009356 44 9906618 32 53 313698 1000 686302 323106 1044 676894 009409 44 990591 3654 314897 998 685703 323733 1043 676267 009452 44 9905618 32 53 313698 1000 686302 323106 1044 676894 009409 44 990558 44 990668 32 53 313698 1000 686302 323106 1044 676894 009409 44 990558 44 590584 44 56 315495 996 684505 324588 1040 675017 009489 45 990611 48 57 316092 994 683908 325607 1039 675307 009489 45 990511 48 57 316092 994 683908 325607 1039 675393 009515 45 990485 52 58 316689 993 683311 326231 1037 673769 009542 45 990581 48 060 317879 990 682121 327475 1035 672525 009596 45 990448 48 060 317879 990 682121 327475 1035 672525 009596 45 990458 52 58 316689 993 683311 326231 1037 673769 009542 45 990458 52 58 316689 993 683311 326231 1037 673769 009542 45 990458 52 58 316689 993 683311 326231 1037 673769 009542 45 990458 52 58 316689 993 683311 326231 1037 673769 009542 45 990458 52 58 316689 993 683311 326231 1037 673769 009542 45 990458 52 58 316689 993 683313 326 | | 12 | 33 | | | | | | 689602 | 008885 | 43 | 991115 | 27 | -4. | 48 |
| 24 36 303364 1025 696636 312327 1068 687673 008962 43 991038 28 37 3033979 1023 696021 312967 1067 687033 008968 43 991012 32 38 304593 1022 695407 313608 1065 686392 009014 43 990986 40 40 305819 1019 694181 314885 1062 685115 009066 44 990934 44 11 306430 1017 693570 315523 1061 684477 009092 44 990986 44 41 306430 1017 693570 315523 1061 684477 009092 44 990986 52 43 307650 1014 692350 316795 1058 683205 009145 44 990882 564 308259 1013 691741 317430 1057 682570 009171 44 990882 564 308259 1013 691741 317430 1057 682570 009171 44 990882 44 63 09474 1010 690526 318697 1054 681303 009223 44 990778 847 310080 1008 689920 319329 1053 680671 009250 44 990724 16 49 311289 1006 688711 320592 1050 679408 009303 44 990724 16 49 311289 1006 688711 320592 1050 679408 009303 44 990672 20 50 311893 1004 688107 321222 1048 678578 009329 44 990671 24 51 312495 1003 687505 321851 1047 678149 009356 44 990671 24 51 312495 1003 687505 321851 1047 678149 009356 44 990671 24 51 312495 1003 687505 321851 1047 678149 009356 44 990671 24 51 312495 1003 687505 321851 1047 678149 009356 44 990671 24 51 312495 1003 687505 321851 1047 678149 009356 44 990671 24 51 312495 1003 687505 321851 1047 678149 009356 44 990671 24 51 312495 1003 687505 321851 1047 678149 009356 44 990671 24 55 314897 997 685104 324388 1041 675642 009409 44 990511 32 53 313698 1000 686302 323106 1044 676894 009409 44 990511 48 57 316092 994 683908 325607 1039 674393 009515 45 990511 48 57 316092 994 683908 325607 1039 674393 009515 45 990485 52 58 316689 993 683311 326231 1037 673769 009542 45 990458 52 58 316689 993 683311 326231 1037 673769 009542 45 990458 52 58 316689 993 683311 326231 1037 673769 009542 45 990458 52 58 316689 993 683311 326231 1037 673769 009542 45 990458 52 58 316689 993 683311 326231 1037 673769 009542 45 990458 52 58 316689 993 683311 326231 1037 673769 009542 45 990458 52 58 316689 993 683311 326231 1037 673769 009542 45 990458 52 58 316689 993 683311 326231 1037 673769 009542 45 990458 52 58 316689 993 683311 326231 1037 673769 009542 | | | | | | | | | | | | 991090 | | | 44 |
| 28 37 303979 1023 696021 312967 1067 687033 008988 43 991012 32 38 304593 1022 695407 313608 1065 686392 009014 43 990966 | | | | | | | | | | | | 991064 | | | 40 |
| 32 38 304593 1022 695407 313608 1065 686392 009014 43 990986 3639 305207 1020 694793 314247 1064 685753 009040 43 9909986 44 40 40 305819 1019 694181 314885 1062 685115 009066 44 990993 44 41 306430 1017 693570 315523 1061 684477 009092 44 990998 68442 307041 1016 692959 316159 1060 683841 009118 44 990882 52 43 307650 1014 692350 316795 1058 683205 009145 44 990882 52 43 307650 1014 692350 316795 1058 683205 009145 44 990882 664 308259 1013 691741 317430 1057 682570 009171 44 990882 44 309474 1010 690526 318697 1054 681303 009223 44 990777 847 310080 1008 689920 319329 1053 680671 009250 44 990750 12 48 310685 1007 689315 319961 1051 680039 009276 44 990750 12 48 310885 1007 689315 319961 1051 680039 009276 44 990750 12 48 310885 1007 689315 319961 1051 680039 009276 44 990672 12 45 311893 1004 688107 321222 1048 678778 009329 44 990677 24 51 312495 1003 687505 321851 1047 678149 009356 44 990674 28 52 313097 1001 686903 322479 1045 677521 009382 44 990618 32 53 313698 1000 686302 323106 1044 676894 009409 44 990581 32 53 313698 1000 686302 323106 1044 676894 009409 44 990581 32 53 313698 1000 686302 323106 1044 676894 009409 44 990581 32 53 313698 1000 686302 323106 1044 676894 009409 44 990581 34897 997 685104 324358 1041 675642 009462 44 990588 44 56 315495 996 684505 324983 1040 675017 009489 45 990511 48 57 316092 994 683908 325607 1039 675393 009515 45 990485 52 58 316689 993 683311 326231 1037 673769 009542 45 990581 48 60 60 317879 990 682121 327475 1035 672525 009596 45 990485 52 58 316689 993 683311 326231 1037 673769 009542 45 990581 48 060 317879 990 682121 327475 1035 672525 009596 45 990443 48 060 317879 990 682121 327475 1035 672525 009596 45 990443 48 060 317879 990 682121 327475 1035 672525 009596 45 990443 48 060 317879 990 682121 327475 1035 672525 009596 45 990443 48 060 317879 990 682121 327475 1035 672525 009596 45 990443 48 060 317879 990 682121 327475 1035 672525 009596 45 990443 48 060 317879 990 682121 327475 1035 672525 009596 45 990443 48 060 317879 990 682121 327475 1035 672525 009 | | | | | | 41.73 | | | THE RESERVE AND ADDRESS OF THE PARTY OF THE | | | | | | 36 |
| 36 39 305207 1020 694793 314247 1064 685753 009040 43 990960 40 40 40 305819 1019 694181 314885 1062 685115 009066 44 990993 44 41 306430 1017 693570 315523 1061 6834477 009092 44 990908 52 43 307650 1014 692359 316159 1060 683841 009118 44 990882 52 43 307650 1014 692350 316795 1058 683205 009145 44 990853 56 44 308259 1013 691741 317430 1057 682570 009171 44 990829 44 63 309474 1010 690526 318697 1054 681303 009223 44 990777 847 310080 1008 689920 319329 1053 680671 009250 44 990750 12 48 310685 1007 689315 319961 1051 680039 009276 44 990724 16 49 311239 1006 688711 320592 1050 679408 009303 44 990671 24 51 312495 1003 687505 321851 1047 678149 009356 44 990671 24 51 312495 1003 687505 321851 1047 678149 009356 44 990661 32 53 313698 1000 686302 323106 1044 676894 009409 44 990581 325 313698 1000 686302 323106 1044 676894 009409 44 990581 44 56 315495 996 684505 324983 1040 675017 009485 44 990561 48 57 316092 994 683908 325607 1039 675017 009485 45 990551 48 57 316092 994 683908 325607 1039 675017 009485 45 990551 48 57 316092 994 683908 325607 1039 67507 009485 45 990551 48 57 316092 994 683908 325607 1039 67507 009485 45 990581 48 57 316092 994 683908 325607 1039 67507 009485 45 990581 48 57 316092 994 683908 325607 1039 675393 009515 45 990485 52 58 316689 993 683113 326231 1037 673769 009542 45 990581 48 50 317284 991 682716 326853 1036 673147 009569 45 990485 52 58 316689 993 683113 326231 1037 673769 009542 45 990485 52 58 316689 993 683311 326231 1037 673769 009542 45 990485 52 58 316689 993 683311 326231 1037 673769 009542 45 990485 52 58 316689 993 683211 326231 1037 673769 009542 45 990485 52 58 316689 993 683311 326231 1037 673769 009542 45 990485 52 58 316689 993 683311 326231 1037 673769 009542 45 990485 52 58 316689 993 683311 326231 1037 673769 009542 45 990485 52 58 316689 993 683311 326231 1037 673769 009542 45 990485 52 58 316689 993 683311 326231 1037 673769 009542 45 990485 52 58 316689 993 683311 326231 1037 673769 009542 45 990485 52 58 316689 993 683311 326231 1037 673769 009542 45 99 | | | | | | 1,1,101 | | | The second second second | E 10 C 10 | - 1 | | | | 32 28 |
| 40 40 305819 1019 694181 314885 1062 685115 009066 44 990934 4441 306430 1017 693570 315523 1061 684477 009092 44 990988 | | | | | | | | | | | | | | | 24 |
| 44 41 306430 1017 693570 315523 1061 684477 009092 44 990908 48 42 307041 1016 692959 316159 1060 683841 009118 44 990852 52 43 307650 1014 692350 316795 1058 683205 009145 44 990852 664 308259 1013 691741 317430 1057 682570 009171 44 990829 47 045 9.308867 1011 10.691133 9.318064 1055 10.681936 10.009197 44 9.990803 44 31080 1008 689920 319329 1053 680671 009250 44 990777 847 310080 1008 689920 319329 1053 680671 009250 44 990777 847 310080 1008 689920 319329 1053 680671 009250 44 990777 1248 310685 1007 689315 319961 1051 680039 009276 44 990754 1649 311289 1006 688711 320552 1050 679408 009303 44 990697 20 50 311893 1004 688107 321222 1048 678778 009329 44 990671 24 51 312495 1003 687505 321851 1047 678149 009356 44 990671 24 51 312495 1003 687505 321851 1047 678149 009356 44 990671 3253 313698 1000 686302 323106 1044 676894 009409 44 990651 32 53 313698 1000 686302 323106 1044 676894 009409 44 990591 36 54 314297 998 685703 323733 1043 676267 009435 44 990658 44 56 315495 996 684505 324983 1040 675017 009489 45 990515 48 57 316092 994 683908 325607 1039 674393 009515 45 990515 48 57 316092 994 683908 325607 1039 674393 009515 45 990515 48 50 317284 991 682716 326853 1036 673147 009569 45 990448 50 317284 991 682716 326853 1036 673147 009569 45 990458 52 58 316689 993 683311 326231 1037 673769 009542 45 990515 48 000 317879 990 682121 327475 1035 672525 009596 45 990404 18 0 60 317879 990 682121 327475 1035 672525 009596 45 990404 18 0 60 317879 990 682121 327475 1035 672525 009596 45 990404 18 0 60 317879 990 682121 327475 1035 672525 009596 45 990404 18 0 60 317879 990 682121 327475 1035 672525 009596 45 990404 18 0 60 317879 990 682121 327475 1035 672525 009596 45 990404 18 0 60 317879 990 682121 327475 1035 672525 009596 45 990404 18 0 60 317879 990 682121 327475 1035 672525 009596 45 990404 18 0 60 317879 990 682121 327475 1035 672525 009596 45 990404 18 0 60 317879 990 682121 327475 1035 672525 009596 45 990404 18 0 60 317879 990 682121 327475 1035 672525 009596 45 990404 18 0 60 317879 990 682121 3274 | | | | | | | | | | | | | | | 20 |
| 52 43 307650 1014 692350 316795 1058 683205 009145 44 990852 47 045 9.308867 1011 10.691133 9.318064 1055 10.681936 10.009197 44 9.990829 48 46 309474 1010 690526 318697 1054 681303 009223 44 990777 84 7 310080 1008 689920 319329 1053 680671 009250 44 990750 12 48 310685 1007 689315 319961 1051 680039 009276 44 990754 16 49 311289 1006 688711 320529 1050 679408 009303 44 990697 20 50 311893 1004 688107 321222 1048 678778 009329 44 990671 24 51 312495 1003 687505 321851 1047 678149 009356 44 990664 28 52 313097 1001 686903 322479 1045 677521 009382 44 990618 32 53 313698 1000 686302 323106 1044 676894 009409 44 990591 36 54 314297 998 685703 323733 1043 676267 009452 44 990558 40 55 314897 997 685104 324358 1041 675642 009462 44 990558 44 56 315495 996 684505 324983 1040 675017 009489 45 990511 48 57 316092 994 683908 325607 1039 675017 009489 45 990511 48 57 316092 994 683908 325607 1039 675017 009489 45 990511 48 57 316092 994 683908 325607 1039 675017 009489 45 990511 48 57 316092 994 683908 325607 1039 675017 009489 45 990511 48 57 316092 994 683908 325607 1039 675017 009489 45 990511 48 57 316092 994 683908 325607 1039 675017 009489 45 990511 48 57 316092 994 683908 325607 1039 675017 009489 45 990511 48 57 316092 994 683908 325607 1039 675017 009489 45 990511 48 57 316092 994 683908 325607 1039 675017 009489 45 990485 52 58 316689 993 683311 326231 1037 673769 009542 45 990485 56 59 317284 991 682716 326853 1036 673147 009569 45 990443 48 060 317879 990 682121 327475 1035 672525 009596 45 990443 48 060 317879 990 682121 327475 1035 672525 009596 45 990443 48 060 317879 990 682121 327475 1035 672525 009596 45 990443 48 060 317879 990 682121 327475 1035 672525 009596 45 990443 48 060 317879 990 682121 327475 1035 672525 009596 45 990443 48 060 317879 990 682121 327475 1035 672525 009596 45 990443 48 060 317879 990 682121 327475 1035 672525 009596 45 990443 48 060 317879 990 682121 327475 1035 672525 009596 45 990443 48 060 317879 990 682121 3274 | | 44 | 41 | | | | | | | | | 990908 | | CC. | 16 |
| 56 44 308259 1013 691741 317430 1057 682570 009171 44 990829 47 0 45 9.308867 1011 10.691133 9.318064 1055 10.681936 10.009197 44 9.990803 446 309474 1010 690526 318697 1054 681303 009223 44 990772 847 310080 1008 689920 319329 1053 680671 009250 44 990772 1248 310685 1007 689315 319961 1051 680039 009276 44 990724 1649 311289 1006 688711 320592 1050 679408 009303 44 990672 20 50 311893 1004 688107 321222 1048 678778 009329 44 990671 2451 312495 1003 687505 321851 1047 677521 009382 44 | | | | 307041 | 1016 | 692959 | 316159 | 1060 | 683841 | | | 990882 | 18 | | 12 |
| 47 0 45 9.308867 1011 10.691133 9.318064 10.55 10.681936 10.009197 44 9.990803 44 66 309474 1010 690526 318697 10.54 661303 009223 44 990777 847 310080 1008 689920 319329 10.53 680671 00.09250 44 990778 12.48 310685 1007 689315 319961 10.51 680039 00.9276 44 990784 16.49 311289 1006 688711 320592 10.50 679408 00.9303 44 990697 20.50 311893 10.04 688107 321222 10.48 678778 00.9329 44 990671 24.51 312495 10.03 687505 321851 10.47 678149 00.9356 44 990671 28.52 313.097 10.01 686903 322479 10.45 677521 00.9382 44 990618 32.53 313698 1000 686302 323106 10.44 676894 00.9409 44 990591 36.54 314297 9.98 685703 323733 10.43 676267 00.9435 44 990536 40.55 314897 9.97 685104 324388 10.41 675642 00.9462 44 990538 44 56 315495 9.96 684505 324983 10.40 675017 00.9489 45 990515 48.57 316092 9.94 683908 325607 10.39 674393 00.9515 45 990485 52.58 316689 9.93 683311 326231 10.37 673769 00.9542 45 990485 52.58 316689 9.93 683311 326231 10.37 673769 00.9542 45 990485 52.58 316689 9.93 683311 326231 10.37 673769 00.9542 45 990485 52.58 316689 9.93 683311 326231 10.37 673769 00.9542 45 990458 52.58 316689 9.93 68311 326231 10.37 673769 00.9542 45 990458 52.58 316689 9.93 683211 326231 10.37 673769 00.9542 45 990458 52.58 316689 9.93 683211 326231 10.37 673769 00.9542 45 990458 52.58 316689 9.93 683211 326231 10.37 673769 00.9542 45 990458 52.58 316689 9.93 683211 326231 10.37 673769 00.9542 45 990458 52.58 316689 9.93 683211 326231 10.37 673769 00.9542 45 990458 52.58 316689 9.93 683211 326231 10.37 673769 00.9542 45 990458 52.58 316689 9.93 683211 326231 10.37 673769 00.9542 45 990458 52.58 316689 9.93 683211 326231 10.37 673769 00.9542 45 990458 52.58 316889 9.93 683211 326231 10.37 673769 00.9542 45 990458 52.58 316889 9.93 683211 326231 10.37 673769 00.9542 45 990458 52.58 316889 9.93 683211 326231 10.37 673769 00.9542 45 990458 52.58 316889 9.93 683211 326231 10.37 673769 00.9542 45 990458 52.58 316889 9.93 683211 326231 10.37 673769 00.9542 45 990458 52.58 316889 9.93 683211 326231 10.37 673769 00.9542 45 990458 52.58 316889 | | | - | | | | | | | | | 990855 | | | 8 |
| 4 46 309474 1010 690526 318697 1054 681303 009223 44 990777 847 310080 1008 689920 319329 1053 680671 009250 44 990750 1248 310685 1007 689315 319961 1051 680039 009276 44 990724 1649 311239 1006 688711 320592 1050 679408 009303 44 990697 20 50 311893 1004 688107 321222 1048 678778 009329 44 990671 24 51 312495 1003 687505 321851 1047 678149 009356 44 990674 28 52 313097 1001 686903 322479 1045 677521 009382 44 990618 32 53 313698 1000 686302 323106 1044 676894 009409 44 990591 36 54 314297 998 685703 323733 1043 676267 009435 44 990538 44 56 315495 996 684505 324983 1040 675017 009489 45 990538 44 56 315495 996 684505 324983 1040 675017 009489 45 990531 48 57 316092 994 683908 325607 1039 674393 009515 45 990485 52 58 316689 993 683311 326231 1037 673769 009542 45 990485 52 58 316689 993 683311 326231 1037 673769 009542 45 990485 52 58 316689 993 68311 326231 1037 673769 009542 45 990485 65 93 17284 991 682716 326833 1036 673147 009569 45 990443 48 0 60 317879 990 682121 327475 1035 672525 009596 45 990404 18. s. / Cosine. Secant. Cotang. Tang. Cosec. Sine. P. P. to 2 30 310 2 30 323 2 30 13 | | _ | | | | | | | | | - | | - | | 4 |
| 8 47 310080 1008 689920 319329 1053 680671 009250 44 990750 1248 310685 1007 689315 319961 1051 680039 009276 44 990724 1649 311289 1006 688711 320592 1050 679408 009303 44 990672 20 50 311893 1004 688107 321222 1048 678778 009329 44 990671 24 51 312495 1003 687505 321851 1047 678149 009356 44 990644 28 52 313097 1001 686903 322479 1045 677521 009382 44 990651 32 53 313698 1000 686302 323106 1044 676894 009409 44 990591 36 54 314297 998 685703 323733 1043 676267 009435 44 990565 40 55 314897 997 685104 324358 1041 675642 009462 44 990558 44 56 315495 996 684505 324983 1040 675017 009489 45 990511 48 57 316092 994 683908 325607 1039 674393 009515 45 990485 52 58 316689 993 683311 326231 1037 673769 009542 45 990485 56 59 317284 991 682716 326853 1036 673147 009596 45 990481 48 060 317879 990 682121 327475 1035 672525 009596 45 990451 18 060 317879 990 682121 327475 1035 672525 009596 45 990450 100 100 100 100 100 100 100 100 100 1 | 67 | | | | | | | | | | | | | | 0 |
| 12 48 310685 1007 689315 319961 1051 680039 009276 44 990724 16 49 311289 1006 688711 320592 1050 679408 009303 44 990671 24 51 312495 1003 667505 321851 1047 678149 009356 44 990644 28 52 313097 1001 686903 322479 1045 677521 009382 44 990618 32 53 313698 1000 686302 323106 1044 676894 009409 44 990581 36 54 314297 998 685703 323733 1043 676267 009485 44 990586 40 55 314897 997 685104 324358 1040 675612 009462 44 990586 44 56 315495 996 684505 324983 1040 675017 009489 45 990511 48 57 316092 994 683908 325607 1039 674393 009515 45 990485 52 58 316689 993 683311 326231 1037 673769 009542 45 990485 56 59 317284 991 682716 326853 1036 673147 009569 45 990451 48 060 317879 990 682121 327475 1035 672525 009596 45 990451 48 060 317879 990 682121 327475 1035 672525 009596 45 990450 45 | | | | | | | | | | | 100 | | | | 56 |
| 16 49 311289 1006 688711 320592 1050 679408 009303 44 990697 20 50 311893 1004 688107 321222 1048 678778 009329 44 990671 24 51 312495 1003 687505 321851 1047 678149 009356 44 990684 28 52 313097 1001 686903 322479 1045 677521 009382 44 990618 32 53 313698 1000 686302 323106 1044 676894 009409 44 990591 36 54 314297 998 685703 323733 1043 676267 009435 44 990558 40 55 314897 997 685104 324358 1041 675642 009462 44 990558 44 56 315495 996 684505 324983 1040 675017 009489 45 990511 48 57 316092 994 683908 325607 1039 674393 009515 45 990485 52 58 316689 993 683311 326231 1037 673769 009542 45 990458 56 59 317284 991 682716 326853 1036 673147 009569 45 990438 48 0 60 317879 990 682121 327475 1035 672525 009596 45 990404 m. s. / Cosine. Secant. Cotang. Tang. Cosec. Sine. P. P. to 2 30 310 2 30 323 2 30 13 | | | | | | | | | | | | | | | 52 48 |
| 20 50 311893 1004 688107 321222 1048 678778 009329 44 990671 24 51 312495 1003 687505 321851 1047 678149 009356 44 990648 28 52 313097 1001 686903 322479 1045 677521 009382 44 990618 32 53 313698 1000 686302 323106 1044 676894 009409 44 990591 36 54 314297 998 685703 323733 1043 676267 009435 44 990558 40 55 314897 997 685104 324358 1041 675642 009462 44 990538 44 56 315495 996 684505 324983 1040 675017 009489 45 990518 48 57 316092 994 683908 325607 1039 674393 009515 45 990485 52 58 316689 993 683311 326231 1037 673769 009542 45 990485 52 58 31689 993 683311 326231 1037 673769 009542 45 990485 66 59 317284 991 682716 326853 1036 673147 009569 45 990431 48 0 60 317879 990 682121 327475 1035 672525 009596 45 990404 m. s. / Cosine. Secant. Cotang. Tang. Cosec. Sine. 5 Hours, or 78 Degrees. P. P. to 2 30 310 2 30 323 2 30 13 | | | | | | | | | A STATE OF THE PARTY OF | | | | | | 44 |
| 24 51 312495 1003 687505 321851 1047 678149 009356 44 990644 285 2 313097 1001 686903 322479 1045 677521 009382 44 990618 32 53 313698 1000 686302 323106 1044 676894 009409 44 990518 40 55 314897 997 685104 324358 1041 676267 009435 44 990565 40 55 314897 997 685104 324358 1041 675642 009462 44 990538 44 56 315495 996 684505 324983 1040 675017 009489 45 990511 48 57 316092 994 683908 325607 1039 674393 009515 45 990485 52 58 316689 993 683311 326231 1037 673769 009542 45 990485 56 59 317284 991 682716 326853 1036 673147 009569 45 990431 48 0 60 317879 990 682121 327475 1035 672525 009596 45 990404 m. s. ' Cosine. Secant. Cotang. Tang. Cosec. Sine. 5 Hours, or 78 Degrees. | | 20 | 50 | 311893 | 1004 | 688107 | 321222 | 1048 | | | | 990671 | | | 40 |
| 32 53 313698 1000 686302 323106 1044 676894 009409 44 990591 3654 314297 998 685703 323733 1043 676267 009435 44 990536 40 55 314897 997 685104 324358 1041 675642 009462 44 990538 44 56 315495 996 684505 324983 1040 675017 009489 45 990511 48 57 316092 994 683908 325607 1039 674393 009515 45 990485 52 58 316689 993 683311 326231 1037 673769 009542 45 990485 56 59 317284 991 682716 326853 1036 673147 009569 45 990434 48 0 60 317879 990 682121 327475 1035 672525 009596 45 990404 18 | | | | 312495 | 1003 | | | | 678149 | | | 990644 | 9 | | 36 |
| 36 54 314297 998 685703 323733 1043 676267 009435 44 990555 40 55 314897 997 685104 324358 1041 675642 009462 44 990558 44 56 315495 996 684505 324983 1040 675017 009489 45 990511 48 57 316092 994 683908 325607 1039 674393 009515 45 990485 52 58 316689 993 683311 326231 1037 673769 009542 45 990485 65 9 317284 991 682716 326853 1036 673147 009569 45 990431 48 0 60 317879 990 682121 327475 1035 672525 009596 45 990404 m. s. / Cosine. Secant. Cotang. Tang. Cosec. Sine. 5 Hours, or 78 Degrees. P. P. to 2 30 310 2 30 323 2 30 13 | | | | | | | | | | | | 990618 | 8 | | 32 |
| 40 55 314897 997 685104 324358 1041 675642 009462 44 990538 44 56 315495 996 684505 324983 1040 675017 009489 45 990511 48 57 316092 994 683908 325607 1039 674393 009514 45 990485 52 58 316889 993 683311 326231 1037 673769 009542 45 990458 56 59 317284 991 682716 326853 1036 673147 009569 45 990431 48 0 60 317879 990 682121 327475 1035 672525 009596 45 990404 m. s. ' Cosine. Secant. Cotang. Tang. Cosec. Sine. 5 Hours, or 78 Degrees. P. P. to 2 18 15" 155 18 15" 162 18 15" 6 30 78 07 13 15" 6 | | | | | | | | | | | | | 7 | | 28 |
| 44 56 315495 996 684505 324983 1040 675017 009489 45 990511 48 57 316092 994 683908 325607 1039 674393 009515 45 990485 52 58 316889 993 683311 326231 1037 673769 009542 45 990485 56 59 317284 991 682716 326853 1036 673147 009569 45 990431 48 0 60 317879 990 682121 327475 1035 672525 009596 45 990404 m. s. ' Cosine. Secant. Cotang. Tang. Cosec. Sine. 5 Hours, or 78 Degrees. P. P. to 2 15 15" 155 16 15" 162 17 15" 6 3 07" 2 30 310 2 30 323 2 30 13 | | | | | | | | | | | | | 6 5 | | 24 20 |
| 48 57 316092 994 683908 325607 1039 674393 009515 45 990485 5258 316689 993 683311 326231 1037 673769 009542 45 990451 45 990451 46 060 317879 990 682121 327475 1035 673147 009569 45 990451 48 0 60 317879 990 682121 327475 1035 672525 009596 45 990404 5 | | | | | | | | | | | | | 4 | | $\frac{20}{16}$ |
| 52 58 316689 993 683311 326231 1037 673769 009542 45 990458 56 59 317284 991 682716 326853 1036 673147 009569 45 990431 48 0 60 317879 990 682121 327475 1035 672525 009596 45 990404 m. s. ' Cosine. Secant. Cotang. Tang. Cosec. Sine. 5 Hours, or 78 Degrees. P. P. to 2 30 310 2 30 323 2 30 13 | | | | | | | | | | | | 990485 | 3 | | 12 |
| Secont S | | 52 | 58 | | | | | | | | | 990458 | 2 | | 8 |
| m. s. ' Cosine. Secant. Cotang. Tang. Cosec. Sine. 5 Hours, or 78 Degrees. P. P. to 1 | | | | 317284 | 991 | | | | | | | 990431 | 1 | | 40 |
| 5 Hours, or 78 Degrees. P. P. to 2 30 310 2 30 323 2 30 13 | 18 | 0 | 60 | 317879 | 990 | 682121 | 327475 | 1035 | 672525 | 009596 | 45 | 990404 | 0 | 12 | 0 |
| 5 Hours, or 78 Degrees. P. P. to 1s 15" 155 1s 15" 162 1s 15" 6 S or " 2 30 310 2 30 323 2 30 13 | n. | 8. | 1 | Cosine. | | Secant. | Cotang. | | Tang. | Cosec. | | Sine. | 7 | m. | 8. |
| P. P. to 2 30 310 2 30 323 2 30 13 | | | | | urs, | | - 01 | or | -0 | | Deg | | | | |
| s or " 2 30 310 2 30 323 2 30 13 | D | p , | +0 | | | 155 | 16 | | 162 | | | | D | D . | - |
| | | | | | 30 | 310 | 2 | 30 | 323 | 2 8 | 0 | 13 | r. | P. t | 0 |
| 3 45 466 3 45 485 3 45 19 | -64 | | | 3 | 45 | 466 | 3 | 45 | 485 | | 5 | 19 | 0 | VI. | |

| 3 |) . | | TABLE | | Log | garithmic | Sine | s, Tangent | | | | | | |
|------|-----|----------|--|------------|------------------|------------------|----------|------------------|------------------|-----|------------------|----|------|----------|
| - | 120 | | 0 Но | | 71 | (T) | or | | | | grees. | | | |
| m. | S. | _ | Sine. | D. | Cosec. | Tang. | D. | Cotang. | Secant. | D. | Cosine. | | m. | S. |
| 48 | 0 | | 9.317879 | 990 | 10.682121 | 9.327474 | | 10.672526 | | 45 | 9.990404 | | 12 | 0 |
| 100 | 4 | 1 2 | 318473 | 988 987 | 681527 | 328095 | | 671905 | 009622 | 45 | 990378 | | 10 | 56 |
| 17 | 12 | 3 | 319066 319658 | 986 | 680934 680342 | 328715 329334 | | 671285 670666 | 009649 009676 | | 990351 990324 | | 16 | 52 48 |
| | 16 | 4 | 320249 | 984 | 679751 | 329953 | | 670047 | 009703 | | 990297 | | 18 | 44 |
| 150 | 20 | 5 | 320840 | 983 | 679160 | | | 669430 | 009730 | | 990270 | | | 40 |
| 1 | 21 | 6 | 321430 | 982 | 678570 | | | 668813 | 009757 | 45 | 990243 | | | 36 |
| 100 | 28 | 7 | 322019 | 980 | 677981 | 331803 | | 668197 | 009785 | | 990215 | | | 32 |
| | 32 | 8 9 | 322607 323194 | 979 | 677393 676806 | | | 667582 666967 | 009812 009839 | | 990188 | | 10- | 28 |
| 1 | | 10 | 323780 | 976 | 676220 | | | 666354 | 009866 | | 990161 | _ | 8 | 24 |
| | 44 | 11 | 324366 | 975 | 675634 | | | 665741 | 009893 | | 990107 | | | 16 |
| 100 | | 12 | 324950 | 973 | 675050 | 334871 | 1019 | 665129 | 009921 | 46 | 990079 | | 20 | 12 |
| | | 13 | 325534 | 972 | 674466 | 335482 | | 664518 | 009948 | | 990052 | | | 8 |
| 10 | | 14 | 326117 | 970 | 673883 | 336093 | | 663907 | 009975 | | 990025 | - | | 4 |
| 49 | 4 | 16 | 9.326700 327281 | 969 968 | | | | | 10.010003 | | 9.989997 | | | - 0 |
| | 8 | 17 | 327862 | 966 | 672719 672138 | 337311 337919 | | 662689 662081 | 010030 010058 | | 989970 989942 | | | 56 |
| | | 18 | 328442 | 965 | 671558 | | | 661473 | 010035 | | 989915 | | 15 | 48 |
| 100 | 16 | 19 | 329021 | 964 | 670979 | 339133 | 1010 | 660867 | 010113 | | 989887 | | | 44 |
| | | 20 | 329599 | | 670401 | 339739 | | 660261 | 010140 | | 989860 | | ** | 40 |
| | 24 | | 330176 | | 669824 | | | 659656 | 010168 | | 989832 | | 35 | 36 |
| | 28 | 23 | 330753 331329 | | 669247 668671 | 340948 341552 | | 659052 658448 | 010196 010223 | | 989804 989777 | | | 32 |
| | | 24 | 331903 | | 668097 | 342155 | | 657845 | 010251 | | 989749 | | 1, | 24 |
| | | 25 | 332478 | 956 | 667522 | | | 657243 | 010279 | | 989721 | | 16 | 20 |
| 2 | | 26 | 333051 | 954 | 666949 | | | 656642 | 010307 | | 989693 | | | 16 |
| 100 | | 27 | 333624 | | 666376 | | | 656042 | 010335 | | 989665 | | | 12 |
| | | 28 29 | 334195 334766 | | 665805 665234 | | 998 | 655442 654843 | 010363 010391 | 47 | 989637 989609 | | -1 | 8 |
| 50 | | | 9.335337 | 949 | 10.664663 | | | 10.654245 | | | 9.989582 | | 10 | 0 |
| | | 31 | 335906 | | 664094 | | | 653647 | 010447 | 1 | 989553 | | | 56 |
| | | 32 | 336475 | | 663525 | | | 653051 | 010475 | | 989525 | | 4 | 52 |
| | | 33 | 337043 | | 662957 | | | 652455 | 010509 | 4.7 | 989497 | | | 4.8 |
| 200 | | 34 | 337610 | | 662390 | | 991 | 651859 | 010531 | | 989469 | | | 44 |
| | | 35 | 338176 338742 | | 661824 661258 | | | 651265 650671 | | | 989441 | | | 40 |
| | | 37 | 339307 | - | 660693 | | | 650078 | 010587 010615 | | 989413 989385 | | | 36 |
| | | 38 | | | 660129 | | | | | | 989356 | | | 28 |
| | | 39 | | | 659566 | | | | 010672 | 4.7 | 989328 | 51 | | 24 |
| | | 40 | | | 659004 | | | | | | 989300 | | | 20 |
| | 41 | | | | 658442 | | | 647713 647124 | | | 989271 | | | 16 |
| | | 43 | | | 657321 | | | | | | 989214 | | | 12 |
| 10. | 56 | 44 | | | 656761 | | | | 010814 | | 989186 | | 1 | 4 |
| 51 | (| 15 | | | 10.656203 | 9.354640 | 977 | 10.645360 | 10.010843 | 47 | 9.989157 | 15 | 9 | 1 |
| 0.5 | 4 | | A STATE OF THE PARTY OF THE PAR | | 655645 | | 976 | 644773 | 010872 | 48 | 989128 | 14 | | 56 |
| 100 | 8 | | | | 655088 | | | | | | | | | 52 |
| 100 | 16 | 148 | | | 654531 | | | | | | | | 13 | 48 |
| 100 | 20 | | | | 653421 | | | 200 | | | | | | 44 |
| 100 | 24 | | | | 652866 | | | | | | | | | 36 |
| | | 52 | 347687 | 921 | 652313 | 358731 | 969 | 641269 | | | | | | 32 |
| 100 | | 53 | | | 651760 | | | | | | | | | 25 |
| 1.00 | | 55 | | | 651208 | | | | | | | | , | 2.1 |
| 17 | | 56 | | | 650657 | | | | | | | | | 20 |
| 1 | 48 | 3 57 | 350443 | | 649557 | | | | | | | | | 13 |
| 2 | | 2 58 | | | 649008 | 362210 | | | | | | | | 8 |
| 20 | | 3 59 | | | 648460 | 362787 | 961 | 637213 | 011247 | 49 | 988753 | | | 4 |
| 52 | | 60 | | 911 | 647913 | 363364 | 960 | 636636 | 011276 | 49 | 988724 | 0 | 8 | (|
| m. | 8 | . ′ | 1 corrier | 1 | Secant. | Cotang. | - | Tang. | Cosec. | | Sine. | 1 | m. | S |
| - | | _ | 5 Hc | | | | or | | | | egrees. | | | - |
| | | to | 18 | 15" | | 1s | 15" | | 18 | 15" | | P | . P. | to |
| 1 | 01 | . " | 2 | 30 | 285 427 | 2 3 | 30 45 | 299 | 2 3 | 30 | 14 22 | | or | |
| - | - | - | | TO | *21 | 0 | 40 | 445 | 3 | 40 | 22 | _ | - | - |

| r | | ī | | | | 1 20 | and | Seca | nts. | SI. | TA | BLE V. | | 3 | 1 |
|----|-----|----------|----------|------------------|-------|------------------|------------------|------|------------------|------------------|----------|--------------------|----|-------|----------|
| | | | | 0. Но | | | | or | | | _ | grees. | | | |
| 15 | n. | S. | _ | Sine. | D. | Cosec. | Tang. | D. | Cotang. | Secant. | D. | Cosine. | | m. | 8. |
| l | 52 | 0 | 0 | 9.352088 | 911 | 10.647912 | | 960 | | 10.011276 | 49 49 | 9.988724 988695 | | 8 | 0 56 |
| ı | | 8 | 2 | 352635 353181 | | 647365 646819 | 363940 364515 | | 636060 635485 | 011305 011334 | 49 | 988666 | | | 52 |
| ı | | 12 | 3 | 353726 | | 646274 | 365090 | | 634910 | 011364 | 49 | 988636 | | | 48 |
| ı | | 16 | 4 | 354271 | 907 | 645729 | 365664 | | 634336 | 011393 | 49 | 988607 | | | 44 |
| ı | | 20 | 5 6 | 354815 | | 645185 | 366237 | 954 | 633763 | 011422 011452 | 49 | 988578 | | | 40 36 |
| ı | | 24 28 | 7 | 355358 355901 | | 644642 644099 | 366810 367382 | | 633190 632618 | 011432 | 49 49 | 988548 988519 | | | 32 |
| 1 | | 32 | S | 356443 | | 643557 | 367953 | | 632047 | 011511 | 49 | 988489 | | 11 | 28 |
| ı | | 36 | | 356984 | 901 | 643016 | 368524 | | 631476 | 011540 | 49 | 988460 | | | 24 |
| ı | | 40 | | 357524 | | 642476 | 369094 | 949 | 630906 | 011570 | | 988430 | | 904 | 20 |
| ı | | 44 | | 358064 358603 | | 641936 641397 | 369663 370232 | | 630337 629768 | 011599 011629 | 49 | 988401 988371 | | œ. | 16 |
| ı | | 52 | | 359141 | 896 | 640859 | 370799 | | 629201 | 011658 | 49 | 988342 | | 1000 | 8 |
| ł | | 56 | 14 | 359678 | | 640322 | 371367 | | 628633 | 011688 | 50 | 988312 | 16 | | 4 |
| 5 | 53 | 0 | 15 | 9.360215 | | 10.639785 | 9.371933 | 943 | 10.628067 | 10.011718 | 50 | 9.988282 | | 7 | C |
| 1 | | 4 | | 360752 | | 639249 | 372499 | | 627501 | 011748 | | 988252 | | | 56 |
| 1 | | | 17 | 361287 361822 | | 638713 638178 | | | 626936 626371 | 011777 011807 | 50 50 | 988223 988193 | | | 52 48 |
| 1 | 3 | | 19 | | | 637644 | | | 625807 | 011837 | 50 | 988163 | | | 44 |
| 1 | H | 20 | 20 | | | 637111 | 374756 | | 625244 | | 50 | 988133 | 40 | 6 | 40 |
| 1 | | 24 | | 363422 | | 636578 | | | 624681 | 011897 | 50 | 988103 | | Ni | 36 |
| ı | , | 32 | 22 | 363954 364485 | | 636046 | 375881 376442 | | 624119 623558 | 011927 011957 | 50 | 988073 988043 | | (b) | 32 |
| ı | | 36 | | 365016 | | 635515 634984 | | | 622997 | 011987 | | 988013 | | | 24 |
| I | | | 25 | | | 634454 | | | 622437 | 012017 | 50 | 987983 | | | 20 |
| I | и | | 26 | 366075 | 881 | 633925 | | | 621878 | | | 987953 | | 800 | 16 |
| ۱ | Å | | 27 | 366604 | | 633396 | | | 621319 | | | 987922 | | 15.12 | 12 |
| ı | | | 28 29 | | | 632869 632341 | 379239 379797 | | 620761 620203 | 012108 | | 987892 987862 | | 147 | 4 |
| ł | 54 | | _ | 9.368185 | - | 10.631815 | | | | 10.012168 | _ | 9.987832 | - | 6 | . (|
| ſ | 0.5 | | 31 | | | 631289 | | | 619090 | | | 987801 | | V | 56 |
| ı | | | 32 | | | 630764 | | 1 | 618534 | | | 987771 | | 0 | 58 |
| ı | н | | 33 | | | 630239 | | | 617980 | | | 987740 | | 1 | 48 |
| ı | Pt. | | 34 | | | 629715 629192 | | | 617425 | | | 987710 987679 | | W1 | 44 |
| ı | - | | 36 | | | 628670 | | | 616318 | | | 987649 | | 0.8 | 36 |
| ı | | 28 | 37 | 371852 | | 628148 | | | 615766 | | | 987618 | | 125 | 32 |
| ı | | | 38 | | | 627627 | | | 615214 | | | 987588 | | | 28 |
| 1 | | | 39 | | | 627106 | | | 614663 | | | 987557 | | be | 24 |
| ı | n | | 40 | | | 626586 626067 | | | 614112 | | | 987526 | | DX | 20 |
| ١ | | | 42 | | | 625548 | | | 613013 | | | 987465 | | 25 | 12 |
| ١ | 6 | 52 | 43 | 374970 | | 625030 | | | 612464 | 012566 | | 987434 | | | 8 |
| ı | | _ | 44 | | | 624513 | - | | 611916 | | | 987403 | | 13 | 4 |
| 1 | 55 | | | 9.376003 | | 10.623997 | | | | 10.012628 | | 9.987372 | | | - |
| 1 | 7 | | 46 | | | 623481 622965 | 389178 389724 | | 610822 | | | 987341 987310 | | | 5 |
| 1 | | | 48 | | | 622451 | | | 609730 | | | 987279 | | | 48 |
| 1 | 11 | 16 | 49 | 378063 | 856 | 621937 | 390815 | 907 | 609185 | 012752 | 52 | 987248 | 11 | | 4 |
| 1 | | | 50 | | | 621423 | | | 608640 | | | 987217 | | | 30 |
| 1 | | | 51 | | | 620911 620399 | | | 608097 | | | | | | 3 |
| 1 | | | 53 | | | 619887 | | | 607011 | | | | | | 28 |
| 1 | | 36 | 54 | 380624 | 850 | 619376 | 393531 | 902 | 606469 | 012908 | 52 | 987098 | 6 | | 2 |
| 1 | | | 55 | | | 618866 | | | 605927 | | | | | | 20 |
| 1 | | | 56 | | | 618357 | | | 604846 | | | | | | 10 |
| 1 | | | 58 | | | 617339 | | | 604306 | | | | | | 1 |
| 1 | 1 | 56 | 55 | 383168 | 845 | 616832 | 396233 | 897 | 603767 | 013064 | 52 | 986936 | 1 | . 3 | 1 |
| 1 | 56 | | 60 | | 844 | 616325 | 396771 | 896 | 603229 | 013096 | 52 | 986904 | 0 | 4 | 1 |
| 1 | m. | S. | - | Cosine. | | Secant. | Cotang. | | Tang. | Cosec. | 1 | Sine. | 1 | m. | 2 |
| 1 | - | | | 5 Hc | ours, | | | or | | 7 | 6 De | egrees. | | | |
| 1 | P | P. | to | 18 | 15" | | 18 | 15" | 1 | | 15" | 8 | P | P. | to |
| 1 | | or | | 2 3 | 30 | 263 | 2 3 | 30 | 278 | | 30 | 15 | | or | |
| ţ | | - | - | 1 3 | 45 | 394 | 3 | 45 | 417 | 13 | 45 | 23 | _ | - | - |

| 1 | 3 | 2 | _ | TABLI | v. | Lo | garıthmic | Sine | es, Tangen | ts, | _ | | | |
|-----|-----|----------|----------|--------------------|------------|---------------------|--------------------|------------|-----------------------------|---------------------|---------------------|--------------------|----|-------|
| ı | | | | 0 Hc | ur, | TI. | | or | | | | grees. | | |
| - 1 | ın. | S. | | Sine. | D. | Cosec. | Tang. | D. | Cotang. | Secant. | D. | Cosine. | = | m. s |
| ı | 56 | 0 | | | | 10.616325 615818 | | 896 896 | 602691 | 10.013096 013127 | 52 53 | 9.986904 986873 | | 4 (|
| ı | | 8 | | | 1 1 4 | 615313 | | | 602154 | 013159 | | 986841 | | 5% |
| ı | | 12 | | | | 614808 | | | 601617 | 013191 | | 986809 | | 4.8 |
| ı | | 16 20 | 5 | 385697 386201 | | 614303 613799 | 398919 399455 | | 601081 600545 | 013222 013254 | | 986778 986746 | | 44 |
| ı | | 24 | 6 | 386704 | 838 | 613296 | 399990 | 891 | 600010 | 013286 | 53 | 986714 | 54 | 36 |
| 1 | | 28 32 | 8 | 387207 387709 | 837 | 612793 612291 | 400524 401058 | | 599476 598942 | 013317 013349 | 53 53 | 986683 986651 | | 32 |
| ı | | 36 | 9 | 388210 | | 611790 | 401591 | 888 | 598409 | 013343 | 53 | 986619 | | 24 |
| ı | | 40 | 10 | 388711 | | 611289 | 402124 | | 597876 | 013413 | | 986587 | | 20 |
| ı | | 44 | 11 | 389211 389711 | | 610789 610289 | 402656 403187 | | 597344 596813 | 013445 013477 | 53 53 | 986555 986523 | | 16 |
| ı | | 52 | | 390210 | | 609790 | 403718 | | 596282 | 013509 | | 986491 | | 3 |
| 1 | | 56 | | 390708 | | 609292 | 404249 | | 595751 | 013541 | 53 | 986459 | _ | 4 |
| 3 | 7 | | _ | 9.391206 391703 | | 10.608794 608297 | 9.404778 405308 | 882 | 10.59522 2 594692 | 10.013573 013605 | | 9.986427 986395 | | 3 (|
| ı | | | 16 17 | 392199 | | 607801 | 405836 | | 594164 | 013637 | | 986363 | | 52 |
| ı | | 12 | 18 | 392695 | 825 | 607305 | 406364 | 879 | 593636 | 013669 | | 986331 | | 48 |
| ı | | 16 20 | | 393191 393685 | - 12 | 606809 606315 | 406892 407419 | 878 | 593108 592581 | 013701 013734 | 54 54 | 986299 986266 | | 44 |
| ı | | 24 | | 394179 | 0.00 | 605821 | 407945 | | 592055 | 013766 | 54 | 986234 | | 36 |
| ı | | 28 | | 394673 | | 605327 | 408471 | 875 | 591529 | 013798 | | 986202 | | 32 |
| ı | ė | 32 36 | | 395166 395658 | | 604834 604342 | 408997 | 874 | 591003 590479 | 013831 013863 | 54 54 | 986169 986137 | | 28 |
| ı | | 40 | | 396150 | | 603850 | 410045 | | 589955 | 013896 | | 986104 | 35 | 20 |
| ı | | 44 | | 396641 | | 603359 | 410569 | | 589431 | 013928 | 54 | 986072 986039 | 34 | 16 |
| ı | | 48 52 | | 397132 397621 | | 602868 602379 | 411092 411615 | | 588908 588385 | 013961 013993 | 54 54 | 986007 | | 12 |
| ı | | 56 | | 398111 | | 601889 | 412137 | 869 | 587863 | 014026 | 54 | 985974 | | 4 |
| I. | 8 | | | 9.398600 | | 10.601400 | | | 10.587342 | | | 9.985942 | | 2 (|
| I | | | 31 32 | 399088 399575 | | 600912 600425 | 413179 413699 | 867 | 586821 586301 | 014091 014124 | 55 55 | 985909 985876 | | 58 |
| ı | | 12 | | 400062 | | 599938 | 414219 | 865 | 585781 | 014157 | 55 | 985843 | 27 | 48 |
| ı | | 16 | | 400549 | | 599451 | 414738 | | 585262 | 014189 | 55 | 985811 | | 4.4 |
| I | | 20 24 | | 401035 401520 | | 598965 598480 | 415257 | | 584743 584225 | 014222 014255 | 55 55 | 985778 985745 | | 36 |
| ı | | 28 | 37 | 402005 | 807 | 597995 | 416293 | 862 | 583707 | 014288 | 55 | 985712 | 23 | 32 |
| 1 | ä | 32 | | 402489 402972 | | 597511 597028 | 416810 417326 | | 583190 582674 | 014321 014354 | 55 55 | 985679 985646 | | 25 |
| 1 | | 40 | | 403455 | | 596545 | 417842 | | 582158 | 014387 | 55 | 985613 | | 20 |
| ı | ã | 44 | 41 | 403938 | 803" | 596062 | 418358 | | 581642 | 014420 | _ | 985580 | | 16 |
| ۱ | ď | 48 52 | | 404420 404901 | | 595580 595099 | 418873 419387 | | 581127 580613 | 014453 014486 | 55 55 | 985547 985514 | | 18 |
| 1 | | 56 | | 405382 | 800 | 594618 | 419901 | | 580099 | 014520 | 55 | 985480 | | 4 |
| | 9 | | | 9.405862 | 799 | 10.594138 | | | | 10.014553 | 55 | 9.985447 | | 1 (|
| I | | _ | 46 | 406341 406820 | 798 797 | 593659 593180 | 420927 421440 | | 579073 578560 | 014586 014619 | 56 56 | 985414 985381 | | 58 |
| 1 | 1 | 12 | | 400820 | | 592701 | 421440 | | 578048 | 014653 | | 985347 | | 48 |
| ı | 3 | 16 | | 407777 | 795 | 592223 | 422463 | | 577537 | 014686 | | 985314 | | 44 |
| ı | ã | 20 24 | | 408254 | | 591746 591269 | 422974 | | 577026 576516 | | | 985280 985247 | | 36 |
| 1 | Ė | 28 | | 409207 | | 590793 | 423993 | 848 | 576007 | 014787 | 56 | 985213 | 8 | 32 |
| ı | | 32 | | | | 590318 | | | 575497 | 014820 014854 | | 985180 985146 | | 28 |
| 1 | 4 | 36 | 55 55 | | | 589843 589368 | | | 574989 574481 | 014834 | | 985113 | | 24 |
| 1 | | 44 | 56 | 411106 | 789 | 588894 | 426027 | 845 | 573973 | 014921 | 56 | 985079 | 4 | 16 |
| 1 | | | 57 58 | | | 588421 | | | 573466 | 014955 014989 | | 985045 985011 | 3 | 12 |
| 1 | | | 59 | | | 587948 587476 | | | 572959 572453 | 014989 | | 984978 | 1 | 4 |
| | 60 | | 60 | | | 587004 | | | 571948 | 015056 | | 984944 | 0 | 0 . (|
| I | m. | S. | 1 | Cosine. | | Secant. | Cotang. | | Tang. | Cosec. | | Sine. | 1 | m. s |
| 1 | | | | 5 Ho | | 1 100 | - | or | 1 100 | | | grees. | | |
| | P. | P. | to | 13 2 | 15" 30 | 122 | 1s 2 | 15" 30 | 130 | | 1 <i>5</i> ′′ 30 | 8 16 | P. | P. to |
| | 3 | or | " | 3 | 45 | 366 | 3 | 45 | 391 | | 45 | 25 | S | or " |

| 1 | | | | | | 16 | and | Seca | ints. | | | BLE'V. | _ | 13 | 3 |
|------|-----|----------------|--------|------------------|------------------------------------|--|------------------------------|-------------|--|--|---------|-------------------|-----|------|----------|
| ш | | _ | | · 1 Ho | - | | | or | | | | grees. | | | I |
| ш | m. | S. | 1 | Sine. | D. | Cosec. | Tang. | D. | Cotang. | Secant. | D. | Cosine. | Ľ | m. | 8. |
| п | 0 | 0 | | 9.412996 | 785 | A U. BOW | | | 10.571948 | | | 9.984944 | | 60 | 0 |
| н | ì | 4 | 1 | 413467 | | 586533 | | Blanch, San | 571443 | | | 984910 | | | 56 |
| в | | 8 | 2 3 | 413938 | MAG | 586062 | | | 570938 570434 | 015124 015158 | | 984876 984842 | | 1 | 52 48 |
| М | | 16 | 4 | 414408 414878 | 1 200 | 585122 | | | 569930 | | | 984808 | | | 44 |
| P | ш | 20 | 5 | 415347 | 781 | 584653 | 430573 | 838 | 569427 | 015226 | | 984774 | | 1 | 40 |
| 8 | | 24 | 6 | 415815 | | 584185 | | | 568925 | 015260 | | 984740 | | 2 | 36 |
| П | | 28 | 7 S | 416283 | 779 | 583717 | | | 568423 567921 | 015294 015328 | | 984706 984672 | | , | 32 |
| Н | | 36 | 9 | 416751 | 777 | 583249 582783 | | | 567420 | 015362 | 57 | 984638 | | 7 | 21 |
| Н | | | 0 | 417684 | 776 | 582316 | 433080 | 833 | 566920 | 015397 | 100 | 984603 | | | 20 |
| и | п | | 1 | 418150 | | 581850 | | | 566420 | | 57 | 984569 | | | 16 |
| ы | | 48 1 52 1 | | 418615 | 774 | 581385 | | | 565920 565421 | 015465 015500 | | 984535 984500 | | | 12 |
| н | | 56 1 | | 419079 419544 | 773 | 580921 580456 | | ASSESSED IN | 564922 | 015534 | | 984466 | | , | 4 |
| 7 | 1 | | | 9.420007 | 772 | 10.579993 | - | - | - | 10.015568 | 58 | 9.984432 | - | 59 | U |
| 1 | | 4.1 | 6 | 420470 | 10.00 | 579530 | | | 563927 | 015603 | | 984397 | | | 56 |
| 1 | | 81 | | 420933 | 770 | 579067 | 436570 | 828 | 563430 | 015637 | 58 | 984363 | 43 | | 52 |
| 1 | | 12 1 | | 421395 | | 578605 | | | 562933 | | | 984328 | | | 48 |
| | 01 | 16 1 20 2 | 9 | 421857 422318 | 768 767 | 578143 577682 | | | 562437 561941 | 015706 015741 | | 984294 984259 | | | 44 |
| ш | | 242 | П | 422778 | | 577222 | | | 561446 | 015776 | | 984224 | | | 36 |
| 4 | | 28,2 | 2 | 423238 | 766 | 576762 | | | 560952 | 015810 | | 984190 | | | 32 |
| П | | 32,2 | | 423697 | 765 | 576303 | | | 560457 | 015845 | | 984155 | | | 28 |
| | | 36 2 40 2 | | 424156 | 764 763 | 575844 | 440036 | | 559964 | 015880 015915 | | 984120 | | | 24 |
| -4 | | 44 2 | | 424615 425073 | 762 | 575385 574927 | 440529 441022 | | 559471 558978 | 015950 | 10.0 | 984085 984050 | | | 20 16 |
| H | | 48 2 | | 425530 | 761 | 574470 | | | 558486 | 015985 | 58 | 984015 | | | 12 |
| | | 52 2 | | 425987 | 760 | 574013 | | | 557994 | 016019 | | 983981 | | , | 8 |
| | | 56 2 | | 426443 | 760 | 573557 | 442497 | | 557503 | 016054 | 58 | 983946 | - | | 4 |
| П | 2 | 0,3 | 0 | 9.426899 | 759 | 10.573101 | | | 10.557012 | | 58 | 9.983911 | | 58 | 0 |
| Н | | 43 83 | | 427354 427809 | 758 757 | 572646 572191 | 443479 443968 | | 556521 556032 | 016125 016160 | | 983875 983840 | | | 56 |
| Ħ | | 123 | | 428263 | 756 | 571737 | 444458 | | 555542 | 016195 | | 983805 | | | 48 |
| п | | 163 | 4 | 428717 | 755 | 571283 | and the second second second | 3 - | 555053 | 016230 | | 983770 | | | 44 |
| П | | 203 | | 429170 | 754 | 570830 | 445435 | | 554565 | 016265 | | 983735 | | | 40 |
| н | | 243 283 | | 429623 | 753 752 | 570377 | 445923 | | 554077 | 016300 | | 983700 | | | 36 |
| 198 | | 323 | | 430075 | 752 | 569925 569473 | 446411 446898 | | 553589 553102 | 016336 016371 | 59 | 983664 983629 | | | 32 28 |
| ш | | 363 | | 430978 | 751 | 569022 | 447384 | | 552616 | 016406 | | 983594 | | | 24 |
| 9 | | 404 | | 431429 | 750 | 568571 | 447870 | 809 | 552130 | 016442 | 59 | 983558 | | | 20 |
| 4 | | 44 4 | | 431879 | 749 | 568121 | 448356 | 809 | 551644 | 016477 | 59 | 983523 | | | 16 |
| 1 | | 48 4 52 4 | | 432329 432778 | 749 | 567671 567222 | 448841 449326 | 808 807 | 551159 550674 | 016513 016548 | 59 | 983487 983452 | | | 12 |
| 1 | | 56.4 | | 433226 | 747 | 566774 | 449320 | 806 | 550190 | 016584 | 59 | 983416 | _ | | 4 |
| 1 | 3 | | | 9.433675 | 746 | 10.566325 | | - | 10.549706 | - | 59 | | 15 | 57 | 0 |
| 1 | | 4.4 | 6 | 434122 | 745 | 565878 | 450777 | 805 | 549223 | 016655 | 59 | 983345 | 14 | | 56 |
| 1 | | 84 | | 434569 | 744 | 565431 | 451260 | 804 | 548740 | 016691 | 59 | 1 1 1 1 1 1 1 1 1 | 13 | | 59 |
| 1 | | 124 | | 435016 | 744 | 564984 | 451743 | 803 | 548257 547775 | 016727 | 60 | 983273 | | | 48 |
| 1 | | 16,4 205 | | 435462 435908 | 742 | 564538 564092 | 452225 452706 | 802 | 547294 | 016762 016798 | 60 | 983238 983202 | | | 40 |
| 1 | | 245 | | 436353 | 741 | 563647 | 453187 | | 546813 | 016834 | | 983166 | | | 36 |
| 1 | - 5 | 28 5 | 2 | 436798 | 740 | 563202 | 453668 | 800 | 546332 | 016870 | 60 | 983130 | 8 | | 32 |
| 1 | | 32 5 | | 437242 | 740 | 562758 | 454148 | | 545852 | | 60 | 983094 | | | 28 |
| 1 | | 36 5. 40 5. | | 437686 | | 562314 561871 | 454628 455107 | _ | 545372 544893 | | 60 | 983058 983022 | 6 | | 24 20 |
| 1 | | 14 5 | | 438572 | | 561428 | 455586 | | 514414 | | 60 | 982986 | 4 | | 16 |
| 1 | - | 18 5 | 7 | 439014 | 736 | 560986 | | 796 | 543936 | | 60 | 982950 | 3 | | 12 |
| 1 | | 52 58 | | 439456 | | 560544 | 456542 | | 543458 | | 60 | 982914 | 2 | | 8 |
| 1 | 4. | 56 59 0 60 | | 439897 | | 560103 | 457019 | | 542931 542504 | | 60 | 982578 | 1 0 | 56 | 4 |
| 1= | _ | | | 440338 | 734 | 559662 | | 794 | ······································ | | - | 982849 | | - | - |
| n | 1 | S. ' | 1 | Cosine. | 18 | Secant. | Cotang. | | Tang. | Cosec. | D | Sine. | 1 | n. | 8: |
| - | - | - | | 4 Hou | Marian San Personal Property Lines | 1 114 | 12 1 | or 15" | 1 100 1 | the second secon | | rees. | - | | - |
| 1 | | e te | 1 | 1s 2 | 30 | 114 | 1s 2 | 30 | 123 | | 5" 0 | 9 | | P. t | |
| - | SC | or " | - | 3 | 4.5 | 341 | 3 | 45 | 368 | 3 4 | | 26 | S | or " | MC. 1801 |
| . 12 | - | Champi | - | - | - | A STATE OF THE PARTY OF THE PAR | - | - | - | THE REAL PROPERTY. | - | - | - | No. | - |

C

| 1 | 34 | ļ | | TABLE | v. | Log | garithmic | Sine | s, Tangen | | | | | | 1 |
|----|----|-------|-----------------|--------------------|------------|---------------------|--------------------|-------|------------------|---------------------|-----|--------------------|----|-------|----------|
| 1 | | | | 1 Ho | | 0 | . m | or | 1 0 | | _ | grees. | | | |
| ۱ | m. | S. | _ | Sine. | D. | Cosec. | Tang. | D. | Cotang. | Secant. | D. | Cosine. | | m. | S. |
| | 4 | 0 | | 9.440338 440778 | 734 733 | 10.559662 559222 | 9.457496 457973 | | 542027 | 10.017158 017195 | | 9.982842 982805 | | 56 | 0 56 |
| В | | 4 8 | 1 2 | 441218 | | 558782 | 458449 | 1000 | 541551 | 017231 | 1 | 982769 | | | 52 |
| М | | 12 | 3 | 441658 | 731 | 558342 | 458925 | | 541075 | 017267 | | 982733 | | | 48 |
| N | | 16 | 4 | 442096 | | 557904 | 459400 | | 540600 | | | 982696 | | | 44 |
| П | | 20 | 5 | 442535 442973 | | 557465 557027 | 459875 460349 | | 540125 539651 | 017340 017376 | | 982660 982624 | | | 36 |
| П | | 24 28 | 7 | 443410 | | 556590 | 460823 | | 539177 | 017413 | | 982587 | | | 32 |
| 9 | - | 32 | 8 | 443847 | | 556153 | 461297 | 788 | 538703 | 017449 | | 982551 | | | 28 |
| Ŋ, | | 36 | 9 | 444284 | | 555716 | 461770 | | 538230 | | | 982514 | | 8 | 24 |
| 7 | | 40 | $\frac{10}{11}$ | 444720 445155 | | 555280 554845 | 462242 | | 537758 537286 | | | 982477 982441 | | | 20 16 |
| П | | 48 | | 445590 | | 554410 | 463186 | | 536814 | | | 982404 | | | 12 |
| 14 | | 52 | | 446025 | | 553975 | 463658 | | 536342 | 017633 | | 982367 | | = 1 | 8 |
| Н | | 56 | | 446459 | | 553541 | 464128 | | 535872 | 017669 | - | 982331 | | | 4 |
| | 5 | | | 9.446893 | | 10.553107 | | | | 10.017706 | | 9.982294 | | | 0 |
| ш | | | 16 17 | 447326 447759 | | 552674 552241 | 465069 465539 | | 534931 534461 | 017743 | | 982257 982220 | | | 56 52 |
| П | | 12 | | 448191 | | 551809 | 466008 | | 533992 | | | 982183 | | | 48 |
| И | | 16 | | 448623 | | 551377 | 466476 | 780 | 533524 | 017854 | 62 | 982146 | 41 | | 44 |
| П | | 20 | - | 449054 | | 550946 | 466945 | | 533055 | | | 982109 | | | 40 |
| П | | 24 28 | | 449485 449915 | | 550515 550085 | 467413 | | 532587 532120 | | | 982072 982035 | | | 36 32 |
| | | 32 | | 450345 | | 549655 | | | 531653 | | | 981998 | | | 28 |
| ı, | | | 24 | | | 549225 | 468814 | 777 | 531186 | | | 981961 | 36 | | 24 |
| n | | | 25 | | | 548796 | | | 530720 | | | 981924 | | | 20 |
| Н | | | 26 | | | 548368 547940 | | | 530254 529789 | | | 981886 981849 | | | 16 12 |
| 9 | | 48 | 27 | | | 547512 | | 1 | 529324 | | | 981812 | | | 8 |
| ۱ | | | 29 | | | 547085 | | | 528859 | | | 981774 | | | 4 |
| | 6 | 0 | 30 | 9.453342 | 710 | 10.546658 | | | | 10.018263 | 1 | 9.981737 | | | 0 |
| | | | | 453768 | 1 | 546232 | | | 527932 | | | 981700 | | | 56 |
| П | | | 32 33 | | | 545806 545381 | | | 527468 527005 | | | 981662 981625 | | | 52 48 |
| u | | | 34 | | 1 | 544956 | | | 526543 | | | 981587 | 26 | | 44 |
| М | | 20 | 35 | 455469 | | - 544531 | 473919 | | 526081 | | | 981549 | 25 | | 40 |
| В | | | 36 | | | 544107 | | | 525619 | | | 981512 | | | 36 |
| ı | | | 37 38 | | | 543684 543261 | | | 525158 524697 | | | 981474 981436 | 22 | 10 | 32 |
| | | | 39 | | | 542838 | | | 524237 | | | 981399 | 21 | | 24 |
| | - | | 40 | | | 542416 | 476223 | | 523777 | 018639 | 63 | 981361 | 20 | | 20 |
| | | 44 | 41 | | | 541994 | | | 523317 | | | 981323 | | | 16 |
| | | | 42 | | | 541573 541152 | | | 522858 522399 | | | 981283 981247 | | | 12 |
| | | | 44 | | | 540732 | | | 521941 | | | 981209 | | 1 | 4 |
| | 7 | | 45 | | | 10.540312 | | 763 | | 10.018829 | 63 | 9.981171 | 13 | 53 | 0 |
| | | 4 | 46 | 460108 | 698 | 539892 | 47897 | 762 | 521025 | | | | | | 56 |
| | | 8 | | | | 539473 | | | 520568 520111 | | | | | | 52 48 |
| | | 12 | | | | 539054 538636 | | | 519655 | | | | | | 4.1 |
| Ш | | | 50 | | | 538218 | | | 519199 | | | | | | 40 |
| | | 24 | 51 | 462199 | 695 | 537801 | 48125 | | 518743 | | | | | | 36 |
| | | | 52 | | | 537384 | | | 518288 | | | | | | 32 |
| | | | 53 54 | | | 536968 | | | 517833 | | | | | | 28 |
| | | | 55 | | | 536136 | | | 516925 | | | | | | 20 |
| | | 44 | 56 | 464279 | | 535721 | 48352 | 9 755 | 516471 | 019250 | | | | | 16 |
| | | | 57 | | | 535306 | | | | | | | | | 12 |
| | | | 58 | | | 534892 | | | | | | | | | 4 |
| | 8 | (| 60 | 465938 | | | | | | | | | | 52 | |
| | m. | e | , | Cosine. | | Secant. | Cotang. | === | Tang. | Cosec. | | Sine. | - | m. | |
| | - | 0 | -1 | | ours. | 1 Secant. | 1 County. | or | 1 rang. | | 3 D | egrees. | - | (-545 | |
| | - | - | | 1 18 1 | 15" | 106 | 1 12 | 15" | 116 | 1 18 | 15" | 9 | L | . P. | to |
| | | P. | | 2 | 30 | 213 | 2 | 30 | 231 | 2 . | 30 | 19 | | or | |
| | 1_ | - | | 3 | 45 | 319 | 3 | 45 | 347 | 3 | 45 | 28 | | _ | |

| - | _ | - | | _ | 74 | and | Seca | nts. | | TA | BLE V. | - | 3 | 5 |
|------|----------|-----|------------------|------------|---------------------|------------------|------------|------------------|---------------------|-----------|------------------|--------------|----------|-----|
| - | | - | 1 Ho | IIIT. | | | or | | 13 | - | grees. | | | _ |
| m. | S. | 17 | Sine. | D. | Cosec. | Tang. | D. | Cotang. | Secant. | D. | Cosine. | 1 | m. | 5 |
| 8 | | = | 9.465935 | | 10.534065 | | - | 10.514661 | | 64 | 9.980596 | = | | - |
| O | 0 | | | | 533652 | | 752 | 514209 | 10.019404 019442 | | 980558 | | | 5 |
| | 8 | | 466761 | 687 | 533239 | | 751 | 513758 | 019481 | 65 | 980519 | | | 5 |
| 80 | 12 | | 467173 | | 532827 | 486693 | | 513307 | 019520 | | 980480 | | | 4 |
| × | 16 | | 467585 | 685 | 532415 | 487143 | | 512857 | 019558 | | 980442 | 56 | | 4.4 |
| | 20 | | 467996 | 685 | 532004 | 487593 | | 512407 | 019597 | 65 | 980403 | | 胚 | 4 |
| | 24 | 6 | 468407 | 684 | 531593 | 488043 | | 511957 | 019636 | | 980364 | | | 3 |
| 8 | 28 | 7 | 468817 | 683 | 531183 | 488492 | | 511508 | 019675 | | 980325 | | | 3 |
| 100 | 32 | 8 | 469227 | 683 | 530773 | 488941 | 747 | 511059 | 019714 | | 980286 | | | 28 |
| 100 | 36 40 | | 469637 470046 | 682 681 | 530363 | 489390 | | 510610 510162 | 019753 019792 | | 980247 980208 | | | 2 |
| | 44 | 11 | 470455 | 680 | 529954 529545 | 489838 490286 | | 509714 | 019792 | 65 | 980169 | | | 2 |
| 86 | 48 | 19 | 470863 | 680 | 529137 | 490733 | | 509267 | 019870 | 1 | 980130 | | | 1 |
| | 52 | | 471271 | 679 | 528729 | 491180 | | 508820 | 019909 | Park. | 980091 | | | - |
| 1 | 56 | | 471679 | 678 | 528321 | 491627 | 744 | 508373 | 019948 | 65 | 980052 | | 1 | - |
| 9 | 0 | 15 | 9.472086 | 678 | 10.527914 | 9.492073 | 743 | 10.507927 | 10.019988 | 65 | 9.980012 | 45 | 51 | 1 |
| 1 | 4 | | 472492 | 677 | 527508 | 492519 | | 507481 | 020027 | 65 | 979973 | | | 5 |
| - | | 17 | 472898 | | 527102 | 492965 | | 507035 | 020066 | 66 | 979934 | | 18. | 5 |
| 1 | 12 | | 473304 | | 526696 | 493410 | | 506590 | 020105 | | 979895 | | | 4 |
| - | | 19 | 473710 | | 526290 | 493854 | | 506146 | 020145 | | 979855 | | | 4. |
| | 20 24 | | 474115 | | 525885 | 494299 | | 505701 | 020184 | | 979816 | | | 4 |
| | 28 | | 474519 474923 | | 525481 | 494743 | | 505257 504814 | 020224 020263 | | 979776 979737 | | | 3 |
| | 32 | | 475327 | 672 | 525077 524673 | 495186 495630 | | 504370 | 020303 | | 979697 | | | 2 |
| 6.4 | 36 | | 475730 | | 524270 | 496073 | | 503927 | 020342 | 1 | 979658 | | | 2 |
| - | 40 | | 476133 | | 523867 | 496515 | | 503485 | 020382 | | 979618 | | JUP | 2 |
| | | 26 | 476536 | | 523464 | 496957 | | 503043 | 020421 | 66 | 979579 | | 1 | 1 |
| | 48 | | 476938 | | 523062 | 497399 | | 502601 | 020461 | 66 | 979539 | 33 | | 1 |
| | 52 | | 477340 | 669 | 522660 | 497841 | 735 | 502159 | 020501 | 66 | 979499 | | f . | 1 |
| | 56 | - | 477741 | 668 | 522259 | 498282 | - | 501718 | 020541 | 66 | 979459 | _ | | 4 |
| 10 | | | 9.478142 | 667 | 10.521858 | | - | | 10.020580 | 66 | 9.979420 | | | (|
| | | | 478512 | | 521458 | 499163 | | 500837 | 020620 | | 979380 | | | 5 |
| | | 32 | 478942 | | 521058 | 499603 | Ma - | 500397 | 020660 | | 979340 | | | 5 |
| | 12 16 | | 479342 479741 | 665 | 520658 | 500042 | 732 731 | 499958 | 020700 | | 979300 979260 | | | 4.8 |
| 10.3 | 20 | | 480140 | 664 | 520259 519860 | 500481 | | 499080 | 020740 | | 979230 | | | 4.4 |
| 4 | 24 | | 480539 | 141.5 | 519461 | 501359 | | 498641 | 020820 | | 979180 | | | 3 |
| 14 | 28 | | 480937 | 663 | 519063 | 501797 | | 498203 | 020860 | 10.00 | 979140 | | | 3 |
| | 32 | | 481334 | 662 | 518666 | 502235 | | 497765 | 020900 | | 979100 | | | 2 |
| 12 | 36 | 39 | 481731 | 661 | 518269 | 502672 | 728 | 497328 | 020941 | 67 | 979059 | 21 | | 2 |
| | 40 | _ | 482128 | | 517872 | 503109 | 100 m | 496891 | 020981 | 67 | 979019 | | | 2 |
| | 44 | | 482525 | 660 | 517475 | 503546 | | 496454 | 021021 | 67 | 978979 | | | 1 |
| | 48 | | 482921 | 659 | 517079 | 503982 | | 496018 | 021061 | 67 | 978939 | | | 1 |
| | 56 | | 483316 483712 | 659 658 | 516684 516288 | 504418 504854 | 726 725 | 495582 495146 | 021102 | 67 | 978898 978858 | | 竑 | 1 |
| 11 | - | | 9.484107 | 657 | | | | 10.494711 | | | | - | 40 | _ |
| 11 | | 4.6 | 484501 | 657 | 10.515893 515499 | 505724 | | 494276 | 10.021183 | 67 | 9.978817 | | | 5 |
| - | | 47 | 484895 | | 515105 | 506159 | | 493841 | 021263 | | 978737 | | | 5 |
| 1 | 12 | | 485289 | | 514711 | 506593 | | 493407 | 021304 | | 978696 | | | 4 |
| 1 | 16 | 49 | 485682 | 655 | 514318 | 507027 | 722 | 492973 | 021345 | 68 | 978655 | | | 4 |
| | 20 | 50 | 486075 | | 513925 | 507460 | | 492540 | 021385 | | 978615 | | | 4(|
| - | 24 | | | | 513533 | | | 492107 | | | 978574 | | | 3 |
| - | | 52 | | | 513140 | | | 491674 | 021467 | | 978533 | | | 35 |
| 1 | 32 | | | | 512749 | | | 491241 | 021507 | | 978493 | | | 28 |
| | 36 | | | | 512357 511966 | | | 490809 490378 | 021548 021589 | | 978452 | | | 2. |
| | 40 | | | | 511576 | | | 489946 | 021589 | | 978411 978370 | | | 20 |
| - 1 | 48 | | | | 511186 | | | 489515 | 021630 | | 978329 | | | 1: |
| 1 | 52 | | | | 510796 | | | 489084 | 021712 | _ | 978288 | | 200 | 4 |
| | | 59 | | | 510407 | 511346 | | 488654 | 021753 | | 978247 | 1 | | 4 |
| 12 | | 60 | | | 510018 | 511776 | | 488224 | 021794 | | 978206 | | 18 | K |
| m. | 9 | - | Cosine. | | Secant. | Cotang. | - | Tang. | Cosec. | - | Sine. | 7 | | |
| | 3. | | 4 Ho | | octant. | Cotang. | or | Lang. | | Do | grees. | 11 | 410 | 8 |
| - | - | - | 1 18 | 15" | 100 | 18 | 15" | 1 110 | | 15" | 10 | | - | - |
| | P. | | 2 | 30 | 200 | 2 | 30 | 220 | | 30 | 20 | | P. t | |
| S | or | " | 3 | 45 | 300 | 3 | 45 | 331 | | 15 | 30 | 3 | or " | |
| - | - | - | | - | | | - | - | - | Carlo ACO | | ATTE VALUE | NO STATE | * |

| ſ | 30 | 5 | - | TABLE | v. | Los | garithmic | Sine | s, Tangen | ts, | | | - | - | - |
|----|----|----------------|-----------------|--------------------|------------|---------------------|------------------|------------|---------------------|------------------|-------|------------------|----|-------|----------|
| ł | _ | | - | 1 Ho | | | | or | , , | | S Do | grees. | | | |
| 1 | n. | 8. | 1 | Sine. | D. | Cosec. | Tang. | D. | Cotang. | Secant. | D. | Cosine. | 1' | m. | S. |
| ı | 2 | 0 | 0 | | 648 | 10.510018 | | ł | 10.488224 | 10.02179 | | 9.978206 | | | 0 |
| ı | | 8 | 2 | | 648 | 509629 509241 | 512206 512635 | | 487794 487365 | 02183 02187 | | 978165 978124 | | | 56 |
| ı | B | 12 | | 490739 | 646 | 508853 | | | 486936 | 02191 | | 978083 | | 9 | 52 48 |
| ı | | 16 | 4 | 491535 | | 508165 | 513493 | | 486507 | 02195 | | 978042 | 56 | | 44 |
| ı | | 20 24 | 5 6 | | | 508078 | | 713 | 486079 485651 | 02199 02204 | | 978001 | | , | 40 |
| ı | | 28 | 7 | 492695 | 644 | 507692 507305 | | | 485223 | 02208 | | 977959 977918 | | | 38 |
| I | | 32 | 8 | 493081 | 643 | 506919 | 515204 | 712 | 484796 | 02212 | 3 69 | 977877 | 52 | | 28 |
| 1 | | 36 | 9 | 493466 | 642 | 506534 | | | 484369 483943 | 02216 | | 977835 | | 8 | 24 |
| ı | | 40 44 | 10 11 | 493851 494236 | 642 | 506149 505764 | | | 483516 | 02220 02224 | | 977794 977752 | | | 20 |
| Ш | | 48 | | 494621 | 641 | 505379 | | | 483090 | 02228 | 9 69 | 977711 | 48 | 4 | 12 |
| ı | | 52 | | 495005 | | 504995 | | | 482665 | 02233 | | 977669 | | | 8 |
| - | | $\frac{56}{0}$ | $\overline{}$ | 495388 | 639 | 504612 | 517761 | 708 | 482239 10.481815 | 02237 | - | 977628 | | AN | 4 |
| 1 | 3 | 4 | 16 | 9.495772 496154 | 639 638 | 10.504228 503846 | | 708 | 481390 | 02245 | | 9.977586 | | +1 | 56 |
| 15 | | | 17 | 496537 | 637 | 503463 | | | 480966 | 02249 | | 977503 | | 1 | 52 |
| п | | | 18 | 496919 | 637 | 503081 | 519458 | | 480542 | 02253 | | 977461 | | 11 | 48 |
| 1 | | 16 20 | 19 | 497301 497682 | 636 636 | 502699 502318 | | | 480118 479695 | 02258 | | 977419 977377 | | 1 | 44 |
| И | | 24 | | 498064 | 635 | 501936 | | | 479272 | 02266 | | 977335 | | 03 | 36 |
| l | | 28 | 55 | 498444 | 634 | 501556 | 521151 | 704 | 478849 | 02270 | | 977293 | | | 32 |
| П | | 32 36 | | 498825 | 634 | 501175 | | | 478427 478005 | 022749 | | 977251 | | | 28 |
| И | | 40 | | 499204 499584 | | 500796 500416 | 2 2 2 2 2 2 | | 477583 | 02283 | | 977167 | | | 20 |
| ĕ | | 44 | | 499963 | 632 | 500037 | 522838 | | 477162 | 02287 | 70 | 977125 | | | 16 |
| п | | 48 | | 500342 | 631 | 499658 | | | 476741 | 02291 | | 977083 | | | 12 |
| U | | 52 56 | | 500721 501099 | 631 630 | 499279 498901 | 523680 524100 | | 476320 475900 | 02295 | | 977041 | | | 8 |
| ī | 4 | | | 9.501476 | 629 | 10.498524 | | 699 | 10.475480 | | - | 9.976957 | | 46 | 0 |
| ľ | | | 31 | 501854 | 629 | 498146 | | | 475061 | 02308 | | 976914 | | - | 56 |
| Г | | | 32 | 502231 | 628 | 497769 | 525359 | | 474641 | 02312 | | 976872 | | Ñ. | 52 |
| ı | | 12 16 | $\frac{33}{34}$ | 502607 502984 | 628 627 | 497393 497016 | | | 474222 473803 | 02317 | | 976830 976787 | | 91 | 48 |
| L | | 20 | | 503360 | 626 | 496640 | 526615 | | 473385 | 02325 | | 976745 | | | 40 |
| L | | 24 | | 503735 | 626 | 496265 | 527033 | | 472967 | 02329 | | 976702 | | | 36 |
| I | | 28 32 | | 504110 | 625 | 495890 | 527451 527868 | 696 695 | 472549 472132 | 023340 | | 976660 976617 | | | 32 |
| П | | 36 | | 504485 504860 | 624 | 495515 495140 | 528285 | | 471715 | 02342 | | 976574 | | | 24 |
| П | | 40 | 40 | 505234 | 623 | 494766 | 528702 | 694 | 471298 | 023468 | 3 71 | 97653? | 50 | | 20 |
| П | | | 41 42 | 505608 | 623 | 494392 | 529119 | | 470881 | 02351 | | 976489 | | | 16 |
| П | | | 43 | 505981 506354 | 622 | 494019 493646 | 529535 529950 | 693 692 | 470465 470050 | 02355 02359 | | 976416 976404 | _ | | 8 |
| Ŀ | | | 44 | 506727 | 621 | 493273 | 530366 | | 469634 | 02363 | | 976361 | 16 | | 4 |
| 1 | 5 | | | 9.507099 | 620 | 10.492901 | | 691 | 10.469219 | | | 9.976318 | | 45 | - 0 |
| | | | $\frac{46}{47}$ | 507471 | 620 | 492529 | 531196 | | 468804 468389 | 02372 | | 976275 | | | 56 |
| | | 12 | _ | 507843 509214 | 619 | 492157 491786 | 531611 | 690 690 | 468389 | 023768 | 10000 | 976232 976189 | | 2. | 52 48 |
| ı | | | 49 | 508585 | 618 | 491415 | 532439 | | 467561 | 023854 | 72 | 976146 | 11 | | 44 |
| l | | 20 | | 508956 | 618 | 491044 | 532853 | | 467147 | 02389 | | 976103 | | | 40 |
| L | | 24 28 | | 509326 509696 | | 490674 490304 | 533266 533679 | | 466734 466321 | 023940 023983 | | 976060 976017 | 9 | | 36 |
| Ш | | 32 | | 510065 | | 489935 | | | 465908 | 024020 | | 975974 | | | 28 |
| ı | | 36 | | 510434 | | 489566 | | | 465496 | 024070 | 72 | 975930 | | | 24 |
| п | | 40 44 | | 510803 511172 | | 489197 488828 | | | 465084 | 024113 024156 | | 975887 975844 | 5 | | 20 |
| 1 | | 48 | | 511540 | | 488460 | _ | | 464672 464261 | 024150 | | 975800 | | 11 | 12 |
| 1 | × | 52 | 58 | 511907 | 613 | 488093 | 536150 | 685 | 463850 | 024243 | 72 | 975757 | 2 | | 8 |
| 1, | | 56 | 59 60 | 512275 | | 487725 | | 684 | 463439 | 024286 024330 | | 975714 | 1 | 1.4 | 4 |
| = | 6 | | - | 512642 | 012 | 487358 | | 034 | 463028 | | 12 | 975670 | = | 44 | 0 |
| n | 1. | 8. | | Cosine. 4 Hor | 1370 | Secant. | Cotang. | 07 | Tang. | Cosec. | l De | Sine. | | m. | S. |
| H | - | - | | 12 | 15" | 94 | 1s | or 15" | 105 | 15 | 15" | grees. | | | |
| | | P. or | | 2 | 30 | 189 | 2 | 30 | 210 | 2 | 30 | 21 | | P. or | |
| L | - | - | | 3 | 45 | 283 | 3 | 45 | 315 | 3 | 45 | 31 | 3 | OI | 1 |

| - | - | _ | _ | _ | . 70 | and | Seca | ints. | Grand Control | Ta | BLE V. | | 37 |
|----|----------|----------|--------------------|------------|---------------------|------------------|------------|------------------|---------------------|----------|--------------------|-------|----------|
| - | - | - | 1 Ho | mr. | | | or . | | 1: | | grees. | | |
| m. | · S. | 11 | I Sine. | D. | Cosec. | Tang. | D. | Cotang. | Secant | D. | Cosine. | l'm | . 5 |
| 16 | | = | 9.512642 | - | 10.487358 | 9.536972 | 684 | | 10.024330 | 73 | 9.975670 | 60 44 | _= |
| 10 | 4 | | | 1 | 486991 | 537382 | 1 | 462618 | 024373 | | 975627 | | 56 |
| Е | 8 | | | | 486625 | | | 462208 | 024417 | | 975583 | | 5% |
| 1 | 18 | | | | 486259 | - | | 461798 | 024461 | | 975539 | | 45 |
| н | 16 | | | | 485893 | | 682 | 461389 460980 | 024504 024548 | | 975496 975452 | | 44 |
| | 20 | | | | 485528 485163 | | | 460571 | 024548 | | 975408 | | 36 |
| Ħ | 28 | | | | 484798 | | | 460163 | 024635 | | 975365 | | 32 |
| ш | 32 | 1 | | | 484434 | | | 459755 | 024679 | 73 | 975321 | | 28 |
| | 36 | | | | 484070 | | | 459347 | 024723 | | 975277 | | 24 |
| ш | 40 | | | 606 | 483706 483343 | | 679 678 | 458939 458532 | 024767 024811 | 73 73 | 975233 975189 | | 20 |
| | 48 | | 516657 517020 | | 482980 | | -0.00 | 458125 | 024855 | | 975145 | | 16 |
| ш | | | | | 482618 | 542281 | 677 | 457719 | 024899 | 73 | 975101 | | 8 |
| ш | | 14 | | 604 | 482255 | 542688 | 677 | 457312 | 024943 | 73 | 975057 | 46 | 4 |
| 17 | 0 | 15 | 9.518107 | 603 | 10.481893 | 9.543094 | 676 | 10.456906 | 10.024987 | 73 | 9.975013 | 45 43 | 0 |
| | 4 | | | | 481532 | | | 456501 | 025031 | 74 | 974969 | | 56 |
| 1 | 8 | | 518829 | | 481171 | 543905 | | 456095 | 025075 | | 974925 | | 52 |
| 11 | 12 | 18 | 519190 519551 | 601 | 480810 480449 | 544310 544715 | | 455690 455285 | 025120 025164 | | 974880 974836 | | 48 |
| | | 20 | 519911 | 600 | 480089 | 545119 | | 454881 | 025208 | | 974792 | | 40 |
| | 24 | 21 | 520271 | 600 | 479729 | 545524 | 673 | 454476 | 025252 | 74 | 974748 | 39 | 36 |
| | 28 | | 520631 | 599 | 479369 | 545928 | | 454072 | 025297 | 74 | 974703 | | 38 |
| | 32 | | 520990 521349 | 599 598 | 479010 478651 | 546331 546735 | | 453669 453265 | 025341 025386 | 74 | 974659 974614 | | 24 |
| | 36 40 | | 521707 | 598 | 478293 | 547138 | | 452862 | 025430 | 74 | 974570 | | 20 |
| | | | 522066 | | 477934 | 517540 | | 452460 | 025475 | | 974525 | | 16 |
| | 48 | 27 | 522424 | | 477576 | 547943 | | 452057 | 025519 | 74 | 974481 | | 12 |
| 17 | 52 | | 522781 | 596 | 477219 | 548345 | | 451655 | 025564 | 74 | 974436 | | 8 |
| | _ | 29 | 523138 | | 476862 | 548747 | 669 | 451253 | 025609 | 74 | 974391 | | 4 |
| 18 | | 30 31 | 9.523495 523852 | 595 594 | 10.476505 476148 | 549550 | 669 | 450450 | 10.025653 025698 | 75 75 | 9.974347 974302 | | 56 |
| | | 32 | 524208 | | 475792 | 549951 | 668 | 450049 | 025743 | 75 | 974257 | | 52 |
| | 12 | | 524564 | 593 | 475436 | 550352 | 1.11.14 | 449648 | 025788 | 75 | 974212 | | 48 |
| | 16 | | 524920 | | 475080 | 550752 | 667 | 449218 | 025833 | 75 | 974167 | | 44 |
| | 20 | | 525275 | 592 | 474725 | 551152 | | 448848 | 025878 | 75 | 974122 | | 40 |
| | 24 28 | | 525630 525984 | 591 591 | 474370 474016 | 551552 551952 | 666 665 | 448448 448048 | 025923 025968 | 75 75 | 974077 974032 | | 36 |
| | 32 | | 526339 | 590 | 473661 | 552351 | 665 | 447649 | 026013 | 75 | 973987 | | 28 |
| 93 | 36 | | 526693 | 590 | 473307 | 552750 | 665 | 447250 | 026058 | 75 | 973942 | 21 | 24 |
| | | | 527046 | 589 | 472954 | 553149 | 664 | 446851 | 026103 | 75 | 973897 | | 20 |
| | 41 | 41 | 527400 | 589 588 | 472600 | 553548 | 664 | 446452 446054 | 026148 | 75 75 | 973852 | | 16 |
| | | 43 | 527753 528105 | 588 | 472247 471895 | 553946 554344 | 663 | 445656 | 026193 026239 | 75 | 973807 973761 | | ,12 8 |
| | 56 | 44 | 528458 | 587 | 471542 | 551741 | 662 | 445259 | 026284 | 76 | 973716 | | 4 |
| 19 | 0 | 45 | 9.528810 | 587 | 10.471190 | 9.555139 | 662 | 10.444861 | 10.026329 | 7.6 | 9.973671 | - | 0 |
| | . 4 | 46 | 529161 | 586 | 470839 | 555536 | 661 | 444464 | 026375 | 76 | 973625 | | 56 |
| | 8 12 | | 529513 | | 470487 470136 | 555933 | | 444067 | 026420 026465 | 76 | 973580 | | 52 |
| | 16 | | 529864 530215 | | 469785 | 556329 556725 | 660 | 443671 443275 | 026465 | 76 76 | 973535 973489 | | 48 |
| 1 | | 50 | | | 469435 | | | 442879 | 026556 | | 973444 | 10 | 40 |
| 1 | 24 | 51 | 530915 | 584 | 469085 | 557517 | 659 | 442483 | 026602 | 76 | 973398 | 9 | 36 |
| 1 | 28 | | 531265 | | 468735 | | | 442087 | 026648 | | 973352 | 8 | 32 |
| | | 53 54 | | | 468386 468037 | 558308 558702 | | 441692 441298 | 026693 | | 973307 973261 | 7 6 | 28 24 |
| | 40 | | | | 467688 | | | 440903 | 026785 | | 973215 | 5 | 20 |
| 1 | | 56 | | | 467339 | | | 440509 | 026831 | | 973169 | 4 | 16 |
| | 48 | | 533009 | | 466991 | 559885 | | 440115 | 026876 | | 973124 | 3 | 12 |
| | 52 | | 533357 | | 466643 | 560279 | | 439721 | 026922 | | 973078 | 2 | 8 |
| 50 | 56 | 60 | 533704 534052 | | 466296 465948 | 560673 561066 | | 439327 438934 | 026968 027014 | | 973032 972986 | 0 40 | 4 0 |
| | _ | - | | === | - | Cotang. | == | Tang. | | - | Sine. | / m. | |
| m. | 5. | | Cosine. | urs | Secant. | Coung. | or | rang. I | | | grees. | m. | S. |
| - | - | | 15 | 15" | 89 | 1: | 15" | 100 | | 5" | 111 | - | |
| | P. | | 2 | 30 | 178 | 2 | 30 | 200 | 2 3 | 0 | 22 | P. P. | |
| LS | OF. | | 3 | 45 | 268 | 3 | 45 | 301 | 3 4 | 5 | 34 | SOF | |

| 3 | 3 | | TABLE | v. | Log | arithmic | Sine | s, Tangent | ts, | - | | | - | |
|-----|----------|---|--------------------|------------|---------------------|--------------------|-----------|---------------------|-----------------|------|--------------------|----------|------|----------|
| | | - | 1 Ho | | | | or | | | | grees. | | | |
| m. | 8- | 1 | Sine. | D. | Cosec. | Tang. | D. | Cotang. | Secant. | D. | Cosine. | = | m. | S. |
| 20 | 0 | | 9.534052 | 578 577 | 10.465948 465601 | | | 10.438934 438541 | | | 9.972986 | 50 | 10 | 0 |
| 58 | 8 | 5 | 534399 534745 | 577 | 465255 | 561459 561851 | 654 | 438149 | 027060 | | 972940 972894 | 59 58 | | 56 52 |
| П | 12 | 3 | 535092 | 577 | 464908 | 562244 | | 437756 | 02715 | 2 77 | 972848 | 57 | | 48 |
| 15 | 16 20 | 5 | 535438 | 576 576 | 464562 | 562636 563028 | | 437364 436972 | 027198 | | 972809 | 56 | | 44 |
| 17 | 24 | 6 | 535783 536129 | 575 | 464217 463871 | 563419 | | 436581 | 02729 | | 972709 | 54 | | 36 |
| | 28 | 7 | 536474 | 574 | 463526 | 563811 | | 436189 | 02733 | | 972663 | | | 32 |
| | 32 36 | 8 9 | 536818 537163 | 574 573 | 463182 462837 | 564202 564592 | | 435798 435408 | 027383 02743 | | 972617 | 52 | L | 28 24 |
| 12 | 40 | | | 573 | 462493 | 564983 | | 435017 | 02747 | | 972524 | 50 | | 20 |
| | 44 | | 537851 | 572 | 462149 | 565373 | 1 | 434627 | 02752 | | 972478 | 19 | | 16 |
| 100 | 48 52 | | | 572 571 | 461806 461462 | 565763 566153 | | 434237 433847 | 027569 02761 | | 972431 972385 | 18 | | 12 |
| 7 | | 14 | | 571 | 461120 | 566542 | | 433458 | 02766 | | 972338 | | | 4 |
| 21 | 0 | 15 | 9.539223 | 570 | 10.460777 | 9.566932 | | 10.433068 | | | 9.972291 | | 39 | 0 |
| | 4 | | 539565 | 570 | 460435 | 567320 | | 432680 | | | 972245 | | | 56 |
| 1 | 8 12 | 17 18 | 539907 540249 | 569 569 | 460093 459751 | 567709 568098 | | 432291 431902 | 02780 | | 972198 972151 | | 1 | 52 48 |
| | 16 | 19 | 540590 | 568 | 459410 | 568486 | 646 | 431514 | 02789 | 5 78 | 972105 | 41 | 211 | 44 |
| 2.5 | 20 | | 540931 | 568 | 459069 | 568873 | | 431127 | 02794 | | 972058 | | 1 | 4.0 |
| | 24 | 21 | 541272 541613 | 567 | 458728 458387 | 569261 569648 | | 430739 430352 | 02798 02803 | | 972011 971964 | | | 36 |
| | | 23 | | | 458047 | 570035 | | 429965 | | . (| 971917 | | | 28 |
| | | 24 | | 566 | 457707 | 570428 | | 429578 | | | 971870 | | | 24 |
| Г | 40 | | | 565 565 | 457368 457029 | 570809 571195 | | 429191 428805 | 02817 02822 | | 971823 971776 | | 1 | 20 |
| 1 | 48 | | | De . | 456690 | | | 428419 | 02827 | | 971729 | | | 12 |
| 10 | | 28 | | 564 | 456351 | 571967 | | 428033 | | | 971682 | | | 8 |
| - | | 29 | | 563 | 456013 | 572352 | | 427648 | 2 | | 971635 | | 00 | 4 |
| 22 | 4 | | 9.544325 544663 | 563 562 | 10.455675 455337 | 9.572738 573123 | | 10.427262 426877 | 02846 | | 9.971588 971540 | | 38 | 56 |
| 10 | - | 32 | | | 455000 | | | 426493 | | | 971493 | | | 52 |
| | | 33 | | 100 | 454662 | | | 426108 | | | 971446 | | | 48 |
| | 16 | 34 | | 561 | 454326 453989 | 574276 | | 425724 425340 | | | 971398 971351 | | | 44 |
| п | | 36 | | | 453653 | | | 424956 | | | 971303 | | | 36 |
| 16 | | 37 | 546683 | 559 | 453317 | 575427 | | 424573 | | | 971256 | 153 | | 32 |
| 1 | | 38 | | | 452981 452646 | 575810 576193 | | 424190 423807 | | | 971208 | | | 28 |
| 19 | | 140 | | | 452311 | 576576 | | 423424 | | | 971113 | | | 20 |
| 15 | 44 | 41 | 548024 | 557 | 451976 | 576959 | | 423041 | 02893 | | 971066 | 19 | 1 | 10 |
| 16 | | 42 | | | 451641 | 577723 | | 422659 | | | 971018 | | | 12 |
| 10 | | 43 | | | 451307 450973 | | 1.0 | 422277 421896 | 02903 02907 | | 970970 | | | 4 |
| 23 | _ | - | | 1 | 10.450640 | | | 10.421514 | | | 9.970874 | 1 | 37 | (|
| P | | 146 | 549693 | 555 | 450307 | 578867 | 635 | 421133 | | | 970827 | 14 | | 56 |
| 1 | | 47 | | | 449974 449641 | 579248 579629 | | 420753 420371 | 02922 02926 | | 970779 | | | 58 |
| ш | | 3 49 | | | 449308 | | | 419991 | | | 97068 | | | 4.4 |
| B | | 50 | 551024 | 553 | 448976 | 580389 | 633 | 419611 | 02936 | 5 80 | 970635 | 10 | 100 | 40 |
| 150 | 2 | 51 3 52 | | | 448644 448313 | | | 419231 | | | 970586 | | | 36 |
| 1 | 32 | 2 53 | 551687 552018 | | | | | 418851 | | | 970535 | | | 28 |
| 1 | 36 | 3 54 | 552349 | 551 | 447651 | 58190 | 632 | 418093 | 02955 | 8 80 | 970442 | 6 | | 24 |
| - | | 55 1 50 | | | 447320 | | | 417714 | | | 970394 | | | 20 |
| 1 | 48 | 3 57 | 553010 | | 446990 446659 | | | 417335 | | | 970345 | | | 16 |
| 8 | 5 | 2 58 | 553670 | 549 | 446330 | 58342 | 630 | 416578 | 02975 | 1 81 | 970249 | 2 | | 8 |
| 24 | | $\begin{array}{c c} 6 & 59 \\ 0 & 60 \end{array}$ | | | 446000 | | | 416200 | | | 970200 | | | 4 |
| | - | = = | | 348 | | | 029 | 415823 | | 0 81 | 970158 | = | 36 | - |
| m | | 3. / | Cosine. | 01170 | Secant. | Cotang. | 1 | Tang. | Cosec. | 30 D | Sine. | Ľ | lm. | S |
| 7 | | - | 1 1s (| 15' | ′ 84 | 18 | or 15' | 1 96 | 1s | 15" | grees. | | - | |
| | s o | | 2 | 30 | 169 | 2 | 30 | 193 | 2 | 30 | 24 | | . P. | |
| 1 | 3 0 | | 3 | 45 | 253 | 3 | 4.5 | 289 | 3 | 45 | 36 | 1 5 | or | |

| | | | | | | an | l Sec | ints. | 100 | TA | BLE V. | | |
|-----|-------|----|------------------|------------|------------------|------------------|-----------------------|------------------|--------------------------|------|------------------|----|-------|
| E | | | 1 Ho | ur, | | | or | | 2 | 1 De | grees. | | _ |
| m. | S. | 1 | Sine. | D. | Cosec. | Tang. | D. | Cotang. | Secant. | D. | Cosine. | 1 | m. |
| 24 | ō | 0 | 9.554329 | 548 | 10.445671 | 9.58417 | 629 | 10.415823 | 10.02984 | 81 | 9.970152 | 60 | 36 |
| | 4 | 1 | 554658 | | 445342 | | | 415445 | | | 970103 | | |
| | 8 | 2 | 554987 | 547 | 445013 | 584939 | 628 | 415068 | 02994 | 81 | 970055 | 58 | 1 |
| | 12 | 3 | 555315 | | 444685 | | | 414691 | 02999 | | 970006 | | |
| | 16 | 4 | 555643 | | 444357 | | | 414314 | | | 969957 | | |
| | 20 | 5 | 555971 | | 444029 | | | 413938 | | | 969909 | | |
| | 24 28 | 6 | 556299 556626 | | 443701 | | | 413561 | 03014 | | 969860 | | |
| | 32 | 3 | 556953 | | 443374 443047 | | | 413185 412810 | | | 969811 | | |
| | 36 | 9 | 557280 | | 442720 | | To the same of | 412434 | | | 969714 | | |
| | | 10 | 557606 | | 442394 | | 1000 | 412059 | | | 969665 | | |
| | | 11 | 557932 | | 442068 | | | 411684 | | | 969616 | | |
| | 48 | | 558258 | | 441742 | | | 411309 | | | 969567 | | |
| | 52 | 13 | 558583 | 542 | 441417 | 589066 | 2.00 | 410934 | 03048 | | 969518 | | |
| Ł | 56 | 14 | 558909 | 542 | 441091 | 589440 | 623 | 410560 | 03053 | 1 82 | 969469 | 16 | |
| 5 | 0 | 15 | 9.559234 | 541 | 10.440766 | 9.589814 | 623 | 10.410186 | 10.03058 | 82 | 9.969420 | 15 | 35 |
| | 4 | | 559558 | | 440442 | 590188 | 623 | 409812 | 03063 | 82 | 969370 | | |
| | 8 | | 559883 | | 440117 | | | 409438 | 03067 | | 969321 | | |
| | 12 | | 560207 | 540 | 439793 | | | 409065 | | | 969272 | | |
| | 16 | | 560531 | | 439469 | | | 408692 | | | 969223 | | |
| | 20 2 | | 560855 | | 439145 | | | 408319 | 03082 | | 969173 | | |
| | 28 2 | | 561178 561501 | 538 538 | 438822 438499 | | | 407946 407574 | 03087 | | 969124 | | |
| | 32 | | 561824 | | 438176 | | | 407202 | 03097 | | 969025 | | |
| | 36 | | 562146 | | 437854 | 593171 | | 406829 | and the second second | | 968976 | | |
| | 40 2 | | 562468 | | 437532 | 593542 | | 406458 | 03107 | | 968926 | | |
| | 44 | | 562790 | 536 | 437210 | 593914 | | 406086 | 03112 | | 968877 | | |
| ٨ | 48 | 27 | 563112 | 536 | 436888 | 594285 | | 405715 | 031173 | | 968827 | 33 | |
| | 52 | | 563433 | 535 | 436567 | 594656 | 618 | 405344 | 031223 | 83 | 968777 | 32 | , LI |
| Ľ. | 56 | 29 | 563755 | 535 | 436245 | 595027 | 617 | 404973 | 03127 | 83 | 968728 | 31 | 1 |
| 6 | 0 | 30 | 9.564075 | 534 | 10.435925 | 9.595398 | 617 | 10.404602 | 10.03132 | 83 | 9.968678 | 30 | 34 |
| | 4 | | 564396 | 534 | 435604 | 595768 | | 404232 | 031372 | | 968628 | | |
| | 8 | | 564716 | 533 | 435284 | 596138 | 616 | 403862 | 03142 | | 968578 | | B. |
| | 123 | | 565036 | 533 | 434964 | 596508 | The second second | 403492 | 031472 | . 00 | 968528 | | |
| | 165 | | 565356 | 532 | 434644 | 596878 | | 403122 | 031521 | | 968479 | | P. |
| | 20 3 | | 565676 | | 434324 | 597247 | | 402753 402384 | 03157 | 100 | 968429 968379 | | |
| | 28 | 36 | 565995 566314 | 531 531 | 434005 433686 | 597616 597985 | The state of the last | 402015 | 031671 | | 968329 | | |
| | 323 | | 566632 | 531 | 433368 | 598354 | | 401646 | 031729 | | 968278 | | |
| | 36,3 | | 566951 | 530 | 433049 | 598722 | | 401278 | 031772 | | 968228 | | 13 |
| | 40 4 | | 567269 | 530 | 432731 | 599091 | | 400909 | 031829 | | 968178 | | 2.5 |
| | | 11 | 567587 | 529 | 432413 | 599459 | | 400541 | 031879 | | 968128 | | 9.5 |
| | 48 4 | | 567904 | 529 | 432096 | 599827 | 613 | 400173 | 031922 | | 968078 | | = 4 |
| | 52,4 | | 568222 | 528 | 431778 | 600194 | 612 | 399806 | 031973 | | 968027 | | |
| | 56 | 14 | 568539 | 528 | 431461 | 600562 | 612 | 399438 | 032023 | 102 | 967977 | | (0) |
| 7 | | | 9.568856 | 528 | 10.431144 | | | 10,399071 | | | | | 33 |
| | 4 4 | | 569172 | 527 | 430828 | 601296 | | 398704 | 032124 | 100 | 967876 | | 1 |
| | 8 | | 569488 | 527 | 430512 | 601662 | | 398338 | 032174 | - | 967826 | | 2 |
| 13. | 124 | | 569804 | 526 | 430196 | 602029 | | 397971 | 032225 | 0 - | 967775 | | 1 |
| | 16 3 | | 570120 | | 429880 | | | 397605 | 03227 <i>5</i> 032326 | | 967725 967674 | | 1 |
| | 24 | 51 | 570135 570751 | | 429565 429249 | | | 397239 396873 | 032376 | 84 | 967624 | | 16 |
| | 28 | | 571066 | | 429249 | 603127 | | 396507 | 032427 | 84 | 967573 | 8 | |
| | 32 | | 571380 | | 428620 | | | 396142 | 032478 | | 967522 | 7 | |
| | 36 | | 571695 | | 428305 | 200000 | | 395777 | 032529 | 85 | 967471 | 6 | |
| | 40 | | 572009 | | 427991 | 604588 | | 395412 | 032579 | 85 | 967421 | 5 | |
| | 44 5 | 56 | 572323 | | 427677 | 604953 | | 395047 | 032630 | 85 | 967370 | 4 | |
| | 48 | | 572636 | | 427364 | | | 394683 | 032681 | 85 | 967319 | 3 | |
| | 52 | | 572950 | | 427050 | | | 394318 | 032732 | | 967268 | 2 | |
| 0 | 56 | | 573263 | | 426737 | 606046 | | 393954 | 032783 | | 967217 | 1 | 200 |
| 8 | 0,0 | 50 | 573575 | 521 | 426425 | 606410 | 606 | 393590 | 032834 | 85 | 967166 | 0 | 32 |
| n. | S. | 1 | Cosine. | | Secant. | Cotang. | | Tang. | Cosec. | | Sine. | 1 | m. |
| | | | 4 Ho | urs. | | | or | -6 | | 3 De | grees. | | |
| D | D . | - | ls | 15" | 1 80 | 18 | 15" | 93 | | 15" | 12 | - | - |
| | P. t | | 2 3 | 30 | 160 | 2 | 30 | 185 | | 30 | 25 | | P. or |
| | or ' | / | | | | | | | | | | | |

| 1 | 40 | | TABL | e V. | Lo | garithm | ic Sin | es, Tangen | its, | | | | |
|------|------|----------|------------------|------|---------------------|--|-----------|---------------------|-------------------|-------|------------------|------|----------|
| | | 1/ | 1 Ho | D. | Cosec. | Tang. | or | Cotang. | 1 Secant. | 22 D | cosine. | 10 | im a |
| 2 | | 0 (|).9.573575 | - | 10.426425 | | _ | | - | | 9.967160 | = | |
| ž | | | 573888 | | 426113 | | | 393227 | | 1 | 967118 | | 56 |
| п | | 8 8 | 574200 | | 425800 | | | 392863 | 0329 | 36 85 | 967064 | | 59 |
| - 8 | 1 | | | 1 | 425188 425176 | | -1 - | 392500 392137 | | | 967013 | | 48 |
| - 15 | 2 | | | | 424864 | | 1000 | 392137 | | | 966910 | | 44 |
| ш | 2 | 1 6 | 575447 | | 424559 | | | 391412 | | | 966859 | | 36 |
| 1 | .28 | | | | 424242 | | | 391050 | | | 966808 | | 32 |
| - 6 | 39 | | | | 423931 423621 | | 100 | 390688 390326 | | | 966705 | | 28 24 |
| | 3 40 | | | | 423311 | | | 389964 | The second second | | 966653 | | 20 |
| | 4 | | | | 423001 | | | 389603 | | | 966602 | | 16 |
| - | 1 49 | | | | 422691 422382 | | | 389241 388880 | 0334 | | 966550 | | 12 |
| 13 | 56 | | | 515 | 422073 | | | 388520 | 0335 | | 966447 | | . 4 |
| 29 |) (| 15 | 9.578236 | 514 | 10.421764 | | _ | 10.388159 | 10.03360 | 5 86 | 9.966395 | 1.5 | - |
| 100 | | 16 | | | 421455 | | | 387799 | | | 966344 | | 56 |
| IX. | 1 9 | 17 | 578853 579162 | | 421147 | | | 387439 387079 | 03370 | | 966293 | | 52 48 |
| 16 | 16 | | 579470 | | 420530 | | 1 | 386719 | 0338 | | 966188 | | 4.4 |
| 10 | | 20 | 579777 | 512 | 420223 | 61364 | 1 599 | 386359 | 03386 | 64 86 | 966136 | 40 | 40 |
| 10 | 24 | 1.0 | 580085 | | 419915 | | | 386000 | 03391 | 1 | 966085 | | 36 |
| 10 | 32 | | 580392 580699 | | 41960s 419301 | 61435 61471 | | 385641 385289 | 03396 | 10000 | 966033 965981 | | 32 |
| 1/2 | 36 | | 581005 | | 418995 | | | 384923 | 03407 | | 965929 | | 24 |
| 10 | - 40 | 1 | 581312 | | 418688 | | | 384565 | 03418 | 1000 | 965876 | | 20 |
| 100 | 44 | 1 | 581618 | | 418382 | | | 384207 383849 | 03417 | | 965824 965772 | | 16 |
| 16 | 52 | | | | 417771 | 61650 | | 383491 | 03428 | | 965720 | | 8 |
| | 56 | 29 | 582535 | 509 | 417465 | 61686 | 7 596 | 383133 | 03433 | 2 87 | 965668 | 31 | 4 |
| 30 | _ | | 9.582840 | 508 | 10.417160 | | | 10.382776 | | | 9.965615 | | |
| Е | . 4 | 31 | 583145 | 508 | 416855 | | 1 1 2 2 2 | 382418 382061 | 03448 | 1 - 1 | 965563 | | 56 |
| 100 | | 33 | 583449 583754 | | 416246 | 61793 61829 | 1000 | 381705 | 03454 | | 965511 965458 | | 52 48 |
| 18 | | 34 | 584058 | | 415942 | 61865 | | 381348 | , 03459 | | 965406 | | 44 |
| 10 | | 35 | 584361 | 506 | 415639 | THE RESERVE OF THE PARTY OF THE | | 380992 | 03464 | - | 965353 | | 40 |
| В | 24 | 36 | 584665 584968 | 506 | 415335 415032 | 61936 | | 380636 380279 | 03469 | | 965301 965248 | | 36 |
| 100 | | 38 | 585272 | | 414728 | | | 379924 | 03480 | | 965195 | | 28 |
| 100 | | 39 | 585574 | 504 | 414426 | 62043 | 15.00 | 379568 | 03485 | - | 965143 | | 21 |
| 10 | | 40 | 585877 586179 | 504 | 414123 413821 | 62078 | 1 4 | 379213 378858 | 03491 | 1 - | 965090 965037 | | 20 16 |
| E | | 42 | 586482 | 503 | 413518 | 62149 | 1 1 1 | 378503 | 03501 | | 964984 | | 12 |
| в | | 43 | 586783 | 503 | 413217 | 62185 | 2 591 | 378148 | 03506 | 9 88. | 964931 | 17 | - 8 |
| | _ | 44 | 587085 | 502 | 412915 | 62220 | _ | 377793 | 03512 | - 00 | 964879 | 16 | 4 |
| 31 | | 45 | 9.587386 | 502 | 10.412614 412312 | 9,62256 62291 | | 10.377439 377085 | 10.03517 | | 9.964826 | 15 | |
| 1 | | 47 | 587688 587989 | 501 | 412312 | 623269 | | 376731 | 03528 | | 964773 964720 | | 56 52 |
| 100 | 12 | 48 | 588289 | 501 | 411711 | 623623 | 1000 | 376377 | 03533 | 4 89 | 964666 | | 48 |
| 100 | | 49 | 588590 | 500 | 411410 | 62397 | | 376024 | 03538 | | 964613 | | 4.4 |
| 100 | | 50 51 | 588890 589190 | 500 | 411110 | 624330 | | 375670 375317 | 03544 03549 | | 964560 964507 | | 40 36 |
| Е | | 52 | 589489 | | 410511 | | | 374964 | 03554 | | 964454 | | 32 |
| в | | 53 | 589789 | | 410211 | 625388 | 100000 | 374612 | 03560 | 0 89 | 964400 | 7 | 28 |
| | 36 | 54 55 | 590088 | | 409912 | 62574 | | 374259 | 03565 | 3 89 | 964347 | 6 | 2.1 |
| 1 | | 56 | 590387 590686 | | 409013 | | | 373907 373555 | 03570 03576 | | 964294 964240 | 5 | 20 16 |
| | 48 | 57 | 590984 | 497 | 409016 | 62679 | 586 | 373203 | 03581 | 3 89 | 961187 | 3 | 12 |
| 1 | | 58 59 | 591282 | | 408718 | | | 372851 | 03586 | | 964133 | 2 | 8 |
| 32 | | 60 | 591580 591878 | | 408420 | | | 372499 372148 | 03592 03597 | | 964080 964026 | 0 2 | 28 0 |
| m. | | | Cosine. | | Secant. | Cotang. | | Tang. | Cosec. | = | Sine. | | - |
| | | - | 4 Hor | ırs. | octant. | Cotang. | or | rang. | | 7 De | | - 11 | n. s. |
| P | . P. | to | 13 | 15" | 76 | 18 | 15" | 89 | 18 | 15" | 1 - 13 - 1 | P | n |
| | or | | 2 | 30 | 152 | 2 3 | 30 | 178 | 2 3 | 30 | 26 | | P. to |
| L | - | | 3 | 45 | 229 | 3 | 45 | 268 | 3. | 45 | 39 | 0 | |

| 2 | | | | | - | | - | | - | - | | | 900 | | | | | |
|------|------|----------|----|------------------|-------|----|----------------------------|------------------|------|--------------|----------------------------|---------|----------------|----------|---------------------------|-----|------------|----------|
| I | | | | | | G | | а | nd | Seca | nts. | 1000 | _ | TA | BLE V. | | . 4 | 41 |
| | | | - | | lour | _ | | - | 5- | or | | | - | | grees. | | | |
| | 1. | S. | | Sine. | '_ |). | | Tang | | D. | Cotang. | 1 Seca | | D. | Cosine. | - | m. | ·S. |
| 3 | 2 | 0 | | 9.5918° 5921° | 78 49 | 16 | 10.408123 | | | 585 585 | 10.372148 371797 | | 5974 6028 | | 9.964026 | | | 56 |
| ж | | 4 8 | 2 | 59247 | | | 407527 | | | | 371446 | | 6081 | | 963919 | | | 52 |
| - 15 | . 1 | 12 | 3 | 59277 | 70 49 |)5 | 407230 | 6289 | 05 | 584 | 371095 | 03 | 6135 | 90 | 963863 | 57 | 1 | 48 |
| в | | 16 | 4 | 59306 59336 | | | 406933 | | | | 370745 | | 6189 | | 963811 | | | 44 |
| ж | | 20 24 | 5 | 59368 | | | 406637 406341 | | | | 370394 370044 | | 6243 6296 | | 963757 | | | 36 |
| в | 2 | 28 | 7 | 59395 | 5 49 | 3 | 406015 | 6303 | 06 | 583 | 369094 | 03 | 6350 | 90 | 963650 | 53 | | 32 |
| E | | 32 | 8 | 59425 59454 | | | 405749 | | | | 369344 | | 6404 | | 963596 | | | 28 |
| т | | 10 | 9 | 59484 | | | 405453 | | | | 368995 368645 | | $6458 \\ 6512$ | | 963488 | | | 20 |
| т | D 4 | 14 | 11 | 59513 | 37 49 | 1 | 404863 | 6317 | 04 | 582 | 368296 | 03 | 6566 | 90 | 963434 | 19 | 1.6 | 16 |
| в | | 18 | | 59543 | | | 404568 | | - 1 | | 367947 | | 6621 | | 963379 | | | 12 |
| в | | 52 | | 59573 59603 | | | 404273 403979 | | | 581 581 | 367599 367250 | | 5675 5729 | | 963323 | | | 8 |
| 3 | _ | | | 9.59631 | | _ | 10.403685 | - | - | 580 | 10.366902 | | | - | 9 963217 | | - | 0 |
| | | 4 | 16 | 59660 | 9, 48 | 9 | 403391 | 6334 | 47 | 580 | 366553 | 036 | 3837 | 90 | 963169 | 4.4 | | 56 |
| | Y . | | 17 | 59690 59719 | | | 403097 | | | 580 | 366205 | | 5892 5046 | | 963108 | | | 52 48 |
| | | 6 | | 59719 | | | 402804 402510 | | | 579 | 365857 365510 | | 5946 7001 | | 963054 962999 | | 1 | 48 |
| В | . 2 | 20 | 20 | 59778 | | | 402217 | 6348 | 38 | 579 | 365162 | 031 | 7055 | 91 | 962945 | | 102 | 40 |
| B | | 4 | | 59807 | | | 401925 | | | 578 | 364815 | | 1110 | | 962890 | | 2 | 36 |
| 10 | | 2 | | 59836 59866 | | | 401632 401340 | | - 1 | 578 578 | 364468 364121 | | 7164 7219 | | 962836 962781 | | 16 | 32 |
| 16 | | 6 | | 59895 | | | 401048 | 6362 | | 577 | 363774 | | 1273 | | 962727 | | JE | 24 |
| Е | | 0 | | 59924 | | | 400756 | | | 577 | 363428 | | 328 | | 962672 | | The second | 20 |
| Е | | 4 | | 59953 59982 | , | _ | 400464 400173 | 6369 | | 577 577 | 363081 362735 | | 7383 7438 | | 962617 962562 | | | 16 |
| 12 | | 2 | | 60011 | | _ | 399882 | 6376 | | 576 | 362389 | | 492 | | 962508 | | 0 | 8 |
| | | 6 | | -60040 | | 4 | 399591 | 6379 | 56 | 576 | 362044 | 037 | 547 | 91 | 962453 | | | 4 |
| 34 | | | | 9.60070 | | | 10.399300 | | | 576 | 10.361698 | | 0.000 | | 9.962398 | | 26 | 0 |
| 12 | | 4 5 | | 60099 | | | 399010 398720 | | | 575 575 | 361353 361008 | | 657 | | 962343 962288 | | | 56 52 |
| 10. | | 2 | | 6)157 | | | 398430 | | | 575 | 360663 | | 767 | 92 | 962233 | | 7 | 48 |
| 16 | . 1 | 6 | 34 | 60186 | | | 398140 | | | 574 | 360318 | | 822 | 100.00 | 962178 | | E. | 44 |
| 100 | | 0 3 | | 6)215 | | | 397850 397561 | 6400° 6403° | | 574 574 | 359973 359629 | | 877 933 | 92 92 | 962123 962067 | | 100 | 40 36 |
| 83 | | 8 | | 60272 | | - | 397272 | 6407 | | 573 | 359284 | | 988 | | 962012 | | 90 | 32 |
| В | 3 | 23 | 38 | 60301 | 7 48 | • | 396983 | 6410 | 60 | 573 | 358940 | 038 | 043 | 92 | 961957 | 22 | - | 28 |
| 16 | | 63 | _ | 60330 | | | 396695 | 64140 | | | 358596 | | 098 154 | | 961902 | | 66 | 24 |
| 18 | | 0 4 | 11 | 60388 | | | 396406 396118 | 64174 | | 572 572 | 358253 357909 | | 209 | 92 92 | 961846 961791 | | 6 | 20 |
| ш | 4 | 8 | 12 | 60417 | 0 47 | 9 | 395830 | 64243 | 34 | 572 | 357566 | 038 | 265 | 92 | 961735 | 18 | St. | 12 |
| н | | 6 | | 60445 | | | 395543 | 64277 | - 1 | 572 | 357223 | | 320 376 | - | 961680 | | 10 | 8 |
| 32 | - | - | | 9.60503 | | - | $\frac{395255}{10.394968}$ | 64313 9.64346 | - | 571 | $\frac{356880}{10.356537}$ | 10.038 | | | $\frac{961624}{9.961569}$ | - | 95 | 0 |
| 136 | | 4 | - | 60531 | _ | | 394681 | 64380 | | 571 | 356194 | | 487 | 93 | 961513 | | ж. | 56 |
| N. | | 8 | | 60560 | | | 394394 | 64414 | | 570 | 355852 | | 542 | 93 | 961458 | 13 | | 52 |
| P | | 6 4 | | 60589 | | | 394108 393821 | 64449 | | 570 570 | 355510 355168 | | 598 654 | 93 | 961402 961346 | | | 48 |
| | | 0 | | 60646 | | | 393535 | | 14 | 569 | 354826 | 038 | 710 | 93 | 961290 | | 02 | 40 |
| п | | 1 5 | | 60575 | | | 393249 | 64551 | 6 | | 354484 | 038 | 765 | 93 | 961235 | 9 | - | 36 |
| Ю | | 2 5 | | 60703 60732 | | | 392964 392678 | 64585 64619 | | | 354143 353801 | | 821 877 | 93 | 961179 961123 | | | 32 |
| 153 | | 6 5 | | 60760 | | | 392393 | 64651 | | | 353460 | | 933 | 93 | 961067 | | | 28 24 |
| 16 | 4 | 0 3 | 55 | 60789 | 2 47 | 4 | 392108 | 64688 | 31 3 | 568 | 353119 | 038 | 989 | 93 | 961011 | 5 | | 20 |
| 1 | | 4 | | 60817 | | | 391823 391539 | 64723 | | | 352778 | | 045 | | 960955 | | | 16 |
| | | 23 | | 60346 60374 | | | 391339 | 64756 64790 | | | 352438 352097 | | 157 | | 960899 960843 | | 1. | 12 |
| F | 5 | 6 5 | 9 | 60902 | 9 47 | 3 | 390971 | 64824 | 3 5 | 567 | 351757 | 039 | 214 | 94 | 960786 | 1 | | 4 |
| 36 | - | 0'6 | - | 60931 | 3 47 | 3. | 390687 | 64858 | 33 4 | 566 | 351417 | 039 | 270 | 94 | 960730 | 0 | 24 | () |
| m. | . 8 | 5. | 11 | Cosine. | | 1 | Secant. | Cotang | _ | | Tang. | Cose | - | | Sine. | 1 | m. | S. |
| - | | | - | | ours, | ** | 1 60 | 7. | - | or | 1 00 | - | _ | | rees. | | | |
| | . P. | | | 18 2 | 30 | | 73 145 | 18 2 | | 15" 30 | 86 | 18 2 | | 5" | 14 28 | | P. t | |
| 1 | 01 | - " | 1 | 3 | 4.5 | | 218 | 3 | | 45 | 259 | 3 | | 5 | 41 | S | or " | |

| 1 | - | 2 | - | Tana | LE V. | T | ocorithr | nia Sin | es, Tanger | nte | | | | | | - |
|----|----|----------|----------|------------------|-----------|----------------------------|----------------|-------------|---------------------|--------------|-----|-----------------|---------------------------|-----------|-------|-----------------|
| ı | 4 | -4 | | | lour, | 1.0 | garrin | or | es, Tanger | 1105, | 94 | D | egrees. | | | |
| ı | m. | S. | 1 / | 1 Sine. | D. | Cosec. | Tang. | | Cotang. | Secan | | D. | Cosine. | . / | m. | S |
| ı | 36 | | = | | | 10.390687 | | | 10.351417 | | | 94 | 9.960730 | | - | 0 |
| ı | 30 | 4 | | | | 390403 | | | 351077 | | | 94 | 960674 | | | 56 |
| ı | N. | 8 | 2 | 60988 | 0 472 | 390120 | 6492 | 566 | 350737 | | | 94 | 960618 | 58 | | 52 |
| ľ | | 12 | | | | 389836 | | | 350398 | | | 94 | 960561 | | | 4.9 |
| ı | 8 | 16 20 | 5 | | | 389553 389271 | 6499 | | 350058 349719 | | | 94 | 960505 960448 | | | 44 |
| ı | | 24 | 6 | | | 388988 | | 100 | 349380 | | | 94 | 960392 | | | 36 |
| ı | F | 28 | 7 | 61129 | | 388706 | 211 | | 349041 | 039 | | 94 | 960335 | 53 | | 32 |
| ı | | 32 | 8 | 61157 | | 388424 | | | 348703 | | | 94 | 960279 | | | 28 |
| ı | | 36 40 | 9 | | | 388142 | | | 348364 | | | 94 | 960222 | | | 24 |
| ı | | | | 61242 | | 387860 387579 | 65197 | | 348026 347688 | | | 95 | 960109 | | | 20 16 |
| ı | 6 | 48 | | 61270 | 1 | 387298 | 65265 | | 347350 | | | 95 | 960052 | | | 12 |
| ı | | | 13 | 61298 | | 387017 | 65298 | | 347012 | 040 | | 95 | 959995 | | | 8 |
| ı | | 56 | - | 61326 | | 386736 | 65333 | | 346674 | 040 | | 95 | 959938 | Section 1 | | 4 |
| P | 37 | *0 | 15 16 | 9.61354 61382 | . 1 | 10.386455 | | | 10.346337 | | | 95 | 9.959882 | | | 0 |
| ı | | | 17 | 61410 | | 386175 385895 | 65400 65433 | | 346000 345663 | 040 | | 95 95 | 959825 959768 | | | 56 52 |
| 1 | | 12 | | 61438 | | 385615 | 65467 | - | 345326 | 040 | - | 95 | 959711 | | | 48 |
| 1 | | 16 | | 61466 | | 385335 | | | 344989 | 040 | | 95 | 959654 | | | 44 |
| 1 | | 20 | | 61494 | | 385056 | 65534 | | 344652 | 040 | | 95 | 959596 | | | 40 |
| ı | | 24 28 | | 61522 | | 384777 384498 | 65568 | | 344316 343980 | 040 | | 95 95 | 959539 959482 | | | $\frac{36}{32}$ |
| ı | | 32 | | 61578 | | 384219 | 65635 | | 343644 | 040 | | 95 | 959425 | | | 34 28 |
| ı | | 36 | | 61606 | 0 464 | 383940 | 65669 | | 343308 | 040 | | 95 | 959368 | 4 | | 24 |
| 1 | | 40 | | 61633 | | 383662 | 65702 | | 342972 | 040 | | 96 | 959310 | | | 20 |
| 1 | | 44 | | 61661 | | 383384 | 65736 | | 342636 | 040 | | 96 | 959253 | | | 16 |
| ١ | | 52 | | 61717 | | 383106 382828 | 65769 65803 | | 342301 341966 | 0408 | | 96 96 | 959195 959138 | | | 12 8 |
| ı | | 56 | | 61745 | | 382550 | 65836 | | 341631 | 040 | | 96 | 959080 | | | 4 |
| 1 | 38 | 0 | 30 | 9.61772 | 7 462 | 10.382273 | 9.65870 | 4 558 | 10.341296 | 10.040 | 977 | 96 | 9.959023 | | 22 | 0 |
| ı | | | 31 | 61800 | | 381996 | 65903 | | 340961 | 0410 | | 96 | 958965 | 29 | | 56 |
| ı | | | 32 | 61828 | | 381719 | 65937 | | 340627 | 0410 | | 96 | 958908 | | | 52 |
| I | | 12 16 | 34 | 618558 | | 381442 381166 | 65970 66004 | | 340292 339958 | 041 | | 96 96 | 958850 958792 | | | 48 44 |
| ı | | 20 | | 61911 | | 380890 | 66037 | | 339624 | 0413 | | 96 | 958734 | | | 40 |
| 1 | | 24 | | 61938 | | 380614 | 66071 | | 339290 | 0413 | | 96 | 958677 | 24 | | 36 |
| ı | | 28 | | 61966 | | 380338 | 66104 | | 338957 | 0413 | | 96 | 958619 | | | 32 |
| ı | | 32 | 39 | 61993 | | 380062 379787 | 66137 | | 338623 338290 | 0414 | | 96 97 | 958561 958503 | | | 28 |
| 1 | | | 40 | 62048 | | 379512 | 66204 | | 337957 | 0413 | | 97 | 958445 | | | 20 |
| ı | | | 41 | 62076 | | 379237 | 66237 | - | 337624 | 0416 | | 97 | 958387 | | | 16 |
| ı | | | 42 | 621038 | | 378962 | 66270 | | 337291 | 0416 | | 97 | 958329 | | U: | 12 |
| ı | | 52 | | 621313 62158 | | 378687 | 66304 | | 336958 | 0417 | | 97 | 958271 | | 100 | 8 |
| 1 | 39 | | - | 9.62186 | | $\frac{378413}{10.378139}$ | 66337 | | 336625 10.336293 | 0417 | - | $\frac{97}{97}$ | $\frac{958213}{9.958154}$ | 200 | 21 | 4 |
| 1 | 33 | - 1 | 46 | 62213 | | 377865 | 66403 | | 335961 | 0419 | | 97 | 958096 | | | 0 56 |
| 1 | | 8 | 47 | 62240 | 9 456 | 377591 | 66437 | | 335629 | 0419 | | 97 | 958038 | _ | | 52 |
| 1 | | | 48 | 62268 | -1 | 377318 | 66470 | | 335297 | 0420 | 21 | 97 | 957979 | 12 | 4 | 18 |
| 1 | | - 1 | 49 50 | 62295 | | 377044 376771 | 66503 | | 334965 | 0420 | | 97 | 957921 | | | 14 |
| ı | | 24 | | 62350 | | 376498 | 66536 66569 | | 334634 334303 | 0421 | | 97 | 957863 957804 | | | 10 36 |
| ı | | 28 | | 62377 | | 376226 | | 9 552 | 333971 | 0422 | 254 | 98 | 957746 | | | 32 |
| ı | | 32 | | 624047 | | 375953 | | 0 551 | 333640 | 0423 | 313 | 98 | 957687 | | | 28 |
| ı | | 36 | | 624319 | | 375681 | | 1 551 | 333309 | 0423 | | | 957628 | | | 24 |
| ı | | 44 | | 62459 624863 | | 375409 375137 | | | 332979 | 0424 0424 | | | 957570 957511 | 5 | | 0 |
| 1 | | 48 | | 62513 | | 374865 | | 2 550 | 332648 332318 | 0424 | | | 957452 | 3 | | 6 |
| 1 | | 52 | 58 | 62540 | 6 452 | 374594 | | 3 550 | 331987 | 0426 | 07 | 98 | 957393 | 2 | 1 | 8 |
| 1 | 10 | 56 | | 625677 | | 374323 | | 3 550 | 331657 | 0426 | | | 957335 | 1 | | 4 |
| I. | 10 | - | 6(| 625948 | 451 | 374052 | | 2 550 | 331328 | 0427 | | 98 | 957276 | 0 2 | - | 0 |
| 1 | n. | 8. | 1 | Cosine. | | Secant. | Cotang. | | Tang. | Cosec | _ | | Sine. | ' I | n. | s. |
| 1 | | | - | 4 H | ours, | 1 60 | | - or | | | | | grees. | | | |
| 1 | | P. 1 | | 2 | 15" 30 | 139 | 1s 2 | - 15" 30 | 84 | 18 | 30 | 5" | 14 29 | P. | P. to | 5 |
| 1 | 8 | or ' | | 3 | 45 | 208 | 3 | 45 | 251 | 2 3 | 48 | | 43 | S | or " | 1 |

| F | _ | - | | | - | and | l Sec | ohta | | m. | BLE V. | _ | - | 10 |
|----|----------|----------|------------------|------------|------------------|------------------|--------------|------------------|------------------|-----|------------------|----|-------|-----|
| - | | | 1 Ho | . LUT | | and | | alits. | 9 | | grees. | | 4 | 13 |
| m. | S | 1/ | Sine. | D. | Cosec. | Tang. | or D. | Cotang. | Secant. | D. | | 1 | m. | S |
| 40 | | = | 9.625948 | 451 | 10.374052 | 9.668673 | - | 10.331327 | 10.042724 | _ | 9.957276 | _ | - | (|
| 40 | 4 | | | | 373781 | 669002 | | 330998 | 042783 | - | | | 20 | 56 |
| в | 8 | 2 | 626490 | | 373510 | | 1 | 330668 | 042842 | 98 | | | ж. | 5% |
| п | 12 | | | | 373240 | | | 330339 | 042901 | .98 | | | 4 | 48 |
| 16 | 16 | | | 450 | 372970 372700 | | | 330009 329680 | 042960 043019 | | | | 100 | 44 |
| Е | 24 | | | 449 | 372430 | | | 329351 | 043079 | | | | | 36 |
| H | 28 | 7 | 627840 | 449 | 372160 | | | 329023 | 043138 | | | | 11 | 39 |
| п | 32 | | 628109 | 449 | 371891 | 671306 | | 328694 | 043197 | 99 | | | 2 | 28 |
| Е | 36 40 | | 628378 628647 | 448 | 371622 371353 | | | 328366 328037 | 043256 043316 | | | | | 24 |
| 1: | 44 | | 628916 | 447 | 371084 | | | 327709 | 043375 | | | | 100 | 16 |
| 1 | 48 | | 629185 | 447 | 370815 | 672619 | | 327381 | 043434 | | | | | 12 |
| П | 52 | | | 447 | 370547 | 672947 | | 327053 | 043494 | | | | | 8 |
| - | - | 14 | 629721 | 446 | 370279 | 673274 | - | 326726 | 043553 | 1 | | - | - | -4 |
| 41 | 0 | - | 9.629989 | 446 446 | 10.370011 | 9.673602 | | | 10.043613 | | | | 19 | 56 |
| | | 16 | 630257 630524 | 446 | 369743 369476 | | | 326071 325743 | 043673 043732 | | | | | 5% |
| - | 12 | 18 | 630792 | | 369208 | | | 325416 | 043792 | | | | 7 | 48 |
| - | 16 | 19 | 631059 | 445 | 368941 | 674910 | 1000 | 325090 | 043852 | 100 | 956148 | | Q. | 4.4 |
| Е | 20 | 20 | 631326 | 444 | 368674 | | | 324763 | | | | | | 40 |
| E | | 21 | 631593 631859 | 444 | 368407 368141 | 675564 675890 | | 324436 324110 | 043971 044031 | | | | | 36 |
| Н | | 23 | 632125 | 444 | 367875 | 676217 | | 323783 | | | | | | 28 |
| Е | | 24 | 632392 | 443 | 367608 | | | 323457 | 044151 | | | | - | 24 |
| E | | 25 | 632658 | 443 | 367342 | 676869 | | 323131 | 044211 | | | | | 20 |
| 1 | | 26 | 632923 633189 | 443 | 367077 366811 | 677194 677520 | | 322806 322480 | 044271 044331 | | | | | 10 |
| г | | 28 | 633454 | 442 | 366546 | 677846 | | 322154 | 044391 | | | | | 8 |
| | 56 | 29 | 633719 | 442 | 366281 | 678171 | | 321829 | 044452 | | | | | 4 |
| 42 | | | 9.633984 | 441 | 10.366016 | 9.678496 | 542 | | 10.044512 | | | | 18 | (|
| Е | | 31 | 634249 | 441 | 365751 | 678821 | | 321179 | | | | | | 56 |
| | | 32 | 634514 634778 | 440 | 365186 365222 | | | 320854 320529 | 044632 044693 | | | | 5.1 | 48 |
| 10 | | 34 | 635042 | 440 | 364958 | | | 320205 | | | | | 5.7 | 44 |
| - | 20 | 35 | 635306 | 439 | 364694 | | | 319880 | | | 955186 | | 10. | 40 |
| | | 36 | 635570 | 439 | 364430 | | | 319556 | 044874 | | | | M.K. | 36 |
| L | | 37 38 | 635834 636097 | 439 | 364166 363903 | 680768 681092 | 1 . | 319232 318908 | 044935 044995 | | 955065 955005 | | - | 32 |
| | | 39 | 636360 | 438 | 363640 | | | 318584 | 045056 | | 954944 | | | 24 |
| | | 40 | 636623 | 438 | 363377 | 681740 | | 318260 | 045117 | | 954883 | | 36 | 20 |
| 17 | | 41 | 636886 | | 363114 | 682063 | | 317937 | 045177 | | 954823 | | 40 | 16 |
| | | 42 | 637148 | 437 | 362852 362589 | 682387 | | 317613 317290 | 045238 045299 | | 954762 954701 | | 22 | 12 |
| н | | 44 | 637673 | 437 | 362327 | 682710 683033 | | 316967 | 045360 | | 954640 | | 100 | 4 |
| 43 | | | 9.637935 | 436 | 10.362065 | | and the same | 10.316644 | | | | - | 17 | (|
| 1 | 4 | 46 | | 436 | 361803 | 683679 | 538 | 316321 | 045482 | | 954518 | 14 | 6 | 56 |
| | 8 | | 638458 | 436 | 361542 | | | 315999 | 045543 | | 954457 | | | 52 |
| | | 48 | 638720 638981 | 435 | 361280 361019 | | | 315676 315354 | 045604 | | 954396 954335 | | | 48 |
| | | 50 | | 404 | 360758 | 684646 684968 | | 315032 | 045665 045726 | | | | | 40 |
| 1 | 24 | 51 | 639503 | 434 | 360497 | 685290 | | 314710 | 045787 | 102 | 954213 | 9 | | 36 |
| | 28 | 52 | 639764 | | 360236 | | | 314388 | 045848 | | | | | 32 |
| - | 32 | 53 54 | 640024 640284 | | 359976 359716 | | | 314066 313745 | | | | | | 28 |
| | | 55 | | | 359456 | | | 313423 | | | | | | 20 |
| 11 | 44 | 56 | 640804 | 433 | 359196 | | | 313102 | 046094 | 102 | 953906 | 4 | | 16 |
| - | | 57 | | | 358936 | 687219 | 535 | 312781 | 046155 | | | | - | 12 |
| 1 | | 58 | | | 358676 358417 | | | 312460 312139 | 046217 046278 | | | | | 8 |
| 44 | | 60 | | | 358158 | | | 311818 | 046340 | | | | 16 | 0 |
| m. | | = | | | | | == | | Cosec. | = | | - | | |
| - | 5. | 1 | Cosine. | Tre | Secant. | Cotang. | or | Tang. | | Do | Sine. | | m. | 8. |
| - | - | | 18 | 15" | 1 66 | 18 | 15" | 81 | _ | 5" | 15 i | | - | - |
| | P. | | 2 | 30 | 132 | 2 | 30 | 163 | 2 3 | 30 | 30 | | P. or | |
| L | OI. | | 3 - | 45 | 199 | 3 | 45 | 244 | 3 4 | 5 | 45 | 8 | UL | |

| - | | | | | | | | | | | _ | - | | - | _ | - |
|------|------|----|----------|--------------------|------|---------------------|---------|--------|------------------|---------------|------------|-----|--------------------|----|------|----------|
| Г | 44 | | | TABL | E V. | Lo | garithm | ic Sin | es, Tangen | its, | | | | | | |
| | | | | 1 H | our, | | | or | | | | _ | grees. | | | |
| m | | s. | _' | Sine. | D. | Cosec. | Tang. | D. | Cotang. | Secan | t. | D. | Cosine. | 4 | m. | 8. |
| 4 | 1 | 0 | 0 | 9.64184 | | 10.358158 | | | 10.311818 | | | | | | 16 | 0 |
| в | | 4 | 1 | 642101 | | 357899 | | | 311498 | | 401 | | | | | 56 |
| | ١., | 8 | 2 | 642360 642618 | | 357640 357382 | | | 311177 310857 | | 463 525 | | 1 | | | 52 |
| Е | | 6 | 3 | 642877 | | 357123 | | | 310537 | | 587 | | | | 13 | 48 |
| 10 | | 20 | 5 | 643133 | | 356865 | | - | 310217 | | 648 | | | | | 40 |
| н | | 4 | 6 | 643393 | 430 | 356607 | 69010 | 3 533 | 309897 | | 710 | | | | Е | 36 |
| 10 | | 8 | 7 | 643650 | | 356350 | | | 309577 | | 772 | | | | - | 32 |
| | | 2 | 8 | 643908 | | 356092 | | | 309258 | | 834 | | | | 0 | 28 |
| Е | | 6 | 9 | 644165 | | 355835 355577 | | | 308938 308619 | | 896 958 | | | | 0.7 | 24 |
| | 4 | | 11 | 644680 | | 355320 | | | 308300 | | 020 | | | | | 16 |
| | 4 | | 12 | 644936 | | 355064 | | | 307981 | | 082 | | | | | 12 |
| 1 | | | 13 | 645193 | | 354807 | | | 307662 | | 145 | | | | | 8 |
| Ŀ | - | | 14 | 645450 | | 354550 | | | 307344 | | 207 | - | 952793 | | - | 4 |
| 4.5 | | | | 9.645706 | | 10.354294 | | | 10.307025 | | | | | | 15 | 0 |
| | | | 16 17 | 645963 | | 354038 353782 | | | 306707 306388 | | 331 | | | | | 56 |
| Е | | | 18 | 646474 | | 353526 | | | 306070 | | 394 456 | | | | 7 | 52 48 |
| 10 | | | 19 | 646729 | | 353271 | 69424 | | 305752 | | 519 | | | 11 | - | 44 |
| 5 | 2 | | 20 | 646984 | 425 | 353016 | 69456 | | 305434 | | 581 | | | | | 4.0 |
| 10 | | | 21 | 647240 | | 352760 | | | 305117 | | 644 | | | | | 36 |
| г | | | 22 | 647494 | 1 | 352506 | | 1 | 304799 | | 706 | | | | | 32 |
| н | | | 23 24 | 647749 | | 352251 351996 | | | 304482 304164 | 047 | 769 | | | | 1 | 28 |
| Е | | | 25 | 648258 | | 351742 | | | 303847 | | 894 | | 952106 | | | 20 |
| 93 | | | 26 | 648512 | | 351488 | | | 303530 | | 957 | | 952043 | | 15, | 16 |
| 10.2 | 4 | | 27 | 648766 | | 351234 | | | 303213 | 048 | 020 | 105 | 951980 | 33 | | 12 |
| 15 | | | 28 | 649020 | | 350980 | | | 302897 | | 083 | | 951917 | | 17, | 8 |
| 1 | - | 1. | 29 | 649274 | - | 350726 | 1 | _ | 302580 | | 146 | | 951854 | | | 4 |
| 46 | | | 30 31 | 9.649527 649781 | | 10.350473 350219 | | | 10.302264 | | | | | | 14 | :0 |
| | | | 32 | 650034 | 1 | 349966 | | | 301947 301631 | | 272 335 | | 951728 951665 | | | 56 52 |
| | | | 33 | 650287 | | 349713 | | | 301315 | | 398 | | | | | 48 |
| 7 | | | 34 | 650539 | 421 | 349461 | 69900 | - 1 | 300999 | | 461 | | 951539 | | 1 | 44 |
| 115 | | | 35 | 650792 | | 349208 | | | 300684 | | 524 | | | | 31 | 40 |
| | | | 36 | 651044 | | 348956 | | | 300368 | | 588 | | 951412 | | ė, | 36 |
| | 3 | | 37 38 | 651297 | | 348703 348451 | | | 300053 299737 | | | | 951349 951286 | | -1 | 32 |
| 1 | | | 39 | 651800 | | 348200 | | | 299429 | | 714 | | 951222 | | | 24 |
| 19 | 4 | 0 | 40 | 652058 | 419 | 347948 | | | 299107 | | 841 | | 951159 | | 84 | 20 |
| 1 | 4 | | 41 | 652304 | | 347696 | | | 298792 | 048 | 904 | 106 | 951096 | | h h | 16 |
| 1 | | | 42 | 652555 | | 347445 | 70152 | | 298477 | 048 | | | 951032 | | 12 | 12 |
| ш | | | 43 44 | 652806 653057 | | 347194 346943 | 70183 | | 298163 297848 | 049 | | | 950968 | | Co | 8 |
| 47 | - | | 4.5 | 9.653308 | - | 10.346692 | | _ | | - | 095 | | 950905 9.950841 | 15 | 10 | 0 |
| 1 | | | 46 | 653558 | 1 | 346442 | | | 297220 | 10.049 049 | | | | _ | 13 | 56 |
| | | | 47 | 653808 | | 346194 | 70309 | | 296905 | 049 | | | | | | 52 |
| 1 | 1 | 2 | 48 | 654059 | 417 | 345941 | 70340 | 9 523 | 296591 | 049 | | | 950650 | 12 | 1) | 48 |
| 1 | | | 49 | 654309 | | 345691 | 70372 | | 296277 | 049 | | | 950586 | | | 44 |
| | | | 50 51 | 654558 654808 | | 345442 | | | 295964 | | 178 | | 950522 | | | 40 |
| | | | 52 | 655059 | | 345192 344942 | | | 295650 295337 | | | | 950458 950391 | | | 36 |
| В | | | 53 | 655307 | | 344693 | | | 295023 | | | | 950330 | | | 28 |
| | 3 | 6 | 54 | | | 344444 | | | 294710 | 049 | | | 950266 | | 11 1 | 21 |
| | | | 55 | 655805 | | 344195 | 705603 | 3 521 | 294397 | 049 | 798 | 107 | 950202 | 5 | | 20 |
| | | | 56 57 | | | 343946 | | | 294084 | 049 | | | 950138 | | | 16 |
| | | | 58 | 656302 656551 | | 343698 343449 | | | 293772 | 049 | | | 950074 | | | 12 |
| | | | 59 | | | 343449 | 70654 | | 293459 293146 | | | | 950010 949945 | | | 4 |
| 48 | 3 (| 0 | 60 | 657047 | | 342953 | | | 292834 | 050 | | | 949881 | | 12 | 0 |
| m. | | 3. | 7 | Cosine. | | Secant. | Cotang. | | Tang. | Cosec | | | Sine. | - | m. | 5. |
| - | | | - | 4 Hc | urs. | CCCATTE | Cotang. | or | rong. | Cusec | | Dec | grees. | | -20 | |
| P | . P. | | 1 | 18 | 15" | 63 | 15 | 15" | 1 79 | 18 | | 5" | 16 | - | - | |
| | 5 OI | | | 2 | 30 | 127 | 2 | 30 | 158 | 2 | | 0 | 31 | | P. | |
| 1_ | | | | 3 | 4.5 | 190 | 3- | 4.5 | 238 | 3 . | 4 | 5 | 47 | 3 | or | 1 |

| TABLE V. | 1 60 12 66 59 56 59 58 55 8 57 44 54 54 54 56 9 53 33 56 44 55 9 53 33 56 45 56 9 55 60 9 51 55 50 9 10 55 48 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 |
|--|--|
| 48 0 0 0 9.657047 413 10.342953 9.707166 520 10 292834 10.050119 107 9.91908 4 1 657295 413 342705 707478 520 292522 050184 107 94981 8 9 657542 412 342458 707790 520 292210 050248 107 94973 12 3 657790 412 342210 708102 520 291898 050312 108 94962 16 4 658037 412 341963 708414 519 291586 050377 108 94962 20 5 658284 412 341716 708726 519 291274 050442 108 94952 21 6 658531 411 341469 709037 519 290963 050506 108 94942 28 7 658778 411 341222 709349 519 290651 050571 108 94942 32 8 659025 411 340975 709660 519 290340 050636 108 94942 32 8 659025 411 340975 709660 519 290340 050636 108 94943 36 9 659271 410 340483 710232 518 289718 050765 108 94932 44 11 659763 410 340237 710593 518 289407 050830 108 94914 48 12 660009 409 339991 710904 518 289006 050895 108 94914 48 12 660009 409 339991 710904 518 289096 050895 108 94914 52 13 660255 409 339745 711215 518 288785 050960 108 94904 56 14 660501 409 339499 711525 517 288475 051025 108 94893 416 660991 408 339009 712146 517 287854 051125 108 94889 12 18 661481 408 338764 712456 517 287854 051125 108 94878 12 18 661481 408 338764 712456 517 287854 051125 109 94878 12 18 661481 408 338764 712456 517 287854 051125 109 94878 12 18 661481 408 338764 712456 517 287854 051125 109 94878 12 18 661481 408 338764 712456 517 287854 051125 109 94878 12 18 661481 408 338764 712456 517 287854 051125 109 94878 12 18 661481 408 338764 712456 517 287854 051125 109 94878 12 18 661481 408 338764 712456 517 287854 051125 109 94878 12 18 661481 408 338764 712456 517 287854 051125 109 94878 12 18 661481 408 338764 712456 517 287854 051125 109 94878 12 18 661481 408 338764 712456 517 287854 051125 109 94878 12 18 661481 408 338764 712456 517 287854 051125 109 94878 12 18 661481 408 338519 712766 516 287234 051255 109 94878 12 18 661481 408 338519 712766 516 287234 051255 109 94878 12 18 661481 408 338519 712766 516 287234 051255 109 94878 12 18 661481 408 338519 712766 516 287234 051255 109 94878 12 18 661481 408 338519 712766 516 287234 051255 109 94878 12 18 661481 408 338519 712766 516 2 | 1 60 12 66 59 56 59 58 55 8 57 44 54 54 54 56 9 53 33 56 44 55 9 53 33 56 45 56 9 55 60 9 51 55 50 9 10 55 48 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 |
| 4 | 6 59 5 5 4 5 8 5 5 4 4 5 4 3 9 5 3 3 3 4 5 2 2 9 5 1 2 5 5 5 0 4 9 1 1 5 5 4 5 1 1 5 5 4 4 5 1 4 5 5 1 4 5 5 4 5 1 5 5 4 5 1 5 5 4 5 1 5 5 4 5 1 5 5 4 5 1 5 5 4 5 1 5 5 4 5 1 5 5 4 5 1 5 5 4 5 1 5 5 4 5 1 5 5 4 5 1 5 5 4 5 1 5 5 4 5 1 5 5 4 5 1 5 5 4 5 5 1 5 5 4 5 1 5 5 4 5 1 5 5 4 5 1 5 5 4 5 1 5 5 4 5 1 5 5 4 5 1 5 5 4 5 1 5 5 4 5 1 5 5 4 5 1 5 5 4 5 1 5 5 4 5 1 5 5 4 5 1 5 5 4 5 1 5 1 |
| 8 | 2 58 5 5 4 4 5 3 5 5 4 5 2 2 5 6 5 6 0 1 5 1 2 5 5 6 0 1 7 5 5 6 6 1 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 |
| 12 3 657790 412 342210 708102 520 291898 050312 108 94968 16 4 658037 412 341963 708414 519 291586 050377 108 94968 20 5 658284 412 341716 708726 519 291274 050442 108 94952 21 6 658531 411 341469 709037 519 290963 050506 108 94948 28 7 655778 411 340775 709660 519 290340 050636 108 94948 36 9 659271 410 340729 709971 518 290029 050700 108 94936 40 10 659517 410 340483 710282 518 289718 050760 108 94936 44 11 659517 410 340337 710593 518 289407 | 8 57 4 4 5 4 4 4 5 4 5 11 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 |
| 16 4 658037 412 341963 708414 519 291586 050377 108 94962 20 5 658284 412 341716 708726 519 291274 050442 108 94962 21 6 658531 411 341469 709037 519 290963 050506 108 94942 28 7 655778 411 341222 709349 519 290651 0505711 108 94942 32 8 659025 411 340729 709600 519 290340 050636 108 94943 36 9 659271 410 340729 709971 518 290029 050700 108 94936 40 10 659517 410 340483 710292 518 289718 050765108 94924 44 11 659763 410 340237 710593 518 289407 050830 | 3 56 4 55 44 54 39 53 3 3 45 22 45 22 0 51 2 2 0 51 2 5 50 0 49 11 5 48 1 0 0 45 11 6 5 44 50 43 5 5 |
| 21 6 658531 411 341469 709037 519 290963 050506 108 94948 28 7 658778 411 341292 709349 519 290651 050571 108 94948 36 9 659251 410 340729 709971 518 290029 050700 108 94936 40 10 659517 410 340483 710232 518 289718 050765 108 94923 44 11 659763 410 340237 710593 518 289718 050765 108 94923 48 12 660099 33991 710904 518 289407 050830 108 94910 52 13 660255 409 339745 711215 518 288785 050960 108 94904 49 0 159.660746 409 339499 711525 517 288475 051025 | 4 54 3 9 53 3 4 52 2 50 51 2 50 20 0 49 1 5 5 48 1 0 45 11 6 5 44 50 0 43 5 5 |
| $\begin{array}{c ccccccccccccccccccccccccccccccccccc$ | 9 53 3 4 52 2: 0 51 2 5 50 20 49 1 5 48 0 17 5 46 0 45 11 6 5 44 50 43 5: |
| 32 8 659025 411 340975 709660 519 290340 050636 108 94936 36 9 659271 410 340729 709971 518 290029 050700 108 94936 40 10 659517 410 340483 710282 518 289718 050765 108 94923 44 11 659763 410 340237 710593 518 289407 050830 108 94917 48 12 660009 409 33991 710904 518 289096 050893 108 94910 52 13 660255 409 339745 711215 518 288785 050960 108 94904 56 14 660501 409 339254 9.711825 517 288475 051025 108 94897 49 0 15 9.660746 409 10.339254 9.711836 517 | 4 52 2:051 2:550 2:00 49 1:55 48 1:00 47 5:55 46 2:00 43 5:55 44 5:00 43 5:55 45 11 0:05 43 5:55 45 11 0:05 45 |
| 40 10 659517 410 340483 710282 518 289718 050765 108 94923 44 11 659763 410 340237 710593 518 289407 050830 108 94917 48 12 660009 409 339991 710904 518 289096 050895 108 94917 52 13 660255 409 339745 711215 518 288785 050960 108 94904 56 14 660501 409 339499 711525 517 288475 051025 108 94894 49 15.9.660746 409 10.339254 9.711836 517 10.288161 10.051090 108 9.4894 4 16 660991 408 339009 712146 517 287854 051155 108 9.4884 8 17 661236 408 338519 712766 516 287234 051250 109 94871 12 18 661 | 5 50 20 0 49 10 5 48 1 5 46 6 0 45 11 0 5 44 50 0 43 5 |
| 44 11 659763 410 340237 710593 518 289407 050830 108 94917 48 12 660009 409 339991 710904 518 289096 050895 108 94910 52 13 660255 409 339745 711215 518 288785 050960 108 94907 56 14 660501 409 339499 711525 517 288475 051025 108 94897 49 0 15 960746 409 10.339254 9.711836 517 10.288164 10.051090 108 9.94891 416 660991 408 339009 712146 517 287854 051155 108 94884 817 661286 408 338764 712456 517 287544 051250 109 94878 12 18 661481 408 338519 712766 516 287234 051255 109 94878 12 18 661481 408 338519 712766 516 287234 051255 109 94878 12 18 661481 408 338519 712766 516 287234 051255 109 94878 12 18 661481 408 338519 712766 516 287234 051255 109 94878 12 18 661481 408 338519 712766 516 287234 051255 109 94878 12 12 12 12 12 12 12 1 | 0 49 10 5 48 11 0 17 5 46 6 0 45 11 6 5 44 5 0 43 5 |
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$ | 5 48 1 0 17 5 5 46 6 0 45 11 6 5 44 5 0 43 5 |
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$ | 5 46 0 45 11 0 5 44 5 0 43 5 5 |
| 49 0 15.9.660746 409 10.339254 9.711836 517 10.288164 10.051090 108 9.94891 4 16 660991 408 339009 712146 517 287854 051155 108 94884 8 17 661236 408 338764 712456 517 287544 051220 109 94878 12 18 661481 408 338519 712766 516 287234 051285 109 94871 | 0 45 11 6 5 44 5 0 43 5 |
| 4 16 660991 408 339009 712146 517 287854 051155 108 94884 8 17 661236 408 338764 712456 517 287544 051220 109 94878 12 18 661481 408 338519 712766 516 287234 051285 109 94871 | 5 44 50 0 43 5 |
| 8 17 661236 408 338764 712456 517 287544 051220 109 94878 12 18 661481 408 338519 712766 516 287234 051285 109 94871 | 0 43 5 |
| 12 18 661481 403 338519 712766 516 287234 051285 109 94871 | |
| 16 19 661726 407 338274 713076 516 286924 051350 109 94865 | |
| 20 20 661970 407 338030 713386 516 286614 051416 109 94858 | |
| 20 20 661970 407 338030 713386 516 286614 051416 109 94858 24 21 662214 407 337786 713696 516 286304 051481 109 94851 | |
| 28 22 662459 407 337541 714005 516 285995 051546 109 94845 | |
| 32 23 662703 406 337297 714314 515 285686 051612 109 94938 | |
| 36 24 662946 406 337054 714624 515 285376 051677 109 94832 40 25 663190 406 336810 714933 515 285067 051743 109 94825 | |
| 40 25 663190 406 336810 714933 515 285067 051743 109 94825 44 26 663433 405 336567 715242 515 284758 051808 109 94819 | |
| 48 27 663677 405 336323 715551 514 284449 051874 109 94812 | 6 33 |
| 52 28 663920 405 336080 715860 514 284140 051940 109 94806 | |
| 56 29 664163 405 335837 716168 514 283832 052005 110 94799 | |
| 50 030,9.664406 404 10.335594 9.716477 514 10.283523 10.052071 110 9.94792 431 664648 404 335352 716785 514 283215 052137 110 94786 | |
| 8 32 664891 404 335109 717093 513 282907 052203 110 94779 | |
| 12 33 665133 403 334867 717401 513 282599 052269 110 94773 | 1 27 48 |
| 16 34 665375 403 334625 717709 513 282291 052335 110 94766 | |
| 20 35 665617 403 334383 718017 513 281983 052400 110 94760 24 36 665859 402 334141 718325 513 281675 052467 110 94753 | |
| 28 37 666100 402 333900 718633 512 281367 052533 110 94746 | 7 23 3 |
| 32 38 666342 402 333658 718940 512 281060 052599 110 94740 | |
| 36 39 666583 402 333417 719248 512 280752 052665 110 94733 40 40 666824 401 333176 719555 512 280445 052731 110 94726 | |
| 41 41 667065 401 332935 719862 512 280138 052797 110 94720 | |
| 48 42 667305 401 332695 720169 511 279831 052864 111 94713 | 6 18 19 |
| 52 43 667546 401 332454 720476 511 279524 052930 111 94707 | |
| 56 44 667786 400 332214 720783 511 279217 052996 111 94700 51 045 9.668027 400 10.331973 9.721089 511 10.27891110.053063 111 9.94693 | |
| 51 0 45 9.668027 400 10.331973 9.721089 511 10.278911 10.053063 111 9.94693 446 668267 400 331733 721396 511 278604 053129 111 94687 | |
| 8 47 668506 399 331494 721702 510 278298 053196 111 94680 | 4 13 52 |
| 12 48 668746 399 331254 722009 510 277991 053262 111 94673 16 49 668986 399 331014 722315 510 277685 053329 111 94667 | |
| 16 49 668986 399 331014 722315 510 277685 053329 111 94667 20 50 669225 399 330775 722621 510 277379 053396 111 94660 | |
| 24 51 669464 398 330536 722927 510 277073 053462 111 94653 | |
| 28 52 669703 398 330297 723232 509 276768 053529 111 94647 | |
| 32 53 669942 398 330058 723538 509 276462 053596 111 94640 36 54 670181 397 329819 723844 509 276156 053663 111 94633 | |
| 36 54 670181 397 329819 723844 509 276156 053663 111 94633 40 55 670419 397 329581 724149 509 275851 053730 112 94627 | |
| 44 56 670658 397 329342 724454 509 275546 053797 112 94620 | 3 4 16 |
| 48 57 670896 397 329104 724759 508 275241 053864 112 94613 | |
| 52 58 671134 396 328866 725065 508 274935 053931 112 94606 56 59 671372 396 328628 725369 508 274631 053998 112 94600 | |
| 52 0 60 671609 396 328391 725674 508 274326 054065 112 94593 | |
| m. s. / Cosine. Secant. Cotang. Tang. Cosec. Sine. | ′ m. s |
| 4 Hours, or 62 Degrees. | ,111. 5 |
| P.P. to 18 15" 61 15 15" 77 18 15" 16 | ID DE |
| s or " 2 30 121 2 30 151 2 30 33 | P. P. to s or " |
| 3 45 182 3 45 231 3 45 49 | |

| 4 | 6 | | TABLE | v. | Lo | garithmic | Sine | s, Tangen | ts, | | - 1 | | |
|------|----------|----------|--------------------|------------|------------------|------------------|------------|------------------|------------------|-----|--|----|----------|
| | | | 1 Ho | | | | or | | | | grees. | | |
| m. | 8 | Ľ | Sine. | D. | Cosec | Tang. | D. | Cotang. | Secant. | D. | Cosine. | 1 | m. s |
| 52 | 0 | | 9.671609 | | 10.328391 | | 508 | | 10.054065 | | | | 8 (|
| | 4 | | 671847 | | 328153 327916 | | | 274021 273716 | 054132 | | | | 56 |
| П | 12 | | | 395 395 | 327679 | | | 273412 | 054200 054267 | | | | 59 48 |
| | 16 | | | | 327442 | 726892 | | 273108 | | | | | 4 |
| п | 20 | | | | 327205 | | | 272803 | | | 1 | | 4 |
| | 24 | 6 | 673032 | | 326968 | | | 272499 | 054469 | 112 | 945531 | 54 | 3 |
| E | 28 | 7 | 673268 | | 326732 | | | 272195 | 054536 | | | | . 3 |
| | 32 36 | 8 9 | 673505 | | 326495 | | | 271891 | 054604 | | | | 2 |
| | 40 | 10 | 673741 673977 | 393 393 | 326259 326023 | | | 271588 271284 | 054672 054739 | | | | 20 |
| 1 | 44 | | 674213 | | 325787 | 729020 | | 270980 | | | | | 1 |
| | 48 | | .674448 | | 325552 | | | 270677 | 054875 | | | | 1 |
| | 52 | | 674684 | | 325316 | 729626 | | 270374 | 054942 | 113 | 945058 | 47 | |
| | 56 | | 674919 | | 325081 | 729929 | | 270071 | 055010 | 113 | 944990 | 46 | 11111 |
| 53 | | | 9.675155 | 392 | 10.324845 | | | | 10.055078 | | | | 7 |
| | 4 | 16 17 | 675390 | | 324610 | | | 269465 | | | | | 5 |
| 1 | 12 | | 675624 675859 | | 324376 324141 | | | 269162 268859 | | | | | 5 |
| | 16 | | 676094 | | 323906 | | | 268556 | | | | | 4 |
| | 20 | | 676328 | | 323672 | | | 268254 | | | | | 4 |
| | 24 | | 676562 | | 323438 | 732048 | 504 | 267952 | 055486 | 114 | 944514 | 39 | 3 |
| | 28 | | 676796 | | 323204 | | | 267649 | | | | | 3 |
| M | 32 36 | | 677030 | | 322970 | | | 267347 | 055623 | | | | 2 |
| | 40 | | 677264 677498 | | 322736 322502 | | | 267045 266743 | | | | 1 | 2 |
| 111 | 44 | اعلط | 677731 | | 322269 | | | 266442 | | | | | 1 |
| | 48 | | 677964 | | 322036 | | | 266140 | 055896 | | | 2 | 1 |
| | 52 | | 678197 | | 321803 | | | 265838 | 055964 | | | 32 | 1 |
| | 56 | - | 678430 | | 321570 | 734463 | 502 | 265537 | 056033 | 114 | 943967 | 31 | 4 |
| 54 | | | 9.678663 | | 10.321337 | | | | 10.056101 | | | | 6 |
| | | 31 32 | 678895 | | 321105 | | | 264934 | | | | | 50 |
| 10 | 12 | | 679128 679360 | | 320872 320640 | | | 264633 264332 | 056239 056307 | | | | 5: 4: |
| D. | 16 | | 679592 | | 320408 | 735969 | | 264031 | 056376 | | | | 4. |
| н | 20 | 35 | 679824 | | 320176 | | | 263731 | 056445 | | | | 40 |
| 2 | 24 | | 680056 | | 319944 | 736570 | | 263430 | 056514 | | | | 3 |
| 83 | 28 32 | | 680288 | | 319712 | 736871 | 501 | 263129 | 056583 | | | | 39 |
| R | 36 | | 680519 680750 | | 319481 319250 | 737171 | 500 | 262829 | 056652 | | | | 21 |
| 100 | 40 | | 680982 | | 319018 | | 500 | 262529 262229 | 056721 056790 | | | | 20 |
| 2 | 44 | | 681213 | | 318787 | 738071 | 500 | 261929 | 056859 | | | | 10 |
| 11 | 48 | | 681443 | | 318557 | 738371 | 500 | 261629 | 056928 | | | | 12 |
| 1 | 52 | | 681674 | | 318326 | 738671 | 499 | 261329 | 056997 | | | | 11 8 |
| F.F. | 56 | _ | 681905 | | 318095 | 738971 | 499 | 261029 | 057066 | | 942934 | - | 4 |
| 55 | | 45 | 9.682135 682365 | | 10.317865 | | 499 | 10.260729 | | | | | 5 . |
| | | 47 | 682595 | | 317635 317405 | 739570 739870 | | 260430 260130 | 057205 057274 | | | | 52 |
| и | 12 | | 682825 | | 317175 | 740169 | 499 | 259831 | 057344 | | | | 4.8 |
| | 16 | | 683055 | 383 | 316945 | 740468 | | 259532 | 057413 | | | | 44 |
| - | 20 | | 683284 | | 316716 | 740767 | 498 | 259233 | 057483 | 116 | 942517 | 10 | 4.0 |
| в | 24 28 | | 683514 | | 316486 | | | 258934 | 057552 | 116 | 942448 | 9 | 36 |
| | 32 | 53 | 683743 683972 | | 316257 316028 | 741365 | | 258635 | | | | | 32 |
| | 36 | | | | 315799 | | | 258336 258038 | 057692 057761 | | | 6 | 28 |
| | 40 | | | | 315570 | | | 257739 | 057831 | | | | 20 |
| - | 44 | 56 | 684658 | 381 | 315342 | 742559 | 497 | 257441 | 057901 | | 942099 | | 16 |
| | 48 | 57 | | | 315113 | 742858 | 497 | 257142 | 057971 | 116 | 942029 | 3 | 12 |
| | 52 56 | | | | 314885 | | | 256844 | 058041 | | 941959 | | 8 |
| 56 | | 60 | | 380 | 314657 314429 | 743454 743752 | | 256546 | 058111 | | 941889 | | 4 |
| | = | = | | === | | | 490 | 256248 | 058181 | 117 | 941819 | | 4 .0 |
| m. | S. | | Cosine. | | Secant. | Cotang. | | Tang. | Cosec. | | Sine. | 1 | m. s. |
| | _ | | 4 Ho | 15" | 1 60 | 10 1 | or 1.5% | | | | grees. | | |
| | P. | | 2 | 30 | 58 116 | 18 | 15" 30 | 75 151 | | 5" | 17 34 | | P. to |
| 5 | or | | 3 | 45 | 175 | 3 | 45 | 226 | | 5 | 51 | 8 | or " |
| - | | - | - | The Parks | - | | | | | | and the same of th | | |

| | | | | _ | | and | Sec | ints. | | TA | BLE V. | 7 | 4 | 7 |
|----|----------|-----------|--------------------|----------|---------------------------|------------------|----------|-------------------|------------------|----------|-------------------|-----|----|-----|
| | | - | 1 Ho | | Cassa | Tone | or | Compa (| | 9 De | grees. | 1/1 | | |
| m. | s. | -0 | Sine. 9.685571 | 380 | Cosec. | Tang. | D. 496 | Cotang. 10.256248 | Secant. | | 9.941819 | | m. | 5 |
| 30 | 4 | 100 | 685799 | _ | 314201 | 744050 | | 255950 | 058251 | | 941749 | | | 50 |
| E. | 8 | | 686027 | | 313973 313746 | 744348 | | 255652 | 058321 | | 941679 941609 | | | 53 |
| H. | 18 | | 686254 686482 | | 313518 | 744645 744943 | | 255355 255057 | 058391 058461 | | | | | 4. |
| | 20 | 5 | 686709 | | 313291 | 745240 | 495 | 254760 | 058531 | 117 | 941469 | | | 40 |
| -1 | 21 | | 686936 687163 | | 313064 312837 | 745538 745835 | | 254462 254165 | 058602 058672 | | | | | 36 |
| | 32 | 8 | 687389 | 378 | 312611 | 746132 | | 253868 | 058742 | | 941258 | 52 | | 28 |
| | 36 40 | | 687616 687843 | | 312384 3121 <i>5</i> 7 | 746429 746726 | | 253571 253274 | 058813 058883 | | | | | 24 |
| 23 | 44 | | 688069 | | 311931 | 747023 | | 252977 | 058954 | | The second second | | ŧ. | 16 |
| r | | 12 | 688295 | | 311705 | 747319 | | 252681 | 059025 | | | | H | 12 |
| | | 13 14 | 688521 688747 | | 311479 311253 | 747616 747913 | | 252384 252087 | 059095 059166 | | | | ĸ. | 4 |
| 57 | 0 | | - | | 10.311028 | | | | | | | - | 3 | . (|
| | | 16 | | 100 | 310802 | 748505 | | 251495 | 059307 | | | | | 56 |
| п | | 17 18 | 689423 689648 | | 310577 310352 | 748801 749097 | | 251199 250903 | 059378 059449 | | | | | 52 |
| | 16 | 19 | 689873 | 375 | 310127 | 749393 | 493 | 250607 | 059520 | 118 | 940480 | 41 | 1 | 44 |
| | | 20 | 690098 690323 | | 309902 309677 | 749689 749985 | | 250311 250015 | 059591 059662 | | - | | | 36 |
| 8 | | 22 | 690548 | | 309452 | 750281 | | 249719 | 059733 | | | | Ü | 32 |
| G | | 23 | | 1000 | 309228 | 750576 | | 249424 | 059804 | | | | | 28 |
| - | | 24 | 690996 | | 309004 308780 | 750872 751167 | | 249128 248833 | 059875 059946 | | | | 5 | 24 |
| 1 | 44 | 26 | 691444 | 373 | 308556 | 751462 | 492 | 248538 | 060018 | 119 | 939982 | 34 | bi | 1 |
| | | 27 | 691668 691892 | | 308332 308108 | 751757 752052 | | 248243 247948 | 060089 060160 | | | | | 15 |
| | | 29 | | | 307885 | | | 247653 | 060232 | | | | 4 | 4 |
| 58 | | | 9.692339 | | 10.307661 | | | | 10.060303 | | | | 2 | |
| | | 31 | | | 307438 307215 | | | 247063 246769 | | | | | | 56 |
| Ь | | 33 | | | 306992 | | - | 246474 | | | | | 1 | 48 |
| | | 34 | | | 306769 | | | 246180 | | | | | Ŀ | 44 |
| 1 | | 35 | | | 306547 306324 | | | 245885 245591 | 060661 060733 | | | | | 30 |
| | 28 | 37 | 693898 | 370 | 306102 | 754703 | 490 | 245297 | 060808 | 120 | 939195 | 23 | E | 3 |
| | | 39 | | | 305880 305658 | | | 245003 244709 | | | | | | 2 |
| | | 40 | | | 305436 | | | 244415 | | | | | | 2 |
| | | 41 | | | 305214 | | | 244122 | | | | | Ď. | 10 |
| | | 42 | | | 304993 304771 | 756172 756465 | | 243828 243535 | 061164 061237 | | | | 3. | 1 |
| _ | - | 44 | | | 304550 | | | 243241 | 061309 | | | 16 | | 4 |
| 59 | | 45 | 9.695671 695892 | | 10.304329 304108 | | | 1 | 10.061381 | | | | 1 | - (|
| | | 3 47 | | | 303887 | | | 242655 242362 | | | | | | 5 |
| | | 48 | | | 303666 | | 488 | 242069 | | | 938402 | 12 | 1 | 4.8 |
| | | 5 49 | | | 303446 | | | 241776 241483 | | | | | | 40 |
| | 24 | 51 | 696995 | 367 | 303005 | 758810 | 488 | 241190 | | | 938185 | 9 | | 30 |
| | | 52 53 | | | 302785 302565 | | | 240898 240605 | | | | 8 | | 35 |
| | | 54 | | | 302346 | | 487 | 240003 | | | | _ | | 28 |
| | | 55 | | | 302126 | 759979 | 487 | 240021 | 062103 | 121 | 937895 | | | 20 |
| | | 56 | | | 301906 301687 | | | 239728 239436 | | | | | | 10 |
| | 59 | 58 | 698532 | 365 | 301468 | 760856 | 486 | 239144 | 062324 | 121 | 937676 | 2 | 37 | 8 |
| 60 | | 5 5 5 6 (| | | 301249 | | | 238852 238561 | | | | | 0 | |
| m. | | | | 501 | Secant. | Cotang. | 700 | Tang. | Cosec. | == | Sine. | | | = |
| | | - | 4 Ho | urs, | Decane | Gotting. | or | 1 rang. | | O De | grees. | | m. | 8 |
| | | to | 15 | 15" | | 1s | 15" | | 18 | 15" | 18 | P. | P. | to |
| S | or | " | 3 | 30 45 | 111 | 2 3 | 30 45 | 147 221 | | 30 45 | 36 | | or | |
| - | | | | - | | | | | | | | | - | - |

| 1 48 | TA | BI.E | v. | Lo | garithr | nic Sir | nes, Tanger | nts, | | | | | | |
|-------------|------------------|------|------------|---------------------|--------------|------------------|---|-------|-----|------------|--------------------|------|--------------|----------|
| | | | urs, | |) m | or | | | | | grees. | | - | |
| m. s. | Sinc | | D. | Cosec. | Tang | | | | | D. | | - | = | S. |
| 0 0 | 0 9.698 | | 364 | 10.301030 300811 | | | | | | 121 | | | 60 | 56 |
| 8 | 2 699 | | | 300593 | | | | | | 122 | | | | 52 |
| 12 | | | 364 | 300374 | 1 | | | | | 122 | | | 4 | 48 |
| 16 20 | 4 6998 5 7000 | | 363 363 | 300156 | | | | | | 122 | | | U | 44 |
| 24 | 6 700 | | 363 | 299720 | | | | 062 | 908 | 122 | 937098 | | H | 36 |
| 28 | | | 363 | 299503 | | | | | | 122 | | | 0 | 32 |
| 32 | | | 363 362 | 299284 299067 | | | 1 54 5 5 5 5 5 5 | | | 122 | | | 10 | 24 |
| 40 | 10 7011 | 51 | 362 | 298849 | 7643 | 52 484 | 235648 | 063 | 201 | 122 | 936799 | 05.0 | 8 | 20 |
| 44 | | | 362 362 | 298633 298415 | | | | | | 122 | | | | 16 12 |
| 52 | | | 361 | 298198 | | | | | | 123 | | | 4 | 8 |
| 56 | | | 361 | 297981 | | | | | | 123 | | | - | 4 |
| 1 0 | | | | 10.297764 | | | | | | | | | 59 | - 0 |
| 8 | | | 361 | 297548 297331 | | | 10.00 | | | 123 123 | | | | 56 |
| 12 | | | 360 | 297115 | | | | | | 123 | | | F | 48 |
| - 16 | 19 7031 | 01 | 360 | 296899 | 7669 | 65 483 | 233035 | 063 | 864 | 123 | 936136 | 41 | | 44 |
| 20 5 | | | 360 | 296683 296467 | | | | | | 123 123 | | | et | 40 36 |
| 28 | | | | 296251 | | | | | | 123 | A Robert Marie Co. | | | 32 |
| 32 | 7039 | | 359 | 296036 | 7681 | 24 482 | 231876 | 064 | 160 | 123 | 935840 | | | 28 |
| 36 | | | 359 359 | 295821 | 7684 | | | | | 124 | 935766 | | | 24 |
| 40 | | | | 295605 295390 | | | A 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 | | | 124 | | | 1 | 16 |
| 48 | 7048 | 25 | 358 | 295175 | 7692 | 81 482 | And the second | 064 | 457 | 124 | 935543 | 33 | - | 12 |
| 52 | | | 358 | 294960 | | | | | | 124 | | | J. | 8 |
| 2 0.5 | 7052 309.7054 | | 358 | 294746 | 7698 | | 230140 | | - | 124 | 935395 | - | 54 | 4 |
| 4.5 | | | 357 | 294317 | 7704 | | 229563 | | | 124 | | | 23 | 56 |
| 8 5 | 7058 | 98 | 357 | 294102 | 7707 | | 229274 | 064 | 829 | 124 | 935171 | 28 | | 52 |
| 125 | | | | 293888 | | | 228985 | | | | 935097 | | 1 | 48 |
| 163 | | | 356 356 | 293674 293461 | 7713 | | 228697 228408 | | | 124 124 | 935022 934948 | | 9 | 44 |
| 243 | 36 7067 | | 356. | 293247 | 7718 | 80 480 | The second second second | | | 124 | 934873 | 24 | 5 | 36 |
| : 283 | | | 356 | 293033 | | | | | | 125 | | | -1 | 32 |
| 32 3 | | | 355 | 292820 292607 | 7724 | | | | | | 934723 934649 | | 2 | 28 |
| 404 | | | | 292394 | 7730 | and the second | | 065 | | | 934574 | | | 20 |
| | 7078 | | 355 | 292181 | 7733 | | 226679 | | | | 934499 | 4 | n | 16 |
| 484 | | 1 | 354 | 291968 291755 | 7736 | | 226392 226104 | | | | 934424 934349 | R | 6 | 12 |
| 56 4 | | 1 | 354 | 291542 | 77418 | | 225816 | 065 | | | 934274 | | 21 | 4 |
| 3 0,4 | | | 354 | 10.291330 | | 1 | 10.225529 | | | | | | 57 | 0 |
| 4.4 | | | 353 | 291118 | 7747 | | 225241 | 065 | | | 934123 | | | 56 |
| 8 4 12 4 | | | 353 353 | 290906 290694 | 7750 7753 | | 224954 224667 | 065 | | | 934048 933973 | | | 52 48 |
| 164 | 9 7095 | 18 | 353 | 290482 | 77569 | | 224379 | 066 | | | 933898 | 11 | ŧΠ | 44 |
| 20 5 | | 1 | 353 | 290270 | 77590 | | 224092 | 066 | | | 933822 | | | 40 |
| 24 5 | | | 352 | 290059 289847 | 77619 | 95 478 32 478 | 223805 223518 | | | | 933747 933671 | | | 36 |
| 32 5 | | | | 289636 | | 39 478 | | | | | 933596 | | | 25 |
| 36 5 | | | | 289425 | | 55 478 | | | | | 933520 | 6 | | 24 |
| 40.5 | | | | 289214 289003 | | 12 478 28 477 | 222658 222372 | 066 | | | 933445 933369 | | | 20 |
| 48 5 | 7112 | | | 288792 | | 15 477 | 222085 | 066 | | | 933893 | | | 12 |
| 52 5 | 8 7114 | | | 288581 | 77820 | | 221799 | 0663 | | | 923217 | | | 8 |
| 4 06 | | | | 288371 288161 | 77848 | 38 477 74 477 | 221512 221226 | 0669 | | | 933141 933066 | 0 4 | 56 | 4 |
| - | ' Cosine | - | | | | | | | | | | | n. | = |
| 2530 00 | | Hou | Irs. | - Secant. | Cotang | or | Tang. | Cosec | | Dec | Sine. | - II | 11. | S. |
| P. P. te | 1 15 | T | 15" | 54 | - 18 | 15" | 72 | Is | | 5" | 19 | D | D | |
| s or " | | - | 30 | 107 | 2 | 30 | 144 | 2 | | 0 | 37 | | P. 1 or ' | |
| - | 3 | 1 | 45 | 161 | 3 | 4.5 | 217 | 3 | 4 | 5 | 56 | | | |

| - | - | - | _ | | | - | and | Seca | ots | | TAR | LE V. | - | 45 | 7 |
|-----|--------------|--------------|----------|-----------------------------|--------------------|---------------------|------------------|-----------|------------------|---------------------|--|---------------------|----|------|----------|
| - | _ | | _ | 2 Ho | nre | | anu | or | iito. | | | grees. | | 7. | -1 |
| m. | | 8. | 1 | Sine. | D. | Cosec. | Tang. | D. | Cotang. | Secant. | D. | Cosine. | 11 | m. | 8. |
| 4 | - | 0 | 0 | 9.711839 | 350 | | 9.778774 | 477 | | 10.066934 | 126 | | 60 | 56 | 0 |
| 1 | | 4 | 1 | 712050 | 350 | 287950 | 779060 | 477 | 220940 | 067010 | | 932990 | | | 56 |
| | r | 8 | 2 | 712260 | 350 | 287740 | 779346 | 476 | 220654 | 067086 | | 932914 | | | 52 |
| | | 12 | 3 | 712469 | 349 | 287531 | 779632 | 476 | 220368 | 067162 | | 932838 | | | 48 |
| | | 16 | 4 5 | 712679 | 349 | 287321 287111 | 779918 780203 | 476 | 220082 219797 | 067238 067315 | | 932762 932685 | | | 44 |
| | | 24 | 6 | 713098 | 349 | 286902 | 780489 | 476 | 219511 | 067391 | | 932609 | | | 36 |
| | | 28 | 7 | 713308 | 349 | 286692 | 780775 | 476 | 219225 | 067467 | | 932533 | | | 32 |
| | | 32 | 8 | 713517 | 348 | 286483 | 781060 | 476 | 218940 | 067543 | | 932457 | | | 28 |
| | | 36 10 1 | 9 | 713726 | 348 | 286274 | 781346 | | 218654 | 067620 067696 | | 932380 932304 | | | 24 20 |
| 51 | | | 0 | 713935 714144 | 348 | 286065 285856 | 781631 781916 | 475 | 218369 218084 | 067772 | | 932228 | | 1.16 | 16 |
| D | | 1 | 2 | 714352 | 347 | 285648 | 782201 | 475 | 217799 | 067849 | | 932151 | | | 12 |
| п | | | 3 | 714561 | 347 | 285439 | 782486 | 475 | 217514 | 067925 | | 932075 | | | 8 |
| 9 | - | 56 1 | - | 714769 | 347 | 285231 | 782771 | 475 | 217229 | 068003 | - | 931998 | - | | 4 |
| 5 | | | | 9.714978 | 347 | 10.285022 | | | 10.216944 | 10.068079 | | | | 55 | 0 |
| | , | | 6 | 715186 715394 | 347 | 284814 284606 | 783341 783626 | 475 | 216659 216374 | 068155 068232 | | 931845 931768 | | 5 | 56 52 |
| | 1 | 121 | | 715394 | | 284398 | 783910 | | 216090 | | | 931691 | | | 48 |
| | | 16 | | 715809 | 346 | 284191 | 784195 | | 215805 | 068386 | | 931614 | | a.f. | 44 |
| | 2 | 20 2 | 0 | 716017 | 346 | 283983 | 784479 | 474 | 215521 | 068463 | 128 | 931537 | 40 | | 40 |
| | | 24 2 | | 716224 | | 283776 | 784764 | | 215236 | 068540 | | 931460 | | | 36 |
| | | 28 2 32 2 | | 716432 716639 | | 283568 283361 | 785048 785332 | | 214952 214668 | 068617 068694 | | 931383 931306 | | | 32 |
| П | | 36 2 | | 716846 | | 283154 | 785616 | | 214384 | 068771 | | 931229 | | | 24 |
| | | 10 2 | | 717053 | | 282947 | 785900 | | 214100 | 068848 | | | | | 20 |
| | | 14 8 | | 717259 | | 282741 | 786184 | | 213816 | 068925 | 1 | 931075 | | - | 16 |
| 17 | | 18 | | 717466 | | 282534 | 786468 | | 213532 | 069002 | 1 | 930998 | | | 12 |
| | | 52 2 | | 717673 | | 282327 | 786752 787036 | | 213248 212964 | 069079 | | 930921 930843 | | | 8 |
| 6 | - | | | $\frac{717879}{9.718085}$ | - | 282121 | | | 10.212681 | 069157 10.069234 | | | | F 4 | 0 |
| 10 | ' | 4.3 | | 718291 | | 10.281915 281709 | 787603 | | 212397 | 069312 | | | | 34 | 56 |
| | | 8 | | 718497 | - | 281503 | | | 212114 | | | | | 0 | 52 |
| | | 123 | | 718703 | 343 | 281297 | 788170 | | 211830 | 069467 | 129 | 930533 | 27 | | 48 |
| п | | 163 | | 718909 | | 281091 | 788453 | | 211547 | 069544 | | 930456 | | C. | 44 |
| | | 20 3 | | 719114 | | 280886 280680 | | 1000 | 211264 210981 | 069622 | | | | | 36 |
| 1 | | 28 | | 719525 | | 280475 | 789302 | | 210698 | | | | | | 32 |
| | | 323 | | 719730 | | 280270 | | | 210415 | | | | | - : | 28 |
| 1 | | 363 | | 719935 | 1 | 280065 | 789868 | | 210132 | | | | | | 21 |
| | | 40 | | 720140 | | 279860 | | | 209849 | | | | | 7 | 20 |
| н | | 44 4 | | 720345 | | 279655 | 790433 | 1 | 209567 | 070089 070167 | | | | | 16 |
| 1 | | 52 | | 720549 720754 | | 279451 279246 | 790716 790999 | | 209284 | 070245 | | | | 1 | 8 |
| | | 56 | _ | 720958 | | 279042 | 791281 | | 208719 | | | | _ | | 4 |
| 7 | 7 | | | 9.721162 | 340 | 10.278838 | 9.791563 | 470 | 10.208437 | | | | 15 | 53 | 0 |
| | , | 4 | | 721366 | | 278634 | | | 208154 | | | | | 1 | 56 |
| | | 12 | 17 18 | 721570 | | 278430 | | | 207872 | | | - 10 - 10 - 10 - 10 | | | 52 |
| | | 16 | | 721774 721978 | | 278226 | | | 207590 | | | | | | 4.8 |
| - | | 20 | | | | 277819 | | | 207026 | | | | | | 40 |
| | - 5 | 24 | 51 | 722385 | 339 | 277615 | | | 206744 | | | | | | 36 |
| F | | 28 | | 722588 | | 277412 | 793538 | 469 | 206462 | 071950 | 131 | 929050 | 8 | | 32 |
| 1 | | 32 | | 722791 | | 277209 | | | | | | | | | 28 |
| 1 | | 36 | | | | 277006 276803 | | | 205899 | | | | | | 24 |
| 1 | | 14 | | 723400 | | 276600 | | | 205336 | | | | | | 16 |
| | - | 48 | 57 | 723603 | 337 | 276397 | 794945 | 469 | 205055 | 071343 | 131 | 928657 | 3 | - | 18 |
| 1 | | 52 | | | | 276195 | | | 204773 | | | | | | 8 |
| 9 | | 56 | | | | 275993 | | | 204492 | | | | | | 4 |
| | - | = | | 724210 | 331 | 275790 | - | - | 204211 | | 131 | | = | 52 | (|
| m | | 8. | 1 | Cosine. | 1 | Secant. | Cotang. | | Tang. | Cosec. | 1 | Sine. | 1' | m. | g |
| - | - | - | | 3 Hc | J5" | 1 61 | 1 1- 1 | or 154 | 1 01 | | and the latest terms of th | grees. | | | |
| | | P. 1 | | 2 | 30 | 103 | 15 2 | 15" 30 | 71 142 | 15 2 | 15" 30 | 19 39 | | P. | |
| | S | or ' | | 3 | 45 | 154 | 3 | 45 | 212 | 3 | 45 | 58 | S | or | " |
| 100 | and the last | - | - | THE OWNER OF TAXABLE PARTY. | THE REAL PROPERTY. | - | - | - 17 | | - | - | - | - | - | - |

D

| Section Color C | I | 50 | | TABL | EV. | Lo | garithm | ic Sin | es, Tanger | nts, | | | |
|--|-----|----|-----|---------|-----------|----------|---------|-----------|------------|--------|-------|----------|---------|
| 8 0 0 0 9.724210 337 10.275790 9.795785 468 10.201211 10.071580 132 9.928420 60 52 0 6 9 7 724614 336 275184 796632 468 203360 071635133 9.928525 85 1 1 2 3 724614 336 275184 796632 468 203366 071817 132 9.92855 85 1 1 2 3 724614 336 275184 796632 468 203366 071817 132 9.92855 85 1 1 2 3 724616 336 274985 796613 468 203366 071817 132 9.92855 85 1 2 2 4 6 7.52419 335 274985 79613 468 202860 071875 132 9.92855 55 1 4 2 2 4 6 7.52420 335 274578 797755 468 202245 072133 132 9.92865 55 1 4 2 2 2 2 72862 335 274375 798956 467 201684 072292 132 9.92765 53 3 3 2 8 72662 334 273374 798877 467 20140 072271 132 9.92865 54 1 4 1 1 726426 334 273374 798177 467 20044 072292 132 9.92765 54 4 1 1 726426 334 273374 798177 467 20044 072292 132 9.92764 46 1 1 726626 334 273374 798177 467 20048 072640 132 9.92764 46 1 1 726626 334 273374 798177 467 20048 072640 132 9.92764 48 1 1 726626 334 273374 798177 467 20048 072693 133 9.92730 47 8 1 5 1 4 77027 334 2721973 799171 467 20048 072693 133 9.92730 47 8 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 | | | _ | | | 1 0 | 1 T | | 1 6-1 | | | | |
| 8 p 7 724614 336 | 0 | | == | | _ | | | | | | - | | - |
| Fig. 7 724614 336 275354 796321 468 203368 071737 132 295825 58 51 16 4 725017 336 274587 796013 468 203368 7071871 132 295818 57 468 20358 7 72552 335 274580 79714 468 202567 071975 132 295923 55 42 6 725420 335 274580 797155 468 202555 072651 33 297946 45 33 274578 79755 468 202555 072651 33 297946 45 33 274578 79755 468 202555 072651 33 297768 53 274578 79755 468 202555 072651 33 297768 52 24 41 17 726466 334 273577 798506 467 201123 072751 132 297768 51 24 41 17 726466 334 273577 798577 467 201123 072753 133 297769 51 24 41 17 72646 334 273577 798577 467 201123 072753 133 297740 48 12 72682 334 273573 799957 467 201123 072753 133 29739 477 15 56 14 720727 33 272973 979977 467 200563 07260 133 29739 477 15 56 14 720727 33 272973 979977 467 200563 07260 133 29739 477 15 56 14 727689 333 273572 500577 466 199423 072849 133 297371 45 56 14 727689 333 271773 801366 466 198644 073299 133 297071 43 51 15 15 15 15 15 15 1 | I | 8 | | | | | | | | | | | 259. 5 |
| 16 | Е | | 8 | 724614 | 4 336 | | | | | | | | 3 58 5 |
| 20 | L | | | | | | | | | | | | |
| Per | T, | | | | | | | | | | | | |
| 36 9 7260c9 335 273177 798036 467 201644 07292 132 927708 512 2 40 10 72622 335 273076 798506 467 201640 07292 132 92768 512 2 5 40 10 72622 335 273775 798506 467 201623 072851 132 927686 32 4 17374 798577 467 200623 072851 132 927684 10 11 48 12 726626 334 273374 798577 467 200623 072851 132 927684 10 11 48 12 726626 334 273374 799157 467 200623 072851 132 927848 10 11 48 12 72002 33 4 273374 799157 467 200623 072851 132 927848 10 11 48 12 727027 334 272973 799171 467 200828 072851 132 927854 10 11 41 46 727482 33 272973 99017 466 10.200003 10.072703 133 92730 47 8 18 17 727628 33 272572 800857 466 199723 072849 133 92751 44 16 727828 333 272572 800857 466 199723 072849 133 92751 43 51 16 19 72882 333 271173 801366 466 198604 073169 133 926991 12 42 12 728427 332 271173 801366 466 198854 073089 133 926991 12 42 12 728427 332 271175 801875 466 19825 073289 133 92691 12 42 12 728427 332 271175 801875 466 19825 073289 133 92691 12 42 12 728427 332 271175 801875 466 19825 073289 133 92691 12 42 12 728427 332 271175 801875 466 19825 073289 133 926671 133 33 223 372882 332 271175 801875 466 19825 073329 133 926671 133 33 223 372882 332 271175 80233 465 19766 073309 133 926671 133 33 326591 37 40 40 25 729223 31 270177 80235 466 19805 073369 134 92651 136 24 40 25 729223 31 270177 80235 465 19708 073369 134 92651 136 24 40 25 729223 31 270177 80235 465 19708 073369 134 92651 136 24 40 25 729223 31 270177 80235 465 19708 073369 134 92651 136 24 44 26 729223 31 270378 80351 465 19708 073369 134 92651 136 24 44 26 729223 31 270378 80351 465 19708 073369 134 92651 136 24 44 26 729223 31 270378 80351 465 19708 073369 134 92651 136 24 44 26 729223 31 270378 80351 465 19708 073369 134 92651 136 24 48 27 72921 31 270378 80351 465 19708 073369 134 92651 136 24 48 27 72921 31 270378 80351 465 19708 073369 134 92651 136 24 48 27 72921 31 270378 80351 465 19708 073369 134 92651 136 24 48 27 72921 31 270378 80351 465 19708 073369 134 92651 136 24 48 27 72921 31 270378 80351 466 19708 073369 134 92643 135 24 8 48 27 72921 31 27037 | F | | - | | | | | | | | | | |
| 36 9 72602 335 273976 798316 467 201664 072992 132 927706 51 24 40 10 726925 335 273975 798506 467 201123 072451 132 927549 49 11 44 12 726626 334 273374 798177 467 200643 072451 132 927549 49 11 52 13 726827 334 273973 799177 467 200643 072630 133 927390 47 18 56 14 727027 334 272973 799177 467 2008263 072690 133 927391 47 18 56 14 727027 334 272973 909277 467 2008263 072690 133 927391 45 6 17 727628 333 272572 800877 466 199723 072849 133 927731 45 7 727628 333 272572 800836 466 19943 072292 133 927731 45 10 19 725027 333 271773 800836 466 198649 073099 133 92691 42 2 2 2 728626 332 271374 801955 466 198649 073099 133 92691 41 4 2 2 2 2 2 2 2 2 2 | L | | | | | | | | | | | | |
| 44 11 726426 334 273574 798877 467 20123 072451 132 927540 49 1 | Е | 3 | 6 9 | 726024 | 335 | 273976 | 79831 | 6 467 | 201684 | 07229 | 2 132 | 927708 | 51 2 |
| ## 12 726626 334 273374 799157 467 200643 072630 133 927470 48 15 15 15 16 17 17 17 18 18 18 18 18 | þ | | | | | | | | | | | | |
| 56 14 720027 334 272073 799471 467 200263 072601 33 92730 47 57 56 14 727428 333 272372 800277 466 10200003 10.072769 133 927301 45 51 41 67 727428 333 272372 800277 466 199423 072849 133 927151 44 51 727628 333 272372 8002577 466 199423 072849 133 927151 44 51 727628 333 272172 800836 466 199164 073009 133 926991 42 44 2728027 333 271173 801136 466 198845 073099 133 926991 42 44 21 728427 332 271173 801366 466 198845 073099 133 926991 44 44 2729024 332 271174 801935 466 198645 073329 133 926671 83 3223 728825 332 271174 801935 466 198045 073329 133 926671 83 3223 728825 332 271174 801935 466 198045 073329 133 926671 83 3223 728825 332 271077 802702 465 197467 073409 133 926671 85 33 48 27 729024 331 270376 802573 465 197467 073409 133 926671 85 33 48 27 729422 331 270376 803951 465 197467 073409 133 926671 85 22 28 278825 332 270376 803951 465 197467 073409 133 926671 85 22 28 28 278825 332 270376 803951 465 197467 073409 133 926671 85 22 28 28 27 28 27 28 28 | Г | | | | | | | | | | | | |
| ## 16 | F | | - 1 | 726827 | 334 | 273173 | 79943 | 467 | | 07261 | 0 133 | 927390 | 17 |
| 1 | | | | | | | - | | | | _ | | - |
| S | ľ | | | | | | | 1 | | | | | |
| 16 19 728027 333 271073 801116 466 19884 073089 133 926911 41 42 42 728427 332 271173 801936 466 19804 073169 133 926811 40 40 40 40 40 40 40 | F | | | | | | | | | | | | |
| 20 20 728927 333 271573 801675 466 198604 073169 133 926831 39 34 34 34 35 35 35 35 35 | 4 | | | | | | | | | | | | |
| 24 21 728427 332 271573 801675 466 198045 07329 133 926751 38 32 23 728825 332 271175 802234 465 197766 073409 133 926571 38 33 32674 729024 332 270976 802613 465 197766 073409 134 926513 66 24 24 25 729223 331 270576 803072 465 197808 073569 134 926513 36 24 24 26 729422 331 270576 803072 465 197808 073569 134 926513 35 22 22 20379 803351 465 196649 073730 134 926270 35 22 20379 803351 465 196649 073730 134 926270 35 22 20379 803908 465 196679 073810 134 92610 32 8 26 29 730016 330 269982 803908 465 196072 073890 134 926110 32 8 24 24 24 24 24 24 24 | 1 | | | | | | | | | | | | |
| Section Sect | Į, | 2 | 121 | 728427 | 332 | | | 5 466 | | | | 926751 | 39 3 |
| 36 24 729024 332 270976 802513 465 197487 073489 134 926511 36 24 40 25 729223 331 270777 802797 465 196928 073569 134 926351 34 16 22 270379 803351 465 196928 073649 134 926351 34 16 22 28 729820 331 270379 803351 465 196649 073730 134 92670 35 12 26 28 729820 331 270180 803630 465 196370 073810 134 92610 31 4 26 26 27 30018 30 269982 803908 465 196092 073890 134 926110 31 4 26 27 32 32 32 32 32 32 32 32 32 32 32 32 32 | Ŀ | | | | | | | | | | | | |
| 40 25 729923 331 270578 803072 465 197808 073369 134 926431 35 26 48 27 729621 331 270578 803072 465 196649 073730 134 926270 33 1 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 | | | | | 1 | | | | | | | | |
| 48 27 729921 331 270180 803630 465 196649 073730 134 926170 32 8 28 729820 331 270180 803630 465 1966370 073810 134 926170 32 8 10 0 30 9.730217 330 10.269783 9.804187 465 10.195813 10.07397 134 9.96029 30 50 0 431 730415 330 269887 804466 464 195534 074051 134 9.926029 30 50 0 3 3 30 269887 804745 464 195534 074051 134 9.926029 30 50 0 4 1 1 1 1 1 1 1 1 1 | Г | 40 | 25 | 729223 | 331 | 270777 | 80279 | 2 465 | 197208 | 07356 | 9 134 | 926431 | 35 2 |
| 52 28 729820 331 270180 803630 465 196370 073810 134 926190 32 8 629 730018 330 269982 803908 465 196092 073890 134 92610 31 8 92610 31 4 31 730415 330 269385 804466 464 195534 074051 134 925049 29 50 50 6 8 32 730613 330 269385 804466 464 195255 074132 134 925049 29 50 6 8 32 730613 330 269385 805023 464 194977 074212 134 925788 27 4 6 16 34 731009 329 268991 805302 464 194977 074212 134 925788 27 4 6 2 3 5 731206 329 268596 805858 464 194420 074374 134 925797 26 44 2 36 731404 329 268596 805859 464 194420 074374 134 925792 26 2 3 5 731206 329 268396 806137 464 193863 074535 135 9255452 3 3 2 3 8 73179 329 268201 806415 463 193855 074616 135 925384 22 2 8 3 6 3 9 731996 328 268004 806693 463 193307 074697 135 925303 21 2 4 4 4 1 732390 328 267610 807249 463 1932751 074859 135 925141 19 16 4 4 1 732390 328 267610 807249 463 192751 074859 135 925141 19 16 4 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 | 14 | | | | | | | 100 | | | | | |
| Second S | L | | | | | | | | | | | | |
| 4 31 730415 330 269585 804466 464 195534 074051 134 925949 29 56 8 8 32 730613 330 269387 804745 464 195255 074132 134 925868 28 52 12 33 730811 330 269189 805023 464 194977 074212 134 925788 27 48 16 34 731009 329 268991 805302 464 194977 074212 134 925788 27 48 20 35 731206 329 268594 805580 464 194420 074374 134 925520 25 40 24 36 731404 329 268596 805859 464 194420 074374 134 925520 25 40 28 37 731602 329 268398 806137 464 193863 074535 135 925545 24 36 32 38 731799 329 268201 806415 463 193863 074535 135 925463 23 38 32 38 731799 329 268201 806415 463 193863 074535 135 925384 22 28 36 39 731996 328 267807 806971 463 193307 074697 135 925303 21 24 40 40 732193 328 267807 806971 463 193209 074778 135 925222 20 20 44 41 732390 328 267610 807249 463 192751 074859 135 925222 20 20 44 41 732390 328 267610 807249 463 192751 074859 135 925222 20 20 44 44 732380 327 267020 80803 463 192751 074859 135 925060 18 12 564 733373 327 266627 808638 462 191362 075265 136 92473 14 8 46 733373 327 266627 808638 462 191362 075265 136 92473 14 8 64 733366 327 267020 808638 463 191917 075103 135 924897 16 4 6 733373 327 266627 808638 462 191362 075265 136 924571 14 8 64 733366 327 266631 808916 462 191084 075346 136 924571 14 8 64 733961 326 266039 809471 462 190529 075509 136 924491 11 44 20 50 734457 326 266634 800748 462 190529 075509 136 924491 11 44 20 50 734457 326 265256 810580 462 190529 075509 136 924491 11 44 20 50 734459 326 265451 810925 462 189975 075672 136 924308 9 36 265451 810925 462 189975 075672 136 924308 9 36 265447 810925 462 189975 075672 136 924308 9 36 265447 810925 462 189975 075672 136 924308 6 24 40 55 735135 325 264865 811134 461 188696 075991 136 924400 10 40 40 55 735135 325 264865 811134 461 188696 075991 136 924301 5 20 44 55 735135 325 264865 811134 461 188696 075991 136 924301 5 20 44 55 735135 325 264865 811134 461 188696 075991 136 924301 5 20 44 55 735135 325 264866 81244 461 188696 075991 136 924301 5 20 44 55 735135 325 264865 811134 461 188696 075991 136 924301 5 20 44 45 67 735525 325 2 | 1 | | | 730018 | 330 | 269982 | 80390 | 8 465 | | | | | 31 . |
| R S 2 730613 S 330 269189 805023 464 194977 074212 134 925785 27 48 16 34 731009 S 29 268991 805302 464 194497 074212 134 925707 26 44 20 35 731206 S 29 268794 805580 464 194490 074374 134 925707 26 44 20 35 731206 S 29 268596 805589 464 194420 074374 134 925520 25 46 28 37 731602 S 29 268398 806137 464 193869 074435 335 925465 23 32 38 731799 S 29 268398 806137 464 193869 074453 335 925465 23 32 38 731799 S 29 268306 806693 463 193307 074697 135 925303 21 24 40 0732193 S 28 267807 806971 463 193307 074697 135 925303 21 24 40 0732193 S 28 267610 807249 463 193307 074697 135 925303 21 24 40 40 40 40 40 40 40 | 10 | | | | | | | | | | | | |
| 12 33 | l: | | | | | | | | | | | | |
| 20 35 731206 329 268794 805580 464 194420 074374 134 925520 25 46 | E | | 33 | 730811 | | | | | | | | 925788 | 27 4 |
| 24 36 731404 329 268596 805859 464 194141 074455 135 925545 24 36 28 37 731602 329 268398 806137 464 193863 074535 135 925545 24 36 38 731799 329 268201 806415 463 193385 074616 135 925584 22 28 36 39 731996 325 268004 806693 463 193307 074697 135 925308 21 24 40 40 732193 328 267610 807249 463 193029 074778 135 925303 21 24 41 732390 328 267610 807249 463 192751 074859 135 925141 19 16 48 42 732587 328 267413 807527 463 192473 074940 135 925060 18 12 52 43 732784 328 267216 807805 463 192195 075021 135 924979 17 56 44 732980 327 267020 808083 463 191917 075103 135 924979 17 464 733373 327 266627 808638 462 191362 075265 136 924571 16 48 733765 327 266431 808916 462 191084 075346 136 924451 13 52 12 48 733765 327 266235 809193 462 190807 075428 136 924451 11 44 20 50 734157 326 265843 809748 462 190807 075509 136 924451 11 42 050 734157 326 265843 809748 462 190807 075509 136 924451 11 42 050 734157 326 265843 809748 462 190807 075509 136 924451 11 42 050 734157 326 265843 809748 462 190807 075509 136 924451 11 42 050 734157 326 265843 809748 462 190807 075509 136 924451 11 42 050 734157 326 265843 809748 462 190252 075509 136 924451 11 44 20 50 734157 326 265843 809748 462 190252 075509 136 924451 11 44 20 50 734157 326 265843 809748 462 190252 075509 136 924409 10 40 24 51 734353 326 265647 810025 462 189975 075672 136 924499 10 40 24 51 734353 326 265647 810025 462 189975 075672 136 924409 10 40 24 51 734353 325 265861 810802 462 189975 075672 136 924409 10 40 24 51 734353 325 265861 810802 462 189975 075679 136 924409 10 40 24 51 734353 325 265861 810802 462 189975 075672 136 924328 9 36 28 52 734549 326 265647 810025 462 189975 075672 136 924328 9 36 28 52 734549 326 265647 810025 462 189975 075672 136 924328 9 36 28 52 734549 326 265647 810025 462 189975 075672 136 924504 63 32 52 5256 810580 462 189420 075836 136 92450 15 20 44456 735330 325 264665 811140 461 188590 076081 136 924083 6 24 40 55 735135 325 2644675 811867 461 188330 076081 136 923919 4 16 48 57 735330 325 264665 811140 461 188036 076945 13 | Ŀ | | | | | | | | | | | | |
| 28 37 731602 329 268398 806137 464 193863 074535 135 925465 23 32 38 731799 329 268201 806415 463 193585 074616 135 925303 21 24 40 40 732193 328 267807 806971 463 193029 074778 135 925303 21 24 41 732390 328 267610 807249 463 193209 074778 135 925322 20 20 44 41 732390 328 267610 807249 463 192751 074859 135 925141 19 16 48 42 732587 328 267413 807527 463 192473 074940 135 925000 18 12 564 732980 327 267020 808083 463 191915 075021 135 924979 17 8 46 733373 327 266627 808638 462 191362 075265 136 9.44735 14 56 8 47 733569 327 266431 808916 462 191084 075346 136 9.44735 14 56 8 47 733569 327 266235 809193 462 190807 075428 136 924451 13 52 12 48 733765 327 266235 809193 462 190807 075428 136 924451 14 42 0550 734157 326 266235 809471 462 190529 075509 136 924451 11 42 0550 734157 326 265265 81 809471 462 190529 075509 136 924409 10 40 24 51 734353 326 265647 810025 462 189975 075507 136 924409 10 40 24 51 734353 326 265647 810025 462 189975 075507 136 924409 10 40 24 51 734353 326 265647 810025 462 189975 075507 136 924409 10 40 24 51 734353 326 265647 810025 462 189975 075507 136 924409 10 40 24 51 734353 326 265647 810025 462 189975 075507 136 924409 10 40 24 51 734353 326 265647 810025 462 189975 075507 136 924409 10 40 24 51 734353 325 265661 810807 462 189975 075507 136 924409 10 40 24 51 734353 325 265661 810807 462 189975 075672 136 924409 10 40 24 51 734353 325 265661 810807 462 189975 075672 136 924409 10 40 24 51 734353 325 265661 810867 462 189975 075672 136 924409 10 40 24 51 734353 325 264665 811134 461 188866 075999 136 924401 5 20 4456 735330 325 264475 81687 461 188313 076163 136 923919 4 16 48 57 735525 325 264475 811687 461 188303 076081 136 923919 4 16 48 57 735525 325 264475 811687 461 188036 076945 137 923755 2 8 56 59 735914 324 264891 812517 461 188036 076049 137 923575 2 8 56 59 735914 324 264891 812517 461 187483 076409 137 923575 2 8 56 59 735914 324 264891 812517 461 187483 076409 137 923591 0 48 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 | | | | | | | | | | | | | |
| 36 39 731996 328 268004 806693 463 193307 074697 135 925303 21 24 40 40 732193 328 267610 807249 463 193029 074778 135 925322 20 20 41 41 732390 328 267610 807249 463 192751 074859 135 925141 19 16 48 42 732587 328 267413 807527 463 192473 074940 135 925060 18 12 52 43 732784 328 267216 807805 463 192195 075021 135 924979 17 8 66 44 732980 327 267020 808083 463 192195 075021 135 924979 17 8 464 733317 327 10.266823 9.508361 463 10.191639 10.075184 135 9.924816 15 49 0 46 733373 327 266627 808638 462 191362 075265 136 9.4735 14 56 847 733569 327 266627 808638 462 191362 075265 136 9.24731 14 56 847 733569 327 266627 808618 462 191084 075346 136 9.24654 13 52 12 48 733765 327 266235 809193 462 190807 075428 136 924454 13 52 20 50 734157 326 265843 809748 462 190807 075509 136 924409 10 40 24 51 734353 326 265843 809748 462 190252 075509 136 924409 10 40 24 51 734353 326 265647 810025 462 189975 075672 136 924409 10 40 24 51 734353 326 265647 810025 462 189975 075672 136 924409 10 40 24 51 734353 326 2656647 810025 462 189975 075672 136 924409 10 40 24 51 734353 326 265256 810580 462 189975 075672 136 924409 10 40 24 51 735330 325 265256 810580 462 189975 075672 136 924409 10 40 325 3734744 325 265256 810580 462 189975 075672 136 924409 10 40 325 3734744 325 265256 810580 462 189975 075672 136 924409 10 40 325 3734744 325 265256 810580 462 189975 075672 136 924409 10 40 325 3734744 325 265256 810580 462 189975 075672 136 924409 10 40 325 3734744 325 265256 810580 462 189975 075672 136 924001 5 20 44 56 735330 325 264670 811410 461 188590 076081 136 923037 3 12 525 264865 811154 461 188590 076081 136 923755 2 56 58 735719 324 264281 811964 461 188036 076245 137 923755 2 56 58 735719 324 264281 811964 461 188036 076245 137 923755 2 56 58 735719 324 264281 811964 461 188036 076245 137 923755 2 56 58 735719 324 264281 811964 461 188036 076245 137 923755 2 56 58 735719 324 264281 811964 461 188036 076245 137 923755 2 56 56 59 735914 324 264281 811964 461 188036 076245 137 923755 2 10 40 40 40 40 40 40 40 40 40 40 40 40 | - | 28 | 37 | 731602 | 329 | 268398 | 80613 | 7 464 | 193863 | 07453 | 5 135 | 925465 | 23 3 |
| 40 40 732193 328 267807 806971 463 193029 074778 135 92522 20 20 44 41 732390 328 267610 807249 463 192751 074859 135 925141 19 16 86744 732587 328 267413 807527 463 192473 074940 135 925060 18 192 566 44 732980 327 267020 808083 463 191917 075103 135 924979 17 8 867020 327 267020 808083 463 191917 075103 135 924979 16 4 10 45 9.733177 327 10.266823 9.808361 463 10.191639 10.075184 135 9.24897 16 4 1733373 327 266627 808638 462 191362 075265 136 9.4735 14 56 847 733569 327 266431 808916 462 191084 075346 136 924451 13 52 12 48 733765 327 266235 809193 462 190807 075428 136 924451 13 52 12 48 733765 327 266235 809193 462 190807 075509 136 924451 14 42 0.50 734157 326 265843 809748 462 190529 075509 136 924491 11 44 20 50 734157 326 265843 809748 462 190529 075509 136 924491 11 44 20 50 734157 326 265843 809748 462 190529 075509 136 924491 11 44 20 50 734157 326 265843 809748 462 190529 075509 136 924409 10 40 24 51 734333 326 265647 810025 462 189975 075672 136 924328 9 36 28 52 734549 326 265647 810025 462 189975 075672 136 924328 9 36 32 53 734744 325 265256 810580 462 189420 075836 136 924464 7 28 36 54 734939 325 265061 810857 462 189420 075836 136 924464 7 28 36 54 734939 325 265061 810857 462 189420 075836 136 924404 7 28 36 54 734939 325 265061 810857 462 189420 075836 136 924404 7 28 36 54 734939 325 265061 810857 462 189420 075836 136 924001 5 20 445 56 735330 325 264475 811857 461 188866 075999 136 924001 5 20 445 56 735330 325 264475 811687 461 188866 075999 136 924001 5 20 445 56 735330 325 264475 811687 461 188866 075999 136 924001 5 20 48 57 735525 325 264475 811687 461 188036 076245 137 923755 2 8 56 59 735914 324 264086 812241 461 18759 0766245 137 923755 2 8 56 59 735914 324 264086 812241 461 18759 0766245 137 923755 2 8 56 59 735914 324 264086 812241 461 18759 0766245 137 923755 2 8 56 59 735914 324 264086 812241 461 18759 0766245 137 923755 2 8 56 59 735914 324 264086 812241 461 18759 076627 137 923573 1 4 12 060 736109 324 264886 812241 461 18759 076627 137 923573 1 4 12 060 736109 324 264886 | | | | | | | | | | | | | |
| 44 41 732390 328 267610 807249 463 192751 074859 135 925141 19 16 48 42 732587 328 267413 807527 463 192473 074940 135 924979 17 52 43 732784 328 267216 807805 463 192195 075021 135 924979 17 56 44 732980 327 267020 808083 463 191917 075103 135 924897 16 4 11 045 9.733177 327 10.266823 9.808361 463 10.191639 10.075184 135 9.24897 16 4 46 733373 327 266627 808638 462 191362 075265 136 9.4735 14 56 847 733569 327 266431 808916 462 191084 075346 136 924454 13 52 12 48 733765 327 266235 809193 462 190807 075428 136 9244572 12 16 49 733961 326 266039 809471 462 190529 075509 136 924409 10 40 24 51 734353 326 265843 809748 462 190252 075509 136 924409 10 40 24 51 734353 326 265647 810025 462 189975 075672 136 924409 10 40 24 51 734353 326 265461 810302 462 189975 075672 136 924409 10 40 24 51 734353 325 265865 810580 462 189975 075672 136 924408 6 36 54 734939 325 265061 810857 462 189143 075917 136 924408 6 24 40 55 735135 325 264465 811134 461 188866 075999 136 924001 5 20 44 56 735330 325 2644675 811687 461 188866 075999 136 924001 5 20 44 56 735330 325 264475 811687 461 188866 076999 136 923919 4 16 48 57 735525 325 264475 811687 461 188036 076245 137 923755 2 8 56 59 735914 324 264086 812241 461 187759 076327 137 923673 1 4 12 060 736109 324 263891 812517 461 187483 076409 137 923591 048 0 m. s. | 0 | | | | | | | | | | | | |
| 52 43 732784 328 267216 807805 463 192195 075021 135 924979 17 8 56 44 732980 327 267020 808083 463 199197 075103 135 924979 16 4 11 045 9.733177 327 10.266823 9.808361 463 10.191639 10.075184 135 9.24816 15 49 0 4 46 733373 327 266627 808638 462 191362 0.75265 136 9.24731 4 56 8 47 733569 327 266235 809193 462 190807 0.75428 136 924572 12 48 16 49 733961 326 266039 809471 462 190807 0.75428 136 9244572 12 48 16 49 733961 326 265843 809748 462 190252 0.75591 136 9244091 14 20 | ő | | | 732390 | 328 | | 80724 | 9 463 | | 07485 | 9 135 | 925141 | 19 16 |
| 56 44 732980 327 267020 808083 463 191917 075103 135 924897 16 4 11 045 9.733177 327 10.266823 9.808361 463 10.191639 10.075184 135 9.924816 15 49 0 4 46 733373 327 266627 808638 462 191362 075265 136 9.24751 14 56 847 733569 327 266431 808916 462 1910807 075346 136 924572 12 48 1649 733961 326 266039 809471 462 190807 075599 136 924472 12 48 1649 733961 326 265843 809748 462 190252 075591 136 924409 10 40 2451 734353 326 265447 810025 462 189975 0755751 136 9 | | | | | | | | | | | | | |
| 4 46 733373 327 266627 808638 462 191362 075265 136 9.4735 14 56 847 733569 327 266431 808916 462 191084 075346 136 924651 13 52 12 48 733765 327 266235 809193 462 190807 075428 136 924572 12 48 164 9 733961 326 266039 809471 462 190529 075509 136 924491 11 44 20.50 734157 326 265843 809748 462 190252 075591 136 924409 10 40 24.51 734353 326 265647 810025 462 189975 075672 136 92428 9 36 28.52 734549 326 2655451 810302 462 189698 075751 136 924246 8 32 32.53 734744 325 265256 810580 462 189420 075836 136 924164 7 28 36.54 734939 325 265061 810857 462 189143 075936 136 924164 7 28 36.54 734939 325 265061 810857 462 189143 075917 136 924083 6 24 40.55 735135 325 264865 811134 461 188866 075999 136 924001 5 20 44.56 735330 325 264670 811410 461 188590 076081 136 923919 4 16 48.57 735525 325 264475 811687 461 188036 076245 137 923755 2 8 56.59 735914 324 264086 812241 461 187759 076327 137 923673 1 4 12 0.60 736109 324 263891 812517 461 187483 076409 137 923591 048 0 m. s. / Cosine. Secant. Cotang. Tang. Cosec. Sine. / m. s. / M. s. / Cosine. Secant. Cotang. Tang. Cosec. Sine. / m. s. / M. s. / D. P. P. to 18 15" 49 15 15" 70 15 15" 20 P. P. to 18 15" 49 15 15" 70 15 15" 20 P. P. to 18 15" 49 15 15" 70 15 15" 20 P. P. to 18 15" 49 15 15" 70 15 15" 20 P. P. to 18 15" 40 P. P. to 18 1 | | - | | | | | | | | | | | |
| 8 47 733569 327 266431 808916 462 191084 075346 136 924651 13 52 12 48 733765 327 266235 809193 462 190807 075428 136 924572 12 48 16 49 733961 326 266039 809471 462 190529 075509 136 924491 11 44 20 50 734157 326 265843 809748 462 190252 075591 136 924491 11 44 22 51 734353 326 265647 810025 462 189975 075591 136 924491 10 40 24 51 734353 326 265647 810025 462 189975 075591 136 924248 9 36 28 52 734549 326 265451 810302 462 189698 075751 136 924246 8 32 32 53 734744 325 265256 810580 462 189420 075836 136 924164 7 36 54 734939 325 265061 810857 462 189143 075917 136 924083 6 24 40 55 735135 325 264865 811134 461 188866 075991 136 924001 5 20 44 56 735330 325 264670 811410 461 188590 076081 136 924001 5 20 44 56 735330 325 264475 811687 461 188313 076163 136 923919 4 16 48 57 735525 325 264475 811687 461 188036 076081 136 923919 4 16 48 57 735525 325 264481 811964 461 188036 0760245 137 923755 2 8 56 59 735719 324 264281 811964 461 188036 076245 137 923755 2 8 56 59 735914 324 264986 812241 461 187759 076327 137 923591 0 48 0 m. s. / Cosine. Secant. Cotang. Tang.' Cosec. Sine. / m. s. P. P. to 18 15" 49 15 15" 70 16 15" 5" 20 P. P. to | 11 | - | | | | | | | | | | | |
| 12 44 733765 327 266235 809193 462 190807 075428 136 924572 12 48 1649 733961 326 266039 809471 462 190529 075509 136 924491 11 40 20 50 734187 326 265843 809748 462 190252 075591 136 924409 10 40 24 51 734353 326 265647 810025 462 189975 075672 136 924288 9 36 28 52 734549 326 265256 810580 462 189698 075751 136 924246 8 32 32 53 734744 325 265256 810857 462 189420 075836 136 924164 7 28 36 54 734939 325 265256 810857 462 189143 075917 136 924083 6 24 40 55 735135 325 264865 811134 461 188866 075999 136 924001 5 20 44 56 735330 325 264670 811410 461 188590 076081 136 923919 4 16 4857 735525 325 264475 811667 461 188313 076163 136 923837 3 12 52 58 735719 324 264281 811964 461 188036 076245 137 923755 2 264281 811964 461 187759 076327 137 923755 2 264281 81241 461 187759 076327 137 923591 048 0 12 060 736109 324 263891 812517 461 187483 076409 137 923591 048 0 0 0 0 0 0 0 0 0 | | | | | | | | | | | | | |
| 16 49 733961 326 266039 809471 462 190529 075509 136 924491 11 44 24 25 25 265843 809748 462 190252 075551 136 924491 10 40 24 51 734353 326 265647 810302 462 189975 075672 136 924328 9 36 28 52 734549 326 265451 810302 462 189698 075751 136 924246 8 32 32 53 734744 325 265256 810580 402 189420 075836 136 924464 7 28 36 54 734939 325 265061 810857 462 189143 075917 136 924083 6 24 40 55 735135 325 264865 811131 461 188866 075999 136 924001 5 20 24 26 26 26 26 26 26 26 | 1 | | | | | | | | | | | | |
| 24 51 734353 326 265647 810025 462 189975 075672 136 924328 9 36 2852 734549 326 265451 810302 462 189698 075751 136 924164 6 32 32 53 734744 325 265256 810580 462 189420 075836 136 924164 7 28 36 54 734939 325 265061 810857 462 189143 075917 136 924083 6 24 40 55 735135 325 264865 811134 461 188866 075999 136 924001 5 20 44 56 735330 325 2648670 811410 461 188590 076081 136 923919 4 16 48 57 735525 325 264475 811687 461 188330 076163 136 923919 4 16 48 57 735525 325 264475 811687 461 188036 076245 137 923755 2 8 56 59 735719 324 264281 811964 461 188036 076245 137 923755 2 8 56 59 735914 324 264281 811964 461 187759 076327 137 923673 1 4 12 0 60 736109 324 263891 812517 461 187483 076409 137 923591 0 48 0 m. s. / Cosine. Secant. Cotang. Tang.' Cosec. Sine. / m. s. Secant. Cotang. Tang.' Cosec. Sine. / m. s. Secant. Cotang. Tang.' Cosec. Sine. / m. s. P. P. to 18 15" 49 15 15" 70 18 15" 20 P. P. to 18 15" 40 P. P. to 18 15" 40 P. P. to 18 15" 20 P. P. to | 11 | | | 733961 | 326 | 266039 | 80947 | 1 462 | 190529 | 07550 | 136 | 924491 | 11 44 |
| 28 52 734549 326 265451 810302 462 189698 075754 136 924246 8 32 32 53 734744 325 265256 810580 462 189420 075836 136 924164 7 28 36 54 734939 325 265061 810857 462 189143 075917 136 924001 5 24 40 55 735135 325 264865 811134 461 188866 075999 136 924001 5 24 45 6 735330 325 264670 811410 461 188590 076081 136 923919 4 16 48 57 735525 325 264475 811687 461 188313 076163 136 923939 4 16 48 57 735525 325 264475 811687 461 188313 076163 136 923837 3 12 52 58 735719 324 264281 811964 461 188036 076245 137 923755 2 8 56 59 735914 324 264281 811964 461 187759 076327 137 923755 2 8 56 59 735914 324 264086 812241 461 187759 076327 137 923755 2 8 56 59 736109 324 263891 812517 461 187483 076409 137 923591 0 48 0 18 10 1 | 100 | | | | | | | | | | | | |
| 32 53 734744 325 265256 810580 462 189420 075836 136 924164 7 28 36 54 734939 325 265061 810857 462 189143 075917 136 924083 6 24 40 55 735135 325 264865 811134 461 188866 075999 136 924001 5 20 44 56 735330 325 264670 811410 461 188590 076081 136 923919 4 16 48 57 735525 325 264475 811687 461 188313 076163 136 9239319 4 16 52 58 735719 324 264281 811964 461 188036 076245 137 923755 2 8 56 59 735914 324 264281 811964 461 188036 076245 137 923755 2 8 56 59 735914 324 264281 81241 461 187759 076327 137 923755 2 8 56 59 735914 324 26486 812241 461 187759 076327 137 923673 1 4 12 0 60 736109 324 263891 812517 461 187483 076409 137 923591 0 48 0 18 10 | | 28 | 52 | | | | - | | | | | | 8 32 |
| 40 55 735135 325 264865 811134 461 188866 075999 136 924001 5 20 44 56 735330 325 264670 811410 461 188590 076081 136 923919 4 16 48 57 735525 325 264475 811687 461 188313 076163 136 923937 3 12 52 58 735719 324 264281 811964 461 188036 076245 137 923755 2 8 56 59 735914 324 264086 812241 461 187759 076327 137 923673 1 4 12 060 736109 324 263891 812517 461 187483 076409 137 923591 0 48 0 m. s. / Cosine. Secant. Cotang. Tang. Cosec. Sine. / m. s. 3 Hours, or 57 Degrees. P. P. to 18 15" 49 15 15" 70 18 15" 20 P. P. to | | | | | | | | | | | | | |
| 44 56 735330 325 264670 811410 461 188590 076081 136 923919 4 16 48 57 735525 325 264475 811687 461 188313 076163 136 923837 3 12 52 58 735719 324 264281 811964 461 188036 076245 137 923755 2 8 56 59 735914 324 264086 812241 461 187759 076327 137 923755 2 8 56 59 735914 324 264086 812241 461 187759 076327 137 923755 1 4 12 0 60 736109 324 263891 812517 461 187483 076409 137 923591 0 48 0 m. s. ' Cosine. Secant. Cotang. Tang.' Cosec. Sine. ' m. s. 3 Hours, or 57 Degrees. P. P. to 18 15" 49 18 15" 70 18 15" 20 P. P. to | | | | | | | | | | | | | |
| 52 58 735719 324 264281 811964 461 188036 076245 137 923755 2 8 56 59 735914 324 264086 812241 461 187759 076327 137 923673 1 4 12 060 736109 324 263891 812517 461 187483 076409 137 923591 0 48 0 m. s. ' Cosine. Secant. Cotang. Tang.' Cosec. Sine. ' m. s. 3 Hours, or 57 Degrees. P. P. to 18 15" 49 15 15" 70 15 15" 20 P. P. to | | 44 | 56 | 735330 | 325 | 264670 | 811410 | 461 | 188590 | 076081 | 136 | 923919 | 4 16 |
| 56 59 735914 324 264086 812241 461 187759 076327 137 923673 1 4 12 0 60 736109 324 263891 812517 461 187483 076409 137 923591 0 48 0 0 0 0 0 0 0 0 0 | | | | | | | | | | | | | |
| 12 0 60 736109 324 263891 812517 461 187483 076409 137 923591 0 48 0 m. s. / Cosine. Secant. Cotang. Tang. Cosec. Sine. / m. s. 3 Hours, or 57 Degrees. P. P. to 18 15" 49 15 15" 170 18 15" 20 P. P. to | | | | | | | | | | | | | |
| 3 Hours, or 57 Degrees. P. P. to 2 20 00 15 15" 70 15 15" 20 P. P. to | 12 | | | | | | | | | | | | |
| P. P. to 16 15" 49 15 15" 70 15 15" 20 P. P. to | m. | S. | 1 | | . 1 | Secant. | Cotang. | | Tang. | - | | - | ' m. s. |
| 1.1.10 9 90 00 00 140 0 90 140 11.1.10 | | | | | | | | | | - | - | - | |
| | | | | 1s 2 | 15" 30 | 49 99 | 2 2 | 15" 30 | 70 140 | | | 20 40 | |
| 8 or " 2 30 99 2 30 140 2 30 45 60 8 or " | 8 | or | " | | | | | | | 3 | | | s or " |

| F | | | | | | and | Seca | ints. | 37 - | TA | BLE V. | 8 |
|------|-------|-----|----------|-------------|------------------|----------|----------|------------------|---|-------------|----------|----------|
| Н | | - | 2 H | ours, | | | or | | 9 | | egrees. | |
| m. | S. | 17 | Sine. | D. | 1. Cosec. | Tang. | D. | Cotang. | I Secant. | D. | Cosine. | / m. |
| 12 | - | = | | | | | | | | | | - |
| IZ | 0 | | 9.73610 | | | | | 10.187482 | | | | |
| | 8 | | 736303 | | 263697 263502 | | | 187200 | | | | |
| | 12 | 3 | | | 263308 | | | 186930 186653 | | | | |
| | 16 | | | | 263114 | | | 186377 | | | | |
| | 20 | 5 | 737080 | | 262920 | | | 186101 | | | | |
| к | 24 | 6 | 737274 | 1 | 262726 | | 1 | 185825 | | | | |
| | 28 | 7 | 737467 | | 262533 | | | 185548 | | | | |
| | 32 | 8 | 737661 | 1 - | 262339 | | | 185272 | | | | |
| | 36 | 9 | 737855 | | 262145 | | | 184996 | | | | |
| | 40 | | 738048 | | 261952 | | | 184721 | | | | |
| | | 11 | 738241 | | 261759 | | 1 | 184445 | 1 | | | |
| | 48 | | 738434 | | 261566 | | 1 4 7 | 184169 | | 4 | | |
| И | 52 | | 738627 | | 261373 | | | 183893 | | | | |
| | 56 | 14 | 738820 | | 261180 | | | 183618 | | 1 | | |
| 3 | _ | 1 | 9.739013 | | 10.260987 | - | | | 10.077645 | | | |
| | | 16 | 739206 | | 260794 | 816933 | | 183067 | | | | |
| | | 17 | 739398 | | 260602 | | | 182791 | | | | |
| | 12 | | 739590 | | 260410 | | | 182516 | | | 922106 | |
| | 16 | 19 | 739783 | | 260217 | | | 182241 | | | | |
| 0.4 | 20 | | 739975 | | 260025 | | | 181965 | | | 921940 | |
| | 24 | | 740167 | | 259833 | | | 181690 | | | 921857 | |
| | 28 | | 740359 | | 259641 | 818585 | | 181415 | | | | |
| | | 23 | 740550 | Contract of | 259450 | | | 181140 | | | | |
| 0 | 36 | | 740742 | | 259258 | | | 180865 | | | | |
| | | 25 | 740934 | | 259066 | | | 180590 | | | | |
| | | 26 | 741125 | | 258875 | | | 180316 | | 1 1 1 1 1 1 | 921441 | |
| ц | 48 | | 741316 | 1 | 258684 | | | 180041 | | | | |
| | 52 | | 741508 | | 258492 | 820234 | | 179766 | | | | |
| | 56 | | 741699 | | 258301 | 820508 | | 179492 | 078810 | | 921190 | |
| 4 | 0 | 30 | 9.741889 | - | 10.258111 | 9.820783 | 457 | | 10.078893 | 130 | | |
| * | | 31 | 742080 | | 257920 | | 457 | 178943 | | | 921023 | |
| | | 32 | 742271 | 100 100 100 | 257729 | 821332 | | 178668 | | | 920939 | |
| | 12 | | 742462 | | 257539 | | | 178394 | | | 920856 | |
| н, | 16 | | 742652 | | 257348 | | | 178120 | | | 920772 | |
| Jal- | 20 | | 742842 | | 257158 | 822154 | | 177846 | 079312 | | 920688 | |
| | 24 | | 743033 | | 256967 | 822429 | | 177571 | 079396 | | 920604 | |
| | 28 | | 743223 | E 200 | 256777 | 822703 | | 177297 | 079480 | | 920520 | |
| | 32 | | 743413 | | 256587 | 822977 | 456 | 177023 | 079564 | | 920436 | |
| | 36 | | 743602 | | 256398 | 823250 | 456 | 176750 | 079648 | | 920352 | |
| | 40 | | 743792 | | 256208 | 823524 | | 176476 | 079732 | | 920268 | |
| | 44 | | 743982 | | 256018 | 823798 | | 176202 | 079816 | | 920184 | |
| | 48 | | 744171 | 316 | 255829 | 824072 | 456 | 175928 | 079901 | 1 | 92009 | |
| | 52 | 43 | 744361 | 315 | 255639 | 824345 | 456 | 175655 | 079985 | 140 | 920015 | |
| | 56 | 44 | 744550 | 315 | 255450 | 824619 | 456 | 175381 | 080069 | 141 | | 16 |
| 5 | 0 | 4.5 | 9.744739 | | 10.255261 | | 456 | 10.175107 | 10.080154 | 141 | 9.91984 | 15 45 |
| | 4 | | 744928 | | 255072 | 825166 | 456 | 174834 | 080238 | | 919762 | |
| | 8 | | 745117 | 315 | 254883 | 825439 | 455 | 174561 | 080323 | | 919677 | |
| 3 | 12 | | 745306 | | 254694 | .825713 | 4.55 | 174287 | 080107 | | 919593 | |
| | 164 | | 7.45494 | | 254506 | 825986 | | 174014 | 080492 | | 919508 | |
| | 20 | | 745683 | | 254317 | 826259 | | 173741 | 080576 | | 919424 | |
| | 24 | | 745871 | | 254129 | 826532 | | 173468 | 080661 | | 919339 | 9 3 |
| | 28 | | 746060 | | 253940 | 826805 | | 173195 | 080746 | | 919254 | 8 |
| | 32 8 | 53 | 746248 | 313 | 253752 | 827078 | | 172922 | 080831 | 141 | 919169 | 7 2 |
| | 36 5 | | 746436 | | 253564 | 827351 | 455 | 172649 | 080915 | 141 | 919085 | 6 2 |
| | 40 8 | | 746624 | 313 | 253376 | 827624 | 455 | 172376 | 081000 | 141 | 919000 | 5 2 |
| 4 | 14.5 | 6 | 746812 | | 253188 | 827897 | 454 | 172103 | 081085 | 142 | 918915 | 4 1 |
| | 48 5 | | 746999 | | 253001 | 828170 | | 171830 | 081170 | | 918830 | 3 1 |
| 4 | 52 5 | 8 | 747187 | 315 | 252813 | 828442 | | 171558 | 081255 | | 918745 | 2 |
| | 56 5 | | 747374 | 312 | 252626 | 828715 | | 171285 | 081341 | | 918659 | 1 |
| 3 | 06 | | 747562 | 312 | 252438 | 828987 | 454 | 171013 | 081426 | 142 | 918574 | 0 44 |
| | S. | , | Cosine. | | Secant. | Cotang. | | Tang. | Cosec. | | Sine. | ' m. |
| | - | - | 3 Hou | re | December | Journ's | or | | | Deg | PAGE . | line. |
| | - | - | | 15" | 1 49 1 | 18 | 15" | 1 60 1 | | 5" | | |
| | | | 18 | | 48 | | | 69 | | | 21 | P. P. to |
| | ?. to | | 9 | 20 | 0.5 | 9 | 20 | 197 | 9 1 0 | 0 . | | |
| | or " | | 2 3 | 30 45 | 95 143 | 2 3 | 30 45 | 137 206 | | 0 5 | 42 63 | s or " |

| 1 | 52 | • | en.to. | TABLE | v. | Log | garithmic | Sine | s, Tangen | ts, | | | | |
|----|----|----------|----------|------------------|------------|---------------------------------|------------------|-----------|------------------|------------------|-------------|------------------|-----|----------|
| | | | | , 2 Ho | - | | | or | | | | grees. | | |
| m | | 5. | 1 | Sine. | D. | Cosec. | Tang. | D. | Cotang. | Secant. | D. | Cosine. | _ | m. s. |
| 1 | 6. | ō | 0 | 9.747562 | | 10.252438 | | 454 | 10.171013 | 10.081426 | | | | |
| П | | 4 | 1 | 747749 | | 252251 | 829260 | 454 | 170740 | 081511 | | | | 56 |
| | ĺ, | 8 | 5 | 747936 | | 252064 | 829532 829805 | | 170468 | 081596 | | | | . 52 |
| п | | 2 | 3 | 748123 748310 | | 251877 251690 | 830077 | 454 | 170195 169923 | 081682 081767 | | 918318 918233 | | 48 44 |
| 1 | | 16 20 | 4 5 | 748497 | | 251503 | 830349 | | 169651 | 081853 | | 918147 | | 40 |
| | | 24 | 6 | 748683 | | 251317 | 830621 | | 169379 | 081938 | | 918062 | | 36 |
| Ш | | 28 | 7 | 748870 | | 251130 | 830893 | 453 | 169107 | 082024 | | 917976 | 53 | 32 |
| 10 | | 32 | 8 | 749056 | | 250944 | 831165 | | 168835 | 082109 | | | | 28 |
| | | 36 | 9 | 749243 | | 250757 | 831437 | | 168563 | 082195 | | 917805 | | 24 |
| ь | | | 10 | 749429 | | 250571 250385 | 831709 831981 | 100 | 168291 168019 | 082281 082366 | | 917719 917634 | | 20 16 |
| | | - 1 | 11 | 749615 749801 | 310 310 | 250199 | 832253 | | 167747 | 082452 | | 917548 | | 12 |
| | | | 13 | | 309 | 250013 | 832525 | | 167475 | 082538 | | 917462 | | 8 |
| 1 | | | 14 | 750172 | 309 | 249828 | 832796 | | 167204 | 082624 | | 917376 | | 4 |
| Ti | - | | | 9.750358 | 309 | 10.249642 | 9.833068 | 452 | 10.166932 | 10.082710 | | | 45 | 43 0 |
| | | | 16 | 750543 | 309 | 249457 | 833339 | 452 | 166661 | 082796 | | | | 56 |
| 1 | | | 17 | 750729 | 309 | 249271 | 833611 | | 166389 | 082882 | | | | |
| | | | 18 | 751914 | | 249086 | | | 166118 | | | | | 48 |
| | | | 19 | 751099 751284 | | 248901 248716 | 834154 834425 | | 165846 165575 | | | | | 44 40 |
| | | 24 | 20 | 751469 | | 248531 | 834696 | | 165304 | | | | | 36 |
| | | | 25 | | | 248346 | | | 165033 | | | | | 32 |
| | | | 23 | | | 248161 | 835238 | 452 | 164762 | 083400 | 144 | 916600 | 37 | 28 |
| | | | 24 | 752023 | | 247977 | | | 164491 | 083486 | | | | 24 |
| В | | | 25 | | | 247792 | | | 164220 | | | | | 20 |
| 16 | | | 26 | | | 247608 | | | 163949 163678 | 083659 083746 | | | | 16 12 |
| 18 | | | 27 28 | | | 247424 247240 | | | 163407 | 083833 | | 916167 | | 8 |
| | | | 29 | | | 247056 | | | 163136 | 083919 | 1 | 916081 | | 4 |
| 1 | - | | | 9.753128 | - | 10.246872 | | | | 10.084006 | - | | - | |
| | 0 | | 31 | 753312 | | 246688 | | | 162595 | | | | | 56 |
| | | | 32 | | | 246505 | | | 162325 | | 145 | 915820 | 28 | 52 |
| | | | 33 | | 306 | 246321 | 837946 | 451 | 162054 | | | | | - 48 |
| п | | | 34 | | | 246138 | | | 161784 | | | | | 44 |
| | | | 35 | | | 245954 | | | 161513 | | | | | 40 36 |
| 10 | | | 36 37 | | | 245771 245588 | 838757 839027 | 100 | 161243 160973 | | | | | |
| | | | 38 | | | 245405 | | | 160703 | | | | | 28 |
| н | | | 39 | | | 245222 | | 1 | 160432 | | | | | 24 |
| н | | | 40 | | | 245040 | | | 160162 | | | | | 20 |
| | | 14 | 41 | | | 244857 | 840108 | | 159892 | | | | | 16 |
| П | | | 42 | | | 244674 | | | 159622 | | | | | 12 |
| н | | | 43 44 | | | 244492 244310 | | | 159353 159083 | | | | | 4 |
| 1 | | 0 | _ | 9.755872 | - | 10.244128 | | | | 10.085315 | | | | |
| 1 | J | 4 | 46 | | | 243946 | | | 158543 | | | | | |
| | | 8 | 47 | | | 243764 | | | 158274 | | | | | 52 |
| | | | 48 | 756418 | | 243582 | 841996 | 449 | 158004 | 085578 | | | | 48 |
| | | | 49 | | | 243400 | | | 157734 | | | | | 44 |
| | | | 50 | | | 243218 | | | 157465 | | | | | |
| | | | 51 52 | | | 243037 242856 | | | 157195 156926 | | | 914158 914070 | | |
| н | | | 53 | | | 242674 | | | 156657 | | | | | 28 |
| 1 | | | 54 | | | 242493 | | | 156388 | | | | | 24 |
| | | 40 | 55 | 757688 | | 242312 | 843882 | 448 | 156118 | 086194 | 147 | 913806 | 5 | 20 |
| | | | 56 | | | 242131 | | | 155849 | | | | | |
| | | | 57 | | | 241950 | | | 155580 | | | | | |
| | | | 58 59 | | | 241770 | | | 155311 155042 | | | 913541 913453 | | 4 |
| 2 | | | 60 | | | 241589 241409 | | | 154773 | | | 913365 | | 40 0 |
| = | - | - | | | | | | 110 | | | | | = | - |
| n | i. | S. | | Cosine. | | Secant. | Cotang. | | Tang. | Cosec. | 5 30 | Sine. | Ľ | m. s. |
| - | | | - | 3 Ho | urs, | 1 40 | 1 10 1 | or | 1 00 | | 5 De | grees. | | |
| 1 | | | to | 1s 2 | 30 | 46 92 | 13 | 15" 30 | 68 135 | 13 2 | 30 | 43 | | P. to |
| - | 8 | or | " | 3 | 45 | 138 | 3 | 45 | 203 | 3 | 45 | 65 | 1 5 | or" |
| | - | - | - | - | - | THE OWNER WHEN PERSONS NAMED IN | - | | - | - | D. SPANNING | - | 1 | - |

| 200 (4 | 4 8 12 16 20 24 28 32 36 40 1 44 1 48 1 55 1 56 1 | 1 760569 760748 3 760927 761106 5 9.761285 761464 7 761642 | D. 301 300 300 300 300 300 299 299 299 299 299 298 298 298 | Cosec. 10.211409 241228 241048 240688 240508 240328 240148 239969 239789 239610 239431 239252 239073 | 845496 845764 846033 846302 846570 846839 847107 847376 847644 | | Cotang. 10.154773 154504 154236 153967 153698 153430 153161 152893 152624 | Secant. 10.086635 086724 086813 086901 086990 087078 087167 087256 | D. 147 148 148 148 148 148 | grees. Cosine. 9.913365 913276 913187 913099 913010 912922 912833 912744 | 59 58 57 56 55 54 53 | |
|--|---|---|--|---|--|--|---|---|--|--|--|----------------|
| 20 (4 | 0 4 8 12 16 6 20 24 8 32 8 6 10 1 14 1 8 1 8 1 8 1 10 1 11 2 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 | Sine. 0 9.758591 1 758772 7 758952 3 759132 7 759312 7 759352 6 760211 0 760569 2 760748 7 761106 5 9.761295 6 761464 7 761642 | D. 301 300 300 300 300 300 299 299 299 299 299 298 298 298 | 10.211409 241228 241048 240688 240688 240508 240328 240148 239969 239789 239610 239431 239252 239073 | 9.845227 845496 845764 846033 846302 846570 846839 847107 847376 847644 847913 | 448 448 448 448 448 447 447 447 | 10.154773 154504 154236 153967 153698 153430 153161 152893 | Secant. 10.086635 086724 086813 086901 086990 087078 087167 087256 | D. 147 148 148 148 148 148 | Cosine. 9.913365 913276 913187 913099 913010 912922 912833 | 59 58 57 56 55 54 53 | 5: 5: 4: 4: 4: |
| 20 (4 | 4 8 8 1 2 1 6 6 1 2 8 1 1 2 1 1 1 2 1 1 1 6 1 1 | 1 758772 758952 759132 759312 759492 759672 759852 760031 760031 760569 760748 760927 761106 59.761285 761644 | 300 300 300 300 299 299 299 299 298 298 298 298 298 | 241228 241048 240688 240688 240508 240328 240148 239969 239789 239610 239431 239252 239073 | 845496 845764 846033 846302 846570 846839 847107 847376 847644 847913 | 448 448 448 447 447 447 447 | 10.154773 154504 154236 153967 153698 153430 153161 152893 | 086724 086813 086901 086990 087078 087167 087256 | 148 148 148 148 148 | 913276 913187 913099 913010 912922 912833 | 59 58 57 56 55 54 53 | 5: 4: 4: 4: 4: |
| 4 | 4 8 8 1 2 1 6 6 1 2 8 1 1 2 1 1 1 2 1 1 1 6 1 1 | 1 758772 758952 759132 759312 759492 759672 759852 760031 760031 760569 760748 760927 761106 59.761285 761644 | 300 300 300 300 299 299 299 299 298 298 298 298 298 | 241228 241048 240688 240688 240508 240328 240148 239969 239789 239610 239431 239252 239073 | 845496 845764 846033 846302 846570 846839 847107 847376 847644 847913 | 448 448 448 447 447 447 447 | 154504 154236 153967 153698 153430 153161 152893 | 086724 086813 086901 086990 087078 087167 087256 | 148 148 148 148 148 | 913276 913187 913099 913010 912922 912833 | 59 58 57 56 55 54 53 | 5: 4: 4: 4: 4: |
| \$\\\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ | 8 12 16 6 20 24 28 32 16 16 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 | 758952 759132 759312 759312 759492 759672 760211 0760300 11760569 760748 760927 761106 59.761295 761642 | 300 300 300 299 299 299 299 298 298 298 298 | 241048 240688 240688 240508 240328 240148 239969 239789 239431 239431 239252 239073 | 845764 846033 846302 846570 846839 847107 847376 847644 847913 | 448 448 447 447 447 447 | 154236 153967 153698 153430 153161 152893 | 086813 086901 086990 087078 087167 087256 | 148 148 148 148 | 913099 913010 912922 912833 | 57 56 55 54 53 | 4: |
| 12 16 20 20 20 20 20 20 20 20 20 20 20 20 20 | 12 16 20 24 28 32 32 40 14 41 41 41 41 41 41 41 41 41 41 41 41 | 33 759132 759312 759492 759672 759852 8 760031 760211 9 760390 760569 760748 3 760927 761106 5 7761285 6 761642 | 300 300 300 299 299 299 299 298 298 298 298 | 240868 240688 240508 240328 240148 239969 239789 239610 239431 239252 239073 | 846033 846302 846570 846839 847107 847376 847644 847913 | 448 447 447 447 447 | 153967 153698 153430 153161 152893 | 086901 086990 087078 087167 087256 | 148 148 148 148 | 913010 912922 912833 | 56 55 54 53 | 4 |
| 20222 (2 | 20 24 28 32 36 40 144 148 148 148 148 148 148 148 148 148 | 5 759492 759672 7 759852 7 60031 7 60390 1 760569 2 760748 7 761106 5 9.761285 6 761464 7 761642 | 300 299 299 299 299 298 298 298 298 298 | 240508 240328 240148 239969 239789 239610 239431 239252 239073 | 846570 846839 847107 847376 847644 847913 | 447 447 447 447 | 153430 153161 152893 | 087078 087167 087256 | 148 148 | 912922 912833 | 55 54 53 | 4 |
| 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 | 24 28 32 36 40 144 144 1452 1 0 1 41 81 121 161 | 6 759672 7 759852 8 760031 9 760310 0 760390 760569 2 760748 3 760927 4 761106 5 9.761285 6 761464 | 299 299 299 299 298 298 298 298 298 | 240328 240148 239969 239789 239610 239431 239252 239073 | 846839 847107 847376 847644 847913 | 447 447 447 | 153161 152893 | 087167 087256 | 148 | 912833 | 54 53 | |
| 288 33 36 44 48 55 55 56 56 56 56 56 56 56 56 56 56 56 | 28 32 36 40 144 148 148 148 166 170 170 181 181 181 181 181 181 181 181 181 18 | 77 759852 760031 760211 760390 760569 2 760748 3 760927 4 761106 5 9.761285 6 761464 | 299 299 299 298 298 298 298 298 | 240148 239969 239789 239610 239431 239252 239073 | 847107 847376 847644 847913 | 447 447 | 152893 | 087256 | | | 53 | . 3 |
| 33 36 44 48 48 48 55 56 11 11 12 12 22 22 22 22 22 22 22 22 23 33 34 44 44 48 48 48 48 48 48 48 48 48 48 48 | 32 36 40 141 162 161 161 | 6 760031 760211 760390 1 760569 2 760748 3 760927 4 761106 5 9.761285 6 761464 | 299 299 299 298 298 298 298 298 | 239969 239789 239610 239431 239252 239073 | 847376 847644 847913 | 447 | | | 148 | 912744 | | |
| 364444445555566666666666666666666666666 | 36 10 14 11 18 11 16 11 11 11 11 11 11 11 11 11 11 11 | 760211 760390 760569 760748 3760927 761106 59.761285 761464 7761642 | 299 299 298 298 298 298 298 | 239789 239610 239431 239252 239073 | 847644 847913 | | 152624 | | 1 40 | | Ital | 3 |
| 40444444444444444444444444444444444444 | 10 1 14 1 18 1 16 1 10 1 10 1 11 2 1 16 1 | 760390 760569 760748 760927 761106 5 9.761285 761464 7 761642 | 299 298 298 298 298 298 | 239610 239431 239252 239073 | 847913 | ** | 152356 | 087345 087434 | | 912655 912566 | | 2 |
| 444 48 | 14 1 18 1 16 1 16 1 16 1 | 1 760569 760748 3 760927 761106 5 9.761285 761464 7 761642 | 298 298 298 298 298 | 239431 239252 239073 | | | 152087 | 087523 | | 912477 | | 2 |
| 488 555 566 568 568 568 568 568 568 568 5 | 18 1 16 1 16 1 18 1 18 1 16 1 | 760748 760927 761106 5 9.761285 6 761464 7 761642 | 298 298 298 298 | 239252 239073 | | 447 | 151819 | 087612 | | 912388 | | ĩ |
| 56 55 56 56 56 56 56 56 56 56 56 56 56 5 | 6 1 0 1 4 1 8 1 12 1 16 1 | 3 760927 4 761106 5 9.761285 6 761464 7 761642 | 298 298 298 | 239073 | 848449 | 447 | 151551 | 087701 | | 912299 | | 1 |
| 21 (4 | 0 1 4 1 8 1 2 1 6 1 | 5 9.761285 6 761464 7 761642 | 298 | 00000 | | 447 | 151283 | 087790 | | 912210 | 47 | |
| 4 | 4 1 8 1 2 1 6 1 | 6 761464 7 761642 | | 238894 | 848986 | 447 | 151014 | 087879 | 149 | 912121 | | |
| 11 10 20 24 22 22 33 34 44 44 45 55 66 55 66 55 66 55 66 66 66 66 66 66 | 4 1 8 1 2 1 6 1 | 6 761464 7 761642 | | 10.238715 | 9.849254 | 447 | 10.150746 | 10.087969 | 149 | 9.912031 | 453 | 9 |
| 12 16 20 22 22 22 33 36 44 44 48 55 56 22 22 22 22 22 33 33 36 44 48 48 48 48 48 48 48 48 48 48 48 48 | 121 | - | 298 | 238536 | | 447 | 150478 | 088058 | | 911942 | | 5 |
| 10 20 22 33 33 34 44 48 48 48 48 48 48 48 48 48 48 48 48 | 161 | | 297 | 238358 | | | 150210 | 088147 | 149 | 911853 | | 5 |
| 20 22 20 44 48 55 55 55 55 55 56 56 68 68 68 68 68 68 68 68 68 68 68 68 68 | | | | 238179 | | | 149942 | 088237 | | 911763 | | 4 |
| 24 28 33 36 44 48 55 55 55 55 55 55 55 55 55 55 55 55 55 | 202 | - | | 238001 | 850325 | 446 | 149675 | 088326 | | 911674 | | 4 |
| 288 338 368 444 488 555 56 56 56 56 56 56 56 56 56 56 56 56 | | | | 237823 | | | 149407 | 088416 | | 911584 | | 4 |
| 32 36 44 48 48 48 55 56 22 22 22 22 22 23 33 36 40 44 44 48 48 48 48 48 48 48 48 48 48 48 | | | | 237644 | | | 149139 | 088505 088595 | | 911495 911405 | | 3 |
| 36 44 44 48 55 55 66 11 11 22 22 22 33 36 44 44 44 45 55 56 56 56 56 56 56 56 56 56 56 56 56 | 32 2 | | | 237466 237288 | 851129 851396 | | 148871 148604 | 088685 | | 911315 | | 2 |
| 444 4855 5665 6675 6775 6775 6775 6775 6775 6 | 36 2 | | | 237111 | 851664 | | 148336 | 088774 | | 911226 | | 2 |
| 44 48 55 56 56 11 11 10 22 22 22 22 22 44 44 48 55 56 56 66 67 67 67 67 67 67 67 67 67 67 67 67 | 102 | | | 236933 | | 446 | 148069 | 088864 | | 911136 | | 2 |
| 55 56 56 11 11 10 20 22 22 33 36 40 44 48 55 56 | 14 2 | | | 236755 | | 446 | 147801 | 088954 | | 911046 | | 1 |
| 56 111116 20222 (1 112116 20222 3336 4444 455 55 55 56 52 56 57 68 68 68 68 68 68 68 68 68 68 68 68 68 | 18 2 | 7 763422 | 296 | 236578 | | | 147534 | 089044 | | 910956 | 33 | 1 |
| 2022 (4 11 10 20 22 22 22 22 33 36 44 48 55 55 55 | 52 2 | | 295 | 236400 | 852733 | 445 | 147267 | 089134 | | 910866 | | |
| 11 11 10 20 24 28 33 36 40 44 48 55 56 | 56 2 | | | 236223 | 853001 | 445 | 146999 | 089224 | 150 | 910776 | 31 | |
| 111 102 222 288 33 36 40 44 48 55 56 | | 0 9.763954 | 295 | 10.236046 | 9.853268 | 445 | 10.146732 | 10.089314 | | | | |
| 11 10 20 22 28 33 36 40 44 48 55 56 56 56 57 10 11 12 12 12 12 12 12 12 12 12 12 12 12 | 43 | | | 235869 | 853535 | | 146465 | 089404 | | 910596 | | 5 |
| 10 20 26 33 36 40 44 48 55 50 23 (12 10 20 20 20 20 20 20 20 20 20 20 20 20 20 | 83 | - | | 235692 | | | 146198 | 089494 | | 910506 | | 5 |
| 20 28 33 36 40 44 48 55 50 28 (8 19 10 20 | 123 | | | 235515 | | | 145931 | 089585 | | 910415 | | 4 |
| 26 26 36 40 46 46 56 50 28 10 20 | 163 | | | 235338 | | | 145664 | 089675 089765 | | 910325 910235 | | 4 |
| 28 36 40 44 48 58 50 28 (19 10 20 | 243 | | | 235162 234985 | | 445 | 145397 145130 | 089856 | | 910144 | | 9 |
| 33 36 40 44 48 55 50 23 (10 10 20 | 83 | | | 234809 | | | 144863 | 089946 | | 910054 | | 3 |
| 36 40 44 48 55 50 23 (8 16 20 20 | 323 | | | 234633 | | | 144596 | 090037 | | 909963 | | 9 |
| 44 48 50 50 50 23 6 10 20 | 363 | | | 234456 | 855671 | 444 | 144329 | 090127 | | 909873 | | 2 |
| 48 50 50 23 (4 19 10 20 | 104 | 765720 | 293 | 234280 | 855938 | 444 | 144062 | 090218 | 151 | 909782 | | 2 |
| 55 50 23 0 4 15 16 20 | 4 | | 293 | 234104 | 856204 | | 143796 | 090309 | | 909691 | | 1 |
| 50 23 (4 19 10 20 | 18 4 | _ | | 233928 | | 444 | 143529 | 090399 | | 909601 | | 1 |
| 23 (13 16 20 | 52 4 | | | 233753 | 856737 | 444 | 143263 | 090490 | | 909510 | | |
| 19 19 10 20 | 56 4 | | | 233577 | 857004 | | 142996 | 090581 | | 909419 | | |
| 13 16 20 | | 5 9.766598 | | 10.233402 | | 444 | | 10.090672 | | | | |
| 19 | 4.4 | | | 233226 | 857537 | 444 | 142463 | 090763 | | 909237 | | 1 |
| 20 | | | | 233051 232876 | 857803 858069 | | 142197 141931 | 090854 090945 | | 909146 909055 | | . 4 |
| 20 | 84 | | | 232700 | | | 141931 | 091036 | | 909055 | | |
| | 84 | | | 232525 | | | 141398 | 091127 | 152 | 908873 | 10 | 4 |
| | 8 4 12 4 16 4 | | | 232351 | | | 141132 | | | | | |
| 28 | 84 | | | 232176 | | | 140866 | 091310 | | | | . 5 |
| | 8 4 12 4 16 4 20 5 | 2 767824 | 291 | 232001 | | | 140600 | | | 908599 | 7 | . 4 |
| | 8 4 12 4 16 4 20 5 24 5 28 5 32 5 | 3 767999 | | 231827 | | | 140334 | 091493 | | 908507 | | , 2 |
| | 8 4 12 4 16 4 20 5 24 5 28 5 32 5 | 3 767999 4 768173 | | 231652 | | | 140068 | 091584 | | | | 1 2 |
| | 8 4 12 4 16 4 20 5 24 5 28 5 36 5 40 5 | 3 767999 4 768173 5 768348 | | 231478 | | | 139802 | 091676 | | | |] |
| | 8 4 12 4 16 4 20 5 24 5 28 5 32 5 36 5 10 5 | 3 767999 4 768173 5 768348 6 768522 | 290 | | 860464 | | 139536 139270 | 091767 | | | | 1 |
| | 8 4 12 4 16 4 20 5 24 5 28 5 36 5 40 5 44 5 | 3 767999 4 768173 5 768348 6 768522 7 768697 | 290 290 | 231303 | | | | 091859 | 103 | 908141 | | |
| | 8 4 12 4 16 4 20 5 24 5 32 5 36 5 10 5 14 5 18 5 52 5 | 3 767999 4 768173 5 768348 6 768522 7 768697 8 768871 | 290 290 290 | 231303 231129 | 860730 | | | | | | | |
| | 8 4 12 4 16 4 20 5 24 5 32 5 33 6 5 36 5 36 5 36 5 36 5 36 5 56 5 5 | 767999 768173 768348 768522 768697 8768871 9769045 | 290 290 290 290 | 231303 231129 230955 | 860730 860995 | 443 | 139005 | 091951 | 153 | 908049 | | |
| n. s | 8 4 12 4 16 4 520 5 24 5 332 5 332 5 540 5 544 5 552 5 6 | 3 767999 4 768173 5 768348 6 768522 7 768697 8 768871 9 769045 0 769219 | 290 290 290 290 | 231303 231129 230955 230781 | 860730 860995 861261 | 443 | 139005 138739 | 091951 092042 | 153 | 908049 907958 | 03 | 6 |
| | 8 4 12 4 16 4 520 5 28 5 32 5 536 5 540 5 552 5 56 5 6 5 | 767999 768173 768348 768522 768697 769871 769045 769219 Cosine. | 290 290 290 290 290 | 231303 231129 230955 | 860730 860995 | 443 443 | 139005 | 091951 092042 Cosec. | 153 153 | 908049 907958 Sine. | | _ |
| P. P. | 8 4 12 4 16 4 520 5 24 5 332 5 332 5 540 5 544 5 552 5 6 | 767999 768173 768348 768522 768697 768871 769045 769219 Cosine. | 290 290 290 290 290 | 231303 231129 230955 230781 Secant. | 860730 860995 861261 Cotang. | 443 443 or | 139005 138739 Tang. | 091951 092042 Cosec. | 153 153 ———————————————————————————————— | 908049 907958 Sine. | 03 | 6 |
| s or | 8 4 12 4 4 5 16 4 5 5 2 5 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 | 767999 768173 768348 768522 77 768871 768971 769045 769219 7 Cosine. | 290 290 290 290 290 | 231303 231129 230955 230781 | 860730 860995 861261 | 443 443 | 139005 138739 | 091951 092042 Cosec. 54 | 153 153 | 908049 907958 Sine. | 03 | n. |

| - | _ | _ | _ | | | | *.1 | a. | m | | | | _ | - | - |
|-----|-----|------------|---------|--------------------|------------|---------------------|--------------------|-----------|---------------------|--------|--|---------|-----|------|----------|
| 5 | 4 | | _ | TABLE | | Log | garithmi | | s, Tangen | ts, | 00 D | - | | | - |
| - | | - | 71 | 2 Ho Sine. | D. | Cosec. | Tang. | D. | Cotono | Sognat | | cosine. | 111 | m | - |
| m. | | 8 | | | | | | | Cotang. | Secant | | | | m. | 8. |
| 24 | | 0 | | 9.769219 769393 | 290 289 | 10.230781 230607 | 9.861261 861523 | 1 | 10.138739 | | 34 153 | | | 36 | 56 |
| 1 | | 8 | 5 | 769566 | | 230434 | 861799 | | 138208 | | 26 153 | | | 7 | 52 |
| | 1 | | 3 | 769740 | | 230260 | 862058 | | 137942 | | 18 153 | | | | 48 |
| 80 | 1 | | 4 | 769913 | 289 | 230087 | 862323 | | 137677 | | 10 153 | | | Tab. | 44 |
| 100 | 2 | | 5 | 770087 | 289 | 229913 | 86258 | | 137411 | | 02 153 | | | | 40 36 |
| | 21 | | 7 | 770260 770433 | 288 288 | 229740 229567 | 862854 863119 | | 137146 136881 | | 94 153 86 154 | | | | 32 |
| | 3 | | 8 | 770606 | 288 | 229394 | 863383 | | 136615 | | 78 154 | | | SE. | 28 |
| - | 30 | | 9 | 770779 | 288 | 229221 | 863650 | | 136350 | | 71 154 | 907129 | 51 | | 24 |
| 100 | 40 | | 0 | 770952 | 288 | 229048 | 863913 | | 136085 | | 63 154 | | | | 20 |
| 16 | | 4 1 1 3 1 | | 771125 771298 | 288 | 228875 228702 | 864180 864443 | 10.00 | 135820 135555 | | 055 154 48 154 | | | | 16 12 |
| 0 | 59 | | 3 | 771470 | 287 | 228530 | 864710 | | 135290 | | 40 154 | | | IJ, | 8 |
| | 50 | 6 1 | | 771643 | 287 | 228357 | 864973 | | 135025 | | 33 15 | | | 14. | 4 |
| 25 | (| 0 1 | 5 | 9.771815 | 287 | 10.228185 | 9.865240 | 441 | 10.134760 | | | | | | 0 |
| | | | 6 | 771987 | | 228013 | 865503 | | 134495 | | 18 154 | | | | 56 |
| | | 3 1 2 1 | | 772159 772331 | 287 | 227841 | 865770 | | 134230 | | 04 153 | | | | 52 48 |
| | | 6 1 | | 772503 | | 227669 227497 | 866034 866300 | | 133965 133700 | | 96 155 | | | Fi. | 44 |
| 21 | | 0 2 | | 772675 | | 227325 | 866564 | | 133436 | | 889 155 | | | 0.6 | 40 |
| - | | 1 2 | | 772847 | | 227153 | 866829 | | 133171 | | 982 155 | | | 44 | 36 |
| | | 3.5 | | 773018 | | 226982 | 867094 | | 132906 | | 75 155 | | | | 32 |
| | | 2 2 6 3 | | 773190 | | 226810 226639 | 867358 867623 | | 132642 132377 | | $\begin{vmatrix} 68 & 155 \\ 61 & 155 \end{vmatrix}$ | | | | 28 24 |
| 10 | | 0 2 | | 773533 | | 226467 | 86788 | | 132113 | - | 355 153 | | | ale. | 20 |
| 10 | | 1 2 | | 773704 | | 226296 | 868152 | | 131848 | | 48 155 | 905552 | 34 | 81) | 16 |
| | | 3,2 | | 773875 | | 226125 | 868416 | 1 | 131584 | | 41 155 | | | 9 | 12 |
| | | 2 2 6 2 | | 774046 | | 225954 | 868680 | 1 | 131320 | | 34 156 | | | - | 8 |
| 96 | | | | 774217 | - | 225783 | 868943 | - | 131055 | | 28 156 | - | _ | 0.4 | 0 |
| 26 | | 43 | | 9.774388 774558 | | 10.225612 225442 | 869473 | | 10.130791 130527 | | 015 156 | | | 34 | 56 |
| 1 | | 3 3 | | 774729 | | 225271 | 86973 | | 130263 | | 008 156 | | | | 52 |
| 0 | | 23 | | 774899 | | 225101 | 87000 | | 129999 | | 102 156 | | 27 | 16 | 48 |
| 1 | | 63 | | 775070 | | 224930 | 87026 | | 129735 | | 196 156 | | | | 44 |
| | | 03 | | 775240 775410 | | 224760 224590 | 870529 870793 | -1 | 129471 | | 289 156 $383 156$ | | | | 40 36 |
| | | 83 | | 775580 | | 224420 | 87105 | 1 | 129207 128943 | | 77 156 | | | | 32 |
| | | 23 | | 775750 | | 224250 | 87132 | | 128679 | | 571 157 | | | | 28 |
| L | | 6 3 | | 775920 | | 224080 | | | 128415 | | 665 157 | | | | 24 |
| 1 | 40 | | 0 | 776090 | | 223910 | 87184 | | 128151 | | 759 15 | | | | 20 |
| | | 1 4 8 4 | | 776259 776429 | | 223741 -223571 | 872113 | | 127888 127624 | | 353 157 $347 157$ | | | | 16 |
| | | 2 4 | | 776598 | | 223402 | 872640 | | 127360 | | 041 15 | | | - | 8 |
| | | 6 4 | | 776768 | | 223232 | 872903 | 1 | 127097 | | 136 15 | | 16 | | 4 |
| 27 | | | | 9.776937 | 282 | 10.223063 | 9.87316 | 439 | 10.126833 | | | | | | . 0 |
| | | 4.4 | | 777106 | | 222894 | 873430 | | 126570 | | 324 15 | | | | 56 |
| | | 8 4 2 4 | | 777275 | 281 | 222725 | 873694 87395 | | 126306 126043 | | 19 157 513 157 | | | | 52 48 |
| | | 6 4 | | 777613 | | 222556 222387 | 874220 | | 125780 | | 508 158 | | | | 44 |
| - | | 0 3 | | 777781 | 281 | 222219 | 87448 | | 125516 | | 702 158 | | | - | 40 |
| н | | | 1 | ****** | | 222050 | | | 125253 | | 797 158 | | | | 36 |
| | | 8 5 | | 778119 | | 221881 | | | 124990 | | 392 158 | | | | 32 |
| | | | 3 54 | | | 221713 221545 | | | 124727 124464 | | 086 158 $081 158$ | | | _ | 28 |
| | | | 55 | | | 221376 | | | 124200 | | 176 158 | | | 14 | 20 |
| 1 | 4 | 4 3 | 56 | 778792 | | 221208 | | | 123937 | | 271 158 | | 4 | 9 | 16 |
| 1 | | | 57 | 778960 | 280 | 221040 | 87632 | 438 | 123674 | 0973 | 366 158 | 902634 | | | 12 |
| | | 6 | 58 | | | 220872 | | | 123411 | _ | 61 159 | | | | 8 |
| 28 | | 0 | | 779295 779463 | | 220705 220537 | 87685 87711 | | 123149 122886 | | 556 159 $551 159$ | | | 32 | 4 |
| = | _ | = : | - | | == | | | 100 | | | | | = | - | - |
| m. | | 0.1 | - | Cosine. | 13700 | Secant. | Cotang. | 1 | Tang. | Cosec | - 1 | Sine. | | m. | 8, |
| - | | - | | 18 | 15" | 1 43 | 1 12 1 | or 15" | 1 00 | A Is | 15" | egrees. | - | - | - |
| | . P | | | 2 | 30 | 85 | 13 | 30 | 132 | 1s 2 | 30 | 47 | | P. | |
| L | 8 0 | | | 3 | 45 | 128 | 3 | 45 | 198 | 3 | 45 | 70 | S | or | |

| 8 2 779798 279 220202 877640 438 122360 097842 159 9021 12 3 779966 279 220034 877903 438 122097 097937 159 9012 20 5 780300 278 219760 878428 438 121572 098128 159 9018 24 6 780467 278 219533 878691 438 121309 098224 159 9018 28 7 780634 278 219366 878953 437 121047 098319 159 9016 32 8 780806 278 219032 879478 437 120784 098415 159 9015 369 98060 278 219032 879474 437 120522 098510 159 9015 9015 9017 98702 160 9012 4812 781468 277 218666 879741 437 | 2. |
|--|---|
| No. Since D. Cosec. Tang. D. Cotang. Secant. D. Cosing. | 49 60 33 53 59 58 58 63 57 663 57 667 56 72 55 76 54 81 53 85 52 90 51 94 50 98 49 02 48 06 47 |
| 28 0 0 9.779463 279 10.220537 9.877114 438 10.122866 10.097651 159 9.9023 | 49 60 33 53 59 58 58 63 57 663 57 667 56 72 55 76 54 81 53 85 52 90 51 94 50 98 49 02 48 06 47 |
| 4 1 779681 279 220369 877377 438 122623 097747 159 9022 877640 438 122360 097842 159 9021 12 3779966 279 220034 877903 438 122097 097937 159 9020 15 780300 278 219700 878428 438 121572 098128 159 9013 28 780664 278 219366 878953 438 121309 908224 159 9013 32 8780801 278 219366 878953 437 121047 098319 159 9016 36 9 780968 278 219032 879478 437 120784 098415 159 9016 36 9 780968 278 219032 879478 437 120522 098510 159 9014 4010 781134 278 218668 879741 437 120522 098510 159 9014 4517 781468 277 | 53 59 58 58 58 58 58 59 57 67 56 54 81 53 85 52 90 51 94 50 98 49 02 48 06 47 |
| 8 2 779798 279 220202 877640 438 122360 097842 159 9021 12 3 779966 279 220034 877803 438 122097 097937 159 9020 20 5 780300 278 219500 878428 438 121572 098128 159 9013 24 6 780467 278 219533 878691 438 121309 098224 159 9017 28 7 780634 278 219533 878691 438 121309 098224 159 9017 32 8 780801 278 219362 879478 437 120784 098415 159 9014 40 10 781134 278 218668 879741 437 120522 098510 159 9014 41 781360 277 218699 880033 437 119970 098706 | 58 58 63 57 67 56 72 55 76 54 81 53 85 52 90 51 94 50 98 49 00 48 00 6 47 |
| 12 3 779966 279 220034 877903 438 122097 097937 159 9090 16 4 780133 279 219867 878428 438 121572 098128 159 9018 24 6 780467 278 219533 878691 438 121309 098224 159 9018 28 7 780634 278 219366 878953 437 121047 098319 159 9016 32 8 780861 278 219199 879216 437 120784 098415 159 9014 40 10 781134 278 218666 879741 437 120259 098606 160 9013 44 11 781301 277 218366 880565 437 119735 098798 160 9012 52 13 7816634 277 218508 88165 437 119742 09 | 63 57 67 56 72 55 76 54 81 53 85 52 90 51 94 50 98 49 02 48 06 47 |
| 16 | 67 56 72 55 76 54 81 53 85 52 90 51 94 50 98 49 02 48 06 47 |
| 20 5 780300 278 219700 878428 438 121572 098128 159 9018 28 7 780634 278 219366 878953 437 121047 098319 159 9016 32 8 780801 278 219199 879216 437 120784 098415 159 9016 36 9 780968 278 219199 879216 437 120522 098510 159 9014 44 11 781301 277 218699 880003 437 11997 098702 160 9012 378 378634 277 218366 880528 437 119735 098798 160 9012 52 13 781634 277 218366 880528 437 119472 098894 160 9011 55 14 781800 277 218366 880528 437 119472 098894 160 9011 55 14 781800 277 218366 880528 437 119472 098894 160 9011 55 14 781800 277 218366 880528 437 119472 098894 160 9011 55 14 781800 277 218366 880528 437 119472 098894 160 9011 55 14 781800 277 218366 880528 437 119472 098894 160 9011 55 14 781800 277 218366 880528 437 119472 098894 160 9011 18 18 18 18 18 18 18 | 72 55 76 54 81 53 85 52 90 51 94 50 98 49 02 48 06 47 |
| 24 6 780467 278 219533 878691 438 121309 098224 159 9017 28 7 780634 278 219199 879216 437 121047 098319 159 9016 36 9 780968 278 219199 879216 437 120784 098415 159 9014 40 10 781134 278 218866 879741 437 120525 098606 160 9013 48 12 781468 277 218532 880265 437 119997 098702 160 9012 48 12 781868 277 218366 880528 437 119735 098798 160 9012 56 14 781806 277 218366 880528 437 119170 098990 160 9012 90 15 9.781966 277 217868 881314 437 10.118948 | 76 54 81 53 85 52 90 51 94 50 98 49 02 48 06 47 |
| 28 7 780634 278 219366 878953 437 121047 098319 159 9016 32 8 780861 278 219199 879216 437 120784 098415 159 9014 36 9 780968 278 219032 879474 437 120522 098510 159 9014 44 11 781301 277 218669 880033 437 11997 098702 160 9012 48 12 781634 277 218366 880528 437 119973 098798 160 9012 52 13 781634 277 218366 880528 437 119735 098798 160 9012 5 13 781966 277 218366 880528 437 119210 098990 160 9012 9 0 15 9.781966 277 10.218034 9.81052 437 10 | 81 53 85 52 90 51 94 50 98 49 02 48 06 47 |
| 32 S 780801 278 219199 879216 437 120784 098415 159 9015 36 | 85 52 90 51 94 50 98 49 02 48 06 47 |
| 40 10 | 94 50 98 49 02 48 06 47 |
| 44 11 781301 277 218699 880003 437 119997 098703 160 9012 48 12 781468 277 218332 880265 437 119735 098798 160 9012 52 13 781634 277 218366 880528 437 119210 098990 160 9011 56 14 781806 277 218200 880790 437 119210 098990 160 9010 9 0 15 9.781966 277 10.218034 9.81052 437 10.118948 10.099086 160 9010 6 17 782298 276 217702 881576 437 118424 099278 160 9007 12 18 782649 276 217536 881839 437 118161 099374 160 9007 20 20 782796 276 217204 882363 436 117637 099567 161 9004 22 27 783127 | 98 49 02 48 06 47 |
| 48 12 781468 277 218532 880265 437 119735 098798 160 9012 52 13 781634 277 218366 880528 437 119472 098894 160 9012 56 14 781800 277 218200 880790 437 119210 098990 160 9010 9 0 15 9781966 277 10.218034 9.851052 437 11818948 10.099086 160 9008 8 17 782298 276 217702 881576 437 118424 099278 160 9007 12 18 782630 276 217536 881839 437 118424 099278 160 9007 16 19 782630 276 217370 882101 437 117637 099567 161 9002 20 20 7827961 276 217039 882625 436 117637 099567 161 9002 22 3 783127 276 <td>02 48 06 47</td> | 02 48 06 47 |
| 52 13 781634 277 218366 880528 437 119472 098894 160 9011 56 14 781800 277 218200 880790 437 119210 098990 160 9010 9 0 15 9.781966 277 10.218034 9.881052 437 10.118948 10.099086 160 9008 8 17 782298 276 217702 881576 437 118424 099278 160 9007 12 18 782464 276 217536 881839 437 118424 099278 160 9006 16 19 782630 276 217370 882101 437 117899 099471 160 9005 20 20 782796 276 217204 882363 436 117637 099663 161 9003 22 27 783127 276 216873 882887 436 117113 099760 161 9002 32 23 783292 275 | 06 47 |
| 56 14 781800 277 218200 880790 437 119210 098990 160 9010 9 0 15 9.781966 277 10.218034 9.881052 437 10.118948 10.099086 160 9.9009 160 9.9009 8 17 782298 276 217702 881576 437 118666 099182 160 9006 16 19 782630 276 217536 881839 437 118161 099374 160 9006 16 19 782630 276 217370 882101 437 117899 099471 160 9005 20 20 782796 276 217039 882625 436 117637 099667 161 9004 24 21 782961 276 216873 882887 436 117375 099667 161 9002 32 23 783292 275 216542 883410 436 116852 099856 161 9002 32 23 783292 275 216542 883410 436 116590 099953 161 9002 36 24 783458 275 216542 883410 436 116650 099953 161 9002 36 24 783458 275 216542 883410 436 116590 099953 161 9002 36 24 783458 275 216542 883419 436 116590 099953 161 9002 36 24 783458 275 216542 883419 436 116590 099953 161 9002 36 24 783458 275 216542 883419 436 116590 099953 161 9002 36 24 215543 215543 215888 88457 436 115543 100436 161 8995 36 27 27 215888 884457 436 115543 100436 161 8995 36 27 27 27 215888 884524 436 115543 100436 161 8995 37 784612 274 215388 885242 436 114497 100727 162 8992 38 784776 274 215224 885503 436 114497 | |
| 9 0 15 9.781966 277 | 1(311-0) |
| 4 16 782132 277 217868 881314 437 118686 099182 160 9008 8 17 782298 276 217702 881576 437 118424 099278 160 9007 12 18 782464 276 217536 881839 437 118161 099374 160 9006 16 19 782630 276 217304 882363 436 117637 099567 161 9004 24 21 782961 276 217039 882625 436 117375 099663 161 9002 28 22 783127 276 216873 882897 436 117113 099760 161 9002 32 23 783292 275 216678 883148 436 116550 099956 161 9001 36 24 783458 275 216377 883672 436 116590 099953 161 9001 44 26 783788 275 216377 883672 436 116328 100049 161 | |
| 8 17 782298 276 217702 881576 437 118424 099278 160 9007 12 18 782464 276 217536 881839 437 118161 099374 160 9006 16 19 782630 276 217370 882101 437 117899 099471 160 9006 20 20 782796 276 217204 882363 436 117637 099567 161 9004 24 21 782961 276 216873 882887 436 117375 099663 161 9003 28 22 783127 276 216873 882887 436 117375 099663 161 9002 32 23 783292 275 216542 883410 436 116550 099956 161 9001 40 25 783623 275 216542 883410 436 116328 100049 161 8998 48 27 783953 275 216047 884196 436 115804 100449 161 | |
| $\begin{array}{c ccccccccccccccccccccccccccccccccccc$ | |
| 16 19 782630 276 217370 882101 437 117899 099471 160 9005 20 20 782796 276 217204 882363 436 117637 099567 161 9004 24 21 782961 276 217039 882625 436 117375 099663 161 9003 28 22 783127 276 216873 882887 436 117113 099760 161 9002 36 24 783458 275 216542 883140 436 116550 099856 161 9001 40 25 783682 275 216542 883410 436 116590 099953 161 9001 48 27 783682 275 216612 883934 436 116590 099953 161 8999 48 27 783953 275 216212 883934 436 116590 099953 161 8993 52 28 784118 | |
| 20 20 782796 276 217204 882363 436 117637 099567 161 9004 24 21 782961 276 217039 882625 436 117375 099663 161 9003 32 23 783127 276 216873 882887 436 117113 099760 161 9002 32 23 783292 275 216708 883148 436 116652 099956 161 9001 36 24 783458 275 216377 883672 436 116590 099953 161 9000 40 25 783768 275 216377 883672 436 116328 100049 161 8993 48 27 783768 275 216047 884196 436 115504 10043 161 8995 52 28 784118 275 215882 884457 436 115543 100340 161 8995 5 29 784282 27 | |
| $\begin{array}{c ccccccccccccccccccccccccccccccccccc$ | |
| 28 22 783127 276 216873 882887 436 117113 099760 161 9002 32 23 783492 275 216708 883148 436 116652 099856 161 9001 36 24 783458 275 216542 883410 436 116590 099953 161 9000 44 26 783788 275 216212 883934 436 116328 100049 161 8998 48 27 783953 275 216047 884196 436 115804 100243 161 8997 52 28 784118 275 215882 884457 436 115504 100340 161 8996 56 29 784282 274 215718 884719 436 115281 100436 161 8996 4 31 784612 274 215388 885242 436 114758 <t< td=""><td></td></t<> | |
| $\begin{array}{cccccccccccccccccccccccccccccccccccc$ | |
| 40 25 783623 275 216377 883672 436 116328 100049 161 8999 44 26 783788 275 216212 883934 436 116066 100146 161 8993 48 27 783953 275 216047 884196 436 115804 100243 161 8997 52 28 784118 275 215882 884457 436 115543 100340 161 8996 56 29 784282 274 215718 884719 436 115281 100436 161 8995 0 0 30 9.784447 274 215388 885242 436 114758 100630 162 8993 4 31 784612 274 215388 885242 436 114758 100630 162 8993 1 2 33 784941 274 215224 885503 436 114497 100727 162 8992 1 2 33 784941 274 215059 885765 436 114235 100824 162 8991 <td>4437</td> | 4437 |
| $\begin{array}{c ccccccccccccccccccccccccccccccccccc$ | 47 36 |
| $\begin{array}{c ccccccccccccccccccccccccccccccccccc$ | 51 35 |
| 52 28 784118 275 215882 884457 436 115543 100340 161 8995 56 29 784282 274 215718 884719 436 115281 100436 161 8995 0 030 9.784447 274 10.215553 9.884980 436 1141758 100630 162 9.8994 4 31 784612 274 215388 885242 436 114758 100630 162 8993 8 32 784776 274 215224 885503 436 114497 100727 162 8992 12 33 784941 274 215059 885765 436 114235 100824 162 8991 16 34 785105 274 214895 886026 436 113974 100922 162 8990 20 35 785269 273 214731 886288 436 113712 101019 162 8989 24 36 785433 273 214403 886810 435 113451 101116 162 8988 | |
| $\begin{array}{c ccccccccccccccccccccccccccccccccccc$ | |
| $ \begin{array}{cccccccccccccccccccccccccccccccccccc$ | |
| 4 31 784612 274 215388 885242 436 114758 100630 162 8993 8 32 784776 274 215224 885503 436 114497 100727 162 8992 12 33 784941 274 215059 885765 436 114235 100824 162 8991 1 634 785105 274 214895 886026 436 113974 100922 162 8990 20 35 785269 273 214731 886289 436 113712 101019 162 8989 24 36 785433 273 214567 886549 435 113451 101116 162 8988 28 37 785597 273 214403 886810 435 113190 101213 162 8987 | |
| 8 32 784776 274 215224 885503 436 114497 100727 162 8992 12 33 784941 274 215059 885765 436 114235 100824 162 8991 1 634 785105 274 214895 886026 436 113974 100922 162 8990 20 35 785269 273 214731 886289 436 113712 101019 162 8989 24 36 785433 273 214567 886549 435 113451 101116 162 8988 28 37 785597 273 214403 886810 435 113190 101213 162 8987 | |
| 12 33 784941 274 215059 885765 436 114235 100824 162 8991 1 6 34 785105 274 214895 886026 436 113974 100922 162 8990 20 35 785269 273 214731 886288 436 113712 101019 162 8989 24 36 785433 273 214731 886549 435 113451 101116 162 8988 28 37 785597 273 214403 886810 435 113190 101213 162 8987 | |
| 16 34 785105 274 214895 886026 436 113974 100922 162 8990 20 35 785269 273 214731 886288 436 113712 101019 162 8989 24 36 785433 273 214567 886549 435 113451 101116 162 8988 28 37 785597 273 214403 886810 435 113190 101213 162 8987 | |
| 20 35 785269 273 214731 886288 436 113712 101019 162 8989 24 36 785433 273 214567 886549 435 413451 101116 162 8988 28 37 785597 273 214403 886810 435 113190 101213 162 8987 | |
| 24 36 785433 273 214567 886549 435 113451 101116 162 8988 28 37 785597 273 214403 886810 435 113190 101213 162 8987 | |
| 28 37 785597 273 214403 886810 435 113190 101213 162 8987 | |
| | 87 23 |
| | 39 22 |
| 36 39 78 59 25 273 214075 887333 435 112667 101408 162 8985 | |
| | 94 20 |
| | 97 19 |
| 48 42 786416 272 213584 888116 435 111884 101701 163 8982 | |
| 52 43 786579 272 213421 888377 435 111623 101798 163 8982 | |
| 56 44 786742 272 213258 888639 435 111361 101896 163 8981 | - |
| 1 0 45 9.786906 272 10.213094 9.888900 435 10.111100 10.101994 163 9.8980 | |
| | 08 14 |
| | 12 12 |
| 16 49 787557 271 212443 889943 435 110057 102386 163 8976 | |
| | 16 10 |
| 24 51 787883 271 212117 890465 434 109535 102582 164 8974 | |
| 28 52 788045 271 211955 890725 434 109275 102680 164 8973 | |
| 32 53 788208 271 211792 890986 434 109014 102778 164 8972 | 22 7 |
| 36 54 788370 270 211630 891247 434 108753 102877 164 8971 | 23 6 |
| 40 55 788532 270 211468 891507 434 108493 102975 164 8970 | 2.5 5 |
| 44 56 788694 270 211306 891768 434 108232 103074 164 8969 | |
| 48'57 788856 270 211144 892028 434 107972 103172 164 8968 | |
| 52.58 789018 270 210982 892289 434 107711 103271 164 8967 | |
| 56 59 | |
| | === |
| n. s. / Cosine. Secant. Cotang. Tang. Cosec. Sine. | / m |
| 3 Hours, or 52 Degrees. | |
| P. P. to 18 15" 41 18 15" 65 18 15" 24 | P. P. |
| 2 30 82 2 30 131 2 30 49 | |
| s or " 3 45 124 3 45 196 3 45 73 | |

| - | | _ | | - | | | - | | 1 | | | | _ |
|-----|------|----------|------------------|-------|---------------------|------------------|-----|---------------------|---------|-------------------------------------|--------------------|------|-----------|
| 1 | 6 | | TABL | | Lo | garithmic | | es, Tangen | its, | | | | |
| | | | | ours, | | 1 (1) | or | - | | 38 De | | | |
| m. | . S. | 1 | Sine. | D. | Cosec. | Tang. | D. | Cotang. | Secan | . D. | Cosine. | 'n | n. s. |
| 32 | 0 | 0 | 9.78934 | | 10.210658 | | | 10.107190 | | | | | |
| п | 4 | | 78950 | | 210496 | 893070 | | 106930 | | 67 165 | | | 56 |
| 1 | 8 | | 78966 | | 210335 | 893331 | | 106669 | | 65 165 | 896335 | | 52 |
| п | 18 | | 78982 78998 | | 210173 200012 | 893591 893851 | | 106409 106149 | | 64 165 63 165 | 896236 896137 | | 48 |
| | 20 | 5 | 79014 | | 209851 | 894111 | | 105889 | | 62 165 | 896038 | | 40 |
| | 21 | 6 | 79031 | | 209690 | 894371 | | 105629 | | 061 165 | 895939 | | 36 |
| П | 28 | 7 | 79047 | | 209529 | 894632 | | 105368 | | 60 165 | 895840 | | 32 |
| н | 32 | 8 | 79063 | | 209368 | 894892 | | 105108 | | 259 165 | 895741 | | 28 |
| | 36 | 9 | 79079 | 3 268 | 209207 | 895152 | 433 | 104848 | | 359 165 | 895641 | 51 | 24 |
| | | 10 | 79095 | | 209046 | 895412 | | 104588 | | 58 165 | 895542 | | 20 |
| 1 | 44 | | 79111. | | 208885 | 895672 | | 104328 | | 557 166 | 895443 | | 16 |
| | | 12 13 | 79127 | | 208725 208564 | 895932 896192 | | 104068 103808 | | 56 166 56 166 | 895343 895244 | | 12 |
| | | 14 | | | 208404 | 896452 | | 103548 | | 355 166 | 895145 | | -4 |
| 33 | - | _ | 9.79175 | | 10.208243 | | | 10.103288 | - | Distance | 9.895045 | - | - |
| 100 | | 16 | 79191 | | 208083 | | 433 | 103029 | | 55 166 | | | 56 |
| | | 17 | 79207 | | 207923 | 897231 | | 102769 | | 54 166 | 894846 | | 52 |
| | | 18 | 79223 | | 207763 | 897491 | | 102509 | | 54 166 | 894746 | | 48 |
| ш | 16 | 19 | 79239 | | 207603 | | | 102249 | | 354 166 | 894646 | 41 | 44 |
| E | | 20 | 79255 | | 207443 | 898010 | 433 | 101990 | | 54 166 | 894546 | | 40 |
| | 24 | | 79271 | | 207284 | 898270 | | 101730 | | 554 167 | 894446 | | 36 |
| | 28 | | 79287 | | 207124 | 898530 | | 101470 | | 554 167 | 894346 | | 32 |
| 1 | | 23 | 79303 | | 206965 | 898789 | | 101211 | | 54 167 | 894246 | | 28 |
| 1 | | 24 25 | 79319 | | 206805 206646 | 899049 899308 | | 100951 100692 | | 354 167 354 167 | 894146 894046 | | 24 20 |
| 10 | | 26 | 79351 | | 206486 | 899568 | | 100432 | | 54 167 | 893946 | | 16 |
| ŀ | 48 | | 793673 | | 206327 | 899827 | | 100173 | | 54 167 | 893846 | | 12 |
| | | 28 | 79383 | | 206168 | 900086 | | 099914 | | 55 167 | 893745 | | 8 |
| F | 56 | 29 | 79399 | | 206009 | 900346 | | 099654 | | 355 167 | 893645 | 31 | 4 |
| 34 | 0 | 30 | 9.79415 | 0 264 | 10.205850 | 9.900605 | 432 | 10.099395 | 10.1064 | 56 167 | 9.893544 | 30 2 | 6 0 |
| | | 31 | 794308 | 8 264 | 205692 | 900864 | 432 | 099136 | 1068 | 556 168 | | | 56 |
| | | 32 | 79446' | | 205533 | | | 098876 | | 557 168 | 893343 | | 52 |
| | 12 | | 79462 | | 205374 | | | 098617 | | 757 168 | | | 48 |
| | 16 | | 794784 | | 205216 | 901642 | | 098358 | | 358 168 | 893142 | | 44 |
| Г | 24 | 35 | 794949 | | 205058 204899 | 901901 | | 098099 097840 | | $059 168 \\ 060 168$ | 893041 892940 | | 36 |
| | 28 | | 79525 | | 204741 | 902419 | | 097581 | | 61 168 | 892839 | | 32 |
| | 32 | | 79541 | | 204583 | 902679 | (| 097321 | | 61 168 | 892739 | | 28 |
| Н | 36 | | 79557 | 5 263 | 204425 | 902938 | | 097062 | | 362 168 | 892638 | | 24 |
| | | 40 | 795733 | | 204267 | 903197 | | 096803 | | 64 168 | 892536 | | 20 |
| | 44 | 1 1 | 79589 | | 204109 | 903455 | | 096545 | | 665 169 | 892435 | | 16 |
| | | 42 | 796049 | | 203951 | 903714 | | 096286 | | 666 169 | 892334 | | 12 |
| | | 43 44 | 796200 796364 | | 203794 203636 | 903973 | | 096027 095768 | | $\frac{767}{368}$ $\frac{169}{169}$ | 892233 892132 | | 8 |
| 9 5 | - | | 9.79652 | - | | | - | | | | | | 4 |
| 35 | _ | 46 | 79667 | | 10.203479 203321 | 9.904491 | 431 | 10.095509 095250 | | 070 169 | 9.892030 891929 | | 5 0 56 |
| 1 | | 47 | 79683 | | 203321 | 904750 | | 093230 | | 173 169 | 891929 | | 52 |
| | | 48 | 79699 | | 203007 | 905267 | | 094733 | | 274 169 | 891726 | | 48 |
| 1 | | 49 | 797150 | 0 261 | 202850 | 905526 | | 094474 | | 376 169 | 891624 | | 44 |
| 1 | | 50 | 79730 | | 202693 | 905784 | 431 | 094216 | 1084 | 177 170 | 891523 | 10 | 40 |
| 6 | | 51 | 79746 | | 202536 | 906043 | | 093957 | | 579 170 | 891421 | | 36 |
| 1 | | 52 | 79762 | | 202379 | | | 093698 | | 81 170 | | | 32 |
| ш | | 53 54 | 79777 | | 202223 | | | 093440 | | 783 170 | | | 28 |
| ١. | | 55 | 79793 79809 | | 202066 201909 | | | 093181 | | 385 170 | | _ | 24 |
| 1 | | 56 | | | 201909 | | | 092923 092664 | | $087 170 \\ 089 170$ | | 4 | 20 |
| | | 57 | 79840 | | 201597 | | | . 092406 | | 91 170 | 890809 | | 12 |
| | 52 | 58 | 79856 | | 201440 | | | 092148 | | 93 170 | | -1 | 8 |
| | | 59 | 79871 | 6 260 | 201284 | 908111 | | 091889 | 1093 | 395 170 | 890605 | 1 | 4 |
| 36 | | 60 | 79887 | 2 260 | 201128 | 908369 | 430 | 091631 | 1094 | 197 170 | 890503 | 0'2 | 4 0 |
| m. | 8. | 7 | Cosine. | | Secant. | Cotang. | | Tang. | Cosec | | Sine. | / n | n. s. |
| | | | 3 H | ours, | | | or | | | 51 De | | - (- | |
| P | . P. | to | 18 | 15" | 40 | 18 | 15" | 65 | 1: | 15" | 25 | P | D 4 |
| 1 5 | or | 11 | 2 | 30 | 79 | 2 | 30 | 130 | 2 | 30 | 50 | P. | P. to |
| - | - | | 3 | 45 | 119 | 3 | 45 | 194 | 3 | 45 | 75 | 3 | |

| _ | | _ | | | | | | | | (1) | | | |
|----------------|----------|----------|------------------|------------|------------------|--------------------|-----------|------------------------------|----------------|--------|------------------|----|-------|
| | | | 2 Ho | TIPE | | and | Seco | ints. | 1. | 39 De | BLE V. | | .57 |
| m. | 8 | , | Sine. | D. | Cosec. | Tang. | D. | Cotang. | Secant. | 1 D. | Cosine. | 1 | m. , |
| $\frac{=}{36}$ | 0 | = | 9.798872 | 260 | 10.201128 | | 430 | 10.091631 | 10.10949 | 7 170 | 9.890503 | 60 | 51 |
| | 4 | 1 | 799028 | 260 | 200972 | 908628 | 430 | 091372 | . 10960 | 0 171 | 890400 | | 5 |
| | 8 | 2 | 799184 | 260 | 200816 | 908886 | | 091114 | 10970 | | 890298 890195 | | 5 4 |
| | 16 | 4 | 799339 799495 | | 200661 | 909144 | | 090856 090598 | 10980 | | 890093 | | 4 |
| | 20 | 5 | 799651 | 259 | 200349 | 909660 | 1 | 090340 | 11001 | 0 171 | 889990 | | 4 |
| | 24 | 6 | 799806 | | 200194 | 909918 | | 090082 | | | | | 3 |
| ľ | 28 32 | 7 8 | 799962 800117 | 259 259 | 200038 199883 | 910177 910435 | | 089823 089565 | 11021 | | 889785 889682 | | . 2 |
| 3 | 36 | 9 | 800272 | 258 | 199728 | 910693 | 430 | 089307 | 11049 | 1 171 | 889579 | 51 | 2 |
| | 40 | 10 | 800427 | 258 | 199573 | 910951 | | 089049 | 11052 | | | | 2 |
| ì | 44 | 11 12 | 800582 800737 | 258 258 | 199418 199263 | 911209 911467 | | 088791 088533 | 11062 | | | | 1 |
| | | 13 | 800892 | | 199108 | 911724 | | 088276 | 11083 | | | | E 1 |
| | 56 | | 801047 | 258 | 198953 | 911982 | | 088018 | 11093 | | | - | 0 |
| 37 | | | 9.801201 | 258 | 10.198799 | | | 10.087760 | | | | | |
| F. | 8 | 16 17 | 801356 801511 | 257 | 198644 193489 | 912498 912756 | | 087502 087214 | 11114 11124 | | | | 5 |
| 4 | 12 | 18 | 801665 | | 198335 | 913014 | | 086986 | 11134 | | | | . 4 |
| | 16 | | 801819 | | 198181 | 913271 | 429 | 086729 | 11145 | | | | 4 |
| Н | 20 24 | | 801973 802128 | | 198027 197872 | 913529 913787 | | 086471 086213 | 11155 | | | | 3 |
| - | 28 | | 802282 | | 197718 | 914044 | | 085956 | | | | | 3 |
| 2 | 32 | | 802436 | | 197564 | 914302 | | 085698 | | | | | . 2 |
| | | 24 25 | 802589 802743 | | 197411 197257 | 914560 914817 | 1 | 085440 085183 | 11197 | | | | 2 |
| | 44 | | 802897 | 256 | 197103 | 915075 | | 084925 | | | | | î |
| Н | 48 | 27 | 803050 | 256 | 196950 | 915332 | 429 | 084668 | 11228 | 32 173 | 887718 | 33 | 1 |
| | | 28 29 | 803204 | | 196796 | 915590 | | 084410 | | 6 173 | | | |
| 38 | | - | 9.803511 | 255 | 196643 | 915847 9.916104 | - | 0841 <i>5</i> 3 10.083896 | 11249 | _ | | | 22 |
| 30 | | 31 | 803664 | | 196336 | 916362 | | 083638 | | | | | 5 |
| | | 35 | 803817 | 255 | 196183 | 916619 | 429 | 083381 | 11280 | 2 174 | 887198 | 58 | 5 |
| | | 33 34 | | | 196030 | 916877 | | 083123 | | | | | 4 |
| ľ | | 35 | 804123 804276 | | 195877 195724 | 917134 917391 | | 082866 082609 | | | | | 4 |
| | 24 | 36 | 804428 | | 195572 | 917648 | | 082352 | 11322 | | | | 3 |
| п | | 37 38 | 804581 | 254 | 195419 | 917905 | | 082095 | 11339 | | | | 3 |
| Н | | 39 | | | 195266 195114 | 918163 918420 | | 081837 081580 | 11348 11353 | | | | 2 2 |
| | 40 | 40 | | | 194961 | 918677 | | 081323 | | | 886362 | 30 | 2 |
| | 44 | | 805191 | | 194809 | 918934 | | 081066 | | | | | 1 |
| | | 42 | | | 194657 194505 | 919191 919448 | | 080809 080552 | 11384 11395 | | | | 1 |
| | | 44 | | 253 | 194353 | 919705 | | 080295 | | | | | 8 |
| 39 | | | 9.805799 | | 10.194201 | 9.919962 | | 10.080038 | 10.11416 | 3 175 | 9.885837 | 15 | |
| | | 46 | | | 194049 | 920219 | 1 | 079781 | 11426 | | | | 5 |
| п | | 48 | | | 193897 193746 | 920476 920733 | 1 | 079524 079267 | 11437 11447 | | | | 5 |
| | 16 | 49 | | | 193594 | 920990 | | 079010 | | 1 2 . | | | 4 |
| | | 50 | | | 193443 | | | 078753 | | | | | 4 |
| | | 51 52 | | | 193291 193140 | | | 078497 078240 | | | | | 3 |
| | | 53 | | | 192989 | | | 077983 | | | | | 2 |
| П | | 54 | | | 192837 | | | 077726 | 11511 | 1 176 | 884889 | | 2 |
| | | 55 56 | | | 192686 192535 | | | 077470 | | | | | 2 |
| | | 57 | | | 192385 | | | 076956 | | | | | 1 |
| | 52 | 58 | 807766 | 251 | 192234 | 923300 | 428 | 076700 | 11553 | 1176 | 884466 | 2 | - |
| 40 | | 59 60 | | | 192083 | | | 076443 076187 | | | | | 20 |
| | | = | | 231 | 191933 | | 421 | | | = | | = | 20 |
| m. | . 8. | - | Cosine. | NIEC . | Secant. | Cotang. | 1 | Tang. | Cosec. | 50 D | Sine. | | m. |
| - | - | | 1 1s | 15" | 38 | 15 | or 15" | 64 | 1 1 1 | 50 De | grees. | | |
| | . P. | | 2 | 30 | 76 | 2 | 30 | 129 | 2 3 | 30 | 52 | P. | P. to |
| _ | , or | | 3 | 45 | 115 | 3 | 45 | 193 | 3 | 45 | 78 | S | or " |

| 1- | _ | | | | | - 11 | - | | | | | | |
|------|---------|-----|--------------------|-------|--------------------------|------------------|------------|------------------|------------------|-------|------------------|-----|----------|
| 58 | 3 | | TABL | | Lo | ogarithmi | | es, Tange | | | | | |
| | - | | | ours, | 1 Const | 4 Tona | or | . Consu | | | egrees. | | |
| m. | S. | _! | Sine. | D. | Cosec. | Tang. | D. | Cotang. | Secant. | D. | | | m. ! |
| 40 | 0 | 0! | 9.808067 808218 | | 10.191933 | | | 075930 | 110.11574 | | | | |
| | 8 | 2 | 808368 | 1 | 191632 | | | 075673 | | | | | 5 |
| 100 | 12 | 3 | 808519 | 1 | 191481 | | | 075417 | | 4 | | | 4 |
| | 16 | 4 | 808669 | | 191331 | | | 075160 | | | | | 4 |
| | 20 | 5 | 808819 | | 191181 | | | 074904 | | | | | 4 |
| | 21 | 6 | 808969 809119 | | 191031 | | | 074648 | | | | | 3 |
| | 32 | 8 | 809269 | | 190731 | | | 074135 | | | | | 2 |
| | 36 | 9 | 809419 | 249 | 190581 | 926122 | 427 | 073878 | 116703 | 3 178 | 883297 | | 2 |
| | - | 0 | 809569 | | 190431 | | | 073622 | | | | | 2 |
| | | 2 | 809718 | | 190282 | | | 073366 | | | | | 1 |
| | - | 3 | 810017 | | 189983 | | | 072853 | | | | | |
| | 56 1 | | 810167 | | 189833 | | | 072597 | | | | | |
| 41 | 0 1 | 5.9 | .810316 | 248 | 10.189684 | 9.927659 | 427 | 10.072341 | | | | 45 | 19 |
| | 4 1 | | 810465 | | 189535 | | | 072085 | | | | | 5 |
| | 8 1 | 7 | 810614 810763 | | 189386 189237 | | 427 | 071829 | | | | | 5 |
| | 61 | | 810703 | | 189237 | | | 071317 | 117771 | | | | 4 |
| , 2 | 20 2 | 0 | 811061 | | 188939 | | | 071060 | 117879 | 179 | 882121 | 40 | 4 |
| | | 1 | 811210 | | 188790 | | | 070804 | | | | | 30 |
| | 28 2 | | 811358 811507 | | 188642 | | | 070548 | | | | | 39 |
| | 32 2 | | 811655 | | 188493 18834 <i>5</i> | | | 070292 070036 | | | | | 24 |
| | 10 2 | | 811804 | | 188196 | | 426 | 069780 | | | | | 20 |
| | 14 2 | | 811952 | | 188048 | | | 069525 | 118523 | | | | 10 |
| | | 7 | 812100 | | 187900 | 930731 | 426 | 069269 | 118631 | | | | 1 12 |
| | 56 2 | 8 | 812348 | | 187752 187604 | 930987 931243 | 426 426 | 069013 068757 | 118739 118847 | | 881261 881153 | | . 4 |
| - | - | - | .812544 | | 10.187456 | | 426 | 10.068501 | 10.118954 | | | - | |
| 12 | 43 | | 812692 | | 187308 | | 426 | 068245 | 119062 | | | 29 | 56 |
| | 8 3 | | 812840 | | 187160 | | 426 | 067990 | 119170 | | 880830 | 28 | 52 |
| | 23 | | 812988 | | 187012 | | 426 | 067734 | 119278 | | 880722 | | 4.8 |
| | 63 | | 813135 | 10000 | 186865 | 932522 | 426 | 067478 | 119387 | | 880613 | | 44 |
| | 0 3 | | 813283 813430 | | 186717 186570 | 932778 933033 | 426 426 | 067222 066967 | 119495 119603 | | 880505 880397 | | 36 |
| | 83 | | 813578 | | 186422 | 933289 | 426 | 066711 | 119711 | | 880289 | | 32 |
| | 323 | | 813725 | | 186275 | 933545 | 426 | 066455 | 119820 | 181 | 880180 | 22 | 25 |
| | 6 3 | | 813872 | | 186128 | 933800 | 426 | 066200 | 119928 | | 880072 | | 24 |
| | 0 4 | | 814019 814166 | | 185981 185834 | 934056 934311 | 426 426 | 065944 065689 | 120037 120145 | | 879963 879855 | | 20 |
| | 84 | | 814313 | | 185687 | 934567 | 426 | 065433 | 120254 | | 879746 | | 12 |
| 5 | 24 | 3 | 814460 | | 185540 | 934823 | 426 | 065177 | 120363 | | 879637 | | 8 |
| | 6 4 | | 814607 | - | 185393 | 935078 | 426 | 064922 | 120471 | | 879529 | | 4 |
| 13 | | | 814753 | | 10.185247 | | 426 | 10.064667 | | | | | 17 (|
| 1. 1 | 4 4 8 4 | | 814900 815046 | 244 | 185100 | 935589 | 426 | 064411 | 120689 | 1 | 879311 879202 | | 56 |
| | 24 | | 815193 | | 184954 184807 | 935844 936100 | 426 426 | 064156 063900 | 120798 120907 | | 879093 | | 52 48 |
| 1 | 6 4 | 9 | 815339 | | 184661 | 936355 | 426 | 063645 | 121016 | 182 | 878984 | | 44 |
| | 05 | | 815485 | | 184515 | 936610 | | 063390 | | 182 | 878875 | | 40 |
| | 45 | | 815632 | | 184368 | | | 063134 | | | 878766 | | 36 |
| | 25 | | 815778 815924 | | 184222 184076 | 937121 937376 | | 062879 062624 | 121344 121453 | | 878656 878547 | 7 | 32 28 |
| | 6 5 | | 816069 | | 183931 | | | 062368 | 121562 | | 878438 | 6 | 24 |
| 4 | 0 5 | 5 | 816215 | 243 | 183785 | 937887 | 425 | 062113 | 121672 | 182 | 878328 | 5 | 20 |
| | 45 | | 816361 | | 183639 | 938142 | | 061858 | | | 878219 | 4 | 16 |
| | 85 | | 816507 816652 | | 183493 183348 | 938398 938653 | | 061602 061347 | 121891 122001 | | 878109 877999 | 3 | 12 8 |
| | 65 | | 816798 | | 183202 | 938908 | | 061347 | 122110 | | 877890 | 1 | 4 |
| 4.4 | 06 | 0 | 816943 | | 183057 | 939163 | | 060837 | 122220 | | 877780 | 0 1 | 6 0 |
| m. | S., | 7 | Cosine. | | Secant. | Cotang. | | Tang. | Cosec. | | Sine. | / r | n. s. |
| | | | 3 Ho | | | | or | | | Des | grees. | | - |
| P. P | . 10 | 1 | 18 | 15" | 37 | 18 | 15" | 64 | | 15" | 27 | p | P. to |
| 8 0 | | | 2 | 30 | 74 | 2 | 30 | 128 | 2 : | 30 | 54 | | or " |
| - | - | 1 | 3 | 45 | 111 | 3 | 45 | 192 | 3 | 45 | 81 | | |

| A | _ | _ | | | | | | | | | m | | _ | |
|--|----|-----|-----|----------|------|---------------------------|--|-------------------|--|-----------|-----|-------------------|----|-------|
| | _ | | | (| | , | and | | nts. | | | | _ | 59 |
| ## 0 0,58,16943 242 [10,183057 9,939165] 425 [10,060837] 10,122220 [183,9,877780] 00 [44] 817080 242 [182912] 939418] 425 [00,0327] 12430 [183] 877870] 85 5 82 817332] 242 [182021] 939928] 425 [00,0072] 12230 [183] 877870] 85 5 123 817379] 422 [182021] 939928] 425 [00,0072] 12230 [183] 877870] 85 5 123 817379] 422 [182021] 939928] 425 [00,0072] 122500 [183] 877830] 85 6 4 4 6 817532] 424 [182032] 939928] 425 [00,0072] 122500 [183] 877830] 85 6 4 4 4 6 817532] 424 [182032] 94043 425 [00,9306] 122580 [183] 87730] 85 4 4 6 817813] 241 [182032] 94044 425 [00,9306] 122580 [184] 87730] 85 4 6 817813] 241 [182032] 94044 425 [00,9306] 122580 [184] 87730] 85 4 6 818103] 241 [181733] 941458 425 [00,9376] 12230 [184] 876789] 94 1 181633] 941245 425 [00,9376] 12230 [184] 876789] 94 1 181633] 941245 425 [00,9376] 12331 [184] 876789] 94 1 181633] 941245 425 [00,9376] 12331 [184] 876789] 94 1 181633] 94125 425 [00,9376] 12331 [184] 876789] 94 1 181633] 94125 425 [00,9376] 12331 [184] 876789] 94 1 181633] 94125 425 [00,9376] 12332 [184] 876578] 94 1 181633] 94125 425 [00,9376] 12332 [184] 876578] 94 1 181633] 94125 425 [00,9376] 12332 [184] 876578] 94 1 181633] 94125 425 [00,9376] 12332 [184] 876578] 94 1 181633] 94125 425 [00,9376] 12332 [184] 876578] 94 1 181633] 94125 425 [00,9376] 12332 [184] 876578] 94 1 181633] 94125 425 [00,9376] 12332 [184] 876578] 94 1 181633 [18477] 94 | - | - 1 | / 1 | | | Corne | Tong | | Cotono | | | | 71 | m. s |
| 1 \$17088 \$227 \$182912 \$299418 \$425 \$060327 \$122300 \$183 \$77670.59 \$5 \$2 \$1817337 \$242 \$182767 \$99087 \$425 \$060072 \$122500 \$183 \$877450.57 \$4 \$1817347 \$241 \$182467 \$901031 \$425 \$059171 \$12560 \$183 \$877450.57 \$4 \$1817347 \$241 \$182187 \$910813 \$425 \$059171 \$12560 \$183 \$877450.57 \$4 \$20 \$4 \$1817547 \$411 \$182187 \$910814 \$425 \$059306 \$122770 \$184 \$877320.55 \$4 \$877120.55 \$4 \$877120.55 \$4 \$877120.55 \$4 \$877120.55 \$4 \$877120.55 \$4 \$877120.55 \$4 \$877120.55 \$4 \$877120.55 \$4 \$877120.55 \$4 \$877120.55 \$4 \$877120.55 \$4 \$877120.55 \$4 \$877120.55 \$4 \$877120.55 \$4 \$877120.55 \$4 \$877120.55 \$4 \$877120.55 \$4 \$4 \$4 \$877120.55 \$4 \$4 \$4 \$4 \$8 \$87677 \$4 \$4 \$4 \$4 \$4 \$4 \$4 | - | | | | | | | - | - | | _ | | | |
| 12 3 17373 242 18277 939673 425 060327 12240 183 877560 85 12 3 817379 242 182676 930183 425 059817 192660 833 877840 56 42 182676 930183 425 059817 192660 833 877840 56 42 42 42 42 50 50817 192660 833 877840 56 42 42 42 50 50817 192660 833 877840 56 42 42 42 50 50817 192660 833 877840 56 42 42 42 50 50817 192670 84 877840 56 42 42 42 42 50 50810 122800 184 877840 54 42 42 42 50 50810 122800 184 877840 54 42 42 42 50 50810 122800 184 877840 54 42 42 42 50 50810 122800 184 877840 52 42 42 42 42 42 50 50810 122801 184 876899 52 42 42 42 42 42 42 42 | 44 | | | | | | | | | 122330 | 183 | 877670 | | 56 |
| 12 3 | | | • | | _ | | | 1 | | | | | | 5% |
| 24 | | | | | | | | | | | | | | 48 |
| 24 0 817913 241 182042 94094 9425 059030 122990 184 877010 33 28 8 18103 241 181605 94104 425 058051 122990 184 877010 33 28 8 18103 241 181605 941014 425 058051 122990 184 877605 12 23 36 9 816247 241 181753 941458 425 058766 123101 184 876990 32 2 3 3 14 58 48 18 18 18 18 18 18 18 18 18 18 18 18 18 | 1 | | | | | | | | | | | The second second | | 4(|
| 17 179.6 241 189.02 94.0940 42.5 0.590.51 129.90 184 8770.10 33 32 8 1810.3 241 1810.87 941.04 42.5 0.5870.6 123.21 184 87678.9 11 23 34 34 11 1810.08 941.714 42.5 0.588.86 12.33.22 184 87678.9 11 24 41 1818.35 240 1811.39 942.22 42.5 0.571.77 123.54 184 8766.56 49 1811.39 942.22 42.5 0.577.77 123.54 184 8766.56 49 1811.39 942.22 42.5 0.577.77 123.54 184 8766.57 48 18 18 18 18 18 18 18 | | | | 2.7 | | | | | Andrew Street World | | | | | 36 |
| 38 | E | | | | | | | | | | | | | 38 |
| A | | 32 | 8 | | 241 | | and the second second | 11111111 | | | | | | 28 |
| ## 111 | | | | | | | | | | | | | | 24 |
| Ass. 12 818681 240 | | | | | | | | | | | | | | 16 |
| Second Color Seco | | | | | | | | | | 1000 | | | | 12 |
| ## 10 15 9.819113 240 10.180887 9.942988 425 10.057012 10.123875 185 9.876125 45 16 18 199401 240 180.059 943494 425 0.566757 12.9986 185 875094 43 16 18 19401 240 180.059 943494 425 0.566757 12.4996 185 875094 43 16 18 19689 239 180.031 944007 425 0.55539 124.198 185 875679 43 16 19 19689 239 180.031 944007 425 0.55538 124.198 185 8756854 14 14 18 18 1976 239 180.031 14 14 14 0.55229 124.658 185 875457 14 14 18 18 1976 239 17.9890 944.711 424 0.55229 124.658 185 875457 30 32 28 28 28 20120 239 17.9890 944.711 424 0.55229 124.658 185 875457 37 33 36 48 804.06 239 17.9937 94.5021 424 0.54719 124.678 185 875427 37 36 42 80.9093 238 17.9307 94.5021 424 0.54719 124.678 185 875427 37 42 42 42 42 42 42 42 4 | | 52 | 13 | | | The state of the state of | | | THE PERSON NAMED IN COLUMN | | | | | |
| 4 16 819257 240 180743 943243 425 056502 124096 85 876014 44 5817 819401 240 180039 943488 425 056502 124096 85 875904 43 5817 819401 240 180039 943488 425 056502 124096 85 875904 43 5818 12 18 819545 299 180455 943752 425 056524 124207 185 875934 42 42 42 42 42 42 42 42 42 42 42 42 42 | _ | | - | | | | | | | | | | | 4 |
| S 17 S 1940 240 180599 943498 425 056502 124096 185 875904 43 16 19 819689 293 180311 944007 425 055993 124318 185 875793 42 42 42 42 42 42 42 4 | 45 | | | | | | | | | 10.123875 | 185 | 9.876125 | | 15 (|
| 19 18 819545 239 180455 943752 425 0.56248 124207 1855 875078 421 1619 819669 239 180311 944007 425 0.55993 124318 185 875673 41 4 4 20 20 819832 239 180168 944262 425 0.55738 124429 185 875571 40 4 4 20 20 20 819832 239 179380 944771 424 0.55229 124632 185 875459 39 3 32 23 820263 239 179780 944571 424 0.55229 124632 185 875348 38 3 2 23 820263 239 179787 945036 424 0.54974 124108 185 875439 39 3 36 24 820406 239 179559 945281 424 0.54974 124108 185 875237 37 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 | 7 | | | | | | | | | | | | | 59 |
| 16 19 819689 239 180311 944007 425 055993 124318 185 875682 14 24 21 819976 239 180021 944262 425 055738 124429 185 875571 10 4 42 42 42 42 42 42 42 | | | | | | The second second | | | | | | | | 1 48 |
| 24 21 819976 239 180021 944517 425 05528 12452 185 875459 39 3 28 28 820120 239 179787 945072 424 054974 124103 185 875237 37 2 2 3 6 24 820406 239 179787 945072 424 054974 124103 185 875237 37 2 3 6 24 820406 239 179594 945281 424 054719 124874 186 875126 36 875126 | | 16 | 19 | 819689 | 239 | | 944007 | 425 | | | | | _ | 4.4 |
| 28 22 820120 239 179980 944771 424 0.55229 124652 185 875348185 3 3 223 82063 239 179373 745026 444 0.54974 124768 185 875327 37 2 2 3 2 3 6 24 8 20406 239 179594 945281 424 0.54974 12468 185 875327 37 2 2 4 0.54974 124768 185 875327 37 2 2 4 0.54974 124768 185 875328 3 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 | | | | | | | | | | | | | | 4(|
| 32 23 820263 239 179737 945076 424 054974 124763 185 87523737 2 36 24 820406 239 179594 945281 424 054719 124874 186 875126 36 2 40 25 820550 238 179450 945535 424 054455 124986 186 875014 35 44 26 820693 238 179307 945790 424 054210 125097 186 874073 34 1 48 27 820836 238 179164 946045 424 053955 125209 186 874680 32 56 29 821122 238 178878 946554 424 053701 125320 186 874680 32 56 29 821122 238 178878 946554 424 053701 125320 186 874680 32 43 18 211407 238 178878 946554 424 053701 125320 186 874680 32 43 18 211407 238 178593 947063 424 052937 125656 186 8745454 28 32 8 32 821550 238 178450 947318 424 052632 125768 187 874344 29 52 12 33 821693 237 178807 947572 424 052428 125879 187 874121 27 4 16 34 821835 237 178165 947826 424 052428 125879 187 874121 27 4 24 36 822120 237 177880 948336 424 05140 126328 187 87309265 42 24 36 822120 237 177880 948336 424 05140 126328 187 87309265 42 28 37 82262 237 177454 94909 424 05140 126328 187 873622 33 32 38 822404 237 177454 94909 424 050091 126552 187 873484 21 24 4 4 4 18 822830 236 177312 949353 424 050647 126666 187 873335 20 24 4 4 4 18 822830 236 177312 949353 424 050647 126666 187 873348 21 2 4 4 4 6 823529 236 176745 950510 424 05091 126552 187 873484 21 2 4 4 6 823529 236 176745 950510 424 05091 126552 187 873484 21 2 4 4 6 823529 236 176745 950510 424 049884 127002 188 872999 17 56 44 18 822852 236 176745 950510 424 049884 127002 188 872999 17 56 44 18 822852 236 176745 950510 424 049884 127002 188 872999 17 56 44 18 822852 236 176745 950510 424 049884 127002 188 872999 17 56 44 18 822852 236 176745 950510 424 049884 127002 188 872999 17 56 44 18 822852 236 176745 950510 424 049884 127002 188 872999 17 56 44 18 822852 236 176745 950510 424 049884 127002 188 872999 17 56 44 18 822852 236 176745 950510 424 049884 127002 188 872999 17 56 44 18 822852 236 176745 950510 424 049884 127002 188 872999 17 56 44 18 822852 236 176745 950510 424 049884 127092 188 872999 17 56 44 18 82882 1235 176779 951388 424 048679 127458 188 98729712 15 13 24 18 82882 1235 176779 951 | | | | | | | | | | | | | | 32 |
| 36 24 | 1 | | | | | | | | | | | | | 25 |
| ## 42 6 820693 238 179307 945790 424 054210 125097 186 87490334 1 48 27 820836 238 179164 946045 424 053955 125209 186 87479133 1 1 1 1 1 1 1 1 1 | E | | | 820406 | | | 945281 | 424 | | | | | | 2 |
| 1980 | | | | | | | | | | | | | | 20 |
| Second S | | | | | | The second second | | | | | | | | 19 |
| Secondary Seco | | | | | | | | | | | | | | |
| ## 311 \$21407 238 178593 947063 424 052937 125656 186 874344 29 52 83 821550 238 178450 947318 424 052682 125768 187 874232 28 52 52 52 52 52 52 5 | | | | | | | | | | | | and the second | _ | 4 |
| 8 32 821550 238 178450 947318 424 052682 125768 187 874232 28 12 33 821693 237 178307 947572 424 052428 125879 187 87412127 4 16 34 821835 237 178165 947826 424 052174 125991 187 874009 26 4 187 874572 424 052174 125991 187 874009 26 4 187 874572 424 052174 125991 187 874009 26 4 187 874572 424 052174 125991 187 874009 26 4 187 874572 424 36 822120 237 177890 948336 424 051664 126216 187 873734 24 36 822120 237 1777596 948844 424 051156 126440 187 873560 22 2 36 39 822546 237 1777596 948844 424 051156 126440 187 873560 22 2 36 39 822546 237 177759 949907 424 050901 126552 187 873448 21 2 4 040 822688 236 177312 949333 424 050647 126666 187 873335 20 2 4 4 4 18 822830 236 177702 9499607 424 050138 126797 187 873223 19 1 5243 823114 236 176886 950116 424 049884 127002 188 872998 17 5644 823255 236 176745 950370 424 049630 127115 188 872885 16 4 6 823539 236 1767603 9.950625 424 0409375 10.127228 188 9.872772 15 13 446 823539 236 176603 9.950625 424 049121 127341 188 8728659 14 5 8 47 823680 235 176320 951133 424 048867 127453 188 872855 14 5 8 47 823680 235 176320 951133 424 048867 127453 188 872855 14 5 8 48 823812 235 176379 951388 424 049121 127341 188 872659 14 5 8 47 823680 235 176379 951388 424 049121 127341 188 872659 14 5 8 47 823680 235 176379 951388 424 048104 127792 188 872208 10 4 245 184245 235 175755 952150 424 049104 127 127453 188 8728577 15 13 16 49 823963 235 176379 951388 424 048104 127792 188 872208 10 4 245 184245 235 175755 952150 424 049104 127 127453 188 8728577 15 13 16 49 823963 235 175355 952150 424 049104 127 127453 188 8728577 15 13 14 14 14 14 14 14 14 14 14 14 14 14 14 | 46 | 0 | 30 | 9.821265 | 238 | 10.178735 | 9.946808 | 424 | | 10.125544 | 186 | | | |
| 12 33 | | | | | | | | | | | | | | 56 |
| 16 34 821835 237 178165 947826 424 052174 125991 187 874009 26 42 20 35 821977 237 178023 948081 424 051919 126104 187 873896 25 42 28 37 82202 237 177789 948336 424 051664 126216 187 873784 24 28 37 82202 237 177759 948844 424 051156 126440 187 873560 22 23 32 38 822404 237 177596 948844 424 051156 126440 187 873560 22 24 040 822688 236 177312 949353 424 050901 126552 187 873448 21 24 040 822688 236 177312 949353 424 050901 126552 187 873348 21 24 040 822688 236 177170 949607 424 050393 126777 187 873335 20 24 049630 127114 286 176886 950116 424 049884 127002 188 872998 17 16745 1 | | | | | | | | | | | | | | 59 |
| 20 35 821977 237 178023 948081 424 051919 126104 187 873896 25 44 36 822120 237 177880 948836 424 051664 126216 187 873784 24 3 28 37 82262 237 177738 9488590 424 051410 126328 187 873672 23 3 23 8 822404 237 177756 948844 424 051416 126328 187 873560 22 2 36 39 822546 237 177454 949099 424 050901 126552 187 873448 21 2 40 40 822688 236 177312 949353 424 050647 126665 187 873335 20 2 44 44 18 22830 236 177170 949607 424 050393 126777 187 873223 19 1 48 42 822972 236 177028 949862 424 050138 126890 188 873110 18 52 43 823114 236 176886 950116 424 049884 127002 188 872998 17 56 44 823255 236 176745 950370 424 049630 127115 188 872865 16 47 0 45 9.823397 236 10.176603 9.950625 424 049630 127115 188 872865 16 46 823539 236 176461 950879 424 049881 127341 188 8726591 14 8 42 823821 235 176320 951133 424 048867 127453 188 872547 13 51 48 823821 235 176179 951388 424 048867 127453 188 872547 13 51 48 823821 235 176179 951388 424 048867 127453 188 872547 13 52 45 18 824245 235 175575 952150 424 048061 127792 188 872208 10 42 45 18 824245 235 175575 952150 424 047850 127905 189 872905 9 32 52 8243866 235 175614 952405 424 047850 127905 189 872905 9 32 52 824686 235 175514 952405 424 047850 127905 189 872905 9 32 52 824686 235 175514 952405 424 047850 127905 189 872905 9 32 52 824686 235 175514 952405 424 047850 127905 189 872905 9 32 52 824686 235 175514 952405 424 047850 127905 189 871986 7 2 40 55 824808 234 1755051 952150 424 047850 127905 189 871986 7 2 40 55 824808 234 1755051 95313 424 047087 128245 189 871868 7 2 40 55 824808 234 1755051 953141 423 046537 128813 189 871864 1 48 56 824949 234 175051 953167 423 046637 128472 189 871868 7 2 40 55 824808 234 1755051 953431 423 046537 128813 189 871861 1 5 65 9825371 234 174489 954437 423 046531 128813 189 871861 1 5 65 9825371 234 174489 954437 423 046531 128813 189 871861 1 5 65 9825371 234 174489 954437 423 045563 128927 190 871073 012 1 18 15" 28 82571 234 174489 954437 423 045563 128927 190 871073 012 1 18 15" 28 82571 234 174489 954437 423 045563 128927 190 8710 | | | | | | | | | | | | | | 44 |
| 28 37 82262 237 177738 948590 424 051410 126328 187 873672 23 32 38 822404 237 177596 948844 424 051156 126440 187 873560 22 23 63 9 822546 237 177454 949099 424 050901 126552 187 873448 21 24 126665 187 873353 20 24 14 41 822830 236 177312 949353 424 050647 126665 187 873335 20 24 14 41 822830 236 177170 949607 424 050393 126777 187 873223 19 125 43 823114 236 176886 950116 424 04984 127002 188 873110 18 125 43 823114 236 176886 950116 424 04984 127002 188 872998 17 17654 44 68 823539 236 176745 950370 424 049630 127115 188 872865 16 176745 950370 424 049630 127115 188 872865 16 176745 950370 424 049630 127115 188 872865 16 176745 950370 424 049630 127115 188 872865 16 176461 950879 424 049121 127341 188 872659 14 54 12 48 823821 235 176379 951388 424 048612 127566 188 872434 12 48 823821 235 176379 951388 424 048612 127566 188 872434 12 48 823862 235 176037 951642 424 048367 127453 188 872547 13 52 12 48 823862 235 176037 951642 424 048368 127679 188 872931 11 4 16 49 823963 235 176037 951642 424 048368 127679 188 872321 11 4 16 49 823963 235 1756149 951388 424 048612 127566 188 872434 12 4 16 49 823963 235 1756149 951896 424 048104 127792 188 872928 10 4 24 51 824245 235 175575 952150 424 048360 127905 189 872095 9 3 28 52 824386 235 1756149 952405 424 047360 127905 189 872095 9 3 28 52 824386 235 1756149 952405 424 047360 127905 189 872095 9 3 28 52 824386 234 175519 953167 423 046633 128329 189 871868 7 2 36 54 824668 234 175332 952913 424 047087 128245 189 871868 7 2 36 54 824668 234 175532 952913 424 047087 128245 189 871868 7 2 36 54 824668 234 175499 953167 423 046679 128472 189 871868 7 2 36 55 825230 234 174469 953437 423 046579 128472 189 871864 1 5 5 5 5 825230 234 174469 953437 423 046579 128472 189 871864 1 5 5 5 5 825230 234 174469 953437 423 046579 128472 189 871864 1 5 5 5 5 825230 234 174489 954437 423 045563 128927 190 871073 0 12 12 12 18 18 18 18 18 18 18 18 18 18 18 18 18 | 1 | | | | | | | | | | | | | 4(|
| 32 38 822404 237 177596 948844 424 0551156 126440 187 873560 22 2 36 39 822546 237 177454 949099 424 050901 126552 187 873448 21 2 4 40 40 822688 236 177312 949353 424 050647 126665 187 873335 20 1 48 42 822972 236 1771028 949862 424 050393 126777 187 873223 19 1 48 42 822972 236 177028 949862 424 050138 126890 188 873110 18 52 43 823114 236 176886 950116 424 049884 127002 188 872998 17 56 44 823255 236 176745 950370 424 049630 127115 188 872865 16 47 045 9.823397 236 10.176603 9.950625 424 049630 127115 188 872865 16 47 045 9.823397 236 10.176603 9.950625 424 049630 127115 188 872865 16 47 823639 236 176461 950879 424 049121 127341 188 872859 14 5 8 47 823680 235 176320 951133 424 048667 127453 188 872547 13 5 12 48 823821 235 176179 951388 424 048612 127566 188 872434 12 4 16 49 823963 235 176037 951642 424 048368 127679 188 872331 11 4 20 50 824104 235 175896 951896 424 04804 127792 188 872321 11 4 20 50 824104 235 175896 951896 424 04804 127792 188 872298 10 4 24 51 824245 235 175155 952150 424 047850 127905 189 872995 9 3 28 52 824386 235 175614 952405 424 047341 128132 189 871868 7 2 2 3 5 824668 234 175333 952913 424 047857 128019 189 871981 8 3 2 53 824527 235 175473 952659 424 047341 128132 189 871868 7 2 2 3 6 5 8 82530 234 174470 953929 423 046677 128425 189 87155 6 2 4 4 56 821949 234 175051 953421 423 046579 128472 189 87155 6 2 4 4 56 821949 234 175051 953421 423 046579 128472 189 87155 8 4 1 4 4 56 821949 234 175051 953421 423 046579 128472 189 87155 8 4 1 4 4 56 821949 234 175051 953421 423 046579 128472 189 87155 8 4 1 4 4 56 821949 234 174679 953167 423 046335 128927 190 871073 012 18 18 18 18 18 18 18 18 18 18 18 18 18 | | | | | | | | | | | | | | 30 |
| 36 39 822546 237 | | | | | | | | | Annual Control of the | | | | | 32 |
| 40 40 822688 236 177312 949353 424 050647 126665 187 873335 20 44 44 11 822830 236 1771170 949607 424 050393 126777 187 873223 19 1 48 42 822972 236 177028 949862 424 050138 126890 188 873110 18 52 43 823114 236 176886 950116 424 049884 127002 188 872988 17 56 44 823255 236 176745 950370 424 049630 127115 188 872865 16 47 045 9.823397 236 10.176603 9.950625 424 10.049375 10.127228 188 9.872772 15 13 4 46 823539 236 176461 950879 424 049121 127341 188 872865 16 8 47 823680 235 176320 951133 424 048867 127453 188 872547 13 512 48 823821 235 176179 951388 424 048612 127566 188 872434 12 4 16 49 823963 235 176037 951642 424 048358 127679 188 872321 11 4 20 50 824104 235 175896 951896 424 048104 127792 188 872321 11 4 20 50 824104 235 175896 951896 424 048104 127792 188 872321 11 4 20 50 824104 235 175896 951896 424 047341 128132 189 871981 8 32 53 824527 235 1755755 952150 424 047350 127905 189 872095 9 3 28 52 824386 235 175614 952405 424 047341 128132 189 871981 8 3 2 53 824527 235 175473 952659 424 047341 128132 189 871981 8 3 2 53 824527 235 175473 952659 424 047341 128132 189 871868 7 2 3 6 54 824668 234 175332 952913 424 047087 128245 189 87155 6 2 4 6 5 8 824909 234 175192 953167 423 046833 128359 189 871641 5 2 5 5 8 82530 234 175470 953929 423 046071 128699 189 871414 3 1 5 6 5 9 825371 234 174489 953437 423 046579 128472 189 87155 6 2 4 6 6 8 82531 234 174489 953437 423 046579 128472 189 87155 6 2 4 6 6 8 82531 234 174489 953437 423 046579 128472 189 871528 4 1 4 6 6 6 8 825511 234 174489 953437 423 046579 128472 189 87155 6 2 4 6 6 6 8 825511 234 174489 953437 423 046579 128472 189 871575 6 2 6 6 6 8 825511 234 174489 953437 423 045563 128927 190 871073 0 12 6 6 6 8 825511 234 174489 953437 423 045563 128927 190 871073 0 12 6 6 6 8 825511 234 174489 953437 423 045563 128927 190 871073 0 12 6 6 6 8 825511 234 174489 953437 423 045563 128927 190 871073 0 12 6 6 6 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 | | | | | | A COLUMN TO SERVICE | THE RESERVE AND ADDRESS OF THE PERSON NAMED IN COLUMN TWO IN COLUMN TO ADDRESS OF THE PERSON NAMED IN COLUMN TO ADDRESS | The second second | | | | | | 24 |
| 48 42 822972 236 177028 949862 424 0550138 126890 188 873910 18 52 43 823114 236 176866 950116 424 049884 127002 188 872998 17 5644 823255 236 1767445 950370 424 049630 127115 188 872865 16 47 045 9.823397 236 10.176603 9.950625 424 10.049375 10.127228 188 9.872772 15 13 446 823539 236 176461 950879 424 049121 127341 188 872659 14 5 8 47 823680 235 176320 951133 424 048867 127453 188 872547 13 12 48 823821 235 176179 951388 424 048612 127566 188 872434 12 4 16 49 823963 235 176037 951642 424 048048 127792 188 872831 11 4 20 50 824104 235 175896 951896 424 048104 127792 188 872208 10 4 24 511 824245 235 175755 952150 424 047850 127905 189 872095 9 3 28 52 824386 235 175614 952405 424 047850 127905 189 872095 9 3 28 52 824386 235 175614 952405 424 047850 127905 189 871981 8 3 253 824527 235 175473 952659 424 047341 128132 189 871868 7 2 3 6 54 824668 234 175332 952913 424 047087 128245 189 871755 6 40 55 824808 234 175031 953421 423 046379 128472 189 871641 5 2 48 57 825090 234 174910 953675 423 046325 128586 189 871414 3 1 56 59 825371 234 174629 954183 423 046579 128472 189 871528 4 1 4 6 6 825371 234 174629 954183 423 046579 128472 189 871528 4 1 4 6 6 6 825371 234 174629 954183 423 046571 128813 189 871641 5 2 6 6 59 825371 234 174629 954183 423 045563 128927 190 871073 012 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 | Ε. | | | | | | | | | | | | | 20 |
| 52 43 823114 236 176886 950116 424 049884 127002 188 872998 17 56 44 823255 236 176745 950370 424 049630 127115 188 872865 16 47 045 9.823397 236 10.176603 9.950625 424 10.049375 10.127228 188 9.872772 15 13 4 46 823539 236 176461 950879 424 049121 127341 188 872659 14 5 8 47 823680 235 176320 951133 424 048667 127453 188 872659 14 5 12 48 823821 235 176179 951388 424 048612 127566 188 872434 12 4 16 49 823963 235 176037 951642 424 048358 127679 188 872921 11 4 20 50 824104 235 175896 951896 424 048104 127792 188 872808 10 42 451 824245 235 175755 952150 424 047850 1277905 189 872095 9 3 28 52 824386 235 175614 952405 424 047850 127905 189 871981 8 3 3 2 53 824527 235 175473 952659 424 047341 128132 189 871868 7 2 3 6 54 824668 234 175332 952913 424 047087 128246 189 87155 6 2 40 55 824808 234 175051 953421 423 046833 128359 189 871641 5 2 4 4 56 824949 234 175051 953421 423 0466579 128472 189 87155 6 2 4 8 57 825090 234 174910 953675 423 046325 128586 189 871414 3 1 56 59 825371 234 174629 954183 423 046579 128472 189 871584 1 5 5 6 59 825371 234 174629 954183 423 046579 128472 189 871575 1 2 6 5 9 825371 234 174629 954183 423 046579 128472 189 871584 1 1 174629 954183 423 045563 128927 190 871073 012 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 | | | | | | | The second second second | | | | | | | 10 |
| 56 44 823255 236 | | | | | | | | | | | | | | 12 |
| 47 0 45 9.823397 236 | | | | | | | | | | | | | _ | . 4 |
| 4 46 823539 236 176461 950879 424 049121 127341 188 872659 14 58 47 823680 235 176320 951133 424 048867 127453 188 87254713 58 1248 823821 235 176179 951388 424 048612 127566 188 672434 12 48 1649 823963 235 176037 951642 424 048368 127679 188 872321 11 40 12759 188 872321 11 40 12759 188 872321 11 40 12759 188 872321 11 40 12759 188 872321 11 40 12759 189 87209 10 40 12759 189 87209 10 40 12759 189 87209 10 40 12759 189 87209 10 40 12759 189 87209 10 40 12759 189 87209 10 40 12759 189 87209 10 40 12759 189 87209 10 40 12759 128019 189 87198 18 180 12759 128019 189 871868 70 128019 189 8718 | 47 | _ | - | | | | | | | | | | _ | - |
| 12 48 823821 235 176179 951388 424 048612 127566 188 872434 12 4 1649 823963 235 176037 951642 424 048358 127679 188 872321 11 4 2 2 5 5 824104 235 175896 951896 424 048104 127792 188 872321 11 4 2 5 1 824245 235 175755 952150 424 047850 127905 189 872095 9 3 2 8 5 2 824386 235 175614 952405 424 047850 127905 189 871981 8 3 2 5 3 824527 235 175473 952659 424 047341 128132 189 871868 7 2 3 6 5 4 824668 234 175332 952913 424 047087 128245 189 87155 6 2 4 0 5 5 824808 234 175192 953167 423 046833 128359 189 871641 5 2 4 0 5 5 824808 234 175051 953421 423 046579 128472 189 871528 4 1 4 5 6 824949 234 175051 953421 423 046579 128472 189 871528 4 1 4 5 6 824949 234 174070 953167 423 046325 128586 189 871414 3 1 5 2 5 8 825230 234 174770 953929 423 046071 128699 189 871301 2 5 6 5 9 825371 234 174629 954437 423 045817 128813 189 871187 1 4 8 0 60 825511 234 174489 954437 423 045563 128927 190 871073 012 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 | 1 | | | | | 176461 | 950879 | 424 | 049121 | 127341 | 188 | 872659 | 14 | 56 |
| 16 49 823963 235 176037 951642 424 048358 127679 188 872321 11 4 20 50 824104 235 175896 951896 424 048104 127792 188 872208 10 4 24 51 824245 235 1755755 952150 424 047850 127905 189 872095 9 3 28 52 824386 235 175614 952405 424 047505 128019 189 871981 8 3 253 824527 235 175473 952659 424 047341 128132 189 871868 7 2 36 54 824668 234 175332 952913 424 047087 128245 189 871656 6 2 40 55 824808 234 175192 953167 423 046833 128359 189 871641 5 4 5 6 821949 234 175051 953421 423 046679 128472 189 871528 4 1 4 56 821949 234 175051 953421 423 046579 128472 189 871528 4 1 5 5 5 8 82530 234 17410 953675 423 046325 128586 189 871414 3 1 5 5 5 8 825371 234 174629 954183 423 046071 128699 189 871301 2 5 6 5 5 825371 234 174489 954437 423 045563 128927 190 871073 0 12 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 | | | | | | | | | | | | | | 52 |
| 20 50 824104 235 175896 951896 424 048104 127792 188 872208 10 24 51 824245 235 175755 952150 424 047850 127905 189 872095 9 3 28 52 824386 235 175614 952405 424 047595 128019 189 871981 8 3 32 53 824527 235 175473 952659 424 047341 128132 189 871868 7 2 356 54 824668 234 175332 952913 424 047087 128245 189 871868 7 2 40 55 824808 234 175192 953167 423 046833 128359 189 871641 5 2 44 56 824949 234 175051 953421 423 046579 128472 189 871528 4 1 48 57 825090 234 174910 953675 423 046325 128586 189 871414 3 1 52 58 825230 234 174770 953929 423 046071 128699 189 871301 2 56 59 825371 234 174770 953929 423 045817 128699 189 871301 2 56 59 825371 234 174489 954183 423 045817 128813 189 871187 1 48 060 825511 234 174489 954437 423 045563 128927 190 871073 0 12 128 128 128 128 128 128 128 128 128 | 1 | | _ | | | | | | | | | | | 44 |
| 24 51 824245 235 175755 952150 424 047850 127905 189 872095 9 3 28 528 824386 235 175674 952405 424 047595 128019 189 871981 8 3 32 53 824527 235 175473 952659 424 047341 128132 189 871868 7 2 36 54 824668 234 175332 952913 424 047087 128245 189 871555 6 2 40 55 824808 234 175192 953167 423 046833 128359 189 871641 5 2 44 56 824949 234 175051 953421 423 046579 128472 189 871528 4 1 48 57 825090 234 174910 953675 423 046325 128586 189 871444 3 1 52 58 825230 234 174770 953929 423 046071 128699 189 871301 2 56 59 825371 234 174770 953929 423 04567 128813 189 871187 1 48 060 825511 234 174489 954437 423 045563 128927 190 871073 0 12 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 | | | | | | | | | | | | | 10 | 40 |
| 32 53 824527 235 175473 952659 424 047341 128132 189 871868 7 2 36 54 824668 234 175332 952913 424 047087 128245 189 871755 6 2 2 4 055 824808 234 175192 953167 423 046833 128359 189 871641 5 2 4 4 56 824949 234 175051 953421 423 046579 128472 189 871528 4 1 48 57 825090 234 174910 953675 423 046325 128586 189 871414 3 1 52 58 82530 234 174770 953929 423 046071 128699 189 871301 2 56 55 825371 234 174629 954183 423 045817 128813 189 87187 1 48 060 825511 234 174489 954437 423 045563 128927 190 871073 0 12 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 | 11 | | | | | 175755 | 952150 | | | 127905 | 189 | 872095 | | 36 |
| 36 54 824668 234 175332 952913 424 047087 128245 189 871755 6 2 40 55 824808 234 175192 953167 423 046833 128359 189 871641 5 2 44 56 824949 234 175051 953421 423 046579 128472 189 871528 4 1 48 57 825090 234 174910 953675 423 046325 128586 189 871414 3 1 52 58 825230 234 174770 953929 423 046071 128699 189 871301 2 56 59 825371 234 174770 953929 423 046071 128699 189 871301 2 48 060 825511 234 174489 954437 423 045517 128813 189 871187 1 48 0 60 825511 234 174489 954437 423 045563 128927 190 871073 0 12 128 128 128 128 128 128 128 128 128 | | | | | | | | | | | | | | 32 |
| 40 55 824808 234 175192 953167 423 046833 128359 189 871641 5 2 44 56 824949 234 175051 953421 423 046579 128472 189 871528 4 1 1 48 57 825090 234 174910 953675 423 046325 128586 189 871414 3 1 52 58 825230 234 174770 953929 423 046071 128699 189 871301 2 56 59 825371 234 174770 953929 423 046071 128699 189 871301 2 48 0 60 825511 234 174489 954437 423 045817 128813 189 871187 1 1 48 0 60 825511 234 174489 954437 423 04563 128927 190 871073 0 12 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 | | | | | | | | | | | | | | 28 |
| 44 56 824949 234 175051 953421 423 046579 128472 189 871528 4 1 48 57 825090 234 174910 953675 423 046325 128586 189 871414 3 1 52 58 825230 234 174770 953929 423 046071 128699 189 871301 2 56 59 825371 234 174709 954183 423 045817 128813 189 871187 1 48 0 60 825511 234 174489 954183 423 045817 128927 190 871073 0 12 1280 1280 1280 1280 1280 1280 1280 | | | | | | | | | | | | | | 20 |
| 52 58 825230 234 174770 953929 423 046071 128699 189 871301 2 56 59 825371 234 174629 954183 423 045817 128813 189 871187 1 48 0 60 825511 234 174489 954437 423 045563 128927 190 871073 0 12 m. s. / Cosine. Secant. Cotang. Tang. Cosec. Sine. / m. s 3 Hours, or 48 Degrees. P. P. to 2 30 71 2 30 71 2 30 56 P. P. t. or 2 2 30 56 P. P. t. or 3 40 2 2 30 56 P. P. P. t. or 3 40 2 2 30 56 P. P. P. t. or 3 40 2 2 30 56 P. P. P. t. or 3 40 2 2 30 56 P. P. P. t. or 3 40 2 2 30 56 P. P. P. t. or 3 40 2 2 30 56 P. P. P. t. or 3 40 2 2 30 56 P. P. P. t. or 3 40 2 2 30 56 P. P. P. t. or 3 40 2 2 30 56 P. P. P. t. or 3 40 2 2 30 2 2 2 30 2 2 2 30 2 2 2 30 2 2 2 30 2 2 2 30 2 2 2 30 2 2 2 2 | 1 | 44 | 56 | | | 175051 | 953421 | 423 | 046579 | 128472 | 189 | 871528 | 4 | 16 |
| 56 59 825371 234 174629 954183 423 045817 128813 189 871187 1 48 0 60 825511 234 174489 954437 423 045563 128927 190 871073 0 12 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 | 1 | | | | | | | | | | | | | 12 |
| 48 0 60 825511 234 174489 954437 423 045563 128927 190 871073 0 12 | - | | | | | | - | | | | | | | 4 |
| Mar. Cosine. Secant. Cotang. Tang. Cosec. Sine. m. s | 48 | | | | | | | | | | | | | |
| 3 Hours, or 48 Degrees. P. P. to 2 30 71 2 30 127 2 30 56 P. P. to 3 0 71 2 30 127 2 30 56 | = | | - | | | | | | | | _ | | | |
| P. P. to 1s 15" 36 1s 15" 64 1s 15" 28 P. P. to 5 or " 2 30 71 2 30 127 2 30 56 P. P. to 5 or " | - | 0. | - | | urs- | becana | Cotang. | or | rang. | | De | | | 210 0 |
| Sor" 2 30 71 2 30 127 2 30 56 P. P. T. TO | - | D | 1 | | | 1 36 | 18 | | 64 | | | | 10 | n |
| 3 45 107 3 45 191 3 45 84 801 | | | | 2 | 30 | 71 | 2 | 30 | 127 | 2 , 3 | 30 | 56 | | |
| | 1_ | | | 3 | 45 | 107 | 3 | 45 | 191 | 3 4 | 5 | 84 | 0 | 51 |

| 1 | - | _ | - | TABLE | . 37 | To | wawithmi. | Sin | s, Tangen | 40 | | | - | - |
|---|----|----------|----------|--------------------|------|------------------|------------------|-----------|---------------------|---------|------------------------|------------------|-----|------------|
| H | 6 | <u> </u> | | 2 Ho | | Lu | garrennin | or | - Tangen | us, | 42 De | OTTO OF | | - |
| ı | m. | S | 1 | Sine. | D. | Cosec. | Tang. | D. | Cotang. | Secant | | Cosine. | 1/1 | m. s. |
| | 48 | _ | = | | | 10.174489 | | 423 | | | | | | |
| ı | 40 | 0 | 0 | 9.825511 825651 | 233 | 174349 | 9.954437 | 423 | 10.045563 045309 | 10.1289 | 27 190 40 190 | | | 12 0 56 |
| ı | | 8 | 2 | | 233 | 174209 | 954945 | | 045055 | | 54 190 | | | 52 |
| ı | | 12 | 3 | | 233 | 174069 | 955200 | 423 | 044800 | 1292 | 68 190 | 870732 | 57 | 48 |
| ı | | 16 | 4 | | 233 | 173929 | 955454 | | 044546 | | 82 190 | | | 44 |
| ı | 4 | 20 24 | 5 | | | 173789 | 955707 | | 044293 | | 96 190 | | | 40 |
| ı | | 28 | 7 | 826351 826491 | | 173649 173509 | 955961 956215 | | 044039 043785 | | 10 190 24 190 | | | 36 32 |
| ı | | 32 | 8 | 826631 | | 173369 | 956469 | | 043531 | | 39 190 | | | 28 |
| I | | 36 | 9 | 826770 | | 173230 | 956723 | | 043277 | | 53 191 | | | 24 |
| ı | | 40 | 10 | 826910 | | 173090 | 956977 | 423 | 043023 | | 67 191 | | | 20 |
| ı | | 44 | 11 | 827049 827189 | | 172951 172811 | 957231 957485 | | 042769 042515 | | 82 191 96 191 | 869818 869704 | | 16 12 |
| ı | | | 13 | | | 172672 | 957739 | | 042313 | | 11 191 | 869589 | | 8 |
| ı | | 56 | | 827467 | 232 | 172533 | 957993 | | 042007 | | 26 191 | 869474 | | 4 |
| I | 49 | 0 | 15 | 9.827606 | 232 | 10.172394 | 9.958246 | 423 | 10.041754 | 10.1306 | 40 191 | 9.869360 | 15 | 11 0 |
| ı | | | 16 | 827745 | 232 | 172255 | 958500 | 423 | 041500 | 1307 | 55 191 | 869245 | | 56 |
| ı | | | 17 | 827884 | | 172116 | 958754 | | 041246 | | 70 191 | 869130 | | 52 |
| 1 | | 12 16 | | 828023 828162 | | 171977 171838 | 959008 959262 | | 040992 040738 | | 85 192 00 192 | | | 48 |
| 1 | | 20 | | 828301 | | 171699 | 959202 | | 040138 | | 15 192 | | | 40 |
| I | | 24 | 21 | 828439 | | 171561 | 959769 | | 040231 | | 30 192 | | | 36 |
| J | | 28 | | 828578 | | 171422 | 960023 | | 039977 | | 45 192 | | | 32 |
| ı | | 32 | | 828716 | | 171284 | 960277 | | 039723 | | 60 199 | | | 28 24 |
| ı | | 40 | | 828855 828993 | | 171145 171007 | 960531 | | 039469 039216 | | 76 192 $91 192$ | | | 20 |
| 1 | η. | 44 | | | | 170869 | 961038 | | 038962 | | 07 192 | | | 16 |
| ı | | 48 | 27 | 829269 | | 170731 | 961291 | | 038709 | | 22 193 | | | 12 |
| 1 | | 52 | | | | 170593 | 961545 | | 038455 | | 38 193 | | | 8 |
| ı | - | 56 | | 829545 | | 170455 | 961799 | | 038201 | | 53 193 | 1 | - | 4 |
| | 50 | | 30 31 | 9.829683 | | 10.170317 | | | 10.037948 | | | 9.867631 | | |
| ı | | | 32 | 829821 829959 | 229 | 170179 170041 | 962306 962560 | | 037694 037440 | | $85 193 \\ 01 193$ | | | 56 52 |
| ı | | 12 | | | | 169903 | 962813 | | 037187 | | 17 193 | - 2.0 | | 48 |
| ı | 8. | 16 | | 830234 | | 169766 | 963067 | | 036933 | 1328 | 33 193 | 867167 | 26 | 44 |
| ı | | 20 | | 830372 | | 169628 | 963320 | | 036680 | | 19 193 | | | 40 |
| ı | | 24 28 | | 830509 830646 | | 169491 169354 | 963574 963827 | 1 | 036426 036173 | | 65 194 81 194 | | | 36 |
| ı | | 32 | | | | 169216 | 964081 | | 035919 | | 97 194 | | | 28 |
| ı | | 36 | | | | 169079 | 964335 | | 035665 | | 14 194 | | | 24 |
| ı | | | | | | 168942 | 964588 | | 035412 | | 30 194 | | | 20 |
| ı | | 44 | | 831195 | | 168805 | 964842 | | 035158 | | 47 194 | | | 16 |
| 1 | | 52 | | 831332 831469 | | 168668 168531 | 965095 965349 | | 034905 034651 | | 63 194 $80 194$ | | | 8 |
| ı | | | 44 | | | 168394 | 965602 | 1 . | 034398 | | 96 195 | | 16 | 4 |
| | 51 | 0 | _ | 9.831742 | | 10.168258 | | | 10.034145 | | | 9.865887 | 15 | 9 0 |
| 1 | | 4 | 46 | 831879 | 228 | 168121 | 966109 | 422 | 033891 | 1342 | 230 195 | | | 56 |
| I | | | 47 | 832015 | | 167985 | | | 033638 | | 47 195 | | | 52 |
| 1 | | 12 16 | | 832152 | | 167848 167712 | 966616 966869 | | 033384 | | $64 195 \\ 81 195$ | | | 48 |
| 1 | | 20 | | | | 167575 | | | 032877 | | 98 195 | | | 40 |
| 1 | | 24 | 51 | 832561 | | 167439 | | | 032624 | 1348 | 15 195 | 865185 | 9 | 36 |
| 1 | 1 | 28 | | 832697 | 227 | 167303 | 967629 | | 032371 | 1349 | 32 195 | 865065 | | 32 |
| 1 | | 32 | | | | 167167 | | | 032117 | | 50 195 | | | 24 |
| 1 | | 40 | | | | 167031 166895 | | | 031864 031611 | | 67 196 84 196 | | | 20 |
| 1 | | 44 | | | | 166759 | | | 031357 | | 02 196 | | 4 | 16 |
| | 1 | 48 | | 833377 | 226 | 166623 | 968896 | 422 | 031104 | 1355 | 19 196 | 864481 | 3 | 12 |
| 1 | | | 58 | | | 166488 | | | 030851 | | 37 196 | | | 8 |
| | 52 | | 59 60 | | | 166352 166217 | | | 030597 030344 | | 55 196 73 196 | | 1 0 | 8 0 |
| 1 | _ | | = | | | | | 422 | | | | | | |
| | m. | s. | | Cosine. | 1376 | Secant. | Cotang. | | Tang. | Cosec | | Sine. | | m. s. |
| | - | | | l ls | 15" | 34 | 18 | or 15" | 63 | 18 | 47 De | grees. | | |
| 1 | | P. or | | 2 | 30 | 69 | 2 | 30 | 127 | 2 | 30 | 58 | | P. to |
| | - | Ul | | 3 | 45 | 103 | 3 | 45 | 190 | 3 | 45 | 87 | S | or " |

| | | | | | . 2001 | and | Seca | nts. | (Charles) | TA | BLE V. | | 6 | 51 |
|-----|----------|------------|--------------------|------------|---------------------|------------------|-----------|---------------------|------------------|-------|------------------|-----|----|-----|
| | | _ | 2 Ho | urs, | | | or | | | 13 De | grees. | | | |
| m. | S. | 1 | Sine. | D. | Cosec. | Tang. | D. | Cotang. | Secant. | D. | Cosine. | - | m. | 1 |
| 52 | 0 | | 9.833783 | | 10.166217 | | 422 | 10.030344 | | | | _ | 8 | 5 |
| | 4 8 | 1 2 | 833919 834054 | | 166081 165946 | | | 030091 029838 | 13599 13610 | | | | | 5 |
| 1 | 12 | 3 | 834189 | | 165811 | 970416 | | 029584 | | | | | ? | 4 |
| Э. | 16 | 4 | 834325 | | 165675 | | | 029331 | 13634 | | | | | 4 |
| | 20 | 5 | 834460 834595 | | 165540 165405 | | | 029078 | | | | | | 3 |
| | 28 | 7 | 834730 | | 165270 | | 422 | 028571 | 13669 | | | | Я | 3 |
| | 32 | 8 | 834865 | | 165135 | | | 028318 | | | | | | 2 |
| Ħ. | 36 | 9 | 834999 835134 | 224 | 165001 164866 | | 422 | 028065 027812 | | | | | | 000 |
| | | 11 | 835269 | 224 | 164731 | 972441 | 422 | 027559 | | | | | 4. | ì |
| r | 48 | | 835403 | | 164597 | 972694 | | 027306 | | | | | | 1 |
| | | 13 | 835538 | 224 | 164462 | | 422 | 027052 | 13741 | | | | | |
| 53 | 56 | | 835672 9.835807 | 224 | 164328 10.164193 | | 422 | 026799 10.026546 | 13752 | _ | | - | 7 | - |
| ,, | | 16 | 835941 | 224 | 164059 | | 422 | 026293 | | | | | 4 | 5 |
| | | 17 | 836075 | 223 | 163925 | | | 026040 | | | | | 14 | E |
| N. | 12 | 18 | 836209 | 223 | 163791 | | | 025787 | 13800 | | 861996 861877 | | | 4 |
| II. | | 20 | 836343 836477 | 223 | 163657 163523 | | | 025534 025281 | 13812 13824 | | | | | 4 |
| | 24 | 21 | 836611 | 223 | 163389 | 974973 | 422 | 025027 | 13836 | 2 199 | 861638 | 39 | | 3 |
| | 28 | | 836745 | 223 | 163255 | | | 024774 | 13848 | | | | | 9 |
| | 32 36 | | 836878 837012 | 223 | 163122 162988 | | | 024521 024268 | 13860 13872 | | | | | 04 |
| | | 25 | 837146 | | 162854 | | 422 | 024015 | 13883 | | | | | 9 |
| | | 26 | 837279 | 222 | 162721 | 976238 | | 023762 | 13895 | | | | | 1 |
| н | 48 | | 837412 | 222 | 162588 | | 422 | 023509 | 13907 | | 860922 860802 | | | 1 |
| | 56 | | 837546 837679 | 222 | 162454 162321 | 976744 976997 | | 023256 023003 | 13919 13931 | | | | | |
| 54 | - | _ | 9.837812 | 222 | 10.162188 | | | 10.022750 | | - | | - | 6 | - |
| | 4 | 31 | 837945 | 222 | 162055 | | | 022497 | 13955 | | | | ŭ | 8 |
| | | 32 | 838078 | | 161922 | | | 022244 | | | | | | 1 |
| ı | 12 | | 838211 838344 | 221 | 161789 161656 | | | 021991 | 13979 13991 | | | | 2 | 4 |
| | | 35 | 838477 | 221 | 161523 | | | 021485 | | | | | | 4 |
| | 24 | | 838610 | 221 | 161390 | | | 021232 | | | 859842 | 24 | | |
| | 28 | | 838742 838875 | 221 221 | 161258 161125 | | 422 | 020979 020726 | | | 859721 859601 | | | |
| | 36 | | 839007 | 221 | 160993 | | | 020120 | | | 859480 | | | 1 |
| | 40 | | 839140 | 220 | 160860 | | 422 | 020220 | 14064 | | 859360 | | | |
| | | 41 | 839272 | 220 | 160728 | | | 019967 | 14076 | | 859239 | | 73 | - 1 |
| | 48 | | 839404 839536 | 220 | 160596 160464 | | 422 | 019714 019462 | 14088 14100 | | 859119 858998 | | | 1 |
| | 56 | | 839668 | | 160332 | | | 019209 | | | 858877 | | - | |
| 55 | 0 | 45 | 9.839800 | 220 | 10.160200 | | 421 | 10.018956 | 10.14124 | 4 202 | 9.858756 | 15 | 5 | - |
| | | 46 | 839932 | 220 | 160068 | | | 018703 | | | | | | |
| | 12 | 47 | 840064 840196 | | 159936 159804 | | - | 018450 018197 | 14148 14160 | | | | | |
| | 16 | | 840328 | 219 | 159672 | | | 017944 | | | | | | |
| | 20 | 4.1 | 840459 | | 159541 | | | 017691 | | | 858151 | 10 | | 4 |
| | 24 28 | | 840591 840722 | | 159409 159278 | | | 017438 | | | | | | 1 |
| | 32 | | | | 159146 | | | 017186 016933 | | | | | | |
| | 36 | 54 | 840985 | 219 | 159015 | 983320 | | 016680 | | | 857665 | 6 | | 3 |
| | 40 | | | | 158884 | | | 016427 | 14245 | | | | 4 | 9 |
| | 44 48 | 57 | 841247 841378 | | 158753 158622 | | | 016174 | | | | | | |
| | 52 | 58 | 841509 | | 158491 | | | 015669 | | | | | 6 | • |
| | 56 | 59 | 841640 | 218 | 158360 | 984584 | 421 | 015416 | 14294 | 4 203 | 857056 | 1 | | |
| 56 | 0 | 6 0 | 841771 | 218 | 158229 | 984837 | 421 | 015163 | 14306 | 6 203 | 856934 | 0 | 4 | |
| n. | S. | 1 | Cosine. | | Secant. | Cotang. | | Tang. | Cosec. | | Sine | 1 | m. | |
| | | | 3 Ho | urs, | 1 99 | 18 | or 15" | 1 69 | | 16 De | grees. | | | _ |
| | P. | | 2 | 30 | 33 | 2 | 30 | 63 | 1 ^s 2 | 30 | 30 | | P. | |
| 8 | or | - | 3 | 45 | 100 | 3 | 45 | 190 | 3 | 45 | 90 | 1 8 | or | 11 |

| 62 | _ | TABLE | V. ! | Logarith | nic Sines. | Tar | gents, and | Secan | ts. | | | | |
|---------------|-----------|--------------------|-------|---------------------|-------------------|------------|---------------------|-------|--|--|-----|-------|----------|
| - | | | ours, | -0 | | or | | | | grees. | | | |
| m. s | - | Sine. | D. | Cosec. | Tang. | D. | Cotang. | Secan | | | | m. | S. |
| 56 0 | 1 | 9.84177 | | 10.158229 158098 | The second second | 421 | 10.015163 014910 | | 066 203 188 203 | | | 4 | 56 |
| . 8 | | 842033 | 1 - | 157967 | 985343 | | 014657 | | 310 204 | | | | 52 |
| 12 | | 842163 | | 157837 | | | 014404 | | 432 204 | | | | 48 |
| 16 | | 842294 842424 | | 157706 157576 | 985848 986101 | 421 | 014152 013899 | | 554 204 677 204 | | | | 44 |
| 24 | 6 | 84255 | | 157445 | 986354 | 421 | 013646 | 143 | 799 201 | 856201 | 54 | | 36 |
| 28 32 | | 842684 842813 | | 157315 | | | 013393 013140 | | 922 204 044 204 | | | | 32 28 |
| 36 | | 842946 | 100 | 157185 157054 | | 421 | 013140 | | 167 204 | | | | 24 |
| 4() | 1 | 843076 | | 156924 | 987365 | | 012635 | | 289 205 | | | | 20 |
| 44 | | 843206 843336 | | 156794 156664 | | 421 | 012382 012129 | | 412 205 535 205 | | | | 16 12 |
| 52 | 1 1 | 843466 | 1 | 156534 | 988123 | 421 | 011877 | 144 | 658 205 | 855342 | 17 | | 8 |
| 56 | - | 843593 | | 156405 | | | 011624 | | 781 204 | | 1 | - | 4 |
| 57 0 | | 9.843725 843855 | | 10.156275 156145 | | 421 421 | 10.011371 011118 | | 904 205 027 205 | | | 3 | 0 56 |
| | 17 | 843984 | | 156016 | | 421 | 010866 | | 150 205 | | 2 1 | 80 | 52 |
| | 18 | 844114 | 1 | 155886 | | 421 | 010613 | | 273 206 | | | 86 | 48 |
| | 19 20 | 844243 | | 155757 155628 | 989640 989893 | | 010360 | | 397 206 520 206 | | | | 44 |
| 24 | 21 | 84450 | 215 | 155498 | 990145 | 421 | 009855 | 145 | 644 206 | 854356 | 39 | | 36 |
| | 25 | 844631 | | 155369 | 990398 990651 | | 009602 009349 | | 76 7 20 6 891 206 | | | | 32 |
| | 23 24 | 844760 | 1 | 155240 155111 | 990903 | 421 | 009349 | | 014 206 | | | | 24 |
| 40 | 25 | 845018 | | 154982 | 991156 | 421 | 008844 | | 138 206 | | | 0.1 | 20 |
| 44 | 26 | 845147 | | 154853 154724 | | | 008591 008338 | | 262 206 386 207 | | | | 16 |
| | 28 | 845403 | | 154595 | | | 008086 | | 510 207 | | | =0, | 8 |
| | 29 | 845533 | | 154467 | 992167 | 421 | 007833 | | 634 207 | - | | - | 4. |
| | | 9.845662 | 1 | 10.154338 | | | 10.007580 | | | | | 2 | °0 |
| | 31 32 | 845790 845919 | 1 | 154210 154081 | 992672 992925 | 421 421 | 007328 | 2000 | 882 207 006 207 | | | 8 | 56 52 |
| 12 | 33 | 816047 | 214 | 153953 | 993178 | 421 | 006822 | 147 | 131 207 | 852869 | 27 | 35 | 48 |
| 16 | 34 35 | 846175 846304 | | 153825 153696 | 993430 993683 | | 006570 | | 255 207 380 207 | | | Si. | 44 |
| | 36 | 846439 | | 153568 | | | 006064 | | 504 208 | | | 81 | 36 |
| | 37 | 846560 | | 153440 | | | 005811 | | 629 208 | | | | 32 |
| | 38 39 | 846688 | | 153312 153184 | | | 005559 005306 | | 753 208 878 208 | | | | 28 |
| 40 | 40 | 84694 | 1 213 | 153056 | 994947 | 421 | 005053 | 148 | 003 208 | 851997 | 50 | | 20 |
| 44 | 41 | 847071 847199 | 1 | 152929 152801 | 995199 995452 | | 004801 004548 | | 128 208 253 208 | | | 80 | 16 |
| | 43 | 847327 | | 152673 | 995705 | 421 | 004346 | | 378 208 | | | al. | 8 |
| 56 | - | 847454 | - | 152546 | 995957 | 421 | 004043 | 148 | 503 209 | 851497 | 16 | | 4 |
| | 45 46 | 9.847589 847709 | | 10.152418 | 9.996210 | | 10.003790 | | | | | 1 | 0 |
| | 47 | 847836 | | 152291 152164 | | 421 | 003537 003285 | | 754 2 09 8 7 9 20 9 | | | | 56 52 |
| - 12 | 48 | 847964 | 212 | 152036 | 996968 | 421 | 003032 | 149 | 004 209 | 850996 | 12 | | 48 |
| | 4.9 50 | 848091 848218 | | 151909 151782 | | 421 | 002779 | | 130 20 9 255 2 09 | | | | 44 |
| 24 | | 848345 | | 151655 | | | 002321 | | 381 209 | | | | 36 |
| | 52 | 848478 | | 151528 | 997979 | 421 | 002021 | 149 | 507 210 | 850493 | | | 32 |
| | 53 54 | 848599 848726 | | 151401 151274 | | | 001769 001516 | | 632 210 758 210 | | | | 28 24 |
| 40 | 55 | 848858 | 211 | 151148 | 998737 | 421 | 001263 | 149 | 884 210 | 850116 | 5 | | 20 |
| | 56 57 | 848979 849100 | | 151021 | | | 001011 | | 010 210 | | | | 16 |
| | 58 | | | 150894 150768 | | | 000758 | | 136 210 262 210 | A COLUMN TO THE REAL PROPERTY AND ADDRESS OF THE PARTY AND ADDRESS OF T | | | 12 |
| 56 | 59 | 849359 | 211 | 150641 | 999747 | 421 | 000253 | 1503 | 389 210 | 849611 | 1 | 1 | 4 |
| - | 60 | - | 211 | | 10.00000 | 421 | 000000 | | 515 210 | | | 0 | 0 |
| m. s. | | Cosine. | 01275 | Secant. | Cotang. | | Tang. | Cosec | | Sine. | 1 | m. | S. |
| D. D | | ls | 15" | 32 | -18 | or 15" | 63 | ls. | 45 De | grees. | | - | |
| P. P. s or | | 2 | 30 | 64 | 2 | 30 | 126 | 2 | 30 | 65 | | P. or | |
| - | | 3 | 45 | 96 | 3 | 45 | 189 | 3 | 45 | 93 | 3 | 04 | |

NATURAL SINES, TANGENTS, SECANTS, AND VERSINES, TO EVERY DEGREE OF THE QUADRANT.

| 1 | Arc. | Sine. | Cosine. | Tangent. | Cotan. | Secant. | Cosec. | Versine | Coversine | Arc. | Ī |
|-----|------|---------|----------|----------|-----------|----------|-----------|---------|-----------|------|---|
| | 00 | 000000 | 1.000000 | 000000 | Infinite. | 1.000000 | Infinite. | 000000 | 1.000000 | 900 | |
| 1 | 1 | 017452 | | | | | 57.29869 | | | | - |
| 1 | 2 | 034899 | | 034921 | 28.63625 | 1.000609 | 28.65371 | 000609 | 965100 | 88 | I |
| 1 | 3 | 052336 | 998630 | 052408 | 19.08114 | 1.001372 | 19.10732 | 001370 | 947664 | 87 | ı |
| ľ | 4 | 069756 | 997564 | | | | 14.33559 | | | 86 | ١ |
| 1 | 5 | 087156 | 996195 | 087489 | 11.43005 | 1.003820 | 11.47371 | 003805 | 912844 | 85 | ı |
| ľ | 6 | 104528 | 994522 | 105104 | 9.514365 | 1.005508 | 9.566772 | 005478 | 895471 | 84 | 1 |
| 1 | 7 | 121869 | | 122785 | 8.144346 | 1.007510 | 8 205509 | 007454 | 878131 | 83 | I |
| r | 8 | 139173 | | 140541 | 7.115370 | 1.009828 | 7.185297 | 009732 | 860827 | 82 | ı |
| 1 | 9 | 156434 | 987688 | 158384 | 6.313752 | 1.012465 | 6.392453 | 012312 | 843565 | 81 | l |
| L | 10 | 173648 | 984808 | 176327 | 5.671282 | 1.015427 | 5.758771 | 015192 | 826352 | 80 | l |
| 1 | 11 | 190809 | 981627 | 194380 | 5.144554 | 1.018717 | 5.240843 | 018373 | 809191 | 79 | ١ |
| 1 | - | 207912 | 978148 | | | | 4.809734 | | 792088 | 78 | İ |
| ı | - | 224951 | 974370 | | | | 4.445411 | | 775049 | 77 | l |
| ı | | 241922 | 970296 | 249328 | 4.010781 | 1.030614 | 4.133566 | 029704 | 758078 | 76 | ŀ |
| 1 | - 60 | 258819 | 965926 | 267949 | 3.732051 | 1.035276 | 3.863703 | 034074 | 741181 | 75 | 1 |
| 1 | | 275637 | 961262 | | | | 3.627955 | | 724363 | 74 | |
| 1 | | 292372 | 956305 | 305731 | 3.270853 | 1.045692 | 3.420304 | 043695 | 707628 | 73 | ŀ |
| ŀ | | 309017 | 951056 | | | | 3.236068 | | 690983 | 72 | ŀ |
| I | | 325568 | 945519 | | | | 3.071554 | | 674432 | 71 | ľ |
| | | 342020 | 939693 | | | | 2.923804 | | 657980 | 70 | |
| 1- | 21 | 358368 | 933580 | | | | 2.790428 | | 641632 | 69 | |
| 1 | | 374607 | 927184 | 404096 | 9.475087 | 1.078535 | 2.669467 | 072816 | 625393 | 68 | > |
| Г | | 390731 | 920505 | 494475 | 2.355859 | 1.086360 | 2.559305 | 079495 | 609269 | 67 | |
| | - | 406737 | 913546 | 445229 | 2.246037 | 1.094636 | 2.458593 | 086454 | | 66 | |
| | | 422618 | 906308 | 466308 | 2.144507 | 1.103378 | 2.366202 | 093692 | 577382 | 65 | |
| | - | 438371 | 898794 | | | | 2.281172 | | 561629 | 64 | |
| | | 453991 | 891007 | 500594 | 1 069611 | 1 199996 | 2.202689 | 108993 | 546009 | 63 | |
| | | 469172 | 882948 | 531700 | 1 880797 | 1 122570 | 2.130055 | 117052 | 530528 | 62 | |
| | | 484810 | 874620 | 554309 | 1 804048 | 1.143354 | 2.062665 | 125380 | 515190 | 61 | ı |
| | - | 500000 | 866025 | 577350 | 1.732051 | 1.154701 | 2.000000 | 133975 | 500000 | 60 | |
| - | - | 515038 | 857167 | | | | 1.941604 | | 484962 | 59 | |
| | | 529919 | 848048 | 694860 | 1.004200 | 1.100033 | 1.887080 | 151952 | 470081 | 58 | 1 |
| | | 544639 | 838671 | 640408 | 1 520265 | 1 109363 | 1.836079 | 161329 | 455361 | 57 | |
| | 4 . | 559193 | 829038 | 674500 | 1 489561 | 1.206218 | 1.788292 | 170962 | 440807 | 56 | |
| | 2.0 | 573576 | 819152 | 700208 | 1.498148 | 1.220775 | 1.743447 | 180848 | 426424 | 55 | - |
| - | - | 587785 | 809017 | | | | 1.701302 | | 412215 | 54 | |
| | 2000 | 501815 | 798636 | 753554 | 1 397015 | 1 959196 | 1.661640 | 201364 | 398185 | 53 | |
| | | 515661 | 788011 | 781986 | 1 970049 | 1 260018 | 1.624269 | 211989 | 384338 | 52 | - |
| | | 529320 | 777146 | 809784 | 1.934807 | 1.286760 | 1.589016 | 222854 | 360680 | 51 | I |
| | | 542788 | 766044 | 839100 | 1.191754 | 1.305407 | 1.555724 | 233956 | 357212 | 50 | |
| 1 | - | 556059 | 754710 | 860297 | 1 150260 | 1 295019 | 1.524253 | 245290 | 343941 | 49 | |
| | | 569131 | 743145 | 900104 | 1110619 | 1 345699 | 1.494477 | 256855 | 330869 | 48 | |
| | | 581998 | 731354 | 939515 | 079360 | 1.367358 | 1.466279 | 268646 | 318002 | 47 | |
| | | 694658 | 719340 | 965689 | 1.035530 | 1.390164 | 1.439557 | 280660 | 305342 | 46 | |
| | - | 707107 | | 1.000000 | 1.0000000 | 1.414214 | 1.414214 | 292893 | 292893 | 45 | |
| = | - | | | | | | | | | | |
| 1 2 | rc. | Cosine. | Sine. | Cotan. | Tangent. | Cosec. | Secant. | Covers. | Versine. | Arc. | |

TABLE VII.

MERIDIONAL PARTS TO EVERY DEGREE OF THE QUADRANT.

| _ | - | - | | - | | _ | Section 14 | - | | - | | | | | | - | - | |
|----|-------|----|--------|----|--------|----|------------|----|--------|----|--------|----|--------|-----|---------|-----|-------|----|
| D. | M. P. | D. | M. P. | D. | M. P. | D. | M. P. | D. | M. P. | D. | M. P. | D. | M. P. | ID. | : M. P. | ID. | M. P | |
| 0 | .0 | 10 | 603.1 | 20 | 1225.1 | 30 | 1888.4 | 10 | 2622.7 | 50 | 3474.5 | 60 | 4527.4 | 70 | 5965.9 | 80 | 8375 | .2 |
| 1 | 60.0 | 11 | 664.1 | 21 | 1289.2 | 31 | 1958.0 | 41 | 2701.6 | 51 | 3568.8 | 61 | 4649.2 | 71 | 6145.7 | 81 | 8739 | .1 |
| 2 | 120.0 | 12 | 725.3 | 22 | 1353.7 | 32 | 2028.4 | 42 | 2781.7 | 52 | 3665.2 | 62 | 4775.0 | 72 | 6334.8 | 82 | 9145 | .5 |
| 3 | 180.1 | 13 | 786.8 | 23 | 14186 | 33 | 2099.5 | 43 | 2863.1 | 53 | 3763.8 | 63 | 4904.9 | 73 | 6534.4 | 83 | 9605 | .8 |
| 4 | 240.2 | 14 | 848.5 | 24 | 1484.1 | 34 | 2171.5 | 44 | 2945.8 | 54 | 3864.6 | 64 | 5039.4 | 74 | 6745.7 | 84 | 10136 | .9 |
| 5 | 300.4 | 15 | 910.5 | 25 | 1550.0 | 35 | 2244.3 | 45 | 3029.9 | 55 | 3968.0 | 65 | 5178.8 | 75 | 6970.3 | 85 | 10764 | .6 |
| 6 | 360.7 | 16 | 972.7 | 26 | 1616.5 | 36 | 2318.0 | 46 | 3115.6 | 56 | 4073.9 | 66 | 5323.5 | 76 | 7210.1 | 86 | 11532 | .5 |
| 7 | 421.1 | 17 | 1035.3 | 27 | 1683.5 | 37 | 2392.6 | 47 | 3202.7 | 57 | 4182.6 | 67 | 5474.0 | 77 | 7467.2 | 87 | 12522 | .1 |
| 8 | 481.6 | 18 | 1098.2 | 28 | 1751.2 | 38 | 2468.3 | 48 | 3291.5 | 58 | 4294.3 | 68 | 5630.8 | 78 | 7744.6 | 88 | 13916 | .4 |
| 9 | 542.2 | 19 | 1161.5 | 29 | 1819.4 | 39 | 2544.9 | 49 | 3382.1 | 59 | 4409.1 | 69 | 5794.6 | 79 | 8045.7 | 89 | 16299 | .6 |

| Cou | rse | | ABLE | | Dist | . 2. | Dis | t. 3. | Dis | t. 4. | Dis | t. 5. | Co | urs |
|------|-----|--------|--------|--------|------------------|---------|---------|---------|----------|---------|---------|---------|------|-----|
| Pts. | D. | T | Lat. | Dep. | Lat | Dep. | Lat | Dep. | Lat | Dep. | Lat. | Dep. | D. | Pt |
| _ | | | | | 1.9997 | 0.0349 | 2.9995 | 0 0524 | 3.9994 | 0.0698 | 4 9992 | 0.0873 | 89 | Т |
| | | | | | 1.9988 | | | | | | | | | |
| 0 4 | | | | | 1.9976 | | | | | | | | | 7 |
| ~ 4 | | | | | 1.9973 | | | | | | | | | |
| | | | | | 1.9951 | | | | | | | | | T |
| | | | | | 1.9924 | | | | | | | | | |
| 0 1 | | 0 | 0959 | 0.0000 | 1.9904 | 0.1960 | 2 9856 | 0.2041 | 3.9807 | 0.3991 | 4. 0750 | 0.4001 | | 7 |
| v 9 | | | | | 1.9890 | | | | | | | | | • |
| | | | | | 1.9851 | | | | | | | | | |
| | | | | | | | | | | | | | | |
| | - | - | | | 1.9805 | | | | - | | | | | |
| 0 3 | | | | | 1.9784 | | | | | | | | | 7 |
| | | | | | 1.9754 | | | | | | | | | |
| | 10 | 0 | .9848 | 0.1736 | 1.9696 | 0.3473 | 2.9544 | 0.5209 | 3.9392 | 0.6946 | 4.9240 | 0.8682 | 80 | |
| | 11 | 0 | .9816 | 0.1908 | 1.9633 | 0.3816 | 2.9449 | 0.5724 | 3.9265 | 0.7632 | 4.9081 | 0.9540 | 79 | M |
| 1 | 1. | 0 | .9808 | 0.1951 | 1.9616 | 0.3902 | 2.9424 | 0.5853 | 3.9231 | 0.7804 | 4.9039 | 0.9755 | | 7 |
| | 12 | o' | 9781 | 0.2079 | 1.9563 | 0.4158 | 2.9344 | 0.6237 | 3.9126 | 0.8316 | 4.8907 | 1.0396 | 78 | |
| | | | | | 1.9487 | | | | | | | | | |
| | | | | | 1.9406 | | | | | | | | | |
| 1 } | | | | | 1.9401 | | | | | | | | | 6 |
| 4 | | | | | 1.9319 | | | | | | | | | 0 |
| | | | | | | | | | | | | | | |
| 1 1 | | | | | 1.9225 | | | | | | | | | 1 |
| l į | | | | | 1.9139 | | | | | | | | | 8 |
| | | | | | 1.9126 | | | | | | | | | |
| | | | | | 1.9021 | | | | | | | | | |
| | | | | | 1.8910 | | | | | | | | | |
| 1 4 | | 10 | .9415 | 0.3369 | 1.8831 | 0.6738 | 2.8246 | 1.0107 | 3.7662 | 1.3476 | 4.7077 | 1.6844 | | 6 |
| | 20 | 0.0 | .9397 | 0.3420 | 1.8794 | 0.6840 | 2.8191 | 1.0261 | 3.7588 | 1.3681 | 4.6985 | 1.7101 | 170 | |
| | 21 | 10 | .9336 | 0.3584 | 1.8672 | 0.7167 | 2.8007 | 1.0751 | 3.7343 | 1.4335 | 4.6679 | 1.7918 | 69 | |
| | 22 | 0 | .9272 | 0.3746 | 1.8544 | 0.7492 | 2.7816 | 1.1238 | 3.7087 | 1.4984 | 4.6359 | 1.8730 | 68 | |
| 2 | | | | | 1.8478 | | | | | | | | | 6 |
| | 99 | - | - | - | 1.8410 | | | | | - | - | - | | - |
| - | | | | | 1.8271 | | | | | | | | | |
| ٠, | 9 | | 0069 | 0.400 | 1.8126 | 0.0130 | 0 7100 | 1.6206 | 9 69 59 | 1.0203 | 4 501 | 9 110 | 00 | |
| 2 1 | - | 10 | 0040 | 0.4220 | 1 0000 | 0.0402 | 0.7109 | 1.2019 | 0.0232 | 1.0900 | 4.5310 | 2.113 | 05 | |
| 4 | | | | | 1.8080 | | | | | | | | | 5 |
| 12 | | | | | 1.7976 | | | | | | | | | |
| | 90 | | 0000 | 0.4340 | 1.7820 | 0.9080 | 2.0730 | 1.3020 | 3.5040 | 1.8100 | 4.455 | 2.2700 | 763 | |
| 0 1 | | | | | 1.7659 | | | | | | | | | |
| 2 } | | | | | 1.7638 | | | | | | | | | 5 |
| 0.3 | 53 | | .8746 | 0.4848 | 1.7492 | 0.9696 | 2.6239 | 1.4544 | 3.4985 | 1.9392 | 4.373 | 2.4240 | 61 | |
| | 30 | | | | 1.7321 | | | | | | | | | |
| 2 3 | | C | .8577 | 0.514 | 1.7155 | 1.0282 | 2.5732 | 1.5423 | 3.4309 | 2.0564 | 4.2886 | 2.570 | 1 | 5 |
| 1 | 3 | LIC | .8572 | 0.5150 | 1.7143 | 1.0301 | 2.5715 | 1.5451 | 3.4287 | 2.0602 | 4.2858 | 2.575 | 259 | |
| | 39 | 5 0 | .8480 | 0.529 | 1.6961 | 1.0598 | 2.5441 | 1.5898 | 3.3922 | 2.1197 | 4.2402 | 2.649 | 5 58 | |
| | 33 | 3 | .8387 | 0.544 | 1.6773 | 1.0893 | 2.5160 | 1.6330 | 3.3547 | 2.1786 | 4.1934 | 2.793 | 57 | |
| 3 | | | | | 1.6629 | | | | | | | | | 15 |
| | 34 | 4 | .8290 | 0.5599 | 1.6581 | 1.1184 | 2,4871 | 1.6776 | 3.3169 | 2.2369 | 4.1459 | 2.796 | 0.56 | 1 |
| 1 | 3 | 50 | .8199 | 0.573 | 1.6383 | 1 1479 | 2 4575 | 1.7902 | 3 9766 | 9.9049 | 84 0050 | 2 267 | DEF | 1 |
| 1 | 3 | 6 | .8000 | 0.5876 | 1.6180 | 1 1756 | 9 4971 | 1 7694 | 3 9961 | 9 951 | 4.0451 | 9 090 | 0 24 | |
| 3 | | | | | 1.6064 | | | | | | | | | |
| - | | 7/ | 7086 | 0.000 | 1.5973 | 1 9096 | 2010 | 1.1011 | 9 104 | 9 4000 | 2 0000 | 2.916 | 1 | 4 |
| - | | | | | | | | | | | | | | |
| 100 | 3 | ٥ ا | .7880 | 0.615 | 1.5760 | 1.2313 | 2.3640 | 1.8470 | 3.1520 | 2.4626 | 3.940 | 3.078 | 3 52 | 10 |
| _ | 3 | 910 | .7771 | 0.629 | 31.5543 | 1.2586 | 2.3314 | 1.8880 | 3.1086 | 2.5173 | 3.885 | 3.146 | 651 | |
| 3 | 2 | K | 1.7730 | 0.634 | 41.546 () | 11.2688 | 12.3190 | 01.9032 | 9i3.0920 | 12.5376 | 3.8650 | 13.1720 | 0 | 14 |
| | 4 | 0[(| .7660 | 0.642 | 31.5321 | 11.2856 | 2.2981 | 1.9284 | 3.0642 | 2.5712 | 23.8302 | 23.213 | 9150 | |
| | 4 | L((|).7547 | 0.656 | 111.5094 | 41.3121 | 12.2641 | 11.9682 | 23.0188 | 2.6249 | 3,773 | 5 3.380 | 3 19 | |
| 711 | 4. | 31(|).7431 | 0.669 | 111.4803 | 11.3388 | 12.2294 | 12.0074 | 2.9726 | 2.676 | 3.715 | 7 3.345 | 7118 | |
| 3 | 2 | - ((| 0.7410 | 0.671 | 611.4819 | 11.3431 | 12.2229 | 12.0147 | 2.9638 | 2.6869 | 3.7048 | 33.357 | 3 | 14 |
| | 4 | 3[(| 0.7314 | 0.682 | 011.4627 | 11.3640 | [2.194] | 12.0460 | 2.9254 | 2.7280 | 3.6568 | 33.410 | 047 | |
| | 4 | 4(| 0.7193 | 0.694 | 1.4387 | 1.3899 | 2.1580 | 2.0840 | 2.8774 | 2.778 | 3.596 | 3.473 | 3 46 | |
| 4 | 4 | 50 | 0.7071 | 0.707 | 11.4142 | 1.4149 | 2.1919 | 2.1919 | 2 8984 | 2.898 | 13.535 | 3.535 | 5 15 | 14. |
| - | | | | Late | | | - | | | | | - | | |
| Pts. | 100 | 3 | | - | | | Dep. | | Dep. | | Dep. | | Deg. | 13. |
| | 1 | -11 | Dis | st. 1. | Dis | t. 2. | Di | st. 3. | Dis | st. 4. | Di | st. 5. | 10 | 1 |
| | | | | | | Th | ELS. | - 11 | 30 | - | 1-1 | T1+ 2 | No. | |

| 1 | _ | | | for | Degre | es and | Quarte | r-Poin | ts. | TABLE | VIII. | . (| 55 |
|-----------|-----|----------------|-------------------------|--------|----------|--------------------------------------|--------|--|---------|--------|------------|---------|--------|
| Cour | | Dist | t. 6. | | t. 7. | Dist | . 8. | Dist | . 9. | Dist | | | ırse |
| Pts. | | Lat. | Dep. | Lat. | Dep. | Lat. | Dep. | Lat | Dep. | Lat. | | D. | Pts. |
| | 9 | | 0.1047 | | | | | | | | | | |
| 0 1 | | | 0.2034 | | | | | | | | | 00 | 7 3 |
| | | | 0.3140 | | | | | | | | | | |
| | | | 0.4185 | | | | | | | | | | |
| 0 1 | | | 0.5229 | | | | | | | | | | 7 1 |
| 1 | | | 0.6272 | | | | | | | | | | * |
| | | | 0.7312 | | | | | | | | | | |
| 0 3 | 8 | | $\frac{0.8350}{0.8804}$ | | | | | | | | - | 82 | 7 1 |
| 4 | 9 | | 0.8804 | | | | | | | | | 81 | 4 |
| | | | 1.0419 | | | | | | | | | | |
| | 11 | | 1.1449 | | | | | | | | | | |
| L | 19 | | 1.1705 | | | | | | | | | | 7 |
| | | | 1.3497 | | | | | | | | | | |
| | 14 | | 1.4515 | | | | | | | | | | |
| 1 4 | 1.5 | | 1.4579 | | | | | | | | | | 6 3 |
| | - | | 1.5529 | | - | | | | | 7 | - | Z | - |
| 1 1 | 10 | | 1.7417 | | | | | | | | | | 6 1 |
| 1 | | 5.7378 | 1.7542 | 6.6941 | 2.0466 | 7.6504 | 2.3390 | 8.6067 | 2.6313 | 9.5630 | 2.9237 | 73 | |
| 1.0 | | | 1.8541 | | | | | | | | | | |
| 1 3 | 19 | | 1.9534 2.0213 | | | | | | | | | | 6 1 |
| 1 4 | 20 | | 2.0521 | | | | | | | | | | 4 |
| | | | 2.1502 | | | | | | | | | | |
| 9 | 22 | | 2.2476 2.2961 | | | | | | | | | | 6 |
| - | 92 | | 2.3444 | | | | - | | - | - | - | - | 0 |
| | | | 2.4404 | | | | | | | | | | |
| | | 5.4378 | 2.5357 | 6.3442 | 2.9583 | 7.2505 | 3.3809 | 8.1568 | 3.8036 | 9.0631 | 4.2262 | 65 | |
| 2 4 | 00 | | 2.5653 | | | | | | | | | | 5 3 |
| | | | 2.6302 2.7239 | | | | | | | | | | |
| | | | 2.8168 | | | | | | | | | | |
| 5 1 | 00 | | 2.8284 | | | | | | | | | | 5 1 |
| | | | 2.9089 23.0000 | | | | | | | | | | |
| 5-3 | - | | 3.0846 | | - | | - | | | - | - | - | 5 1 |
| 1 4 | | | 3.0902 | | | | | | | | | | |
| | | | 3.1795 | | | | | | | | | | |
| 2 | 33 | | 3.2678 3.3334 | | | | | | | | | | E 1 |
| 1 | 34 | | 3.3552 | | | | | | | | | | 3 |
| | 35 | 4.914 | 9 3.4415 | 5.734 | 14.0150 | 6.5532 | 4.5886 | 7.3724 | 5.1629 | 8.191 | 5.7358 | 3 55 | |
| 10 1 | | | 13.5267 | | | | | | | | | | 1 |
| 3 1 | | | 2 3.5742 8 3.6109 | | | | | | | | | | 1 4 |
| | | | 1 3.6940 | | | | | | | | | | |
| | 39 | 4.662 | 9 3.7759 | 5.440 | 0 4.405 | 6.2179 | 5.0346 | 6.9943 | 5.663 | 7.771 | 6.293 | 251 | |
| 3 1 | | 4.638 | 1 3.8064 | 5.411 | 1 4.4408 | 6.1841 | 5.0751 | [6.957] | 5.709 | 7.730 | 16.3439 | 9 | 4 1 |
| 1 | 4(| 4.596 | 3 3.8567 3 3.9363 | 5.282 | 4.499 | 6.037 | 5.1423 | 6.8944 | 5.785 | 7.660 | 6.427 | 150 | |
| 1 | 4.2 | 4.458 | 9 4.0148 | 5.202 | 1.683 | 0.5.9452 | 5.3530 | 6.6883 | 3 6.022 | 7.431 | 6.691 | 3 18 | |
| 3 § | 1 | 4.445 | 7 4.0291 | 5.186 | 7 4.700 | 95.9276 | 5.3725 | 6.6686 | 6.0440 | 7.409 | 6.715 | 5 | 4 3 |
| 1 | 4: | 34.388 | 1 4.0920 | 5.119 | 14.774 | 5.8508 | 5.4560 | 6.582 | 6.1380 | 7.313 | 6.8200 | 0 47 | |
| 1.4 | 4 | 54.249 | 04.1680 64.2426 | 34,940 | 7 4.949 | 7)5.6569 | 5.6560 | (0.474) (6.364) | 0.251 | 7.071 | 7.071 | 146 | 1 |
| 1 | | o Dep. | | | - | Dep. | _ | 1 Dep. | | Dep. | _ | 21, | - |
| Pts. | De | | ist. 6. | | st. 7. | - | st. 8. | | st. 9. | | t. 10. | Dec | |
| - Comment | - | PARTY NAMED IN | | | | Name and Address of the Owner, where | E | No. of Concession, Name of Street, or other Designation of Concession, Name of Street, or other Designation of Concession, Name of Street, Original Property and Concession, Original Property and Concession, Name of Street, Original Property and Concession, Name of Street, Original Property and Concession, Original Prop | | - | - Williams | Heraigh | V63300 |

100

E

| | 0 | 6 | - | TABLE | IX. | | | Diurr | nal L | ogai | rithr | ns. | II. | | | | | - | |
|-------|-----|---------------|----------|-------------------------------|--------------------|-------|------------|---------|---------|--------|-------|---------|----------|----------------|---------|-------------------------|------|---------|---------------|
| | М | 00 N | | h. m. 0 0 | h. m. 0 30 | h. | m. 0 | h. m. | | | · m. | h. 3 | m. 0 | h. m. 3 30 | | n. h. m. 0 4 30 | h. 5 | m. 0 | h. m. 5 30 |
| | ın. | S | SUN. | h. 0 | h. 1 | h. 2 | | h. 3 | h. 4 | h 5 | | h. 6 | | h. 7 | h. 8 | h. 9 | h. | Ī | h. 11 |
| | 0 | () | 0 | 3.15836 | 1.38021 | 1.07 | 918 558 | 90309 | 7781 | 5 68 | 3124 | 602 | 06 86 | 53511 53408 | 4771 | 2 42597 | 380 | 21 | 33882 |
| ١ | 1 | 30 | 2 | 2.85733 | 1.36597 1.35902 | 1.07 | 200 | 89829 | 7745 | 5 67 | 7836 | 599 | 66 | 53305 | 4753 | 2 42436 | 378 | 377 | 33751 |
| | 2 2 | 0 30 | 4. | 2.55630 | 1.35218 | 1.06 | 494 | 89355 | 7709 | 7 67 | 7549 | 597 | 26 | 53090 | 4735 | 2 42276 | 377 | 33 | 33620 |
| | 3 | 0 30 | 6 | 2.38021 2.31327 | 1.33882 | 1.05 | 799 | 88885 | 7674 | 3 67 | 264 | 594 | 38 | 52895 | 4717 | 3 42117 | 375 | 89 | 33489 |
| | 44 | 0 30 | 8 | 2.25527 | 1.32585 | 1.05 | 115 | 88421 | 7639 | 1 66 | 3981 | 592 | 52 | 52692 | 4699 | 4 41958 | 374 | 46 | 33359 |
| Ì | 5 5 | 0 30 | 10 | 2.15836 | 1.31327 1.30711 | 1.64 | 442 | 87961 | 7604 | 2 66 | 3700 | 590 | 16 | 52490 | 4681 | 7 41800 | 373 | 03 | 33229 |
| ı | 6 | 0 30 | 12 | 2.07918 | 1.30103 | 1.03 | 779 | 87506 | 7569 | 6 66 | 3421 | 5878 | 32 | 52288 | 4664 | 0 41642 | 371 | 61 | 33099 |
| 1 | 7 | 0 30 | 14 | 2.04442 2.01224 1.98227 | 1.28913 | 1.03 | 126 | 87056 | 7535 | 3 66 | 143 | 585 | 19 | 52087 | 4646 | 4 41485 | 370 | 20 | 32970 |
| ı | 8 | 0 30 | 16 | 1.95424 1.92791 | 1.27755 | 1.02 | 182 | 86611 | 7501 | 2 65 | 868 | 583 | 18 | 51888 | 4628 | 8 41329 | 368 | 78 | 32842 |
| 1 | 9 | 0 30 | 18 19 | 1.90309 1.87961 | 1.26627 | 1.019 | 348 | 86170 | 7467 | 4 65 | 594 | 5808 | 37 | 51689 | 4611 | 3 41173 | 367 | 38 | 32713 |
| | 0 | 0 | 20 | 1.85733 | 1.25527 | 1.01 | 224 | 85733 | 7433 | 9 65 | 321 | 578 | 8 | 51491 | 4593 | 9 41018 | 365 | 97 | 32585 |
| 1 | 0 | 30 | 22 | 1.83614 | 1.24455 | 1.000 | 608 | 85301 | 7400 | 6 65 | 051 | 5763 | 30 | 51294 | 4576 | 6 40863 | 364 | 57 | 32458 |
| 1 | 1 2 | 30 | 24 | 1.79664 | 1.23408 | 1.000 | 000 | 84873 | 7367 | 6 64 | 782 | 5740 | 3 | 51098 | 4559 | 3 40709 | 363 | 18 | 33331 |
| 1 | 233 | 30 | 26 | 1.76042 | 1.22387 | 994 | 101 | 84450 | 7334 | 8 64 | 515 | 5717 | 8 | 50903 | 4542 | 1 40555 | 361 | 79: | 32204 |
| 1 | 4 | 30 0 30 | 28 | 1.72700 | 1.21388 | 988 | 310 | 84030 | 7302 | 3 64 | 249 | 5695 | 3 | 50709 | 4525 | 6 40478 0 40402 | 360 | 40 | 32078 |
| ī | 5 | 0 | 30 | 1.69597 | 1.20412 | 0.982 | 27 | 83614 | 7270 | 63 | 985 | 5673 | 0 | 50515 | 1507 | $\frac{5 40325}{40249}$ | 359 | 02 | 31951 |
| 111 | 6 | 30 | 32 | 1.66700 | 1.19458 | 976 | 552 | 83203 | 7237 | 9 63 | 723 | 5650 | 8 | 50323 | 4490 | 4 40173 9 40097 | 357 | 65 | 31826 |
| 111 | 7 | 30 | 34 | 1.63985 | 1.18524 | 970 | 84 | 32795 | 7206 | 1 63 | 462 | 5628 | 7 | 50131 | 4474 | 5 40021 0 39945 | 356 | 273 | 31700 |
| 111 | 8 | 30 | 36 | 1.61430 | 1.17609 | 965 | 24 | 32391 | 7174 | 63 | 505 | 5606 | 7 4 | 19940 | 1457 | 39870 39794 | 354 | 913 | 31575 |
| i | 9 | 30 0 30 | 38 | 1.57858 | 1.16714 | 959 | 71 8 | 31991 | 71432 | 62 | 945 | 5584 | 8 4 | 19750 | 1440: | 7 39719 3 39644 | 353 | 54 5 | 31451 |
| 2 | 0 | 0 | 40 | 1.55630 | 1.15836 | 0.954 | 24 | 31594 | 71121 | 62 | 688 | 5563 | 0 4 | 9561 | 1423 | 39569 39494 | 352 | 18 3 | 31327 |
| 2 2 | 1 | 30 | 42 | 1.53511 | 1.14976 | 948 | 85 8 | 31201 | 70811 | 62 | 434 | 5541 | 4.4 | 19372 | 14069 | 39419 39344 | 3508 | 33 3 | 31203 |
| 2 2 2 | 2 | 30 | 44 | 1.52490 | 1.14133 | 943 | 52 8 | 30812 | 70505 | 62 | 181 | 5519 | 8 4 | 9185 | 13905 | 39270 39195 | 349 | 18 3 | 1079 |
| 2 | 3 | 30 | 46 | 1.50515 | 1.13306 | 938 | 26 8 | 80426 | 70200 | 61 | 929 | 5498 | 44 | 8998 | 13738 | 39121 | 3481 | 133 | 0956 |
| 2 2 | 1 | 30 | 48 | 1.48627 | 1.12494 | 933 | 05 8 | 30043 | 69897 | 61 | 678 | 5477 | 0 4 | 88124 | 13573 | 38973 38899 | 3467 | 193 | 0833 |
| 2. | 5 | 30 | 50 | 1.46817 1.45939 | 1.11697 | 0.927 | 91 7 | 9664 | 69597 | 614 | 130 | 455 | 5 4 | 8627 4 | 3409 | 38825 38751 | 3451 | 5 3 | 0711 |
| 2 | 6 | 30 | 52 | 1.45079 1.44236 | 1.10915 | 922 | 84 7 | 9288 | 69298 | 611 | 182 5 | 434 | 74 | 81424 | 3245 | 38678 38604 | 3441 | 23 | 0588 |
| 5. | 7 | 30 | 54 | .43409 I .42597 I | .10146 | 917 | 81/7 | 8915 | 69002 | 609 | 36 5 | 413 | 5 4 | 8259 4 | 3082 | 38531 38458 | 3427 | 93 | 0467 |
| 21 | 3 | 30 | 56 | .41800 I | .09391 | 912 | 85 7 | 8545 | 58707 | 606 | 91 5 | 392 | 7 4 | 8076 4 | 2920 | 38385 38312 | 3414 | 63 | 0345 |
| 2 | 9 | 0 | 58 1 | .40249 1 .39494 1 | .08648 | 907 | 94 7 | 8179 | 58415 | 601 | 48 5 | 3719 | 4 | 7894 4 | 2758 | 38239 38166 | 3401 | 43 | 0224 |
| 2 | , | 30 | 59 1 | .38751 1 | .08282 | 905 | 51 7 | 7997 | 68269 | 603 | 27 5 | 3615 | 4 | 7803 4 | 2677 | 38094 | 3394 | 8 3 | 0163 |

| 1 | - | _ | _ | | | | | | | | | | _ | | - |
|-----|----------|---------|----------|----------------|----------------|----------------|------------------------|----------------|----------------|------------------------|------------------|----------------|------------------|----------|----------------|
| | | | | _ 11 | | | | rnal I | | 11 | | | LE IX | | 67 |
| ı | Mo | ON | | h. m. 6 0 | h. m. 6 30 | h. m. | h. m. 7 30 | h. m. | h. m. 8 30 | h. m. 9 0 | h. m. 9 30 | h. m. 10 0 | h. m. 10 30 | h. m. | |
| | m. | , S. | Sun. | h. 12 | h. 13 | h. 14 | h. 15 | h. 16 | h. 17 | h. 18 | h. 19 | h. 20 | h. 21 | h. 22 | h. 23 |
| | 0 | 0 | 0 | 30103 | 26627 | 23408 | 20412 | 17609 | 14976 | 12494 | 10146 | 07918 | 05799 | 03779 | 01848 |
| ı | 0 | 30 | 2 | | | | | | | 12454 12414 | | | | | |
| 1 | 1 2 | 30 | 3 4 | 29923 | 26460 | 23254 | 20268 | 17474 | 14849 | 12374 12333 | 10032 | 07810 | 05696 | 03680 | 01754 |
| | 2 | 30 | , 5 | 29803 | 26349 | 23151 | 20172 | 17384 | 14764 | 12293 | 09956 | 07738 | 05627 | 03615 | 01691 |
| ı | 3 | 30 | 6 | 29683 | 26239 | 23048 | 20076 | 17294 | 14679 | 12253 12213 | 09880 | 07666 | 05559 | 03549 | 01629 |
| ı | 4 | 30 | 8 | | | | | | | 12173 12134 | | | | | |
| | 5 | 0 | 10 | | | | | | | 12094 | | | | | |
| 1 | 5 6 | 30 | 11 | 29385 | 25964 | 22792 | 19837 | 17070 | 14468 | 12054 12014 | 09691 | 07486 | 05388 | 03386 | 01472 |
| 1 | 6 | 30 | 13 14 | | | | | | | 11974 | | | | | |
| | 7 8 | 30 | 15 16 | | | | | | | 11895 11855 | | | | | |
| | 8 | 30 | 17 | 29090 | 23691 | 22538 | 19599 | 16847 | 14258 | 11816 | 09503 | 07307 | 05217 | 03223 | 01317 |
| ١ | 9 | 30 | 18 | | | | | | | 11737 | | | | | 01286 01255 |
| | 10 | 30 | 20 | | | | | | | 11697 | | | | | 01224 01193 |
| ١ | 11 | 0 | 22 | 28796 | 25419 | 22286 | 19363 | 16625 | 14050 | 11618 | 09316 | 07129 | 05048 | 03061 | 01162 |
| | 11 | 30 | 23 | 28679 | 25311 | 22185 | 19269 | 16537 | 13966 | 11579 11539 | 09241 | 07058 | 04980 | 02996 | 01100 |
| | 12 | 30 | 25 | 28621 28562 | 25257 25203 | 22135 22085 | 1922 2 19175 | 16493 16449 | 13925 13883 | 11500 11461 | $09204 \\ 09167$ | 07023 06987 | $04946 \\ 04912$ | 02964 | 01069 |
| | 13 | 30 | 27 | 28504 | 25149 | 22034 | 19128 | 16405 | 13842 | 11422 | 09129 | 06952 | 04879 | 02900 | 01007 |
| - 1 | 14 | 30 | 29 | 28388 | 25042 | 21934 | 19035 | 16317 | 13759 | 11343 | 09055 | 06881 | 04811 | 02835 | 00945 |
| | 15 | 30 | 30 | | | | | | | 11304 11265 | | | | | 00914 |
| 1 | 16 16 | 0 30 | 32 | 28215 | 24881 | 21785 | 18895 | 16185 | 13635 | 11226 11187 | 08944 | 06775 | 04710 | 02739 | 00853 |
| 1 | 17 | 0 | 34 | 28099 | 24774 | 21685 | 18802 | 16098 | 13552 | 11148 | 08870 | 06705 | 04643 | 02675 | 00791 |
| | 17 18 | 30 | 35 36 | 27984 | 24667 | 21586 | 18709 | 16010 | 13470 | 11109 11070 | 08796 | 06635 | 04576 | 02610 | 00730 |
| | 18 19 | 30 | 37 38 | | | | | | | 11031 10992 | | | | | |
| 1 | 19 | 30 | 39 | 27812 | 24508 | 21437 | 18570 | 15880 | 13347 | 10953 | 08685 | 06529 | 04475 | 02514 | 00638 |
| 1 | 50 50 | 30 | 40 41 | 27698 | 24402 | 21339 | 18477 | 15793 | 13265 | 1091 <i>5</i> 10876 | 08611 | 06459 | 04409 | 02451 | 00577 |
| | 21 | 30 | 42 | | | | | | | 10837 10798 | | | | | |
| | 22 | 0 30 | 44 | | | | | | | 10760 10721 | | | | | |
| 1 | 23 | 0 | 46 | 27413 | 24138 | 21093 | 18247 | 15577 | 13061 | 10683 | 08428 | 06285 | 04242 | 02291 | 00424 |
| ١ | 23 | 30 | | 27300 | 24033 | 20995 | 18156 | 15490 | 12979 | | 08355 | 06215 | 04176 | 02228 | 00364 |
| | 24 | 30 | | | | | | | | | | | | | 00333 |
| ı | 25 | 30 | 51 | 27132 | 23876 | 20849 | 18018 | 15361 | 12857 | 10490 | 08245 | 06111 | 04076 | 02133 | 00272 |
| 1 | 26 26 | | 53 | 27018 | 23772 | 20751 | 17927 | 15275 | 12776 | | 08172 | 06041 | 01010 | 02069 | 00212 |
| | 27 | 0 30 | 55 | 26906 | 23668 | 20654 | 17836 | 15190 | 12696 | 10375 10337 | 08100 | 05972 | 03944 | 02006 | 00151 |
| | 28 | 0 30 | 56 | 26850 | 23616 | 20606 | 17791 | 15147 | 12655 | 10299 10260 | 08063 | 05937 | 03911 | 01975 | 00121 |
| ı | 29 | 0 30 | 58 | 26738 | 23512 | 20509 | 17700 | 15062 | 12574 | | 07991 | 05868 | 03845 | 01911 | 00060 |
| (| 29 | 30 | 59 | 20053 | 23±00 | 20.F00 | 17055 | 15019 | 12034 | 10184 | 11904 | 03834 | 13812 | 01380 | 00030 |

0 Degree, or 0 Hour.

| | " S | 0m | 1m | 2m | 3m | 4.m | 5m | 6 ^m | 7m | 8m | 9m |
|-----|--------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|---------|---------|
| | 0 | | 2.25527 | 1.95424 | 1.77815 | | | | 1.41017 | 1.35218 | 1.30103 |
| | 1 | 4.03342 | | 95064 | 77575 | | | 47592 | 40914 | 35128 | 30023 |
| | 2 | 3.73239 | | | | | | | 40811 | 35038 | 29942 |
| | 3 | 55630 | | 94352 | | | | | 40708 | 34948 | 29862 |
| | 4 | 43136 | | 94000 | | | | | 40600 | 34858 | 29782 |
| | 5 | 33445 | | 93651 | 76625 | | | | | 34768 | 29703 |
| - | 6 | 25527 | 21388 | 93305 | 76391 | 64249 | | | | 34679 | 29623 |
| 1 | 7 | 18833 | | 92962 | 76158 | | | | | | 29544 |
| 1 | 8 | 13033 | | 92621 | 75927 | 63897 | | | | | 29464 |
| 1 | 9 | 07918 | 19457 | 92283 | 75696 | 63722 | 54347 | 46640 | 40097 | 34411 | 29385 |
| 1 | 10 | 3.03342 | 2.18833 | 1.91948 | 1.75467 | 1.63548 | 1.54206 | 1.46522 | 1.39996 | 1.34323 | 1.29306 |
| 3 | 11 | 2.99203 | 18217 | 91615 | 75239 | 63375 | 54066 | 46405 | 39895 | 34234 | 29227 |
| | 12 | 95424 | 17609 | 91285 | 75012 | | | | 39794 | 34146 | 29148 |
| 1 | 13 | 91948 | | 90957 | 74787 | 63030 | 53788 | 46171 | 39694 | 34058 | 29070 |
| 1 | 14 | 88730 | | 90632 | 74562 | | | | 39593 | 33970 | 28991 |
| | 15 | 85733 | 15836 | 90309 | 74339 | 62688 | | | 39493 | 33882 | 28913 |
| 1 | 16 | 82930 | 15261 | 89988 | 74117 | 62518 | | | 39394 | 33794 | 28835 |
| 1 | 17 | 80297 | 14693 | 89670 | 73896 | | 53236 | | 39294 | 33707 | 28757 |
| 1 | 18 | 77815 | 14133 | 89354 | 73676 | 62180 | 53100 | | 39195 | 33619 | 28679 |
| 1 | 19 | 75467 | 13580 | 89041 | 73457 | 62012 | 52963 | 45478 | 39096 | 33532 | 28601 |
| ŀ | 20 | 2.73239 | 2.13033 | 1.88730 | 1.73239 | 1.61845 | 1.52827 | 1.45364 | 1.38997 | 1.33445 | 1.28524 |
| 1 | 21 | 71120 | 12494 | 88420 | 73023 | 61678 | 52692 | | 38899 | 33359 | 28446 |
| 1 | 22 | 69100 | 11961 | 88114 | 72807 | 61512 | 52557 | 45136 | 38800 | 33272 | 28369 |
| | 23 | 67170 | 11435 | 87809 | 72593 | | 52422 | | 38702 | 33186 | 28292 |
| 1 | 24 | 65321 | 10914 | 87506 | 72379 | 61182 | 52288 | | 38604 | 33099 | 28215 |
| | 25 | 63548 | 10400 | 87206 | 72167 | 61018 | 52154 | 44796 | 38506 | 33013 | 28138 |
| | 26 | 61845 | 09893 | 86907 | 71956 | 60854 | 52021 | 44684 | 38409 | 32927 | 28061 |
| | 27 | 60206 | 09390 | 86611 | 71745 | 60691 | 51888 | 44571 | 38312 | 32842 | 27984 |
| | 28 | 58627 | 08894 | 86316 | 71536 | 60529 | 51755 | 44459 | 38215 | 32756 | 27908 |
| | 29 | 57103 | 08403 | 86024 | 71328 | 60367 | 51623 | 44347 | 38118 | 32671 | 27831 |
| ш | | | | 1.85733 | 1.71120 | | 1.51491 | 1.44236 | 1.38021 | | 1.27755 |
| | 31 | 54206 | 07438 | 85445 | 70914 | 60045 | 51360 | 44125 | 37925 | 32500 | 27679 |
| | 32 | 52827 | 06964 | 85158 | 70709 | 59885 | 51229 | 44014 | 37829 | 32415 | 27603 |
| | 33 | 51491 | 06494 | 84873 | 70504 | 59726 | 51098 | 43903 | 37733 | 32331 | 27527 |
| | 34 | 50194 | 06030 | 84590 | 70301 | 59567 | 50968 | 43793 | 37637 | 32246 | 27451 |
| | 35 | 48936 | 05570 | 84309 | 70099 | 59409 | 50838 | 43683 | 37541 | 32162 | 27376 |
| | 36 | 47712 | 05115 | 84030 | 69897 | 59251 | 50708 | 43573 | 37446 | 32077 | 27300 |
| | 37 | 46522 | 04665 | 83752 | 69696 | 59094 | 50579 | 43463 | 37351 | 31993 | 27225 |
| | 38 | 45364 | 04220 | 83477 | 69497 | 58938 | 50451 | 43354 | 37256 | 31909 | 27150 |
| | 39 | 44236 | 03779 | 83203 | 69298 | 58782 | 50322 | 43245 | 37161 | 31826 | 27075 |
| 16- | | | | | 1.69100 | | 1.50194 | 1.43136 | | 1.31742 | |
| | 11 | 42064 | 02910 | 82660 | 68903 | 59472 | 50067 | 43028 | 36972 | 31659 | 26925 |
| | 12 | 41017 | 02482 | 82391 | 68707 | 58317 | 49940 | 42920 | 36878 | 31575 | 26850 |
| | 13 | 39996 | 02060 | 82124 | 68512 | 58164 | 49813 | 42812 | 36784 | 31492 | 26776 |
| | 14 | 38997 | 01639 | 81858 | 68318 | 58011 | 49687 | 42704 | 36691 | 31409 | 26701 |
| | 15 | 38021 | 01039 | 81594 | 68124 | 57858 | 49560 | 42597 | 36597 | 31326 | 26627 |
| | 6 | 37067 | 00812 | 81332 | 67932 | 57706 | 49435 | 42490 | 36504 | 31214 | 26553 |
| | 17 | 36133 | 00404 | 81071 | 67740 | 57554 | 49309 | 42383 | 36411 | 31161 | 26479 |
| | 18 | 35218 | 00000 | 80811 | 67549 | 57403 | 49184 | 42276 | 36318 | 31079 | 26405 |
| | 9 | | 1.99600 | 80554 | 67359 | 57253 | 49060 | 42170 | 36225 | 30997 | 26331 |
| | | | | | | 1.57103 | | | | 1.30915 | |
| | - | | | | | | | | | | |
| | 1 | 32585 | 98810 | 80043 | 66981 | 56953 | 48812 | 41958 | 36040 | 30833 | 26184 |
| | 52 | 31742 | 98421 | 79790 | 66794 | 56804 56656 | 48688 48565 | 41853 | 35948 | 30751 | 26037 |
| | | 30915 | 98035 | 79538 | 66607 | | | | 35856 | 30588 | 25964 |
| | 4 | 30103 | 97652 | 79287 | 66421 | 56508 | 48442 | 41642 | 35765 | 30588 | 25904 |
| | 55 | 29306 | 97273 | 79039 | 66236 | 56360 | 48320 | 41538 | 35673 | 30426 | 25891 |
| | 66 | 28524 27755 | 96897 96524 | 78791 78545 | 66051 65868 | 56213 | 48197 | 41433 | 35582 35491 | 30345 | 25745 |
| | 8 | 27000 | 96324 | | | | 47954 | 41329 | 35400 | 30264 | 25672 |
| | 9 | 26257 | 95788 | 78300 | 65685 | 55921 55775 | 47954 | 41121 | 35309 | 30183 | 25600 |
| L | 01 | 40201 | 33103 | 78057 | 65503 | 00110 | 41000 | 41121 | 30300 | 30103 | 23000 |

| | | | | | Propor | tional I | ogarith | ms. | TABL | EX. | 69 |
|---|----------|------------------|------------------|------------------|------------------|------------------|------------------|-----------------|----------------|---------------------------|------------------|
| ı | | | | - | 0 D | egree, or | 0 Hour. | | | | |
| 1 | " | 10 ^m | 11 ^m | 12 ^m | 13 ^m | 14m | 15 ^m | 16 ^m | 17m | 18m | 19m |
| ı | 0 | 1.25527 | | 1.17609 | 1.14133 | | 1.07918 | | | | 0.97652 97614 |
| 1 | 1 2 | 25455 25383 | 21322 | 17489 | 14077 | 10863 10811 | 07870 07822 | 05070 | 02397 | 0.99960 999 2 0 | 97576 |
| 1 | 3 | 25311 25239 | 21191 21126 | 17429 | 13966 | 10760 | 07774 07726 | 04980 04935 | 02355 02312 | 99880 99839 | |
| 1 | 4 5 | 25167 | 21060 | 17369 17309 | 13911 13855 | 10657 | 07678 | 04933 | 02312 | 99799 | |
| 1 | 6 | 25095 | 20995 | 17249 | 13800 | 10605 | 07630 | 04845 | 02228 | 99759 | 97424 |
| | 8 | 25024 24952 | 20930 20865 | 17189 17129 | 13745 13690 | 10554 10503 | 07582 07534 | 04800 04755 | 02185 02143 | | |
| ١ | 9 | 24881 | 20800 | | 13635 | 10452 | 07486 | 04710 | 02101 | 99640 | |
| I | 10 | 1.24809 | | 1.17010 | | | | | | | 0.97273 |
| 1 | 11 | 24738 24667 | 20670 20605 | 16951 16891 | 13525 13470 | 10349 10298 | 07391 07343 | 04620 04576 | 02017 | 99560 99520 | |
| 1 | 13 | 24596 | 20541 | 16832 | 13415 | 10247 | 07295 | 04531 | 01932 | 99480 | |
| ı | 14 | 24526 | 20476 | 16773 | 13360 | 10197 | 07248 | 04486 | 01890 | 99441 | 97122 |
| 1 | 15 16 | 24455 24384 | 20412 20348 | 16714 16655 | 13306 13251 | 10095 | 07200 | 04442 | 01848 01806 | 99401 99361 | 97084 97047 |
| 1 | 17 | 24314 | 20284 | 16596 | 13197 | 10044 | 07105 | 04353 | 01764 | 99322 | 97009 |
| 1 | 18 19 | 24244 24173 | 20219 20155 | 16537 16478 | 13142 13088 | 09994 09943 | 07058 07011 | 04308 04264 | 01723 | 99282 99243 | 96972 |
| ł | 20 | | 1.20091 | | 1.13033 | - | | | | | 0.96897 |
| ı | 21 | 24033 | 20028 | 16361 | 12979 | 09842 | 06916 | 04175 | 01597 | 99164 | 96859 |
| 1 | 22 23 | 23963 23894 | 19964 19900 | 16302 16243 | 12925 12871 | 09792 09741 | 06869 06822 | 04131 04087 | 01556 01514 | | |
| ١ | 24 | 23824 | | 16185 | 12817 | 09691 | 06775 | 04043 | 01472 | 99045 | |
| 1 | 25 | 23754 | 19773 | 16127 | 12763 | 09641 | 06728 | 03999 | 01431 | 99006 | |
| 1 | 26 | 23685 23616 | 19710 19647 | 16068 16010 | 12709 12655 | 09591 09540 | 06681 06634 | 03955 | 01389 01348 | 98967 98928 | |
| ١ | 28 | 23546 | 19584 | 15952 | 12601 | 09490 | 06588 | 03867 | 01306 | 98888 | |
| | 29 | 23477 | 19520 | 15894 | 12548 | 09440 | 06541 | 03823 | 01265 | 98849 | 96561 |
| 1 | 30 | 1.23408 23339 | 1.19457 19395 | 1.15836 15778 | 1.12494 12440 | 1.09390 09341 | 1.06494 06447 | 1.03779 | 01182 | 98771 | 0.96524 96487 |
| ı | 82 | 23271 | 19332 | 15721 | 12387 | 09291 | 06401 | 03691 | 01141 | 98732 | |
| ١ | 33 34 | 23202 | 19269 | 15663 | 12333 | 09241 | 06354 | 03647 | 01100 | | |
| ı | 35 | 23133 23065 | 19206 19144 | 15605 15548 | 12280 12227 | 09191 09142 | 06308 06261 | 03604 03560 | 01058 | 98654 98615 | |
| | 36 | 22997 | 19081 | 15490 | 12173 | 09092 | 06215 | 03516 | 00976 | 98576 | 96302 |
| 1 | 37 38 | 22928 22860 | 19019 18957 | 15433 15375 | 12120 12067 | 09042 08993 | 06168 | 03473 03429 | 00935 | 0.1770 | 96265 |
| 1 | 39 | 22792 | 18895 | 15318 | 12014 | 08943 | 06076 | 03386 | 00853 | 98459 | |
| 1 | 40 | 1.22724 | | | 1.11961 | 1.08894 | 1.06030 | | | 0.98421 | |
| 1 | 41 | 22657 22589 | 18771 18709 | 15204 15147 | 11908 11855 | 08845 08796 | 05983 05937 | 03299 03256 | 00771 | 98382 98343 | |
| 1 | 43 | 22521 | 18647 | 15090 | 11802 | 08746 | 05891 | 03230 | 00689 | 98304 | 96044 |
| | 44 | 22454 | 18585 | 15033 | 11750 | 08697 | 05845 | 03169 | 00648 | 98266 | 96007 |
| - | 45 | 22386 22319 | 18523 18462 | 14976 14919 | 11697 11644 | 08648 08599 | 05799 05753 | 03126 03083 | 00607 00567 | 98227 98189 | 95971 95934 |
| | 47 | 22252 | 18400 | 14863 | 11592 | 08550 | 05707 | 03039 | 00526 | 98150 | 95897 |
| 1 | 48 49 | 22185 22118 | 18339 18278 | 14806 14750 | 11539 11487 | 08501 08452 | 05662 05616 | 02996 02953 | 00485 | 98111 98073 | 95861 95824 |
| | 50 | | | 1.14693 | | | | | | | |
| 1 | 51 | 21984 | 18155 | 14637 | 11382 | 08355 | 05524 | 02867 | 00363 | 97996 | 95751 |
| | 52 53 | 21918 21851 | 18094 18033 | | 11330 11278 | | 05479 05433 | 02824 02781 | 00323 | 97958 97919 | |
| | 54 | 21785 | 17973 | | 11226 | | 05388 | 02739 | 00242 | 97881 | |
| | 55 | 21718 | 17912 | 14412 | 11174 | 08160 | 05342 | 02696 | 00202 | 97843 | |
| 1 | 56 57 | 21652 21586 | 17851 17790 | 14356 14300 | 11122 | 08112 08063 | 05297 05251 | 02653 02610 | 00161 | 97805 97766 | |
| | 58 | 21520 | 17730 | 14244 | 11018 | 08015 | 05206 | 02568 | 00080 | 97728 | 95497 |
| 1 | 59 | 21454 | 17669 | | 10966 | | .3 .4 | 02525 | .6 | 97690 | |
| 1 | | | s of "o | | 5 | | 16 21 | | .6 | | 8 .9 2 48 |

| 70 | | TABLE : | X. | Propor | tional L | ogarithn | ns. | | | |
|----------|----------------|----------------|----------------|----------------|----------------|------------------------|----------------|------------------------|----------------|----------------|
| | | | | 0 D | egree, or | 0 Hour. | | | | |
| "S | 2()m | 21m | 22m | 23m | 24m | 25m | 26m | 27m | 28m | 29m |
| 0 | 95424 | 93305 | 91285 | 89354 | 87506 | 85733 | 84030 | 82391 | 80811 | 79287 |
| 1 2 | 95388 95352 | 93271 | 91252 | 89323 | 87476 87446 | 85704 85675 | 84002 83974 | 82364 82337 | 80786 | 79263 79238 |
| 3 | 95316 | 93202 | 91186 | 89260 | 87416 | 85646 | 83946 | 82311 | 80734 | 79213 |
| 4 5 | 95280 95244 | 93168 93133 | 91154 | 89229 | 87386 87356 | 85618 85589 | 83919 83891 | 82284 82257 | 80708 | 79188 |
| 6 | 95208 | 93099 | 91088 | 89166 | 87326 | 85560 | 83863 | 82230 | 80657 | 79138 |
| 7 8 | 95172 95136 | 93065 93030 | 91055 91023 | 89135 | 87296 87266 | 85531 85502 | 83835 83808 | 82204 82177 | 80631 80605 | 79113 |
| 9 | 95100 | 92996 | 90990 | 89072 | 87236 | 85473 | 83780 | 82150 | 80579 | 79063 |
| 10 11 | 95064 95028 | 92962 | 90957 90925 | 89041 89010 | 87206 87176 | 85445 85416 | 83752 83725 | 82124 82097 | 80554 80528 | 79039 79014 |
| 12 | 91992 | 92928 92894 | 90923 | 88978 | 87146 | 85387 | 83697 | 82070 | 80502 | 78989 |
| 13 | 94956 | 92860 | 90859 | 88947 | 87116 | 85358 | 83670 | 82044 | 80477 | 78964 |
| 14 15 | 94921 94885 | 92825 92791 | 90827 | 88916 | 87086 87056 | 85330 85301 | 83642 83614 | 82017 81991 | 80451 | 78939 78915 |
| 16 | 94849 | 92757 | 90762 | 88854 | 87026 | 85272 | 83587 | 81964 | 80100 | 78890 |
| 17 18 | 94813 94778 | 92723 | 90729 | 88823 | 86996 | 85244 85215 | 83559 83532 | 81938 81911 | 80374 | 78865 78840 |
| 19 | 94742 | 92655 | 90664 | 88761 | 86937 | 85187 | 83504 | 81884 | 80323 | 78816 |
| 20 21 | 94706 | 92621 | 90632 | 88730 88699 | 86907 86877 | 85158 85129 | 83477 83449 | 81858 8183 2 | 80297 80272 | 78791 78766 |
| 22 | 94671 94635 | 92587 | 90599 | 88668 | 86848 | 85101 | 83422 | 81805 | 80246 | 78742 |
| 23 | 94600 | 92520 | 90535 | 88637 | 86818 | 85072 | 83394 | 81779 | 80221 | 78717 |
| 24 25 | 94564 94529 | 92486 92452 | 90502 | 88606 88575 | 86788 86759 | 85044 85015 | 83367 83339 | 81752 | 80195 | 78693 78668 |
| 26 | 94493 | 92418 | 90438 | 88544 | 86729 | 84987 | 83312 | 81699 | 80144 | 78643 |
| 27 28 | 94458 94423 | 92385 92351 | 90406 | 88513 88482 | 86699 | 84958 84930 | 83285 | 81673 81647 | 80119 | 78619 78594 |
| 29 | 94387 | 92317 | 90341 | 88451 | 86640 | 84902 | 83230 | 81620 | 80068 | 78570 |
| 30 | 94352 | 92283 | 90309 | 88120 | 86611 | 84873 | 83203 | 81594 | 80043 | 78515 |
| 31 | 94317 | 92250 92216 | 90277 | 88390 88359 | 86581 | 84845 | 83175 83148 | 81568 81541 | 80017 79992 | 78521 78196 |
| 33 | 94246 | 92183 | 90213 | 88328 | 86522 | 84788 | 83121 | 81515 | 79967 | 78472 |
| 34 35 | 94211 | 92149 | 90181 | 88297 88267 | 86493 | 84760 84732 | 83094 | 81489 | 79941 | 78147 |
| 36 | 94141 | 92082 | 90116 | 88236 | 86434 | 84703 | 83039 | 81436 | 79891 | 78398 |
| 37 38 | 94105 | 92048 92015 | 90084 | 88205 88175 | 86404 | 84675 | 83012 82985 | 81410 81384 | 79865 79840 | 78374 78349 |
| 39 | 94035 | 91981 | 90020 | 88144 | 86346 | 84619 | 82958 | 81358 | 79815 | 78325 |
| 40 | 94000 | 91948 | 89988 | 88114 | 86316 | 84590 | 82930 | 81332 | 79790 | 78300 |
| 41 42 | 93965 93930 | 91915 91881 | 89957 89925 | 88083 88052 | 86287 | 84562 84534 | 82903 82876 | 81305 | 79764 | 78276 78252 |
| 43 | 93895 | 91848 | 89893 | 88022 | 86228 | 84506 | 82849 | 81253 | 79714 | 78227 |
| 44 45 | 93860 93825 | 91815 | 89861 89829 | 87991 87961 | 86199 | 84478 84450 | 82822 82795 | 81227 | 79689 79663 | 78203 |
| 46 | 93791 | 91748 | 89797 | 87930 | 86141 | 84121 | 82768 | 81175 | 79638 | 78154 |
| 47 | 93756 93721 | 91715 91682 | 89766 89734 | 87900 87870 | 86111 | 84393 8436 5 | 82741 82714 | 81149 81123 | 79613 79588 | 78130 78106 |
| 49 | 93686 | | | | | | | | | |
| 50 | 93651 | 91615 | 89670 | 87809 | 86024 | 84309 | 82660 | 81071 | 79538 | 78057 |
| 51 52 | 93617 93582 | 91582 91549 | 89639 89607 | 87778 87748 | 85995 85965 | 84281 84253 | 82633 82606 | 81045 81019 | 79513 79488 | 78033 78009 |
| 53 | 93517 | 91516 | 89575 | 87718 | 85936 | 84225 | 82579 | 80993 | 79453 | 77984 |
| 54 | 93513 93478 | 91483 91450 | 89514 89512 | 87687 87657 | 85907 85878 | 84197 84169 | 82552 82525 | 80967 80941 | 79437 | 77960 |
| 56 | 93443 | 91417 | 89481 | 87627 | 85849 | 84141 | 82198 | 80915 | 79387 | 77912 |
| 57 58 | 93409 93374 | 91384 91351 | 89449 89417 | 87597 87566 | 85820 85791 | 84114 84086 | 82471 | 80889 80863 | 79362 79337 | 77888 |
| 59 | 93340 | 91318 | 89386 | 87536 | 85762 | 84058 | 82445 82418 | 80837 | 79312 | 77839 |
| -11 | Propor | tional Pa | art to | .1 | | 3 .4 | | .6 | | 8 .9 |
| - | tenth | s of " or | 8. | 3 | 6 | 9 12 | 15 | 18 | 21 2 | 4 27 |

| 1 | NOT THE | | | | Propor | rtional I | Logarith | ms. | TABL | EX. | 71 |
|----------|----------|----------------|-------------------|----------------|----------------|----------------|-----------------|----------------|----------------|----------------|-----------------|
| | | | | | 0 D | egree, or | 0 Hour. | | | | |
| | 8 | 30m | 31m | 32m | 33m | 34m | 35 ^m | 36m | 37m | 38m | 39 ^m |
| ı | 0 | 77815 | 76391 | 75012 | 73676 | 72379 72358 | 71120 | 69897 69877 | 68707 68688 | 67549 67530 | 66421 66402 |
| ı | 2 | 77791 | 76368 | 74990 | 73654 | 72337 | 71079 | 69857 | 68668 | 67511 | 66384 |
| Cheering | 3 | 77743 | 76321 | 74944 | 73610 | 72316 | 71058 | 69837 | 68648 | 67492 | 66365 |
| | 4 5 | 77719 | 76298 76275 | 74922 74899 | 73588 | 72294 | 71038 | 69817 69797 | 68629 68609 | 67473 | 66347 |
| ı | 6 | 77671 | 76251 | 74877 | 73544 | 72252 | 70997 | 69777 | 68590 | 67435 | 66310 |
| - | 7 8 | 77647 | 76228 76205 | 74854 74832 | 73523 73501 | 72231 72209 | 70976 | 69756 69736 | 68570 68551 | 67416 67397 | 66291 66273 |
| 1 | 9 | 77599 | 76181 | 74809 | 73479 | 72188 | 70935 | 69716 | 68531 | 67378 | 66254 |
| - | 10 | 77575 | 76158 | 74787 | 73457 | 72167 | 70914 | 69696 | 68512 | 67359 | 66236 |
| ۱ | 11 | 77551 | 76135 | 74764 | 73435 73413 | 72146 72125 | 70894 | 69676 69656 | 68492 68473 | 67340 | 66217 |
| ı | 13 | 77527 | 76112 | 74742 | 73392 | 72103 | 70852 | 69636 | 68454 | 67302 | 66180 |
| ı | 14 | 77479 | 76065 | 74697 | 73370 | 72082 | 70832 | 69616 | 68434 | 67283 | 66162 |
| ı | 15 16 | 77455 77431 | 76042 76019 | 74674 74652 | 73348 73326 | 72061 72040 | 70811 | 69596 69576 | 68415 68395 | 67264 67245 | 66143 |
| ı | 17 | 77407 | 75996 | 74629 | 73305 | 72019 | 70770 | 69557 | 68376 | 67226 | 66106 |
| ı | 18 | 77385 | 75973 | 74607 | 73283 | 71998 | 70750 | 69537 69517 | 68356 68337 | 67207 67188 | 66088 |
| ŀ | 19 20 | 77359 | 75950 75927 | 74585 | 73261 | 71956 | 70709 | 69497 | | 67170 | 66051 |
| ı | 21 | 77311 | 75903 | 74540 | 73218 | 71935 | 70688 | 69477 | 68298 | 67151 | 66033 |
| ۱ | 22 | 77288 | 75880 | 74517 | 73196 | | 70668 70647 | 69457 | 68279 | 67132 67113 | 66014 |
| ı | 23 | 77264 | 75857 75834 | 74495 74473 | 73174 | 71892 71871 | 70627 | | 68259 68240 | 67094 | 65996 65978 |
| ı | 25 | 77216 | 75811 | 74450 | 73131 | 71850 | 70606 | 69397 | 68221 | 67075 | 65959 |
| ı | 26 | 77192 | 75788 75765 | 74428 74406 | 73109 73088 | 71829 | 70586 70566 | 69377 69358 | 68201 68182 | 67056 67038 | 65941 65923 |
| ı | 28 | 77145 | 75742 | 74383 | 73066 | 71787 | 70545 | 69338 | 68163 | 67019 | 65904 |
| 1 | 29 | 77121 | 75719 | 74361 | 73044 | 71766 | 70525 | 69318 | 68143 | 67000 | 65886 |
| | 30 | 77097 | 75696 75673 | 74339 74317 | 73023 73001 | 71745 | 70504 | 69298 69278 | 68124 68105 | 66981 66962 | 65868 65849 |
| | 32 | 77050 | 75650 | 74294 | 72980 | 71703 | 70464 | 69258 | 68086 | 66944 | 65831 |
| | 33 | 77026 | 75627 | 74272 | 72958 | 71682 | 70443 | 69239 | 68066 | 66925 | 65813 |
| | 34 35 | 77002 | 75604 75581 | 74250 74228 | 72936 72915 | 71662 | 70423 70403 | 69219 69199 | 68047 68028 | 66906 | 65794 65776 |
| 1 | 36 | 76955 | 75559 | 74205 | 72893 | 71620 | 70382 | 69179 | 68008 | 66869 | 65758 |
| | 37 | 76931 76908 | 75536 75513 | 74183 74161 | 72872 72850 | 71599 71578 | 70362 70342 | 69159 69140 | 67989 67970 | 66831 | 65739 65721 |
| | 39 | 76884 | 75490 | 74139 | 72829 | 71557 | 70321 | 69120 | 67951 | 66812 | 65703 |
| Ī | 40 | 76861 | 75467 | 74117 | 72807 | 71536 | 70301 | 69100 | 67932 | 66794 | 65685 |
| ۱ | 41 42 | 76837 | 75444 75421 | 74095 74072 | 72786 72764 | 71515 71494 | 70281 | 69080 69061 | 67912 67893 | 66775 | 65666 65648 |
| 1 | 43 | 76790 | 75398 | 74050 | 72743 | 71473 | 70240 | 69041 | 67874 | 66737 | 65630 |
| ۱ | 44 | 76766 | 75376 | 74028 | 72721 | 71453 | 70220 | 69021 | 67855 | 66719 | 65612 |
| - | 45 | 76743 | 75353 75330 | 74006 | 72700 | 71432 | 70200 | 69002 68982 | 67836 67816 | 66700 66681 | 65594 65575 |
| ١ | 17 | 76696 | 75307 | 73962 | 72657 | 71390 | 70159 | 68962 | 67797 | 66663 | 65557 |
| ı | 48 | 76672 | 75285 | 73940 | 72636 | 71369 | 70139 | 68942 68923 | 67778 | 66644 | 65539 |
| - | 50 | 76649 | 75262 75239 | 73918 | 72614 | 71349 | 70119 | 68903 | 67759 67740 | 66625 | 65521 65503 |
| - | 51 | 76602 | 75216 | 73874 | 72571 | 71307 | 70078 | 68884 | 67721 | 66588 | 65484 |
| | 52 | 76578 | 75194 | 73852 | 72550 | 71286 | 70058 | 68864 | 67702 | 66570 | 65466 |
| | 53 54 | 76555 76531 | 75171 75148 | 73830 73808 | 72529 72507 | 71265 71245 | 70038 | 68844 68825 | 67682 67663 | 66551 66532 | 65448 65430 |
| | 55 | 76508 | 75125 | 73786 | 72486 | 71224 | 69998 | 68805 | 67644 | 66514 | 65412 |
| 1 | 56 57 | 76485 76461 | 75103 75080 | 73764 | 72465 72443 | 71203 | 69977 | 68785 68766 | 67625 67606 | 66495 | 65394 65376 |
| 1 | 58 | 76438 | 75058 | 73720 | 72122 | 71162 | 69937 | 68746 | 67587 | 66458 | 65357 |
| 1 | 59 | 76414 | 75035 | 73698 | 72401 | 71141 | 69917 | 68727 | 67568 | 66439 | 65339 |
| 1 | | | ional Passof " or | | .1 | .2 . | 3 .4 6 8 | .5. 10 | .6 13 | .7 .1 15 1 | |
| | - | tentin | 01 01 | 71 | | | . 0 | 10 | - | | |

| 79 | 2 | TABLE | x. | Propor | tional I | Logarith | ms. | | | |
|-----------------|----------------|---------------------|------------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|
| | | | | 0 D | egree, or | O Hour | - | | | |
| s s | 40m | 41m | 4.2m | 43m | 4.1m | 4.5m | 4.6m | 47m | .18m | 49m |
| 0 1 | 65321 65303 | 64249 64231 | 63202 63185 | 62180 62164 | 61182 | 60206 | 59251 59236 | 58317 58302 | 57403 57388 | 56508 56493 |
| 2 | 65285 | 64214 | 63168 | 62147 | 61149 | 60174 | 59220 | 58287 | 57373 | 56478 |
| 3 4 | 65267 | 64196 | 63151 63133 | 62130 | 61133 61116 | 60158 | 59204 59189 | 58271 58256 | 57358 57343 | 56463 56449 |
| 5 | 65231 | 64161 | 63116 | 62096 | 61100 | 60126 | 59173 | 58241 | 57328 | 56434 |
| 6 7 | 65213 65195 | 64143 | 63099 | 62080 62063 | 61083 | 60110 | 59157 | 58225 58210 | 57313 | 56419 56404 |
| 8 | 65177 | 64108 | 63065 | 62046 | 61051 | 60078 | 59126 | 58194 | 57283 | 56390 |
| 9 | 65159 | 64090 | 63048 | 62029 | 61034 | 60061 | 59110 | 58179 | 57268 57253 | 56375 |
| 11 | 65123 | 64055 | 63013 | 61996 | 61001 | 60029 | 59079 | 58148 | 57238 | 56360 56345 |
| 12 | 65105 | 64038 64020 | 62996 | 61979 | 60985 | 60013 | 59063 | 58133 | 57223 | 56331 |
| 14 | 65087 65069 | 64002 | 62979 | 61962 61945 | 60952 | 59997 59981 | 59047 | 58118 | 57208 57193 | 56316 56301 |
| 15 | 65051 | 63985 | 62945 | 61929 | 60936 | 59965 | 59016 | 58087 | 57178 | 56287 |
| 16 17 | 65033 65015 | 63967 | 62927 62910 | 61912 | 60920 | 59949 59933 | 59000 58985 | 58072 58056 | 57163 57148 | 56272 56257 |
| 18 | 64997 | 63932 | 62893 | 61878 | 60887 | 59917 | 58969 | 58041 | 57133 | 56243 |
| $\frac{19}{20}$ | 64979 64961 | 63915 | 62876 | 61862 | 60871 | 59901 | 58954 | 58026 58011 | 57118 | 56228 |
| 21 | 64943 | 63880 | 62842 | 61828 | 60838 | 59870 | 58922 | 57995 | 57088 | 56213 |
| 22 23 | 64925 | 63862 | 62825 | 61812 | 60822 | 59854 | 58907 | 57980 | 57073 | 56184 |
| 24 | 64907 64889 | 63845 63827 | 62808 62791 | 61795 61778 | 60805 60789 | 59838 59822 | 58891 58875 | 57965 57949 | 57058 57043 | 56169 56155 |
| 25 | 64871 | 63810 | 62774 | 61762 | 60773 | 59806 | 58860 | 57934 | 57028 | 56140 |
| 26 27 | 64853 64835 | 63792 63775 | 62757 62739 | 61745 | 60756 | 59790 59774 | 58844 58829 | 57919 57904 | 57013 56998 | 56125 56111 |
| 28 | 64818 | 63757 | 62722 | 61712 | 60724 | 59758 | 58813 | 57888 | 56983 | 56096 |
| 30 | 64800 | 63740 | 62705 62688 | 61695 | 60708 | 59742 | 58798 58782 | 57873 57858 | 56968 | 56081 |
| 31 | 64764 | 63705 | 62671 | 61662 | 60675 | 59710 | 58766 | 57843 | 56953 56938 | 56067 56052 |
| 32 | 64746 | 63688 | 62654 | 61645 | 60659 | 59694 | 58751 | 57827 | 56923 | 56037 |
| 34 | 64728 64710 | 63670 63653 | 62637 62620 | 61628 | 60642 | 59678 59663 | 58735 58720 | 57812 57797 | 56908 56893 | 56023 56008 |
| 35 36 | 64692 | 63635 | 62603 | 61595 | 60610 | 59647 | 58704 | 57782 | 56879 | 55994 |
| 37 | 64675 64657 | 63618 63601 | 62586 62569 | 61579 | 60594 60578 | 59631 59615 | 58689 58673 | 57767 57751 | 56864 56849 | 55979 55965 |
| 38 | 64639 | 63583 | 62552 | 61515 | 60561 | 59599 | 58658 | 57736 | 56834 | 55950 |
| $\frac{39}{40}$ | 64621 | 63566 | 62535 | 61529 | 60545 | 59583 | 58642 | 57721 | 56819 | 55935 |
| 41 | 64586 | 63531 | 62501 | 61496 | 60513 | 59551 | 58611 | 57691 | 56789 | 55906 |
| 42 43 | 64568 64550 | 63514 63496 | 62484 62468 | 61479 61463 | 60496 60480 | 59536 59520 | 59596 | 57675 | 56774 | 55892 |
| 44 | 64532 | 63479 | 62451 | 61446 | 60464 | 59504 | 58580 58565 | 57660 57645 | 56759 56745 | 55877 55862 |
| 45 | 64514 | 63462 | 62434 | 61429 | 60448 | 59488 | 58549 | 57630 | 56730 | 55848 |
| 46 | 64497 64479 | 63444 | 62417 | 61413 | 60432 | 59472 59457 | 58534 58518 | 57615 57600 | 56715 56700 | 55833 55319 |
| 48 | 64461 | 63410 | 62383 | 61380 | 60399 | 59441 | 58503 | 57584 | 56685 | 55804 |
| 49 50 | 64443 | 63392 | 62366 | 61363 | 60383 | 59425 | 58487 | 57569 57554 | 56656 | 55775 |
| 51 | 64408 | 63358 | 62332 | 61330 | 60351 | 59393 | 58456 | 57539 | 56641 | 55761 |
| 52 53 | 64390 64373 | 63340 63323 | 62315 62298 | 61314 | 60335 | 59378 59362 | 58441 58425 | 57524 57509 | 56626 56611 | 55746 55732 |
| 54 | 64355 | 63306 | 62282 | 61281 | 60303 | 59346 | 58425 | 57494 | 56596 | 55717 |
| 55 56 | 64337 64320 | 63289 63271 | 62265 62248 | 61264 | 60286 60270 | 59330 | 58395 | 57479 57463 | 56582 56567 | 55703 55688 |
| 57 | 64302 | 63254 | 62231 | 61248 61231 | 60254 | 59314 59299 | 58379 58364 | 57418 | 56552 | 55674 |
| 58 59 | 64284 | 63237 | 62214 | 61215 | 60238 | 59283 | 58348 | 57433 | 56537 | 55659 |
| 7 | Proport | 63220 ional Pa | 62197 rt to | 61198 | .2 . | 3 .4 | 58333 | .6 | .7 | 55645 |
| | tenth | s of " or | S. | 2 | | 5 6 | 8 | 10 | 11 1: | |

0 Degree, or 0 Hour.

| - | | | | | B-00, 01 | | | | | |
|----------|----------------|----------------|----------------|----------------|----------------|-----------------|----------------|----------------|----------------|----------------|
| 8 | 50m | 51m | 52m | 53m | 54m | 55 ^m | 56m | 57m | 58m | 59m |
| | | 54770 | 53927 | 53100 | 52288 | 51491 | 50708 | 49940 | 49184 | 48412 |
| | | 54756 | 53913 | 53086 | 52274 | | 50696 | 49927 | 49172 | 48430 |
| 2 | | 54742 | 53899 | 53072 | 52261 | 51465 | 50683 | 49914 | 49159 | 48418 |
| 5 | 55587 | 54728 | 53885 | 53059 | 52248 | | 50670 | 49902 | 49147 | 48405 |
| 4 | | 54714 | 53871 | 53045 | 52234 | | 50657 | 49889 | 49135 | 48393 |
| 1 | | 54699 | 53857 | 53031 | 52221 | 51425 | 50644 | 49876 | 49122 | 48381 |
| 6 | | 54685 | 53843 | 53018 | 52208 | | 50631 | 49864 | 49110 | 48369 |
| 1 7 | | 54671 | 53830 | 53004 | 52194 | | 50618 | 49851 | 49097 | 48356 |
| 8 | | 54657 | 53816 | 52991 | 52181 | 51386 | 50605 | 49838 | 49085 | 48344 |
| 9 | | 54643 | 53802 | 52977 | 52167 | 51373 | 50592 | 49826 | 49072 | 48332 |
| 10 | | 54629 | 53788 | 52963 | 52154 | 51360 | 50579 | 49813 | 49060 | 48320 |
| 11 | | 54614 | 53774 | 52950 | 52141 | 51346 | 50566 | 49800 | 49047 | 48307 |
| 12 | | 54600 | 53760 | 52936 | 52127 | 51333 | 50554 | 49788 | 49035 | 48295 48283 |
| 13 | | 54586 | 53746 | 52922 | 52114 | 51320 | 50541 | 49775 | 49023 | 48283 |
| 14 | | 54572 | 53732 | 52909 52895 | 52101 52087 | 51307 | 50528 | 49750 | 48998 | 48258 |
| 16 | | 54555 | 53705 | 52882 | 52051 | 51291 | 50502 | | 48985 | 48246 |
| 17 | | 54530 | 53691 | 52868 | 52061 | 51268 | 50489 | 49724 | 48973 | 48234 |
| 18 | | 54516 | 53677 | 52855 | 52047 | 51255 | 50476 | 49712 | 48960 | 48222 |
| 19 | | 54501 | 53663 | 52841 | 52034 | 51242 | 50464 | 49699 | 48948 | 48210 |
| 20 | | 54487 | 53649 | 52827 | 52021 | 51229 | 50451 | 49687 | 48936 | 48197 |
| 21 | | 54473 | 53636 | 52814 | 52007 | 51215 | 50431 | 49674 | 48923 | 48185 |
| 22 | | 54459 | 53622 | 52800 | 51994 | 51202 | 50425 | 49661 | 48911 | 48173 |
| 23 | 55299 | 54445 | 53608 | 52787 | 51981 | 51189 | 50412 | 49649 | 48898 | 48161 |
| 24 | 55284 | 54431 | 53594 | 52773 | 51967 | 51176 | 50399 | 49636 | 48886 | 48149 |
| 25 | 55270 | 54417 | 53580 | 52760 | 51954 | 51163 | 50387 | 49623 | 48874 | 48136 |
| 26 | | 54403 | 53567 | 52746 | 51941 | 51150 | 50374 | 49611 | 48861 | 48124 |
| 27 | | 54389 | 53553 | 52732 | 51927 | 51137 | 50361 | 49598 | 48849 | 48112 |
| 28 | | 54375 | 53539 | 52719 | 51914 | 51124 | 50348 | 49586 | 48836 | 48100 |
| 29 | | 54361 | 53525 | 52705 | 51901 | 51111 | 50335 | 49573 | 48824 | 48088 |
| 30 | | 54347 | 53511 | 52692 | 51888 | 51098 | 50322 | 49560 | 48812 | 48076 |
| 31 | 55184 | 54332 | 53498 | 52678 | 51874 | 51085 | 50310 | 49548 | 48799 | 48063 |
| 32 | | 54318 | 53484 | 52665 | 51861 | 51072 | 50297 | 49535 | 48787 | 48051 |
| 33 | | 54304 | 53470 | 52651 | 51848 | 51059 | 50284 | 49523 | 48775 | 48039 |
| 34 | | 54290 | 53456 | 52638 | 51835 | 51046 | 50271 | 49510 | 48762 | 48027 |
| 36 | 55127 | 54276 54262 | 53442 53429 | 52624 | 51821 | 51033 | 50258 | 49498 49485 | 48750 | 48015 48003 |
| 37 | 55098 | 54262 | 53429 | 52611 52597 | 51808 51795 | 51020 | 50246 50233 | 49485 | 48737 | 47990 |
| 38 | 55084 | 54234 | 53401 | 52584 | 51795 | 50994 | 50233 | 49460 | 48713 | 47978 |
| 39 | 55069 | 54220 | 53387 | 52570 | 51768 | 50981 | 50207 | 49447 | 48700 | 47966 |
| 40 | 55055 | 54206 | 53374 | 52557 | 51755 | 50968 | 50194 | 49435 | 48688 | 47954 |
| 41 | 55041 | 54192 | 53360 | 52543 | 51755 | 50955 | 50194 | 49433 | 48676 | 47942 |
| 42 | 55026 | 54178 | 53346 | 52530 | 51742 | 50942 | 50169 | 49410 | 48663 | 47930 |
| 43 | 55012 | 54164 | 53332 | 52516 | 51715 | 50929 | 50156 | 49397 | 48651 | 47918 |
| 44 | 54998 | 54150 | 53319 | 52503 | 51702 | 50916 | 50143 | 49385 | 48639 | 47906 |
| 4.5 | 54984 | 54136 | 53305 | 52489 | 51689 | 50903 | 50131 | 49372 | 48626 | 47893 |
| 46 | 54969 | 54122 | 53291 | 52476 | 51676 | 50890 | 50118 | 49360 | 48614 | 47881 |
| 47 | 54955 | 54108 | 53278 | 52462 | 51662 | 50877 | 50105 | 49347 | 48602 | 47869 |
| 48 | 54941 | 54094 | 53264 | 52449 | 51649 | 50864 | 50092 | 49334 | 48590 | 47857 |
| 49 | 54927 | 54080 | 53250 | 52136 | 51636 | 50851 | 50080 | 49322 | 48577 | 47845 |
| 50 | 54912 | 54066 | 53236 | 52122 | 51623 | 50838 | 50067 | 49309 | 48565 | 47833 |
| 51 | 54898 | 54052 | 53223 | 52409 | 51610 | 50825 | 50054 | 49297 | 48553 | 47821 |
| 52 | 54881 | 54038 | 53209 | 52395 | 51596 | 50812 | 50041 | 49284 | 48540 | 47809 |
| 53 54 | 54870 | 54024 | 53195 | 52382 | 51583 | 50799 | 50029 | 49272 | 48528 | 47797 |
| 55 | 54855 54841 | 54011 53997 | 53182 53168 | 52368 | 51570 | 50786 | 50016 | 49259 | 48516 | 47785 |
| 56 | 51827 | 53997 | 53154 | 52355 52342 | 51557 51544 | 50773 | 50003 49991 | 49247 | 48503 48491 | 47772 |
| 57 | 54813 | 53969 | 53141 | 52328 | 51530 | 50747 | 49991 | 49234 | 48479 | 47748 |
| 58 | 54799 | 53955 | 53127 | 52315 | 51517 | 50734 | 49965 | 49209 | 48467 | 47736 |
| 59 | | 53941 | 53113 | 52301 | 51504 | 50721 | 49952 | 49197 | 48454 | 47724 |
| | Proport | ional Pa | rt to | .1 | | .3 .4 | .5 | .6 | | 8 .9 |
| | tenth | s of "or | S | 1 | 3 | 4 5 | 6 | 8 | 9 1 | |
| | - | | - | - | | | () | () | J I | 12 |

| 74 | - | TABL | EX. | P | roporti | ional L | ogarith | ıms. | | | | |
|----------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|
| | | | | | 1 De | gree, or | 1 Hou | | | | | |
| ıı S | 0m | 1m | 2m | 3m | 4.m | 5m | 6m | 7m | 8m | 9m | 10m | 11m |
| 0 | 47712 47700 | 46994 46982 | 46288 46276 | 45593 45582 | 44909 44898 | 44236 44225 | 43573 43562 | 42920 42909 | 42276 42266 | 41642 41632 | 41017 | 40401 |
| 2 | 47688 | 46971 | 46265 | 45570 | 44887 | 44214 44203 | 43551 | | 42255 42244 | 41621 | 40997 40986 | 40381 |
| 3 4 | 47676 47664 | 46959 46947 | 46253 46241 | 45559 45547 | 44875 44864 | 44191 | 43529 | 42877 | 42234 | 41600 | 40976 | 40371 |
| 5 | 47652 47640 | 46935 46923 | 46230 46218 | 45536 45524 | 44853 44841 | 44180 44169 | | | | | 40966 40955 | 40350 40340 |
| 7 8 | 47628 47616 | 46911 46899 | 46206 46195 | 45513 45501 | 44830 44819 | 44158 44147 | | | 42202 42191 | 41569 41559 | 40945 40935 | 40330 40320 |
| 9 | 47604 | 46888 | 46183 | 45490 | 44808 | 44136 | 43474 | 42823 | 42181 | 41548 | 40924 | 40310 |
| 10 11 | 47592 47580 | 46876 46864 | 46171 46160 | 45478 45467 | 44796 44785 | 44125 44114 | 43463 43452 | | 42170 42159 | | 40914 40904 | 40300 40289 |
| 12 13 | 47568 47556 | 46852 46840 | 46148 46137 | 45456 45444 | 44774 44762 | 44102 44091 | 43441 43431 | 42790 42780 | 42149 42138 | | 40894 40883 | 40279 |
| 14 | 47544 | 46828 | 46125 | 45433 | 44751 | 44080 | 43420 | 42769 | 42128 | 41496 | 40873 | 40259 |
| 15 16 | 47532 47520 | 46817 46805 | 46113 46102 | 45421 45410 | 44740 44729 | 44069 44058 | | | 42117 42106 | 41475 | 40852 | 40249 40239 |
| 17 18 | 47508 47496 | 46793 46781 | 46090 46078 | 45398 45387 | 44717 | 44047 44036 | | | 42096 42085 | | | 40228 |
| 19 | 47484 | 46769 | 46067 | 45375 | 44695 | 44025 | 43365 | 42715 | 42075 | 41443 | 40821 | 40208 |
| 51 50 | 47472 | 46758 46746 | 46055 46044 | 45364 45353 | 44684 44672 | 44014 44003 | | | 42064 42053 | | 40811 | 40198 40188 |
| 22 23 | 47448 47436 | 46734 46722 | 46032 46020 | 45341 45330 | 44661 44650 | 43992 43981 | 43332 43321 | 42683 42672 | 42043 42032 | | | 40178 40168 |
| 24 | 47424 | 46710 | 46009 | 45318 | 44639 | 43969 | 43310 | 42661 | 42022 42011 | | 40770 | 40157 |
| 25 26 | 47412 47400 | 46699 46687 | 45997 45986 | 45307 45295 | | 43958 43947 | 43289 | 42640 | 42000 | 41370 | 7 7 7 7 7 | |
| 27 28 | 47388 47376 | 46675 | 45974 45962 | 45284 45273 | 44605 44594 | 43936 43925 | | 42629 42618 | 41990 41979 | | | 40127 |
| 29 | 47364 | 46652 | 45951 | 45261 | 44583 | | | 42608 | 41969 | 41339 | 40719 | 40107 |
| 30 31 | 47352 47340 | 46640 46628 | 45939 45928 | 45250 45238 | 44571 44560 | 43903 43892 | 43234 | 42597 42586 | | 41318 | 40708 40698 | |
| 32 33 | 47328 47316 | 46616 46604 | 45916 45905 | 45227 45216 | 44549 44538 | 43881 43870 | 43223 43212 | | | 41308 41298 | | 40076 |
| 34 35 | 47304 47292 | | 45893 45881 | 45204 45193 | 44526 | 43859 43848 | 43202 | 42554 | 41916 | 41287 | 40667 40657 | 40056 40046 |
| 36 | 47280 | 46569 | 45870 | 45182 | 44504 | 43837 | 43180 | 42533 | 41895 | 41266 | 40647 | 40036 |
| 37 38 | 47268 47256 | | 45858 45847 | 45170 45159 | 44493 44482 | 43826 43815 | | | 41884 41874 | | | 40026 40016 |
| 39 40 | 47244 | 46534 | 45835 | 45147 | 44470 | 43804 | | 42500 | 41863 | | | 40006 39996 |
| 41 | 47220 | 46510 | 45812 | 45125 | 44448 | 43782 | 43126 | 42479 | 41842 | 41214 | 40596 | 39985 |
| 42 43 | 47208 47196 | | 45800 45789 | 45113 45102 | 44437 | 43771 43760 | 43115 43104 | | 41832 | 41204 | | 39975 39965 |
| 44 45 | 47185 47173 | | 45777 45766 | 45091 45079 | 44414 44403 | 43749 43738 | | | 41811 41800 | 41183 | | |
| 46 | 47161 | 46452 | 45754 | 45068 | 44392 | 43727 | 43071 | 42426 | 41789 | 41162 | 40544 | 39935 |
| 48 | 47149 47137 | 46428 | 45731 | 45045 | 44370 | 43716 43705 | 43050 | 42404 | 41768 | 41152 41142 | 40524 | 39915 |
| 49 50 | | | 45720 | | | | 43039 | | | | | |
| 51 | 47101 | 46393 | 45697 | 45011 | 44336 | 43672 | 43017 | 42372 | 41737 | 41111 | 40493 | 39885 |
| 52 53 | 47077 | 46370 | 45674 | 44988 | 44314 | 43650 | 43006 42995 | 42351 | 41716 | 41090 | 40473 | 39364 |
| 54 55 | 47066 47054 | 46358 46346 | 45662 45651 | 44977 | 44303 | 43639 | 42985 42974 | 42340 | 41705 | 41080 | 40463 | 39854 39844 |
| 56 57 | 47042 | 46335 | 45639 45628 | 44955 | 44280 | 43617 | 42963 42952 | 42319 | 41684 | 41059 | 40142 | 39834 |
| 58 | 47018 | 46311 | 45616 | 44932 | 44258 | 43595 | 42941 | 42298 | 41663 | 41038 | 40422 | 39814 |
| 59 F | | onal Pa | 45605 | | 44247 | .2 | .3 | 42287 | | | 7 . | |
| _ | | of " or | | | î | 2 | 3 | 4 | 5 | | | 9 10 |

| 1 Degree, | or 1 | Hour. |
|-----------|------|-------|
|-----------|------|-------|

| ı | _ | | | | | | B, | | | | | | |
|---|----|---------|---------|-------|-----------------|-------|-------|-------|-------|-------|-------|-------|-------|
| ı | 11 | 10- | 100 | 1400 | 2000 | 1201 | 1 | 201 | - 1 | 201 | -1 | / | |
| I | S | 12m | 13m | 14m | 15 ^m | 16m | 17m | 18m | 19m | 20m | 21m | 22m | 23m |
| I | 0 | 39794 | 39195 | 38604 | 38051 | 37446 | 36878 | | | 35218 | 34679 | 34146 | |
| I | 1 | 39784 | 39185 | 38594 | 38011 | 37436 | 36869 | 36309 | | 35209 | 34670 | 34137 | |
| ı | 2 | 39774 | 39175 | 38585 | 38002 | 37427 | 36859 | | | 35200 | 34661 | 34128 | |
| 1 | 3 | 39764 | 39165 | 38575 | 37992 | 37417 | 36850 | | | 35191 | 34652 | 34119 | |
| ı | 4 | 39751 | 39155 | 38565 | 37983 | 37408 | | 36281 | | 35182 | 34643 | 34111 | 33585 |
| ı | 5 | 39744 | 39145 | 38555 | 37973 | 37398 | 36831 | 36271 | 35719 | 35173 | 34634 | 34102 | 33576 |
| ł | 6 | 39734 | 39136 | 38545 | 37963 | 37389 | 36822 | | | 35164 | 34625 | 34093 | |
| ł | 7 | 39724 | 39126 | 38536 | 37954 | 37379 | 36812 | 36253 | | 35155 | 34616 | 34084 | 33558 |
| ı | 8 | 39714 | 39116 | 38526 | 37944 | 37370 | 36803 | | 35691 | 35146 | 34607 | 34075 | 33550 |
| ı | 9 | 39704 | 39106 | 38516 | 37934 | 37360 | 36794 | 36234 | 35682 | 35137 | 34598 | 34066 | 33541 |
| - | 10 | 39694 | 39096 | 38506 | 37925 | 37351 | 36784 | 36225 | 35673 | 35128 | 34589 | 34058 | 33532 |
| I | 11 | 39684 | 39086 | 38497 | 37915 | 37341 | 36775 | 36216 | 35664 | 35119 | 34581 | 34049 | 33524 |
| 1 | 12 | 39674 | 39076 | 38487 | 37905 | 37332 | 36766 | 36207 | 35655 | 35110 | 34572 | 34040 | 33515 |
| 1 | 13 | 39664 | 39066 | 38477 | 37896 | 37322 | 36756 | 36197 | 35646 | 35101 | 34563 | 34031 | 33506 |
| I | 14 | 39653 | 39056 | 38467 | 37886 | 37313 | 36747 | 36188 | 35636 | 35092 | 34554 | 34022 | 33498 |
| 1 | 15 | 39643 | 39046 | 38458 | 37877 | 37303 | 36737 | 36179 | | 35083 | 34545 | 34014 | 33489 |
| I | 16 | 39633 | 39037 | 38448 | 37867 | 37294 | 36728 | 36170 | 35618 | 35074 | 34536 | 34005 | 33480 |
| I | 17 | 39623 | 39027 | 38438 | 37857 | 37284 | 36719 | 36160 | 35609 | 35065 | 34527 | 33996 | 33471 |
| ı | 18 | 39613 | 39017 | 38428 | 37848 | 37275 | 36709 | 36151 | 35600 | 35056 | 34518 | 33987 | 33463 |
| - | 19 | 39603 | 39007 | 38419 | 37838 | 37265 | 36700 | 36142 | | 35047 | 34509 | 33978 | 33454 |
| ľ | 20 | 39593 | 38997 | 38409 | 37829 | 37256 | 36691 | 36133 | 35582 | 35038 | 34500 | 33970 | 33445 |
| - | 21 | 3958 | 38987 | 38399 | 37819 | 37246 | 36681 | 36123 | | 35029 | 34491 | 33961 | 33437 |
| 1 | 22 | 39573 | 38977 | 38389 | 37809 | 37237 | 36672 | | | | | | |
| 1 | 23 | 39563 | 38968 | 38380 | 37800 | 37227 | 36663 | | | 35011 | 34474 | 33943 | |
| ı | 24 | 39553 | 38958 | 38370 | | 37218 | | | | | 34465 | 33935 | |
| ı | 25 | 39543 | 38948 | 38360 | | 37208 | 36644 | | | 34993 | 34456 | 33926 | |
| 1 | 26 | 39538 | 38938 | 38351 | 37771 | 37199 | 36634 | | 35527 | 34984 | 34447 | 33917 | |
| ı | 27 | 39523 | 38928 | 38341 | 37761 | 37189 | 36625 | | 35518 | 34975 | 34438 | 33908 | |
| ı | 28 | 39519 | 38918 | 38331 | 37752 | 37180 | 36616 | 36059 | 35509 | 34966 | 34429 | 33899 | |
| ı | 29 | 39503 | 38908 | 38321 | 37742 | 37171 | 36606 | | | 34957 | 34420 | 33891 | 33367 |
| ı | 30 | 3949. | 38899 | 38312 | 37733 | 37161 | 36597 | 36040 | | 31948 | 34411 | 33882 | |
| ı | 31 | 3948 | 38889 | 38302 | 37723 | 37152 | 36588 | | | 34939 | 34403 | 33873 | |
| ı | 32 | 3917: | 38879 | 38292 | | 37142 | 36578 | | | 34930 | 34394 | 33864 | |
| ı | 33 | 39464 | 38869 | 38282 | 37704 | 37133 | 36569 | 36013 | | 34921 | 34385 | 33856 | |
| ı | 34 | 39451 | 38859 | 38273 | 37694 | 37123 | 36560 | | | 34912 | 34376 | 33847 | |
| ı | 35 | 39444 | 38849 | 38263 | | 37114 | 36550 | | | 34903 | | 33838 | |
| 1 | 36 | 39434 | 38839 | 38253 | 37675 | 37104 | 36541 | 35985 | | | | 33829 | |
| ı | 37 | 39424 | 38830 | 38244 | 37665 | 37095 | 36532 | | | 34885 | 34349 | 33820 | |
| ı | 38 | 39414 | 38820 | 38234 | 37656 | 37085 | 36522 | | 35418 | 34876 | 34340 | 33812 | |
| 1 | 39 | 39404 | 38810 | 38224 | 37646 | 37076 | 36513 | | 35409 | 34867 | 34332 | 33803 | |
| ı | 40 | 3939 | 38800 | 38215 | 37637 | 37067 | 36504 | 35948 | 35400 | 34858 | 34323 | 33794 | 33272 |
| ı | 41 | 39384 | 38790 | 38205 | | 37057 | 36494 | | | 34849 | 34314 | 33785 | |
| 1 | 12 | 39374 | 38781 | 38195 | | 37048 | 36485 | | | 34840 | 34305 | 33777 | 33255 |
| | 43 | 39364 | 38771 | 38186 | | 37038 | | | 35372 | 34831 | 34296 | 33768 | |
| ı | 44 | 39354 | 38761 | 38176 | | 37029 | 36467 | | 35363 | 34822 | 34287 | 33759 | |
| | 45 | 39344 | 38751 | 38166 | | 37019 | 36457 | 35902 | | 34813 | 34278 | 33750 | |
| ı | 46 | 39334 | 38741 | 38156 | | 37010 | 36448 | 35893 | | 34804 | 34270 | 33742 | |
| ı | 47 | 39324 | 38731 | 38147 | | 37001 | 36439 | | | 34795 | 34261 | 33733 | |
| ı | 48 | 39314 | 38722 | 38137 | | 36991 | 36429 | 35875 | | 34786 | 34252 | 33724 | |
| ŀ | 49 | 39304 | 38712 | 38127 | 37551 | 36982 | 36420 | | | 34777 | 34243 | 33715 | |
| ı | 50 | 39291 | 38702 | 38118 | 37541 | 36972 | 36411 | 35856 | 35309 | 34768 | 34234 | 33707 | 33186 |
| | 51 | 39284 | 38692 | 38108 | | 36963 | | 35847 | 35300 | 34759 | 34225 | 33698 | |
| | 52 | 39274 | 38682 | | | 36953 | 36392 | 35838 | 35291 | 34750 | 34217 | 33689 | 33168 |
| | 53 | 39264 | 38673 | | | 36944 | 36383 | | 35282 | 34741 | 34208 | | 33160 |
| 1 | 54 | 39254 | 38663 | | | | 36374 | | | 34732 | 34199 | 33672 | |
| | 55 | 39245 | | | | 36925 | 36364 | | | 34723 | | 33663 | |
| 1 | 56 | 39235 | | | | | | | 35254 | 34715 | 34181 | 33654 | |
| | 57 | 39225 | | | | | | | | | | 33646 | |
| | 58 | 39215 | | 1 - | 1 | | | | | 34697 | 34161 | 33637 | |
| | 59 | 39205 | | | 37455 | | | 35774 | | 34688 | 34155 | 33628 | |
| | P | roporti | onal Pa | | | .1 | .2 | .3 | .4 | | | 7 | 1 |
| | | | of" or | | | 1 | 2 | 3 | 4 | 4 | 5 | 6 | 7 8 |
| | | | | | | | | | | | | | |

| 76 | | TABLI | ε X. | 1 | Proport | ional I | ogaritl | hms. | | - | | |
|----------|----------------|--------------------|----------------|----------------|----------------|----------------|----------------|-----------------|----------------|----------------|----------------|--------------|
| | | | | | 1 De | gree, or | 1 Hou | r. | | | | |
| " S | 24m | 25m | 26m | 27m | 28m | 29m | 30m | 31 ^m | 32m | 33m | 34m | 35m |
| 0 | 33099 | 32585 | 32077 | 31575 | 31079 | 30588 | 30103 | | 29148 | 28679 | 28214 | |
| 1 | 33091 | 32577 | 32069 | 31567 | 31071 | 30580 | 30095 | 29615 | 29141 | 28671 | 28207 | 27747 |
| 2 | 33082 33073 | 32568 32560 | | 31559 31550 | | 30572 30564 | 30087 | | 29133 29125 | 28663 28656 | | 27740 |
| 4 | 33065 | 32551 | 32044 | | | | 30071 | 29591 | 29117 | 28648 | | |
| 5 | 33056 | 32543 | | | 31038 | 30548 | 30063 | | | 28640 | | |
| 6 | 33048 33039 | 32534 32526 | | | 31030 31021 | 30539 30531 | 30055 | 29575 29567 | 29101 29093 | 28632 28625 | | 2770 |
| 8 | 33030 | 32517 | 32019 | | 31013 | 30523 | 30039 | 29560 | 29086 | 28617 | 28153 | |
| 9 | 33022 | 32509 | 35005 | | 31005 | 30515 | 30031 | 29552 | 29078 | 28609 | | |
| 10 | 33013 | 32500 | 31993 | | 30997 | 30507 | 30023 | | 29070 | 28601 | | |
| 11 | 33005 | 32492 | 31985 | | 30989 | 30499 | 30015 | 29536 | 29062 | 28593 | | |
| 12 13 | 32996 32987 | 32483 32475 | 31977 31968 | | 30980 30972 | 30491 30483 | 30007 29999 | | 29054 29046 | 28586 28578 | | |
| 14 | 32979 | 32466 | 31960 | | 30964 | 30475 | 29991 | 29512 | 29038 | .28570 | | 2764 |
| 15 | 32970 | 32458 | 31951 | | 30956 | 30466 | 29983 | | 29031 | 28562 | | |
| 16 | 32962 | 32449 | 31943 | | 30948 | 30458 | 29975 | 29496 | 29023 | 28555 28547 | | |
| 17 18 | 32953 32944 | 32441 32432 | 31935 31926 | | 30939 30931 | 30450 30442 | 29967 29958 | 29488 29480 | 29015 29007 | 28539 | | |
| 19 | 32936 | 32424 | 31918 | | | 30434 | 29950 | 29472 | 28999 | | 28068 | |
| 20 | 32927 | 32415 | 31909 | 31409 | 30915 | 30426 | 29942 | 29464 | 28991 | 28524 | 28061 | 2760 |
| 21 | 32919 | 32407 | 31901 | 31401 | 30907 | 30418 | 29934 | | | | | |
| 22 23 | 32910 | 32398 32390 | | | | 30410 30402 | 29926 | | 28976 | 28508 28500 | | |
| 24 | 32902 32893 | 32381 | 31884 31876 | | 30890 30882 | 30393 | 29918 29910 | 29433 | 28968 28960 | | 1 | |
| 25 | 32884 | 32373 | | | | 30385 | 29902 | | | | | |
| 26 | 32876 | 32365 | 31859 | | | 30377 | 29894 | | 28944 | | 1 | |
| 27 28 | 32867 | 32356 | | | 30857 | 30369 | 29886 | | | | | |
| 29 | 32859 32850 | 32348 32339 | 31842 31834 | | 30849 30841 | 30361 30353 | 29878 29870 | 29393 | 28929 28921 | 28462 28454 | | 100 |
| 30 | 32842 | 32331 | 31826 | | 30833 | 30345 | 29862 | 29385 | 28913 | 28446 | | |
| 31 | 32833 | 32322 | 31817 | 31318 | | 30337 | 29854 | | 28905 | | | |
| 32 | 32824 | 32314 | 31809 | | 30817 | 30329 | 29846 | | 28897 | 28431 | 27969 | |
| 33 34 | 32816 32807 | 32305 32297 | 31801 31792 | | 30808 30800 | 30321 30313 | 29838 29830 | | 28890 28882 | | | |
| 35 | 32799 | 32288 | 31784 | | 30792 | 30305 | 29822 | 29346 | 28874 | 28407 | | |
| 36 | 32790 | 32280 | 31775 | 31277 | 30784 | 30296 | 29814 | 29338 | 28866 | 28400 | 27938 | 2748 |
| 37 | 32782 | 32271 | 31767 | | | 30288 | 29806 | | | 28392 | | 2747 |
| 38 39 | 32773 | 32263 32255 | 31759 31750 | | 30768 30759 | 30280 30272 | 29798 29790 | | 28851 28843 | 28384 28376 | | 2746 2745 |
| 40 | 32756 | 32246 | 31742 | | 30751 | 30264 | 29782 | | 28835 | 28369 | | |
| 41 | 32747 | 32238 | 31734 | | 30743 | | 29775 | 29298 | 28827 | 28361 | 27900 | |
| 42 | 32739 | 32229 | 31725 | | 30735 | 30248 | 29767 | 29290 | 28819 | | | |
| 43 44 | 32730 | | 31717 | | | 30240 | 29759 | | | 28346 | | |
| 45 | 32722 | 32212 32204 | 31709 31700 | | 30719 30710 | 30232 30224 | 29751 29743 | 29275 29267 | 28804 28796 | | | |
| 46 | 32705 | 32195 | 31692 | | | | 29735 | | | | | 2740 |
| 47 | 32696 | 32187 | 31684 | 31186 | 30694 | 30208 | 29727 | 29251 | 28780 | 28315 | 27854 | 2739 |
| 48 49 | 32688 | 32179 | 31675 | 31178 | 30686 | 30200 | 29719 | 29243 | 28772 | 28307 | 27846 | |
| 50 | | | | 31170 | 30678 | | | | | 28299 | - | - |
| 51 | 32662 | 32153 | | | 30670 30662 | | 29703 29695 | | 28757 28749 | 28292 28284 | | 2737 2736 |
| 52 | 32654 | 32145 | 31642 | 31145 | 30653 | 30167 | 29687 | | | | 27816 | |
| 53 | 32645 | 32136 | 31634 | 31137 | 30645 | 30159 | 29679 | 29204 | 28733 | 28268 | 27808 | 2735 |
| 54 55 | 32636 | 32128 | 31625 | 31128 | 30637 | 30151 | 29671 | | | 28261 | | |
| 56 | 32619 | 32111 | 31609 | 311120 | 30629 30621 | 30143 30135 | | | | 28253 | 27793 27785 | |
| 57 | 32611 | 32103 | 31600 | 31104 | 30613 | | | | | | | |
| 58 | 32602 | 32094 | 31592 | 31095 | 30605 | 30119 | 29639 | 29164 | 28695 | 28230 | 27770 | 2731 |
| 59 | 32504 | 32086 | 31584 | 31087 | 30596 | | | | | | 27763 | |
| P | roportio | onal Pa of " or | ert to te | nths | .1 | .2 | .3 | .4 | | | 7 | |
| - | | J 01 | M* | - | 1 | 5 | 2 | 3 | 4 | 5 | 6 | 6 |

| | | | | | 1 De | gree, or | 1 Hour | • | | | | |
|----------|----------------|----------------|-----------------|-----------------|-----------------|----------------|----------------|----------------|----------------|----------------|-----------------|----------------|
| 8 | 36m | 37m | 38 ^m | 39 ^m | 40 ^m | 41m | 42m | 43m | 44m | 45m | 46 ^m | 47m |
| 0 | 27300 | 26850 | 26405 | 25964 | 25527 | 25095 | 24667 | 24244 | 23824 | 23408 | 22997 | 22589 |
| 1 2 | 27293 27285 | 26843 26835 | 26397 26390 | 25956 25949 | 25520 25513 | | 24660 24653 | 24237 24229 | 23817 23810 | 23401 23395 | 22990 22983 | 22582 22575 |
| 3 | 27278 | 26828 | 26382 | 25942 | 25506 | | | 24222 | 23803 | 23388 | | 22569 |
| 4 | 27270 | 26820 | | 25934 | 25498 | | | 24215 | 23796 | 23381 | 22969 | 22562 |
| 5 | 27262 | 26813 | 26368 | 25927 | 25491 | 25059 | | 24208 | | 23374 | | 22555 |
| 6 | 27255 | 26805 | 26360 | 25920 | 25484 | | 24625 | 24201 | 23782 | 23367 | | 22548 |
| 8 | 27247 | 26798 26790 | 26353 26346 | 25913 25905 | 25477 25469 | 25045 25038 | | 24194 24187 | | 23360 23353 | | 22542 22535 |
| 9 | 27232 | 26783 | | 25898 | 25462 | | 24603 | 24180 | | 23346 | | 22528 |
| 10 | 27225 | 26776 | | 25891 | 25455 | | - | - | | 23339 | | |
| 11 | 27217 | 26768 | | 25883 | | 25016 | 24589 | 24166 | 23747 | 23333 | | 22515 |
| 12 | 27210 | | | 25876 | | | | | | 23326 | | |
| 13 | 27202 | | | 25869 | | 25002 | | 24152 | | | | 22501 |
| 14 | 27195 27187 | 26746 26738 | | 25861 25854 | | 24995 24988 | | | | 23312 23305 | | 22494 22488 |
| 16 | 27180 | | | 25847 | | 24981 | | 24131 | | | | 22481 |
| 17 | 27172 | 26723 | | 25840 | 25404 | | | | | | | |
| 18 | 27165 | 26716 | 26271 | 25832 | 25397 | 24966 | | | | | | |
| 19 | 27157 | 26709 | - | 25825 | 25390 | | - | 24110 | | | | 22161 |
| 50 | 27150 | 26701 | 26257 | 25818 | 25383 | | | | | 23271 | 22860 22854 | 22454 |
| 21 | 27142 27135 | | | 25810 25803 | | | | | | 23264 23257 | | |
| 23 | 27127 | | | | | 24931 | | | | | | |
| 24 | 27120 | | | | 25354 | 24923 | | 24075 | 23657 | 23243 | | |
| 25 | 27112 | | | | 25347 | | | | | | | |
| 26 27 | 27105 | | | | 25339 | | | | | | | |
| 28 | 27097 27090 | | 26206 26198 | | 25332 25325 | | | | | | | |
| 29 | 27082 | 26634 | 26191 | 25752 | 25318 | | | | | | | |
| 30 | 27075 | 26627 | 26184 | | 25311 | 24881 | 24455 | 24033 | 23616 | 23202 | 22792 | 22386 |
| 31 | 27067 | 26619 | 26176 | | | 24874 | 24448 | | | | | |
| 32 | 27060 | | | | | | | | | | | 100000 |
| 33 | 27052 27045 | | | | 25289 25282 | | | | | | | |
| 35 | 27037 | | | | | | | | | | | |
| 36 | 27030 | | | | | | | | | | 22752 | |
| 37 | 27022 | | | | | | | | | | | |
| 38 39 | 27015 27007 | | 26125 26118 | | 25253 | | | 23977 23970 | | | | |
| 40 | 27000 | 26560 26553 | | | 25246 25239 | | - | | | | _ | |
| 41 | 26992 | | | | | | | | | | | |
| 42 | 26985 | | | | | | | | | | | |
| 43 | 26977 | | | | | | | | | | | |
| 44 45 | 26970 26962 | | | | | | | | | | | |
| 46 | 26955 | | | | | | | | | | | |
| 47 | 26947 | | | | | | | | | | | |
| 48 | 26940 | | | 25614 | | 24752 | 24328 | | 23491 | | | |
| 49 | 26932 | - | - | | | | | 23901 | | | - | |
| 50 | 26925 | | | | | | | | | | | |
| 51 52 | 26917 | | | | | 24731 | | | | 23058 | 22650 | 22245 |
| | | | | | | | | | | | | 22239 |
| 54 | 26895 | 26449 | 26008 | 25571 | 25138 | 24710 | 24286 | 23866 | 23450 | 23038 | 22629 | 22225 |
| 55 | | 26442 | 26000 | 25563 | 25131 | 24703 | 24279 | 23859 | 23443 | 23031 | 22623 | 22218 |
| 56 57 | | 26434 26427 | | | | | | | | | 22616 22609 | 22212 |
| 58 | 26865 | 26419 | 25978 | 25549 | 25117 | 24681 | 24203 | 23838 | 23429 | 23017 | 22609 | 22205 |
| | 26858 | 26412 | 25971 | 25534 | 25102 | 24674 | 24251 | 23831 | | | | 22192 |
| - | | onal Pa | rt to te | - | .1 | .2 | .3 | .4 | .5 | | 1 | 8 .9 |
| | = | of" or | S. | | 1 | 1 | 2 | 3 | 3 | 4 | | 6 6 |

| The color of the | 78 | | TABLE | X. | P | roporti | ional L | ogarith | ıms. | | | | |
|--|---------|-------------------|-------|-------|-------|---------|----------|---------|-------|-----------------|-------|-------|----------------|
| The color of the | 1 | | | | | 1 De | gree, or | 1 Hour | | | | | |
| 1 29178 21776 21381 20988 20599 20213 19830 19451 19075 18702 18333 1796 2 22171 21773 2375 20982 20583 20907 19824 19454 19666 18327 1792 4 22158 21765 21362 20969 20580 20200 19818 19439 19063 18690 18321 1793 4 22158 21765 21362 20969 20580 20194 19811 19432 19056 18684 18315 1793 6 22145 21745 21345 20049 20560 20573 20187 19803 19466 19050 18678 18309 1795 6 22145 21745 21349 20056 20567 20181 19799 19420 19044 18678 18309 1795 20181 21732 21335 20943 20554 20166 19786 19407 19032 18653 18296 1795 20181 21712 21335 20943 20554 20166 19786 19407 19032 18653 18294 1799 21225 21722 21329 20936 20547 20162 19780 19401 19023 18653 18284 1799 1792 1792 21215 21722 21329 20936 20547 20162 19780 19401 19023 18653 18284 1799 1792 | // S | . 48 ^m | | | | | | | | and the same of | | | 59m |
| \$\frac{9}{3} \ 22171 21771 21375 20982 20586 20200 19818 19439 19063 18690 18321 1792 \$2115 21758 21368 20969 20586 20200 19818 19439 19063 18690 18321 1793 \$5 22151 21751 21355 20962 20573 20187 19803 19426 19050 18678 18305 1793 \$7 22138 21738 21342 20949 20560 20175 19792 19413 19038 18665 18296 1793 \$8 22131 21732 21335 20943 20547 20168 19786 19407 19032 18663 18296 1793 \$8 22131 21732 21335 20943 20547 20168 19786 19407 19032 18663 18296 1793 \$8 22131 21732 21335 20943 20547 20168 19786 19407 19032 18663 18284 1793 \$1 22118 21718 21322 20033 20547 20162 19780 19401 19025 18653 18284 1793 \$1 22118 21718 21332 20033 20547 20162 19780 19401 19025 18653 18284 1793 \$1 22111 21712 21316 20923 20534 20149 19767 19388 19013 18647 18787 1794 \$1 22015 21705 21309 20917 20528 20143 19761 19382 19007 18634 18664 18787 1794 \$1 22098 21699 21303 20910 20528 20143 19761 19382 19007 18634 18664 18787 1794 \$1 22091 21692 21296 20904 20515 20130 19748 19369 18994 18622 1853 1786 1794 \$1 22091 21692 21296 20904 20515 20130 19748 19369 18994 18622 1853 1786 1794 \$1 22091 21665 21287 20865 20469 20111 19729 19351 18976 18604 18233 1786 18928 1786 \$1 22054 21665 21257 20865 20476 20091 19710 19332 18956 18604 18233 1786 \$2 22058 21659 21247 20858 20447 20072 19691 19313 18978 18591 1878 1879 1810 1888 \$2 22058 21659 21247 20858 20447 20072 19691 19313 18978 18545 18192 1786 \$2 22014 21662 21276 20865 20447 20072 19691 19313 18956 18654 18192 1786 \$2 22014 21662 21276 20865 20446 | | | | | | | | | | | | | 17973 |
| \$\frac{9}{4} \$2156 \$2156 \$21368 \$20905 \$20580 \$20181 \$19432 \$19063 \$18690 \$1831 \$1794 \$52151 \$21751 \$21355 \$20962 \$20573 \$20187 \$19805 \$19426 \$19050 \$18678 \$18315 \$1794 \$6721 \$1792 \$1932 \$1932 \$19420 \$19044 \$18672 \$18302 \$1795 \$1798 \$1738 \$21342 \$20945 \$20560 \$20175 \$19792 \$19413 \$19033 \$18655 \$18296 \$1795 \$1922 \$1932 \$21725 \$21329 \$20936 \$20547 \$20162 \$19780 \$19401 \$19025 \$18659 \$18296 \$1795 \$1922 \$1323 \$20345 \$20547 \$20162 \$19780 \$19401 \$19025 \$18659 \$18296 \$1795 \$1922 \$1323 \$20345 \$20547 \$20162 \$19780 \$19401 \$19025 \$18659 \$18296 \$1795 \$1921 \$19112 \$1118 \$21322 \$20930 \$20541 \$20155 \$19773 \$19385 \$19013 \$18641 \$18772 \$1797 \$1922 \$1303 \$20107 \$20528 \$20133 \$19767 \$19388 \$19013 \$18641 \$18772 \$1797 \$12 \$2105 \$21705 \$21309 \$20173 \$20528 \$20133 \$19754 \$19376 \$19007 \$18634 \$18266 \$1795 \$1309 \$20162 \$21705 \$21605 \$21905 \$20094 \$20155 \$20130 \$19748 \$19369 \$19007 \$18634 \$18266 \$1795 \$1652 \$12859 \$20897 \$20136 \$19754 \$19376 \$19007 \$18634 \$18266 \$1795 \$1652 \$12859 \$20897 \$20136 \$19754 \$19366 \$19007 \$18634 \$18266 \$1795 \$1652 \$12859 \$20897 \$20163 \$19744 \$19363 \$18984 \$18625 \$18477 \$1885 \$18661 \$18447 \$1785 \$18260 \$18260 \$18260 \$18260 \$18260 \$18260 \$18260 \$18260 \$18260 \$18260 \$1976 \$19324 \$18665 \$18260 \$18260 \$18260 \$18260 \$19260 \$19260 \$19260 \$19260 \$19260 \$19260 \$19260 \$19260 \$18260 \$18260 \$19260 \$1 | | | | | | | | | | | | | 17960 |
| Second Color | 3 | 22165 | 21765 | 21368 | 20975 | 20586 | 20200 | 19818 | 19439 | 19063 | 18690 | 18321 | 17954 |
| The color of the | | | | | | | | | | | | | 17948 |
| 7 29138 21732 21342 20949 20556 20175 19792 19413 19038 18665 18296 1799 20125 21725 21329 20936 20547 20162 19780 19401 19032 18655 18294 1791 11 22111 21712 21316 20923 20534 20145 19767 19388 19013 18641 18272 1791 12 21110 21712 21316 20923 20534 20149 19767 19388 19013 18641 18272 1791 12 2005 21705 21309 20917 20528 20143 19761 19382 19007 18634 18266 1799 18292 1990 21692 21296 20904 20515 20130 19748 19369 18994 18622 18253 1781 182908 21698 21303 20910 20522 20136 19754 19376 19000 18628 18295 1781 182908 21698 21298 20994 20515 20130 19748 19369 18994 18622 18253 1781 182908 21685 21283 20891 20509 20123 19742 19363 18988 18616 18241 1782 1792 1971 21672 21276 20884 20166 20111 19723 19351 18976 18604 18241 1782 178 | | | | | | | | | | | | | 17942 17936 |
| S 2213 21732 21335 20943 20554 20168 19766 19401 19025 18653 18290 1790 | | | | | | | | | | | | | |
| The color of the | 8 | 22131 | 21732 | 21335 | 20943 | 20554 | 20168 | 19786 | 19407 | 19032 | 18659 | 18290 | 17924 |
| 11 22111 21712 21316 20023 20534 20143 19761 19382 19007 18634 18266 1796 138 22098 21505 21505 20130 20512 20136 19754 19376 19000 18634 18266 1796 148 1 | - | | | - | | - | | | | | | | 17918 |
| 12 22105 21705 21303 20917 20528 20143 19761 19382 19007 18634 18266 1794 182091 21692 21996 20904 20515 20130 19748 19369 18994 18622 18253 1786 182091 21692 21996 20904 20515 20130 19748 19369 18994 18622 18253 1786 16 22078 21678 21289 20897 20509 20123 19742 19363 18988 18616 18247 1786 17909 20137 21672 21676 20884 20196 20111 19729 19351 18976 18604 18235 1786 182064 21665 21270 20878 20189 20104 19723 19344 18869 18597 18229 1786 182064 21655 21270 20878 20189 20104 19723 19344 18669 18597 18229 1786 192044 21645 21250 20588 20476 20091 19710 19332 18963 18591 18235 1786 122044 21645 21250 20588 20476 20091 19710 19332 18947 18553 18271 1788 12202 22038 21639 21243 20852 20464 20079 19697 19319 18944 18573 18204 1788 12202 22038 21639 21237 20845 20445 20079 19697 19319 18944 18573 18204 1788 12202 21626 21230 20839 20445 20066 19685 19307 18932 18560 18199 1788 1829 1788 1829 1788 1829 1788 1829 1788 1829 182 | | | | | | | | | | | | | 17912 17906 |
| 14 22098 21698 21396 20904 20515 20130 19744 19376 19000 18628 18239 1784 152094 21695 21296 20997 20509 20131 19742 19363 18988 18616 18247 1785 1785 1792071 21672 21276 20884 20196 20111 19729 19351 18976 18604 18235 1786 182064 21665 21270 20878 20897 20509 20117 19735 19357 18982 18610 18241 1786 182064 21665 21263 20871 20483 20098 20104 19723 19344 18969 18597 18229 1786 18220 | | | | | | | | | | | | | |
| 15 22084 21685 21283 20897 20509 20123 19742 19363 18988 18616 18247 1788 1782 17207 21672 21276 20884 20196 20111 19729 19351 18976 18604 18235 1781 1882 18616 18247 1788 1782 1782 1882 18616 18247 1788 1882 18616 18247 1788 1882 18616 18247 1788 1882 18616 18247 1788 1882 18616 18247 1788 1882 18616 18247 1788 1882 18616 18247 1788 1882 18616 18247 1788 1882 | 13 | 22098 | 21698 | 21303 | 20910 | 20522 | 20136 | 19754 | 19376 | 19000 | 18628 | 18259 | 17894 |
| 16 | | | | | | | | | | | | | 17887 |
| 17 | | | | | | | | | | | | | 17881 17875 |
| 18 | | | | | | | | | | | | | 17869 |
| 20 | 18 | 22064 | 21665 | 21270 | 20878 | 20189 | 20104 | 19723 | 19344 | 18969 | 18597 | 18229 | 17863 |
| 21 | - | | | - | | - | - | | - | - | | | |
| 22 22038 21639 21247 20845 20464 20079 19697 19319 18944 18573 18204 17868 18204 21237 20845 20457 20072 19691 19313 18936 18567 18193 17888 22024 21626 21230 20839 20451 20066 19685 19307 18932 18560 18192 17888 25 22018 21619 21247 20826 20438 20053 19672 19294 18920 18548 18180 17888 21994 21606 21211 20819 20131 20047 19666 19288 18913 18542 18174 17888 17898 21994 21592 21198 20424 20832 20444 20060 19678 19300 18926 18548 18180 17888 21998 21599 21204 20813 20425 20040 19659 19282 18907 18536 18168 17888 21991 21592 21198 20806 20418 20034 19659 19225 18907 18536 18168 17888 21991 21592 21198 20800 20412 20028 19647 19269 18895 18533 18162 1778 21971 21573 21178 20787 20399 20015 19634 19257 18882 18511 18143 1778 21937 21553 21158 20761 20380 20009 19628 19250 18876 18505 18131 1778 21938 21540 21152 20761 20373 19989 19609 19231 18857 18487 18119 1778 21938 21540 21152 20761 20373 19989 19609 19231 18857 18487 18119 1778 18882 18517 18143 1778 18882 18517 18143 1778 18882 18517 18143 1778 18882 18517 18143 1778 18882 18517 18143 1778 18882 18884 1888 | | | | | | | | | | | | | |
| 23 | | | | | | | | | | | | | |
| 24 29024 21626 21230 20839 20451 20066 19685 19307 18932 18560 18192 178 25 22018 21619 21242 20832 20444 20060 19678 19300 18926 18554 18186 178 26 22011 21606 21211 20819 20131 20047 19666 19288 18913 18542 18180 178 27 22004 21599 21204 20813 20425 20040 19659 19282 18907 18536 18168 178 29 21991 21592 21198 20806 20418 20034 19657 19282 18907 18536 18168 178 30 21582 21591 20806 20418 20034 19657 18951 18533 18162 177 31 21978 21573 21184 20737 20399 20015 19634 19257 | 23 | 22031 | 21632 | 21237 | 20845 | 20457 | 20072 | 19691 | 19313 | 18938 | 18567 | 18193 | 17833 |
| 26 | | | | 21230 | | | | | | | | | |
| 27 | | | | | | | | | | | | | |
| 28 | 27 | | | | | | | | | | | | |
| 30 | 28 | 21998 | 21599 | 21204 | 20813 | 20425 | 20040 | 19659 | 19282 | 18907 | 18536 | 18168 | 17803 |
| 31 21978 21579 21184 20793 20406 20021 19640 19263 18888 18517 18149 1773 1832 21971 21573 21178 20787 20399 20015 19634 19257 18882 18511 18143 1773 1832 11964 21958 21559 21165 20774 20386 20002 19621 19244 18870 18499 18131 1773 1773 1774 1855 21553 21158 20767 20380 19996 19615 19238 18864 18493 18125 1774 1857 18882 1857 18882 18517 1874 1875 18882 18517 1874 1875 18882 18517 1874 1875 18882 18517 1874 1875 18882 18517 1874 1875 18882 18517 1874 1875 18882 18517 1874 1875 1875 18882 18518 1874 1875 1875 18882 18884 18893 18882 18884 18893 18882 18884 18893 18884 1889 | - | | | | | | | | - | | - | | - |
| 32 21971 21573 21178 20787 20399 20015 19634 19257 18882 18511 18143 1777 1832 1158 21566 21171 20780 20393 20009 19628 19250 18876 18505 18137 1777 1777 1778 1779 17 | | | | | | | | | | | | | |
| 34 21964 21566 21171 20780 20393 20000 19628 19250 18876 18505 18137 1777 1778 19505 21158 20767 20386 20002 19621 19244 18870 18499 18131 1777 1778 1779 19596 19615 19238 18644 18493 18125 1777 1879 187 | | | | | | | | | | | | | |
| 35 | 33 | 21964 | 21566 | 21171 | 20780 | 20393 | 20009 | 19628 | 19250 | 18876 | 18505 | 18137 | 17772 |
| 36 | | | | | 20774 | | | | | | | | |
| 37 21938 21540 21145 20754 20367 19983 19602 19225 18851 18480 18113 177 178 19983 19983 19984 19215 18845 18474 18107 177 178 19845 18485 | | | | | | | | | | | | | |
| 39 | 37 | 21938 | 21540 | 21145 | 20754 | 20367 | 19983 | 19602 | 19225 | 18851 | 18480 | 18113 | 17748 |
| 40 | | | | | | | | | | | | | 17742 |
| 41 21911 21513 21119 20728 20341 19958 19577 19200 18826 18456 18088 1777 42 21904 21507 21112 20722 20335 19951 19571 19194 18820 18450 18082 177 43 21898 21500 21106 20715 20328 19945 19565 19188 18814 18443 18076 177 44 21891 21493 21099 20709 20322 19938 19552 19181 18803 18437 18070 177 45 21884 21487 21093 20702 20316 19932 19552 19175 18803 18431 18064 1776 46 21487 21086 20696 20391 19926 19546 19169 18795 18425 18052 176 47 21871 21474 21080 20690 20303 19913 19533 <th>-</th> <th></th> | - | | | | | | | | | | | | |
| 42 21904 21507 21112 20722 20235 19951 19171 19194 18820 18450 18082 177 43 21898 21500 21106 20712 20328 19945 19565 19181 18801 18431 18076 177 44 21891 21493 21099 20709 20322 19938 19552 19175 18802 18431 18064 177 45 21884 21487 21086 20696 20309 19926 19546 19169 18795 18425 18058 176 46 21878 21474 21080 20690 20303 19919 19539 19163 18795 18425 18052 176 48 21864 21467 21073 20683 20966 19913 19533 19156 18783 18413 18046 1766 49 21853 21460 21067 20677 20290 19907 19527 19144 18771 18400 1800 1806 50 21851 21454 21060 20670 20284 19900 19520 19144 18771 18400 18033 1760 | | | | | | | | | | | | | |
| 43 21898 21500 21106 20715 20328 19945 19565 19188 18814 18443 18076 177 44 21891 21493 21099 20709 20322 19938 19558 19181 18808 18437 18070 177 45 21884 21487 21093 20702 20316 19932 19552 19175 18802 18431 18064 177 46 21878 21480 21086 20696 20309 19926 19546 19169 18795 18425 18058 176 47 21871 21474 21080 20690 20303 19919 19539 19163 18789 18419 18052 176 48 21864 21467 21073 20683 20296 19913 19533 19156 18783 18413 18046 176 49 21858 21460 21067 20677 20290 19907 19527 19150 18777 18407 18040 176 50 21851 21454 21060 20670 20284 19900 19520 19144 18771 18400 18033 1760< | 42 | | | | | | | | | | | | |
| 45 21884 21487 21093 20702 20316 19932 19552 19175 18802 18431 18064 1776 46 21878 21480 21086 20396 20309 19926 19546 19169 18425 18058 1766 47 21871 21474 21080 20690 20303 19919 19539 19163 18789 18419 18052 1766 48 21864 21467 21073 20683 20296 19913 19533 19156 18783 18413 18064 1766 49 21858 21460 21067 20677 20290 19907 19527 19150 18777 18407 18040 1766 50 21851 21454 21060 20670 20284 19900 19520 19144 18771 18400 18033 1766 | 43 | 21898 | 21500 | 21106 | 20715 | 20328 | 19945 | 19565 | 19188 | 18814 | 18443 | 18076 | 17712 |
| 46 21878 21480 21086 20696 20309 19926 19546 19169 15795 18425 18058 1766 47 21871 21474 21080 20690 20303 19919 19539 19163 18789 18419 18052 1766 48 21864 21467 21073 20683 20296 19913 19533 19156 18783 18413 18046 1769 49 21858 21460 21067 20677 20290 19907 19527 19150 18777 18407 18040 1769 50 21851 21454 21060 20670 20284 19900 19520 19144 18771 18400 18033 1760 | | | | | | | | | | | | | |
| 47 21871 21474 21080 20690 20303 19919 19539 19163 18789 18419 18052 1766 48 21864 21467 21073 20683 20296 19913 19533 19156 18783 18413 18046 1768 49 21858 21460 21067 20677 20290 19907 19527 19150 18777 18407 18040 1769 50 21851 21454 21060 20670 20284 19900 19520 19144 18771 18400 18033 1760 | | | | | | | | | | | | | |
| 48 21864 21467 21073 20683 20296 19913 19533 19156 18783 18413 18046 1766 49 21858 21460 21067 20677 20290 19907 19527 19150 18777 18407 18040 1766 50 21851 21454 21060 20670 20284 19900 19520 19144 18771 18400 18033 1760 | 47 | 21871 | 21474 | 21080 | 20690 | 20303 | 19919 | 19539 | 19163 | 18789 | 18419 | 18052 | 17688 |
| 50 21851 21454 21060 20670 20284 19900 19520 19144 18771 18400 18033 1760 | | | | 21073 | 20683 | 20296 | 19913 | 19533 | 19156 | 18783 | 18413 | 18046 | 17682 |
| 10111 | | | | | | | | | | | | | |
| | | | | | | | | | | | | | |
| 52 21838 21441 21047 20657 20271 19888 19508 19131 18758 18388 18021 176. | 52 | 21838 | 21441 | 21047 | 20657 | 20271 | 19888 | 19508 | 19131 | 18758 | 18388 | 18051 | 17657 |
| 53 21831 21434 21041 20651 20264 19881 19502 19125 18752 18382 18015 176 | 53 | 21831 | 21434 | 21041 | 20651 | 20264 | 19881 | 19502 | 19125 | 18752 | 18382 | 18015 | 17651 |
| | | | | | | | | | | | | | |
| 1010 1010 1010 | | | | | | | | | | | | | |
| | | | | | | | | | | | | | |

58 21798 21401 21008 20618 20232 19849 19470 19094 18721 18351 17985 17621 59 21791 21395 21001 20612 20226 19843 19464 19088 18715 18345 17979 17615 Proportional Part to tenths of " or s. .1 .2 .5 .7 .3 .4 .6 .8 1 1 2 3 5 6

| 1 | 1 | | | | Ė | roporti | ional L | ogarith | ims. | 7 | ABLE | X. | . 79 |
|-----|----------|-------------------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|-----------------|------------------------|
| ١ | | | | | | 2 Deg | rees, or | 2 Hour | 18. | | | | |
| ı | 3 | 0m | 1m | 2m | 3m | 4,m | 3m | 6 ^m | 7m | 8m | 9m | 10 ^m | 11m |
| ı | 0 | 17609 17603 | 17249 17243 | 16891 16885 | 16537 16531 | 16185 16179 | 15836 15830 | 15490 15484 | | 14806 14801 | 14468 14463 | 14133 14127 | 13800 13795 |
| l | 2 | 17597 17591 | 17237 17231 | 16879 16873 | 16525 | 16173 16168 | 15825 | 15479 15473 | | 14795 | 14457 14451 | 14122 14116 | 13789 |
| ı | 4 | 17585 | 17225 | 16868 | 16513 | 16162 | 15813 | 15467 | 15124 | 14784 | 14446 | 14111 | 13778 |
| ı | 6 | 17579 17573 | 17219 17213 | 16862 16856 | 16507 16501 | 16156 16150 | 15807 15802 | 15461 15456 | | 14778 14772 | 14440 14435 | 14105 14100 | 13773 13767 |
| ١ | 7 8 | 17567 17561 | 17207 17201 | 16850 16844 | 16496 16490 | 16144 16138 | 15796 15790 | 15450 15444 | | 14767 14761 | 14429 14423 | 14094 14088 | |
| ı | 9 | 17555 | 17195 | 16838 | 16484 | 16133 | 15784 | 15439 | 15096 | 14755 | 14418 | 14083 | 13750 |
| ı | 10 | 17549 17543 | 17189 17183 | 16832 16826 | 16478 16472 | 16127 16121 | 15778 15773 | 15433 15427 | 15090 15084 | 14750 14744 | 14412 | 14077 | 13745 13739 |
| ١ | 12 | 17537 17531 | 17177 17171 | 16820 | 16466 16460 | 16115 16109 | 15767 15761 | 15421 15416 | 15079 15073 | 14738 | | 14066 14061 | |
| ı | 13 | 17525 | 17165 | 16814 16808 | 16454 | 16103 | 15755 | 15410 | 15067 | 14727 | 14390 | 14055 | 13723 |
| ı | 15 | 17519 17513 | | 16802 16796 | 1.5 | 16098 16092 | 15749 15744 | 15404 15398 | 15061 15056 | 14722 14716 | 14384 14379 | 14049 14044 | |
| ı | 17 | 17507 17501 | 17147 17141 | 16791 16785 | 16437 16431 | 16086 16080 | 15738 15732 | | | | 14373 14367 | 14038 14033 | 13706 |
| ı | 18 19 | 17495 | 17135 | 16779 | 16425 | 16074 | 15726 | 15381 | 15039 | 14699 | 14362 | 14027 | 13695 |
| I | 20 21 | 17489 17483 | 17129 17123 | 16773 16767 | 16419 16413 | 16068 16063 | 15721 15715 | 15375 15370 | 15033 15027 | 14693 14688 | 14356 14351 | 14022 | 13690 13684 |
| | 22 | 17477 | 17117 | 16761 | 16407 | 16057 | 15709 | 15364 | 15022 | 14682 | 14345 | 14011 | 13679 |
| 1 | 23 24 | 17471 17465 | 17111 17105 | 16755 16749 | | 16051 16045 | 15703 15697 | 15358 15353 | | 14676 14671 | 14339 14334 | 14005 14000 | |
| ı | 25 26 | 17459 17453 | 17099 17093 | 16743 16737 | | 16039 16034 | 15692 15686 | 15347 15341 | 15005 14999 | 14665 14659 | 14328 14323 | 13994 13988 | |
| ١ | 27 | 17447 | 17087 | 16731 | 16378 | 16028 | 15680 | 15335 | 14993 | 14654 | 14317 | 13983 | 13651 |
| ı | 28 29 | 17441 17435 | 17082 17076 | 16725 16720 | 16372 16366 | 16022 16016 | 15674 15669 | 15330 15324 | 14988 14982 | 14648 14643 | 14311 14306 | 13977 13972 | 13646 13640 |
| ı | 30 31 | 17429 17423 | 17070 17064 | 71614 | 414- 914 | 16010 | 15663 | 15318 | 14976 | 14637 | 14300 14295 | 13966 13961 | 13635 13629 |
| ı | 32 | 17417 | 17058 | 16708 16702 | 16349 | 16005 15999 | 15657 15651 | 15312 15307 | 14971 14965 | 14631 14626 | 14289 | 13955 | 13624 |
| ı | 33 34 | 17411 17405 | 17052 17046 | 16696 16690 | | 15993 15987 | 15646 15640 | 15301 15295 | 14959 14954 | 14620 14614 | 14284 14278 | 13950 13944 | THE RESERVE AND PARTY. |
| ı | 35 36 | 17399 1 739 3 | 17040 17034 | 16684 16678 | 16331 16325 | 15981 | 15634 15628 | 15290 15284 | | 14609 14603 | 14272 14267 | 13938 13933 | 13607 |
| ı | 37 | 17387 | 17028 | 16672 | 16320 | 15975 15970 | 15623 | 15278 | 14937 | 14598 | 14261 | 13927 | 13596 |
| I | 38 | 17381 17375 | 17022 17016 | 16666 16660 | 16314 16308 | 15964 15958 | 15617 15611 | 15272 15267 | 14931 14925 | 14592 14596 | 14256 14250 | 13922 13916 | 13591 13585 |
| ۱ | 40 | 17369 | 17010 | 16655 | 16302 | 15952 | 15605 | 15261 | 14919 | 14581 | 14244 | 13911 | 13580 |
| ı | 41 | 17363 17357 | 17004 16998 | 16649 16643 | 16296 16290 | 15946 15941 | 15599 15594 | 15255 15250 | 14914 14908 | 14575 14569 | 14239 14233 | 13905 13900 | 13574 13569 |
| ı | 43 44 | 17351 | 16992 16986 | 16637 16631 | 16284 16279 | 15935 15929 | 15588 15582 | 15244 15238 | 14902 14897 | 14564 14558 | 14228 14222 | 13894 13889 | 13563 13558 |
| ı | 45 | 17339 | 16980 16974 | 16625 | 16273 | 15923 | 15576 | 15232 | 14891 | 14553 | 14217 | 13883 | 13552 |
| ı | 46 | 17333 17327 | 16968 | 16619 16613 | 16267 16261 | 15917 15912 | 15571 15565 | 15227 15221 | 14885 14880 | 14547 | 14211 14205 | 13878 13872 | |
| ı | 48 49 | 17321 | 16963 16957 | 16607 16602 | 16255 16249 | 15906 15900 | 15559 15553 | | 14874 14869 | 14536 14530 | 24404 | 13866 13861 | 1000 |
| - | 50 | 17309 | 16951 | 16596 | 16243 | 15894 | 15548 | 15204 | 14863 | 14524 | 14189 | 13855 | 13525 |
| | 51 52 | 17297 | | 16584 | 16232 | 15883 | 15536 | 15192 | 14852 | 14513 | 14177 | 13850 13844 | 13514 |
| | 53 54 | 17291 | 16933 | | 16226 | 15877 | 15530 | 15187 | 14846 | 14508 | 14172 | 13839 13833 | 13508 |
| | 55 | 17279 | 16921 | 16566 | 16214 | 15865 | 15519 | 15175 | 14835 | 14496 | 14161 | 13828 | 13497 |
| 1 | 56 57 | 17267 | 16909 | 16554 | 16203 | | | | | | | 13822 13817 | |
| - | 58 59 | | | 16549 16543 | | | | | | | | 13811 13806 | |
| - | | roportio | nal Pa | rt to ter | | .1 | .2 | .3 | .1 | .5 . | 6 . | 7 .8 | .9 |
| \$. | | | of " or | 8. | | 1 | 1 | 2 | 2 | 3 | 4 4 | 1. 5 | 5 |

| 80 |) | TABL | EX. | I | Proport | | | | | | | |
|----------|-----------------|-----------------|----------------|----------------|----------------|----------------|----------------|-----------------------|----------------|----------------|----------------|----------------|
| | | | | | 2 Deg | grees, or | 2 Hour | rs. | | | | |
| "S | 12 ^m | 13 ^m | 14m | 15m | 16m | 17m | 18m | 19m | 20m | 21m | 22m | 23m |
| 0 | 13470 | 13142 | 1 - | 12494 | 12173 | | | | | 10605 | | 09994 |
| 1 2 | 13464 13459 | 13137 | | 12489 12483 | | | | 11221 11215 | 10909 | | 10293 10288 | 09989 09984 |
| 3 | 13453 | | | | | | | | | | | |
| 4 | 13448 | | | | 12152 | | | | | | | 09973 |
| 5 | 13442 | 13115 13109 | | | 12147 12141 | | 11513 11508 | | | | | 09968 09963 |
| 7 | 13431 | 13104 | | | | | | 11189 | | | | |
| 8 | 13426 | 13099 | | | 12131 | 11813 | | 11184 | | | | 09953 09948 |
| 9 | 13421 | 13093 | | | 12125 | | 11492 | $\frac{11179}{11174}$ | | | | 09943 |
| 11 | 13410 | 13082 | | | 12115 | | | | | | | 09938 |
| 12 | 13404 | 13077 | | | 12110 | | | | | | | 09933 |
| 13 14 | 13399 13393 | 13071 13066 | 12747 12741 | 12424 12419 | 12104 12099 | | 11471 11466 | | | | | 09928 09923 |
| 15 | 13388 | 13061 | 12736 | 12414 | 12094 | 11776 | 11461 | 11148 | 10837 | 10528 | 10222 | 09918 |
| 16 | 13382 | 13055 | | 12408 12403 | | | 11456 | | 10832 | | | 09913 |
| 17 18 | 13377 | 13050 13044 | | 12397 | 12083 12078 | | | | | 10518 10513 | | 09908 |
| 19 | 13366 | 13039 | | | 12072 | 11755 | 11440 | | 10816 | | | 09898 |
| 20 | 13360 | 13033 | | 12387 | 12067 | 11750 | | 11122 | 10811 | 10503 | 3 | 09893 |
| 21 | 13355 13349 | 13028 13023 | | | 12062 12056 | 11744 11739 | | | 10806 | 10498 10493 | | 09887 09882 |
| 23 | 13344 | 13017 | 12693 | 12371 | 12051 | 11734 | 11419 | 11106 | 10796 | 10487 | 10181 | 09877 |
| 24 | 13338 | 13012 | | 12365 12360 | 12046 12041 | 11729 11723 | | | 10791 10785 | 10482 10477 | | 09872 09867 |
| 25 | 13333 13328 | 13001 | | 12355 | 12035 | 11718 | | | | | 10166 | 09862 |
| 27 | 13322 | 12995 | 12671 | 12349 | 12030 | 11713 | 11398 | 11085 | 10775 | | 10161 | 09857 |
| 28 29 | 13317 13311 | 12990 12985 | 12666 12660 | 12344 12339 | 12025 | 11708 | 11393 11387 | | 10770 | | | 09852 09847 |
| 30 | 13306 | 12979 | 12655 | 12333 | 12014 | | 11352 | 11070 | 10760 | 10452 | | 09842 |
| 31 | 13300 | 12974 | 12650 | 12328 | 12009 | 11692 | 11377 | 11065 | 10754 | 10446 | 10141 | 09837 |
| 32 33 | | 12968 12963 | 12644 12639 | 12323 12317 | 12003 11998 | | 11372 | 11059 11054 | 10749 10744 | | 10136 10131 | 09832 09827 |
| 34 | | 12957 | 12634 | 12312 | 11993 | | 11361 | 11049 | | | 10131 | 09822 |
| 35 | 13278 | 12952 | 12628 | 12307 | 11987 | 11671 | 11356 | 11044 | 10734 | 10426 | 10120 | 09817 |
| 36 | 13273 13267 | 12947 12941 | 12623 12617 | 12301 12296 | 11982 | 11660 | 11351 | 11039 11034 | 10729 | 10421 10416 | 10115 | 09812 |
| 38 | 13262 | 12936 | 12612 | 12291 | 11972 | 11655 | 11340 | 11028 | 10718 | 10411 | 10105 | 09802 |
| 39 | 13257 | 12930 | 12607 | 12285 | 11966 | - | 11335 | 11023 | 10713 | 10406 | 10100 | |
| 40 41 | 13251 | 12925 12920 | 12601 12596 | 12280 | 11961 11956 | 11644 11639 | 11330 11325 | 11018 | 10708 10703 | 10400 | 10095 | 09792 |
| 42 | 13240 | 12914 | 12590 | 12269 | 11950 | 11634 | 11320 | 11008 | 10698 | 10390 | 10085 | 09782 |
| 43 | | 12909 12903 | | 12264 12259 | 11945 | | 11314 | 11002 | 10693 | 10385 | | |
| 45 | | 12898 | 12530 12574 | 12253 | 11940 11935 | | 11309 11304 | 10997 10992 | 10688 10682 | 10380 | 10075 | 09772 09766 |
| 46 | 13218 | 12892 | 12569 | 12248 | 11929 | 11613 | 11299 | 10987 | 10677 | 10370 | 10065 | 09761 |
| 47 | | 12887 | 12564 12558 | 12243 | 11924 11919 | 11608 | | | 10672 | 10365 | 10059 | 09756 |
| 49 | | | | | 11913 | | | | | | | |
| 50 | 13197 | 12871 | 12548 | 12227 | 11908 | 11592 | 11278 | 10966 | 10657 | 10349 | 10044 | 09741 |
| 51 52 | | 12865 12860 | 12542 12537 | | 11903 11897 | 11587 11581 | | 10961 | 10652 | | | |
| 53 | 13180 | | | 12211 | | | 11565 | | 10646 10641 | | | |
| 54 | 13175 | 12849 | 12526 | 12205 | 11887 | 11571 | 11257 | 10945 | 10636 | 10329 | 10024 | 09721 |
| 55 56 | 13169 13164 | | | 12200 | | 11566 11560 | | | 10631 10626 | | | 09716 |
| 57 | 13158 | 12833 | 12510 | 12189 | 11871 | 11555 | 11241 | | 10621 | | 10009 | 09706 |
| 58 59 | 13153 | 12828 | 12505 | 12184 | 11866 | 11550 | 11236 | | | | | |
| | roportio | nal Pa | rt to te | nths | 11860 | .2 | 11531 | .4 | .5 | 10304 | 7 .8 | |
| | | of " or | | in the | 0 | 1 | 1 | 2 | 2 | | | 4 4 |

l,

2 Degrees, or 2 Hours.

| | | | - | 1 | 1 1 | | 1 | | 1 1 | | | A 11 |
|-------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|--|----------------|----------------|----------------|
| " | 24m | 25m | 26m | 27m | 28m | 29m | 30m | 31m | 32m | 33m | 34m | 35m |
| 8 | | | | - | | | | | | | | - |
| 0 | 09691 | 09390 | | 08796 | 08501 | 08209 | | 07630 | | 07058 | 06775 | 06494 |
| 1 | 09686 | 09385 | 09087 | 08791 | 08496 | 08204 | 07913 07908 | 07625 | 07338 07333 | 07053 | 06770 | 06489 |
| 2 | 09681 | 09380 | 09082 | 08786 | 08491 | 08199 | | 07620 07615 | | 07049 07044 | 06766 06761 | 06485 |
| 3 | 09676 | | | 08781 | 08486 | | 07904 07899 | 07610 | 07329 07324 | | | 06480 |
| 4 | 09671 | 09370 | 09072 | 08776 | 08482 08477 | 08189 | | | | 07039 07034 | 06756 06752 | 06475 |
| 5 | 09666 | 09365 09361 | 09062 | 08771 | 08472 | 08184 | | 07606 07601 | 07314 | 07034 | 06747 | 06471 |
| 6 | 09661 | 09356 | 09057 | 08766 08761 | 08467 | 08179 08175 | | 07596 | | 07025 | 06742 | |
| 7 8 | 09656 09651 | 09351 | 09052 | 08756 | 08462 | 08170 | | 07591 | 07305 | 07020 | 06738 | 06461 |
| 9 | 09646 | 09346 | 09047 | 08751 | 08457 | 08165 | | 07586 | 07300 | 07016 | 06733 | |
| | | | - | | | | - | - | | - | | - |
| 10 | 09641 | 09341 | 09042 | 08746 | 08452 | 08160 | | 07582 | 07295 | 07011 | 06728 | 06447 |
| 11 | 09636 | 09336 | 09037 | 08741 | 08447 | 08155 | | 07577 | 07291 | 07006 07001 | | 06443 |
| 12 | 09631 09626 | 09331 09326 | 09033 09028 | 08736 | 08442 08438 | 08150 | | 07572 07567 | 07286 07281 | 06997 | 06719 06714 | 06438 06433 |
| 13 | 09621 | 09320 | 09028 | 08732 08727 | 08433 | 08146 08141 | | 07562 | 07276 | 06992 | | 06429 |
| 14 15 | 09616 | 09316 | 09023 | 08722 | 08433 | 08136 | | 07558 | 07272 | 06987 | 06705 | 06424 |
| | 09611 | 09311 | 09013 | 08717 | 08423 | 08131 | 07841 | 07553 | 07267 | 06982 | 06700 | 06419 |
| 16 17 | 09606 | | | 08712 | 08418 | 08126 | | 07548 | 07262 | 06978 | 06695 | 06415 |
| 18 | 09601 | 09301 | 09003 | | 08413 | 08121 | 07831 | 07543 | 07257 | 06973 | | 06410 |
| 19 | 09596 | 09296 | 08998 | 08702 | 08408 | 08116 | | 07539 | 07253 | 06968 | 06686 | |
| 20 | 09591 | 09291 | 08993 | 08697 | 08403 | 08112 | | 07534 | 07248 | 06964 | 06681 | 06401 |
| 21 | 09591 | 09291 | 08993 | 08692 | 08398 | 08112 | 07817 | 07534 | 07248 | 06959 | 06677 | 06396 |
| 22 | 09581 | 09280 | 08983 | 08687 | 08394 | 08107 | | 07524 | 07238 | 06954 | 06672 | 06391 |
| 23 | 09576 | 09276 | 08978 | 08682 | 08389 | 08097 | 07807 | 07519 | 07234 | 06949 | | 06387 |
| 24 | 09571 | 09271 | 08973 | 08678 | 08384 | 08092 | | 07515 | | 06945 | | |
| 25 | 09566 | 09266 | 08968 | 08673 | 08379 | 08087 | 07798 | 07510 | 07224 | 06940 | | 06377 |
| 26 | 09561 | 09261 | 08963 | 08668 | 08374 | 08083 | | 07505 | 07219 | 06935 | 06653 | |
| 27 | 09555 | 09256 | 08958 | 08663 | 08369 | 08078 | | 07500 | | 06931 | 06648 | |
| 28 | 09550 | 09251 | 08953 | 08658 | 08364 | 08073 | | 07496 | 07210 | 06926 | 06644 | 06364 |
| 29 | 09545 | 09246 | 08948 | 08653 | 08359 | 08068 | 07778 | 07491 | 07205 | 06921 | 06639 | 06359 |
| 30 | 09540 | 09241 | 08943 | 08648 | 08355 | 08063 | 07774 | 07486 | 07200 | 06916 | 06634 | 06354 |
| 31 | 09535 | 09236 | 08939 | 08643 | 08350 | 08058 | 07769 | 07481 | 07196 | | | 06350 |
| 32 | 09530 | 09231 | 08934 | | 08345 | 08053 | | 07476 | | | 06625 | |
| 33 | 09525 | 09226 | 08929 | 08633 | 08340 | 08049 | | 07472 | 07186 | 06902 | | 06340 |
| 34 | 09520 | 09221 | 08924 | 08628 | 08335 | 08044 | 07754 | 07467 | 07181 | 06898 | 06616 | 06336 |
| 35 | 09515 | 09216 | 08919 | 08624 | 08330 | 08039 | 07750 | 07462 | | 06893 | 06611 | 06331 |
| 36 | 09510 | 09211 | 08914 | 08619 | 08325 | 08034 | | 07457 | 07172 | | 06606 | 06326 |
| 37 | 09505 | 09206 | 08909 | | 08320 | 08029 | | 07453 | 07167 | 06883 | | 06322 |
| 38 | 09500 | 09201 | 08904 | 08609 | 08316 | 08024 | | 07448 | 07162 | 06879 | 06597 | 06317 |
| 39 | 09195 | 09196 | 08899 | 08604 | 08311 | 08020 | 07730 | 07443 | 07158 | 06874 | 06592 | 06312 |
| 40 | 09490 | 09191 | 08894 | | 08306 | 08015 | 07726 | 07438 | 07153 | 06869 | 06588 | 06308 |
| 41 | 09185 | 09186 | 08889 | 08594 | 08301 | 08010 | 07721 | 07433 | 07148 | 06865 | 06583 | 06303 |
| 42 | 09480 | 09181 | 08884 | 08589 | 08296 | 08005 | | 07429 | 07143 | 06860 | | 06298 |
| 43 | 09475 | 09176 | 08879 | 08584 | 08291 | 08000 | | 07424 | 07139 | 06855 | | 06294 |
| 44 | 09470 | 09171 | 08874 | 08579 | 08286 | 07995 | | 07419 | 07134 | 06850 | | 06289 |
| 45 | 09465 09460 | 09166 09161 | 08869 08865 | 08575 | 08282 | 07991 | 07702 | 07414 | | 06846 | | |
| 46 | 09460 | 09156 | 08860 | 08570 08565 | 08277 08272 | 07986 | | 07410 | | 06841 | 06560 | |
| 48 | 09450 | 09151 | 08855 | 08560 | 08267 | 07981 07976 | 07692 | 07405 | | 06836 | | 06275 |
| 48 | 09430 | 09147 | 08850 | | 08262 | 07971 | 07687 07682 | 07400 07395 | 07115 | 06832 06827 | 06550 06545 | 06271 |
| Finance III | 09440 | 09142 | 08845 | 08550 | 08257 | _ | | | - | | | - |
| 50 | 09440 | 09142 | 08840 | 08545 | | 07966 | 07678 | 07391 | 07105 | 06822 | 06541 | 06261 |
| 51 52 | 09435 | 09137 | 08835 | | 08252 08248 | 07962 07957 | | 07386 | 07101 | 06817 | 06536 | |
| 53 | 09425 | 09132 | 08830 | | 08248 | 07957 | 07668 07663 | 07381 07376 | 07096 07091 | 06813 06808 | 06531 06527 | 06252 |
| 54 | 09420 | 09122 | 08825 | 08530 | 08238 | 07947 | 07658 | 07371 | 07091 | 06803 | 06522 | 06243 |
| 55 | 09415 | 09117 | 08850 | 08526 | 08233 | 07942 | 07654 | 07367 | 07082 | 06799 | 06517 | 06238 |
| 56 | 09410 | 09112 | 08815 | 08521 | 08228 | 07937 | 07649 | 07362 | 07077 | 06794 | | |
| 57 | 09405 | 09107 | 08810 | | 08223 | 07933 | | 07357 | 07072 | 06789 | | 06229 |
| 58 | 09100 | 09102 | | | 08218 | 07928 | | | 07068 | | | |
| 59 | 09395 | | | 08506 | | 07923 | | 07348 | | | | |
| P | roportio | | | | .1 | .2 | .3 | .4 | .5 | 1 | 1 | 8 .9 |
| | | of " or | | - | 0 | 1 | 1 | 2 | 2 | 3 | | 4 4 |
| - | _ | - | ALUKATINE BURE | - | | - | - | - | Name and Post Office Address of the Owner, where | | - | |

| 9 | Degrees. | or 2 | Hours. |
|---|----------|------|--------|
| | | | |

| 1 | " 36m 37m 38m 39m 40m 41m 42m 43m 44m 45m 46m 47m | | | | | | | | | | | | | |
|---|---|----------------|----------------|----------------|----------------------|----------------|----------------|----------------|----------------|-----------------------|----------------|--------------------------------------|-------|--|
| | s S | 36m | 37m | - | - | | - | 42m | - | | | | 47m | |
| | 0 | 06215 | | 05662 | | | 04845 | | | | | 03516 | 03256 | |
| 1 | 1 | 06210 | | | 05383 | | 04840 04836 | | 04304 | | | | 03251 | |
| | 5 | 06206 | | | | | | 04567 | | | | | 03247 | |
| | 3 | 06201 | 05923 | | THE RESERVE TO SERVE | | 04831 | 04558 | | 04030 | | 03503 | 03243 | |
| - | 5 | 06196 06192 | | | 05365 | | | 04553 | | | 03757 | 03499 | 03238 | |
| | 6 | 06192 | | | 05360 | | | 04535 | | | | | 03234 | |
| 1 | 7 | 06182 | 7 | | | | | 04544 | 04277 | 04012 | 03748 | | 03230 | |
| 1 | 8 | 06178 | | 05625 | 05351 | 05079 | 04809 | 04540 | 04273 | 04008 | 03744 | 03482 | 03221 | |
| 1 | 9 | 06173 | | 05620 | 05347 | 05075 | | 04536 | | 04003 | 03739 | 03477 | 03217 | |
| 1 | 10 | 06168 | | 05616 | 05342 | 05070 | | | 04264 | | 03735 | 03473 | 03212 | |
| 1 | 11 | 06164 | | 05611 | 05337 | 05066 | 04795 | 04527 | 04260 | 03994 | 03731 | 03469 | 03308 | |
| 1 | 12 | 06159 | 05882 | 05607 | 05333 | 05061 | 04791 | 04522 | 04255 | 03990 | 03726 | 03464 | 03204 | |
| | 13 | 06155 | 05877 | 05602 | 05328 | 05056 | 04786 | 04518 | 04251 | 03986 | | 03460 | 03199 | |
| | 14 | 06150 | 05873 | 05597 | 05324 | 05052 | 04782 | 04513 | | | 03717 | 03455 | 03195 | |
| | 15 | 06145 | 05868 | 05593 | | 05047 | 01777 | 04509 | 04242 | 03977 | 03713 | 03451 | 03191 | |
| | 16 17 | 06141 | 05864 | 05588 05584 | | | 04773 | 04504 | | 03972 | | | 03186 | |
| | 18 | 06136 | 05859 05854 | 05584 | 05310 | | 04768 | 04495 | | 03968 | | | 03182 | |
| | 19 | 06127 | 05854 | 05575 | 05300 | 05034 | 04759 | 04493 | 04229 | 03959 | 03696 | 03434 | 03178 | |
| | 20 | 06122 | 05845 | 05570 | 05297 | 05025 | 04755 | 04486 | 04224 | 03955 | 03691 | 03434 | 03169 | |
| | 21 | 06122 | 05845 | 05565 | 05297 | 05025 | 04750 | 04480 | 04220 | 03955 | 03691 | 03429 | 03169 | |
| | 22 | 06117 | 05836 | 05561 | 05288 | 05016 | 04746 | 04478 | 04211 | 03946 | 03682 | 03421 | 03160 | |
| ı | 23 | 06108 | 05831 | 05556 | 05283 | 05011 | 04741 | 01473 | 04206 | 03941 | 03678 | 03416 | 03156 | |
| ı | 24 | 06104 | 05827 | 05552 | 05278 | 05007 | 04737 | 04469 | 04202 | 03937 | 03674 | 03412 | 03152 | |
| ١ | 25 | 06099 | 05822 | 05547 | 05274 | 05002 | 04732 | 01464 | 04198 | 03933 | 03669 | 03408 | 03147 | |
| | 26 | 06094 | | 05543 | | 04998 | 04728 | 04460 | | 03928 | | 03403 | 03143 | |
| | 27 | 06090 | | | 05265 | | 04723 | 04455 | | 03924 | 03661 | 03399 | 03139 | |
| | 28 29 | 06085 | 05808 | 05533 05529 | 05260 05256 | 04989 04984 | 04719 04714 | 04451 | 04184 | 03919 03915 | 03656 | 03395 03390 | 03134 | |
| | 29 30 | 06080 | 05804 | | | | - | | | CONTRACTOR CONTRACTOR | 03652 | Name and Address of the Owner, where | | |
| | 30 31 | 06076 06071 | 05799 05795 | 05524 05520 | 05251 05247 | 04980 04975 | 04710 | 04442 | 04175 04171 | 03911 03906 | 03647 | 03386 03381 | 03126 | |
| | 35 | 06071 | 05795 | 05520 | 05247 | 04975 | 04706 | 04437 | | 03906 | 03643 | | 03121 | |
| | 32 33 | 06067 | 05785 | 05511 | 05238 | 04971 | | 04433 | | | 03634 | | 03117 | |
| 1 | 34 | 06057 | 05781 | 05506 | 05233 | 04962 | | 04424 | | 03893 | | 03368 | 03108 | |
| ľ | 35 | 06053 | 05776 | 05501 | 05228 | 04957 | 04688 | 04420 | 04153 | 03889 | 03626 | 03364 | 03104 | |
| | 36 | 06048 | 05772 | 05497 | 05224 | 04953 | 04683 | 04415 | 04149 | 03884 | 03621 | 03360 | 03100 | |
| | 37 | 06043 | 05767 | 05492 | | 04948 | 04679 | 04411 | 04144 | | 03617 | 03355 | 03096 | |
| | 38 | 06039 | 05762 | 05488 | 05215 | 04944 | 04674 | 04406 | | | 03612 | 03351 | 03091 | |
| | 39 | 06034 | 05758 | 05483 | 05210 | 04939 | 01670 | 04402 | 04136 | 03871 | 03608 | 03347 | 03097 | |
| | 40 | 06030 | 05753 | 05479 | 05206 | 04935 | 04665 | 04397 | 04131 | 03867 | 03604 | 03342 | 03083 | |
| | 41 42 | 06025 | 05749 | 05474 | 05201 05197 | 04930 04926 | 04661 | 04393 04388 | 04127 04122 | 03862 | 03599 03595 | 03338 03334 | 03078 | |
| | 43 | 06020 | 05744 | 05470 | 05197 | 04926 | 04656 | 04388 | 04122 | 03858 | 03595 | 03334 | 03074 | |
| | 44 | 06010 | 05735 | 05460 | 05198 | 04921 | 04647 | 04384 | 04118 | 03853 | 03591 | 03329 | 03070 | |
| | 45 | 06006 | 05730 | 05456 | 05183 | 04912 | 04643 | 04375 | 04109 | 03845 | 03582 | 03323 | 03065 | |
| ľ | 46 | 06003 | 05726 | 05451 | 05179 | 04908 | 04638 | 04371 | 04105 | 03840 | 03578 | 03316 | 03057 | |
| | 47 | 05997 | 05721 | 05447 | 05174 | 04903 | 04634 | 04366 | 04100 | 03836 | 03573 | 03312 | 03052 | |
| | 48 | 05993 | 05717 | 05442 | 05170 | 04899 | 04629 | 04362 | 04096 | 03832 | 03569 | 03308 | 03048 | |
| | 49 | 05988 | 05712 | 05438 | 05165 | 04894 | 04625 | 04357 | 04091 | 03827 | 03564 | 03303 | 03044 | |
| | 50 | 05983 | 05707 | 05433 | 05161 | 04890 | 04620 | 04353 | 04087 | 03823 | 03560 | 03299 | 03039 | |
| | 51 | 05979 | 05703 | 05429 | 05156 | 04885 | | 04348 | 04083 | 03818 | 03556 | 03295 | 03035 | |
| | 52 53 | 05974 | 05698 05694 | 05424 | 05151 | 04881 | | 04344 | | | 03551 | 03290 | 03031 | |
| | 53 54 | | 05694 | 05419 | 05147 | 01876 | | | | | 03547 | 03236 | 03026 | |
| | 55 | | - | 05410 | | 04867 | | | | | | | 03018 | |
| ŀ | 56 | | | 05406 | 05133 | 04863 | | | | | | | 03014 | |
| ŀ | 57 | 05951 | | 05401 | | 04858 | | | | | | | 03009 | |
| | 58 | 05947 | 05671 | 05397 | 05124 | 04854 | 04585 | 04317 | 04052 | 03788 | 03525 | 03264 | 03005 | |
| L | 59 | | | | | | | | | | - | | 03001 | |
| 1 | P | roportio | nal Par | t to ter | nths | .1 | .2 | .3 | | | 6 . | | | |
| L | | | of" or | S. | 1 | 0 | l | 1 | 2 | 2 | 3 3 | 3 3 | 4 | |
| | | | | | | | | | | | | | | |

| - | | | | Lagran. | I | roporti | ional L | ogarith | ins. | J | ABLE | x. | 83 |
|---|----------|----------------|----------------|------------------------|----------------|----------------|----------------|----------------|--|-----------------------|----------------|-------------|--------|
| I | | | -11- | | . 1 | 2 Deg | rees, or | 2 Hour | 9- 1 1 | | 2.(10)(| will a | iy i |
| ı | 3 | 48m | 49m | 50m | 51m | 52m | 53m | 54m | 55m | 56 ^m | 57m | 58m | 59m |
| I | 0 | 02996 | 02739 | 02482 | 02228 | 01974 | 01723 | 01472 01468 | 01223 | 00976 | 00730 | 00185 | 00242 |
| ı | 1 2 | 02992 | | 02474 | 02223 | | 01714 | 01464 | 01215 | 00968 | 00722 | | 00238 |
| ı | 3 | 02983 | 02726 | 02470 | | | | 01460 | | 00964 | 00718 | 00179 | 00230 |
| ı | 4 5 | 02979 | 02721 | 02465 | 02211 | 01958 01953 | | 01456 01452 | 01207 | 00960 | 00714 | 00469 | 00226 |
| ١ | 6 | | 02713 | 02457 | 02202 | 01949 | 01698 | 01447 | 01199 | 00951 | 00705 | 00461 | 00218 |
| 1 | 7 | 02966 | | 02453 | 02198 | | 01693 | | 01195 | 00947 | 00701 | 00151 | 00214 |
| ı | 8 9 | 02962 | 02704 | 02448 | 02194 | | 01689 01685 | | | 00939 | 00693 | | |
| ł | 10 | | 02696 | 02440 | 02185 | | 01681 | 01431 | 01182 | 00935 | 00689 | 00445 | 0(202 |
| ı | 11 | 02949 | | 02436 | 02181 | | | | | 00931 | 00685 | | 00197 |
| ı | 12 | 02945 | | 02431 | 02177 | 01924 | | | | 00927 | 00681 | 00436 | 1 4 |
| I | 14 | 02936 | 02679 | 02423 | 02168 | 01916 | 01664 | 01414 | 01166 | 00918 | 00673 | 00425 | 00185 |
| 1 | 15 | 02932 | 02674 | 02419 02414 | 02164 | | 01660 01656 | | | 00914 | | | 00181 |
| 1 | 16 17 | 02927 | | 02110 | | 01903 | | 01402 | 01153 | | 00660 | | |
| ı | 18 | 02919 | 02662 | 02406 | 02152 | | | | A COLUMN TO SERVICE AND ADDRESS OF THE PARTY | | 0065 | | 00109 |
| I | 19 | 02915 | | 02402 | 02147 | - | 01643 | - | | 00898 | 00659 | 00408 | |
| ı | 20 | 02910 | | 02393 | 02139 | | 01635 | | | | 00644 | 0(400 | |
| ١ | 22 | 02903 | 02644 | 02389 | 02135 | | 01631 | 01381 | 01133 | | 00640 | | 00153 |
| ı | 23 | 02897 02893 | | 02385 | | 01878 01874 | | | 01128 01124 | | 00636 00632 | | 00149 |
| 1 | 24 25 | 02889 | | 02376 | | | | | | | 00658 | | |
| ı | 26 | 02884 | 02627 | 02372 | | | | | | | 00624 | | |
| ı | 27 28 | 02880 02876 | | 02368 02363 | | | 01610 | | | | 00620 00616 | 00376 | |
| ı | 29 | 02872 | 02615 | | 02105 | | | 01352 | | 00857 | 00611 | 00367 | 00125 |
| ı | 30 | 02867 | | | | | 01597 | 01348 | | 00853 | 00607 | 00363 | |
| ı | 31 | 02863 02859 | 02608 | 02351 02346 | 02097 | 01844 | 01593 01589 | | | | 00603 00599 | | |
| ı | 33 | 02854 | | 02342 | | | | | 01087 | | 00595 | | |
| ı | 34 | 02850 | | | 02084 | | 01581 | | | | 00591 | 00347 | |
| ı | 35 36 | 02846 02841 | 02589 02585 | | 02080 02076 | | 01576 01572 | | | | 00587 00583 | | |
| H | 37 | 02837 | 02580 | 02325 | | 01819 | 01568 | 01319 | | 00824 | | | |
| ١ | 38 | 02833 | | 02321 | 02067 | | 01564 | | | 00820 00816 | 00575 | 00331 | 00089 |
| ŀ | 39 40 | 02829 | - | sales and the later of | 02059 | - | - | | - | - Commercial Contract | 00567 | - | 0 n 80 |
| 1 | 41 | | 02563 | 02308 | 02054 | 01802 | 01551 | 01302 | 01054 | 00808 | 00563 | 00319 | 00076 |
| 1 | 42 | 02816 | | | 02050 02046 | | 01547 | | 01050 | | 00559 | A Section 1 | 00072 |
| - | 43 | 02811 | | | 02040 | | | 01294 | | 00799 | 00554 | | 00068 |
| 1 | 45 | 02803 | 02546 | 02291 | 02038 | 01785 | 01535 | 01286 | 01038 | 00791 | 00546 | 00303 | 00060 |
| 1 | 46 | 02799 | | 02287 | 02029 | | 01531 | 01281 | 01031 | 00787 | 00542 | 00299 | 00056 |
| 1 | 48 | 02790 | 02533 | 02278 | 02025 | -01773 | 01522 | 01273 | 01025 | 00779 | 00534 | 00290 | 00048 |
| 1 | 49 | | | 02274 | | | | | | | | | |
| 1 | 50 | 02781 | | 02270 02266 | | | | | | 00771 | | | 00040 |
| 1 | 51 52 | | | 02262 | | | | | | | | | 00030 |
| 1 | 53 | 02769 | 02512 | 02257 | 02001 | 01752 | 01501 | 01252 | 01005 | 00759 | 00514 | 00270 | 00058 |
| 1 | 54 55 | 02764 | | 02253 | | | | | 01001 | | | | 00024 |
| 1 | 56 | | | 02245 | | | 01489 | | 00992 | | | | |
| 1 | 57 | 02751 | 02495 | 02240 | 01987 | 01735 | 01485 | | | | 00497 | | 00012 |
| | 58 59 | | | 02236 02232 | | | 01481 01476 | | | | | 00250 | |
| f | | roporti | onal Pa | rt to te | | 7.1 | .2 | .3 | .4 | .5 | 6 | 7 . | 3 .9 |
| Ī | | | of " or | S. | | 0 | 1 | 1 | 2 . | 2 | | | 3 4 |

84 TABLE XI. TABLE XIII.—Correction to be added to the Observed Altitude of the Sun's Lower Limb, when taken by a Depression or Dip of Fore Observation, to find the True Altitude. the Horizon. Height of the Eye above the Sea in Feet. H. of Dip of Height Dip of Eye. Horiz. Obs 10 Alt. 8 12 | 14 | 16 18 20 22 24 26 30 6 28 11 Feet. 0 1 0 3 58 16 5 3.8 3.5 3.1 2.8 2.5 2.3 2.1 0.8 1.8 1.4 1.2 1.6 1.0 161 14 1 7 4 2 4.9 4.3 3.7 6 5.3 4.6 4.0 3.5 3.3 2.2 3.0 2.8 2.6 2.4 1į 1 13 4 5 17 5.4 7 6.4 6.0 5.7 5.1 4.8 4.6 4.4 4.1 3.9 3.7 3.5 3.3 13 1 19 171 4 9 8 6.8 6.2 5.9 4.2 7.2 6.5 5.7 5.4 5.3 5.0 4.8 4.6 4.4 2 1 24 18 4 12 9 7.9 7.5 7.2 6.9 6.6 6.4 6.1 5.9 5.7 5.3 4.9 5.5 5.1 21 29 184 1 4 16 10 8.5 8.1 7.8 7.5 7.2 6.9 6.7 6.5 6.2 6.0 5.8 5.6 5.4 21 1 34 19 4 19 11 8.9 8.6 8.2 7.9 7.6 7.4 7.2 6.9 6.7 6.5 6.3 5.9 6.1 23 1 39 191 4 23 12 9.3 9.0 8.7 8.3 8.0 7.8 7.6 7.3 7.1 6.9 6.5 6.3 6.7 3 1 43 20 4 26 14 9.9 9.6 9.2 8.9 8.7 8.4 8.2 7.9 7.7 7.5 7.3 6.9 7.1 1 47 21 4 33 16 10.4 10.1 9.7 9.4 9.1 8.9 8.7 8.4 8.2 8.0 7.8 7.6 7.4 31 51 22 4. 39 18 10.8 10.4 10.1 9.8 9.5 9.3 9.0 8.8 8.6 8.4 8.2 8.0 7.8 34 55 23 1 4 46 20 11.1 10.7 10.4 10.1 9.8 9.6 9.3 9.1 8.9 8.7 8.5 8.2 8.1 4 1 59 24 4 52 22 11.4 11.0 10.7 10.4 10.1 9.8 9.6 9.4 9.1 8.9 8.5 8.3 8.7 2 3 25 4. 58 41 26 11.7 11.4 11.0 10.7 10.5 10.2 10.0 9.7 9.5 9.3 9.1 8.9 8.7 2 41 6 26 5 4 30 |12.0 |11.7 |11.3 |11.0 |10.8 |10.5 |10.3 |10.0 | 9.8 9.6 9.4 9.2 9.0 43 2 10 27 5 10 12.3 11.9 11.6 11.3 11.0 10.7 10.6 10.3 10.1 35 9.9 9.7 9.4 9.2 2 13 28 5 16 5 12.5 12.2 11.8 11.5 11.3 11.0 10.8 10.5 10.3 10.1 40 9.9 9.7 9.5 51 2 5 17 29 22 45 12.7 12.4 12.0 11.7 11.5 11.2 11.0 10.7 10.5 10.2 10.1 9.8 9.7 51 20 2 30 5 27 50 12.8 12.5 12.2 11.9 11.6 11.3 11.1 10.9 10.6 10.4 10.3 10.0 9.8 2 23 5 32 53 31 55 13.0 12.6 12.3 12.0 11.7 11.5 11.2 11.0 10.7 10.5 10.3 10.1 9.9 6 2 26 32 5 37 60 13.1 12.7 12.4 12.1 11.8 11.6 11.3 11.1 10.9 10.6 10.4 10.2 10.1 61 2 32 33 5 42 13.2 12.8 12.5 12.2 11.9 11.7 11.4 11.2 11.0 10.7 10.5 10.3 10.1 7 2 38 34 5 47 71 2 5 43 35 53 2 8 48 36 5 58 90 13.6 13.2 12.9 12.6 12.3 12.0 11.8 11.6 11.3 11.1 10.9 10.7 10.5 2 37 2 81 53 6 Month. May, Jan. Feb. Mar. April, June. 2 58 38 6 7 + 0'.3 + 0'.2 + 0'.1 0'.0 -0'.1 Correction, -0'.2 91 3 3 39 6 12 Month, July, Aug. Sept. Oct. Nov. Dec. 3 8 40 6 17 -0'.3 - 0'.2 -0'.1 +0'.1Correction, + 0'.2 +0'.33 12 42 6 26 10분 3 44 17 35 11 6 TABLE XIV.—Correction to be subtracted from the Ob-3 111 21 46 6 44 served Altitude of a Fixed Star, to find the True Altitude. 12 3 26 48 6 52 Height of the Eye above the Sea in Feet. Obs 121 3 31 50 7 1 Alt. 10 | 12 | 14 | 16 | 18 | 20 | 22 | 24 | 26 | 28 30 6 8 13 3 35 55 7 21 0 7 3 41 131 39 60 7 12.3 12.7 13.0 13.3 13.6 13.8 14.1 14.3 14.6 14.8 15.0 15.2 15.3 43 14 3 70 8 18 10.9 11.3 11.6 11.9 12.2 12.4 12.7 12.9 13.2 13.4 13.6 13.8 13.9 6 141 3 47 80 8 53 7 9.8 10.2 10.5 10.8 11.1 11.3 11.6 11.8 12.1 12.3 12.5 12.7 12.8 3 25 15 51 90 9 9.9 10.2 10.4 10.7 10.9 11.2 11.4 11.6 11.8 11.9 8 8.9 9.3 9.6 151 3 55 100 9 56 9 8.2 8.6 8.9 9.2 9.5 9.7 10.0 10.2 10.5 10.7 10.9 11.1 11.2 9.7 10.0 10.2 10.4 10.6 10.7 TABLE XII. 10 7.7 8.1 8.4 8.7 9.0 9.2 9.5 11 7.2 7.6 7.9 8.2 8.5 8.7 9.0 9.2 9.5 9.7 9.9 10.1 10.2 Dip at differ. Distances 8.1 9.3 12 6.8 7.2 7.5 7.8 8.3 8.6 8.8 9.1 9.5 9.7 9.8 from the Observer. 14 6.2 6.6 6.9 7.2 7.5 7.7 8.0 8.2 8.5 8.7 8.9 9.1 Height of the Eye 16 5.7 6.1 6.4 6.7 7.0 7.2 7.5 7.7 8.0 8.2 8.4 8.6 8.7 in Feet. 18 5.3 5.7 6.0 6.3 6.6 6.8 7.1 7.3 7.6 7.8 8.0 8.2 8.3 15 115 |20 |25 |30 10 20 5.0 5.4 5.7 6.0 6.3 6.5 6.8 7.0 7.3 7.5 7.7 7.9 8.0 34' 45' 57' 11' 23' 68 22 4.8 5.2 5.8 6.1 6.3 6.8 7.1 7.3 7.5 7.7 7.8 5.5 6.6 17 23 28 7.4 6 12 34 26 4.4 4.8 5.1 5.4 5.7 5.9 6.2 6.4 6.7 6.9 7.1 7.3 4 8 12 15 19 23 30 4.1 4.5 4.8 5.1 5.4 5.6 5.9 6.1 6.4 6.6 6.8 70 7.1 1 3 9 12 15 6 17 6.8 4.2 5.1 5.3 6.3 6.5 6.7 35 3.8 4.5 4.8 5.6 5.8 6.1 14 3 7 5 10 12 14 4.9 6.1 6.3 6.5 6.6 40 3.6 4.0 4.3 4.6 5.1 5.4 5.6 5.9 11 3 4.7 5.9 6.1 6.3 6.5 4 6 8 10 12 45 3.4 3.8 4.1 4.4 4.9 5.2 5.4 5.7 2 6.3 5 7 9 3.2 4.2 4.5 5.2 5.5 5.7 5.9 6.1 4 8 50 3.6 3.9 4.7 5.0 21 2 3 4 6.2 6 7 8 4.1 5.4 5.6 5.8 6.0 55 3.1 3.5 3.8 4.4 4.6 4.9 5.1 3 4.3 2 3 4 5 7 5.3 5.5 5.7 5.9 6.1 6 60 3.0 3.4 3.7 4.0 4.5 4.8 5.0 31 2 5.8 3 4 5 3.3 4.2 4.9 5.4 6.0 6 65 2.9 3.6 3.9 4.7 5.2 5.6 4.4 2 3 4 5 5 6 70 2.8 3.2 3.5 4.1 4.6 5.1 5.3 5.5 5.7 5.9 3.8 4.3 4.8 5 2 3 4 4 5 6 80 2.6 3.0 3.3 3.7 3.9 4.1 4.9 5.1 53 5.5 5.7 4.4 4.6 4 4 5 5 90 2.4 2.8 3.1 3.4 3.7 3.9 4.4 4.7 4.9 5.1 5.3 5.5 4.2

9.4 2 30.3 9.99

13.4 2 31.6 9.99

14.5 2 31.9 9.99

10.8 2

12.22

10.0 16 15.5 2 32.2 9.99

10.5 16 16.3 2 32.4 9.99

10.8 16 16.9 2 32.6 9 99 19 1 10.9 16 17.4 2 32.8 9.99

11.0 16 17.7 2 32.9 9.99

30.7 9.99

31.2 9.99

11

7 1

131

19 1

25 1

131

25 1

11

November.

December. 71 6.8 16

7.5 16

8.3 16

8.9 16

9.6 16

TABLE XVI.

| | - | ~ | | TAB | - | AVI | | | 89 | |
|----------------|----------|-------|--------------|--------------|------|-------|--------------|------|-------|---|
| | | Sun | 's Pa | | | Altit | | | | |
| ın's irithm | - | | Tom | Feb. | Mar. | April | May | June | Tuler | |
| ance. | Z.D. | Alt | Jan. | Dec. | Nov. | Oct. | Sept. | Aug. | July. | Н |
| | | | Par. | Par. | Par. | Par. | Par. | Par. | Par. | Н |
| 0120 | 0 | Ü | " | " | " | " | " | " | " | П |
| 2659 2727 | 0 | 90 | 0.00 | | | | 0.00 | 0.00 | 0.00 | |
| 2852 | 1 | 89 | 0.15 | 0.15 | 0.15 | 0 15 | 0.15 | 0.15 | 0.15 | П |
| 3046 | 3 | 88 | 0.31 | 0.31 | 0.31 | 0.30 | 0.30 | 0.30 | 0.30 | ı |
| 3329 | 4 | 86 | 0.46 | 0.46 | 0.46 | 0.45 | 0.45 | 0.45 | 0.45 | , |
| 3779 | 5 | 85 | 0.77 | 0.77 | 0.76 | | 0.76 | | 0.74 | ı |
| 4231 | 6 | 84 | 0.93 | 0.93 | | | 0.90 | | 0.88 | ı |
| 4722 | 7 | 83 | 1.08 | 1.08 | | | 1.05 | 1.04 | 1.03 | П |
| 5267 | 8 | 82 | 1.23 | 1.23 | | 1.21 | 1.20 | 1.19 | 1.18 | L |
| 5879 6323 | 9 | 81 | 1.38 | 1.38 | 1.37 | - | 1.35 | 1.34 | | ı |
| 7016 | 10 | 80 | 1.53 1.69 | 1.53 | | 1.51 | 1.50 | 1.49 | 1.48 | L |
| 7719 | 12 | 79 | 1.84 | 1.69 1.84 | | | 1.64 1.78 | 1.63 | 1.62 | I |
| 8431 | 13 | 77 | 1.99 | | | 1.95 | 1.93 | | | |
| 9170 | 14 | 76 | 2.14 | | 2.12 | 2.10 | 2.08 | | 2.06 | 1 |
| 0068 | 15 | 75 | 2.29 | | | | 2.23 | | | 1 |
| 0826 | 16 | 74 | 2.44 | | | | 2.37 | 2.36 | | - |
| 1554 2254 | 17 | 73 | 2.59 2.73 | 2.58 | | | 2.52 | | | Ł |
| 2948 | 19 | 71 | 2.88 | | | | 2.80 | | | н |
| 3626 | 20 | 70 | 3.02 | 3.01 | | | 2.94 | | - | 1 |
| 4254 | 21 | 69 | 3.17 | 3.16 | | | 3.09 | | | L |
| 4817 | 22 | 68 | 3.31 | 3.30 | | 3.25 | 3.23 | | | н |
| 5323 | 23 | 67 | 3.45 | | | | 3.36 | | | ı |
| 5794 | 24 | 66 | 3.59 | | | | | 3.48 | | ı |
| 6281 | 25 26 | 64 | 3.73 3.87 | | | | 3.64 | 3.61 | | |
| 6616 | 27 | 63 | 4.01 | | | | 3.91 | 3.88 | | L |
| 7043 | 28 | 62 | 4.14 | 4.13 | | 4.07 | 4.04 | 4.01 | 4.00 | L |
| 7173 | 29 | 61 | 4.28 | 4.27 | 4.25 | | 4.17 | 4.15 | - | |
| 7237 | 30 | 60 | 4.41 | 4.40 | | | 4.30 | 4.28 | | |
| 7212 | 32 | 58 | 4.68 | | | | | | | ı |
| 7095 | 34 | 56 | 4.94 5.19 | | | | 4.80 5.05 | | | ı |
| 6910 6675 | 38 | 52 | 5.44 | | | | | | | ı |
| 6325 | 40 | 50 | 5.68 | | | | | | | L |
| 5933 | 42 | 48 | 5.92 | | | | 5.76 | | | L |
| 5463 | 44 | 46 | 6.15 | | | | | | | ı |
| 4949 | 46 | 44 | 6.36 6.57 | 6.34 | | | | | | ı |
| 1403 | 50 | 40 | 6.77 | 6.75 | | 6.65 | - | | - | 1 |
| 3705 | 52 | 38 | 6.97 | 6.95 | | | | 1 | | 1 |
| 3040 2333 | 54 | 36 | 7.15 | 7.13 | | | 1 | - | 1 | 1 |
| 1617 | 56 | 34 | 7.33 | 7.31 | | | | | | 1 |
| 0898 | 58 | 32 | 7.49 | 7.47 | | | | | | 1 |
| 0162 | 60 | 30 28 | 7.65 7.80 | | | | | | | 1 |
| 9398 | 64 | 26 | 7.94 | | | - | | | | 1 |
| 8633 | 66 | 24 | 8.07 | | | | | | | 1 |
| 7898 7200 | 68 | 22 | 8.19 | | 8.12 | - | 7.98 | 7.93 | - | |
| 6411 | .70 | 20 | | 8.28 | | | | | 8.02 | |
| 5749 | 72 | 18 | 8.41 | | | | | 8.14 | | |
| 5135 | 76 | 14 | 8.57 | | | | | 8.30 | | |
| 4592 | 78 | 12 | 8.64 | | | | | | | - |
| 4120 | 80 | 10 | 8.70 | 8.68 | 8.63 | 8.55 | 8.48 | 8.43 | 8.41 | - |
| 3697 | 82 | 8 | 8.75 | | | | | 8.48 | | - |
| 3322 | 84 86 | 6 4 | 8.78 8.81 | | | | | | | - |
| 2823 | 88 | 2 | 8.82 | | | | _ | 8.54 | | |
| 2714 | 90 | ō | | | | 8.68 | | | 8.54 | |
| - | _ | | | - | - | - | - | - | - | |

Fahrenheit's Thermometer 50°. English Barometer 30 Inches.

| Z. D. | 8 | 0 1 | Log. 80 | Diff. | Z. 1 | D. | - | 80 | Log. 80 | Diff. | Z. | D. | • | 80 | Log. 80 | Diff. |
|------------|-----|--------------|---------------------|------------|------|----------|------|----------------|---------|-------|------|----------|----|----------------|---------|-------|
| 0 / | 1 | 11 | 1 -7 11 | | 0 | 1 | 7 | " | | | 0 | 1 | 1. | " | | |
| 0 0 | | 0.00 | 0.0000 | 7 | 10 | 0 | 0 | 10.30 | 1.0129 | 72 | 20 | | 0 | 21.26 | 1.3277 | 38 |
| 10 | | 0.17 | | 3011 | | 10 | | 10.47 | 1.0901 | 72 | | 10 | | 21.45 | 1.3315 | 39 |
| 20 | | 1.34 | 9.5315 | 1761 | | 20 | | 10.65 | 1.0273 | 71 | | 20 | | 21.65 | 1.3354 | 39 |
| 30 | | 0.51 | 9.7076 | 1249 | | 30 | | 10.82 | 1.0344 | 70 | 0.10 | 30 | | 21.84 | 1.3393 | 38 |
| 40 | | 0.68 | 9.8325 | 969 | | 40 | | 11.00 | 1.0414 | 69 | 140 | 40 50 | | 22.03 22.23 | 1.3431 | 38 |
| 5 0 | - | 0.85 | 9.9294 | 791 | | 50 | | 11.17 | 1.0483 | 69 | | - | - | | 1.3469 | 38 |
| 1 0 | | 1.02 | 0.0085 | 670 | 11 | 0 | 0 | 11.35 | 1.0552 | 66 | 21 | 0 | 0 | 22.42 | 1.3507 | 37 |
| 10 | | 1.19 | 0.0755 | 580 | (CA) | 10 | | 11.53 | 1.0618 | 66 | - | 10 | | 22.62 22.81 | 1.3544 | 38 |
| 20 30 | | 1.36 1.53 | 0.1335 | 512 457 | 63 | 20 30 | П | 11.71 11.89 | 1.0684 | 65 | 3.8 | 30 | | 23.01 | 1.3619 | 37 |
| 40 | | 1.70 | 0.1841 | 414 | | 40 | п | 12.06 | 1.0815 | 64 | 7.0 | 40 | | 23.21 | 1.3656 | 37 |
| 50 | | 1.87 | 0.2718 | 379 | 5 | 50 | П | 12.24 | 1.0879 | 62 | - | 50 | | 23.40 | | 36 |
| | - | 2.04 | 0.3097 | 347 | 12 | 0 | 0 | 12.42 | 1.0941 | 62 | 22 | 0 | - | 23.60 | 1.3729 | 37 |
| 2 0 | | 2.21 | 0.3097 | 322 | 12 | 10 | U | 12.42 | 1.1003 | 61 | 22 | 10 | | 23.80 | | 36 |
| 20 | | 2.38 | 0.3766 | 301 | 537 | 20 | | 12.78 | 1.1064 | 60 | 200 | 20 | | 24.00 | | 36 |
| 30 | | 2.55 | 0.4067 | 280 | ALT. | 30 | Ľ | 12.95 | 1.1124 | 60 | | 30 | | 24.20 | | 36 |
| 40 | | 2.72 | 0.4347 | 263 | | 40 | ú | 13.13 | 1.1184 | 58 | | 40 | 1 | 24.40 | 1.3874 | 35 |
| 50 | | 2.89 | 0.4610 | 250 | | 50 | | 13.31 | 1.1242 | 58 | | 50 | | 24.60 | | 36 |
| 3 0 | | 3.06 | 0.4860 | 235 | 13 | 0 | 0 | 13.49 | 1.1300 | 57 | 23 | - | - | 24.80 | 1.3945 | 36 |
| 10 | | 3.23 | 0.5095 | 224 | - | 10 | | 13.67 | 1.1357 | 57 | | 10 | | 25.00 | 1.3981 | 34 |
| 20 | | 3.40 | 0.5319 | 211 | | 20 | 1 | 13.85 | 1.1414 | 55 | | 20 | | 25.20 | | 34 |
| 30 | | 3.57 | 0.5530 | 203 | 1 1 | 30 | | 14.02 | 1.1469 | 55 | 100 | 30 | | 25,41 | 1.4049 | 35 |
| 4.0 | 15 | 3.74 | 0.5733 | 193 | 1 | 40 | | 14,20 | 1.1524 | 54 | 100 | 40 | | 25.61 | 1.4084 | 34 |
| 50 | 5 | 3.91 | 0.5926 | 186 | | 50 | | 14.38 | 1.1578 | 56 | | 50 | | 25.81 | 1.4118 | 33 |
| 4 0 | 0 4 | 1.08 | 0.6112 | 178 | 14 | 0 | 0 | 14,56 | 1.1634 | .52 | 24 | 0 | 0 | 26.01 | 1.4151 | 34 |
| 10 | | 1.26 | 0.6290 | -171 | 100 | 10 | 9 | 14.74 | 1.1686 | 54 | | 10 | | 26.21 | 1.4185 | 34 |
| 20 | | 1.43 | 0.6461 | 165 | un. | 20. | , | 14,93 | 1.1740 | 53 | | 20 | | 26.42 | | 34 |
| 30 | | .60 | 0.6626 | 158 | 1 | 30 | | 15.11 | 1.1793 | 52 | | 30 | 1 | 26.62 | | 33 |
| 40 | | 1.77 | 0.6784 | 153 | 153 | 40 | 1 | 15.29 | 1.1845 | 52 | 7 | 40 | | 26.83 | 1 | 33 |
| 50 | 1 | 1.94 | 0.6937 | 149 | | 50 | | 15.48 | 1.1897 | 50 | | 50 | - | 27.03 | | 33 |
| 5 0 | | 5.11 | 0.7086 | 142 | 15 | 0 | 0 | 15.66 | 1.1947 | 51 | 25 | | | 27.24 | 1.4352 | 33 |
| 10 | | 5.28 | 0.7228 | 139 | 143 | 10 | V | 15.81 | 1,1998 | 50 | | 10 | | 27.45 | 1.4385 | 33 |
| 20 | | 5.45 | 0.7367 | 135 | | 20 | 1 | 16.03 | 1.2048 | 50 | 18 | 20 | 1 | 27.66 | | 33 |
| 30 | | 5.63 | 0.7502 | 131 | 0.07 | 30 | ΕÝ | 16.21 | 1.2098 | 49 | | 30 | | 27:86 | | 32 |
| 40 50 | | 5.80 | 0.7633 | 127 122 | 193 | 50 | | 16.39 16.58 | 1.2147 | 46 | | 50 | | 28.07 28.28 | 1.4483 | 32 |
| - | | 5.14 | - | - | 1.0 | | 0 | 16.75 | - | - | 26 | - | - | | | |
| 6 0 | | 5.31 | 0.7882 | 120 116 | 16 | 10 | υ | 16.75 | 1.2241; | 46 | 20 | 10 | 0 | 28.49 28.70 | | 32 |
| 20 | | 3.48 | 0.8118 | 114 | | 20 | 4 | 17.12 | 1.2334 | 46 | | 20 | | 28.91 | 1.4611 | 32 |
| 30 | | 5.66 | 0.8232 | 111 | 100 | 30 | id) | 17.30 | 1.2380 | 46 | | 30 | | 29.13 | | 31 |
| 40 | | 5.83 | 0.8343 | 108 | | 40 | 1 | 17.48 | 1,2426 | 46 | 13 | 40 | | 29.34 | | 32 |
| 50 | 1 | 7.00 | | 106 | - | 50 | 15 | 17.67 | 1.2472 | 47 | 10 | 50 | | 29.55 | | 30 |
| 7 0 | | 7.17 | 0.8557 | 102 | 17 | 0 | ō | 17.86 | 1.2519 | 4.5 | 27 | 0 | - | 29.76 | - | 32 |
| 10 | | 7.34 | 0.8659 | 101 | 120 | 10 | - | 18.05 | 1.2564 | 45 | | 10 | | 29.97 | 1.4768 | 31 |
| 20 | | 7.52 | 0.8760 | . 99 | 12 | 20 | | 18.23 | 1.2609 | 44 | 1.5 | 20 | | 30.19 | | 30 |
| 30 | | 7.69 | 0.8859 | 97 | 120 | 30 | 1 | 18.42 | 1.2653 | 44 | - | 30 | | 30.40 | | 31 |
| 40 | | 7.86 | 0.8956 | 9.5 | -78 | 40 | | 18.61 | 1.2697 | 43 | 1 | 40 | | 30.62 | _ | 30 |
| 50 | | 3.04 | 0.9051 | 93 | - | 50 | | 18.79 | 1.2740 | 44 | | 50 | | 30.83 | | 31 |
| | | 3.21 | 0.9144 | 90 | 18 | U | 0 | 18.98 | 1.2784 | 42 | 28 | | | | | 31 |
| 10 | | 3.38 | 0.9234 | 89 | | 10 | 1 | 19.17 | 1.2826 | 42 | 800 | 10 | | 31.27 | | 30 |
| 20 | | 3.56 | 0.9323 | 87 | 101 | 20 | | 19.36 | 1.2868 | 42 | | 20 | | 31.49 | | 31 |
| 30 | | 3.73 | 0.9410 | 85 | 750 | 30 | | 19.55 | 1.2910 | 42 | | 30 | | 31.72 | | 30 |
| 50 | | 8.90 | 0.9495 | 84 | - | 40 | | 19.73 | 1.2952 | 42 | | 40 | | 31.94 | | 30 |
| - | | 9.08 | 0 9579 | 84 | - | 50 | - | 19.92 | 1.2994 | 42 | | 50 | | 32.16 | | 29 |
| | | 9.25 | 0.9663 | 80 | 19 | 0 | 0 | 20.11 | 1.3036 | 39 | 29 | | | 32.38 | 1.5102 | 31 |
| 20 | _ | 9.42 9.60 | 0.9743 | 80 | 11 | 10 | | 20.30 | 1.3075 | 39 | | 10 | | 32.60 | | 30 |
| 30 | | 9.00 | 0.9823 | 78 | 100 | 20 | | 20.49 | 1.3116 | 41 | | 20 30 | | 32.83 33.05 | 1.5162 | 29 |
| 40 | | 9.95 | | 76 | 10 | 4.0 | 1 | 20.88 | 1.3157 | 40 | 14 | 40 | | 33.27 | 1.5221 | 29 |
| 50 | | 0.12 | 1.0054 | 75 | 100 | 50 | | 21.07 | 1.3237 | 4.0 | | 50 | | 33.50 | | 29 |
| 10 (| | | 1.0129 | 72 | 20 | 0 | | 21.26 | 1.3277 | 38 | 30 | | | 33.72 | | 29 |
| - | - | - | STREET, ASSOCIATION | - | - | - | 4900 | | - | - | | - | - | | | _ |

| Fahrenheit's Thermometer 50°. | English Barometer 30 Inches. |
|-------------------------------|------------------------------|
|-------------------------------|------------------------------|

| Z. | D. | 1 30 | Log. 8 0 | Diff. | Z. | D. | 1 30. | Log. 80 | Diff. | Z. | D. | 80 | Log. 8 A | Diff. |
|------|----------|------------------|----------|----------|------|--------------|---------|--------------------|------------|------|----------|---------|--------------------|-------|
| 0 | , | " | | | o | 1 | , " | | | 0 | 1 | ' " | 7 0 1 0 0 0 | |
| 30 | 10 | 0 33.72 33.95 | | 29 | 40 | 10 | | 1 | | 50 | 10 | | 1.84209 | |
| | 20 | | | 29 | | 20 | 49.28 | | | | 20 | | 1.84721 | 256 |
| | 30 | | | 29 | | 30 | | 1.69780 | | | 30 | | 1.84977 | 257 |
| 0.13 | 40 | 34.63 | | 28 | | 40 | | 1.70037 | 256 | | 40 | | 1.83234 | |
| | 50 | 34.86 | 1.5423 | 29 | | 50 | 50.46 | 1.70293 | 257 | | 50 | | 1.85490 | 257 |
| 31 | 0 | 0 35.09 | 1.5452 | 29 | 41 | 0 | 0 50.75 | | | 51 | 0 | | 1.85747 | 258 |
| | 10 | 35.32 | 1.5481 | 29 | | 10 | 51.06 | | | | 10 | | 1.86005 | |
| | 20 30 | 35.56 35.79 | 1.5510 | 28 | | 30 | | 1.71058 | 253 | | 30 | | 1.86264 | |
| .01 | 40 | 36.02 | | 28 | | 40 | | 1.71564 | | | 40 | | 1.86781 | 1 |
| | 50 | 36.26 | 1.5594 | 28 | 110 | 50 | 52.27 | | | 150 | 50 | | 1.87039 | |
| 32 | 0 | 0 36.49 | 1.5622 | 28 | 42 | U | 0 52.57 | 1.72070 | 252 | 52 | 0 | 1 14.64 | 1.87298 | 260 |
| | 10 | 36.73 | 1.5650 | 28 | | 10 | 52.88 | | 252 | 4.5 | 10 | | 1.87558 | |
| | 20 | 36.97 | 1.5678 | 29 | | 20 | | 1.72574 | | | 20 | | 1.87819 | 1 |
| | 30 | 37.21 | 1.5707 | 28 | | 30 | | 1.72826 | | | 30 | | 1.88080 1.88341 | |
| | 40 50 | 37.45 | 1.5735 | 27 28 | | 40 50 | 54.12 | 1.73078 | | 0 | 50 | | 1.88601 | |
| 33 | 0 | 0 37.93 | 1.5790 | 28 | 43 | 0 | - | 1.73580 | | 53 | 0 | | 1.88863 | |
| 1 55 | 10 | 38.17 | 1.5818 | 27 | 23 | 10 | 54.75 | | 1 | 3 | 10 | | 1.89125 | |
| | 20 | 38.42 | 1.5845 | 28 | | 20 | 55.07 | 1.74087 | 253 | | 20 | 18.33 | 1.89387 | 263 |
| | 30 | 38.66 | 1.5873 | 27 | | 30 | | 1.74340 | | | 30 | | 1.89650 | |
| 1 | 40 50 | 38.90 39.15 | 1.5900 | 27 | | 40 | | 1.74593 | | | 40 50 | | 1.89913 | |
| 0.4 | - | 0 39.39 | | - | 44 | 50 | | | | E4 | - | | 1.90440 | |
| 34 | 10 | 39.39 | 1.5954 | 27 | 44 | 10 | | 1.75100 | | 54 | 10 | | 1.90705 | |
| 100 | 20 | 39.89 | 1.6009 | 27 | | 20 | | 1.75604 | 1 | | 20 | | 1.90970 | |
| | 30 | 40.14 | 1.6036 | 27 | | 30 | | 1.75856 | | | 30 | | 1.91236 | |
| | 4.0 | 40.39 | 1.6063 | 27 | 5.33 | 40 | | 1.76108 | | | 40 | | 1.91502 | |
| | 50 | 40.64 | 1.6090 | 26 | | 50 | | 1.76360 | | | 50 | | 1.91769 | - |
| 35 | 0 | 0 40.89 | 1.6116 | 27 | 45 | 0 | | 1.76611 | 252 | 55 | 0 | | 1.92036 | |
| | 10 | 41.14 | 1.6143 | 27 | | 10 | | 1.76863 | 252 252 | | 10 | | 1.92304 | 269 |
| -93 | 30 | 41.65 | 1.6197 | 26 | | 30 | | 1.77367 | 252 | | 30 | | 1.92841 | 271 |
| | 40 | 41.91 | 1.6223 | 27 | | 40 | | 1.77619 | 252 | | 40 | | 1.93112 | |
| | 50 | 42.16 | 1.6250 | 26 | 2.05 | 50 | 1 0.08 | 1.77871 | 252 | 2 | 50 | 25.88 | 1.93382 | 270 |
| 36 | - | 0 42.42 | 1.6276 | 27 | 46 | 0 | 1 0.43 | 1.78123 | 252 | 56 | 0 | | 1.93653 | 271 |
| 100 | 10 | 42 68 | 1.6303 | 27 | 120 | 10 | | 1.78375 | 253 | | 10 | | 1.93924 | 272 |
| - 6 | 30 | 42.95 43.21 | 1.6330 | 26 26 | | 20 | | 1.78628 | 252 252 | | 20 30 | | 1.94196 1.94469 | 273 |
| 1 | 40 | 43.47 | 1.6382 | 26 | | 30 | | 1.78880 1.79132 | 253 | | 40 | | 1.94469 | 273 |
| 1 | 50 | 43.74 | 1.6408 | 27 | 1.9 | 50 | 2.21 | 1.79385 | 252 | | 50 | | 1.95016 | 275 |
| 37 | 0 | 0 44.00 | 1.6435 | 26 | 47 | 0 | 1 2.57 | 1.79637 | 253 | 57 | 0 | 1 29.73 | 1.95291 | 275 |
| | 10 | 44.27 | 1.6461 | 26 | 10 | 10 | | 1.79890 | 253 | -11 | 10 | 30.31 | 1.95566 | 277 |
| | 20 | 44.54 | 1.6487 | 26 | 100 | 20 | | 1.80143 | 253 | | 20 | | 1.95843 | |
| L | 30 | 44.80 | 1.6513 | 26 26 | | 30 | | 1.80396 1.80649 | 253 253 | | 30 | 31.48 | 1.96120 | 278 |
| 1 | 50 | 45.34 | 1.6565 | 26 | 1 | 50 | | 1.80902 | 253 | | 50 | | 1.96676 | 279 |
| 38 | - | 0 45.61 | 1.6591 | 26 | 48 | 0 | - | 1.81155 | 254 | 58 | - | - | 1.96955 | 280 |
| 1 | 10 | 45.89 | 1.6617 | 26 | 1 | 10 | | 1.81409 | 254 | 1 | 10 | 33.85 | 1.97235 | 281 |
| - 7 | 20 | 46.16 | 1.6643 | 26 | | 20 | | 1.81663 | - | | 20 | 34.46 | 1.97516 | 281 |
| | 30 | 46.44 | 1.6669 | 26 | | 30 | | 1.81916 | 254 | | 30 | | 1.97797 | 283 |
| 160 | 40 50 | 46.72 | 1.6695 | 25 26 | 100 | 40 50 | | 1.82170 | 254 | | 40 50 | | 1.98080 1.98362 | 282 |
| 39 | - | 0 47.27 | 1.6746 | 26 | 49 | 0 | | 1.82678 | 255 | 59 | 0 | | 1.98646 | 285 |
| 39 | 10 | 47.56 | 1.6772 | 26 | 49 | 10 | | 1.82933 | 255 | 03 | 10 | | 1.98931 | 285 |
| | 20 | 47.84 | 1.6798 | 26 | | 20 | | 1.83188 | | | 20 | | 1.99216 | 287 |
| - | 30 | 48.13 | 1.6824 | 26 | 111 | 30 | | 1.83443 | 255 | | 30 | 38.89 | 1.99503 | 287 |
| 3 | 40 | 48.42 | 1.6850 | 26 | | 40 | | 1.83698 | 255 | | 40 | | 1.99790 | 289 |
| 40 | 50 | 48.70 | 1.6876 | 25 | ŁO. | 50 | | 1.83953 | 255 | 60 | 50 | | 2.00079 | 289 |
| +0 | U | 40.99 | 1.0901 | 26 | 50 | 0 | 9.52 | 1.84208 | 256 | 0(1) | U | 90.80 | 2.00368 | 200 |

Fahrenheit's Thermometer 50°. English Barometer 30 Inches.

| | _ | | | | il a | _ | | | - 14 | 2541 | | | | | - | 254 | 1 26. |
|-------|-----|-------|-------------|----------------|-------|-----|-------|-------------------------------|-------|-------------------------------|-------|------------|-------|------------------------------|-------|-------------------------------|------------------------|
| Z.D. | | 80 | Log. 80 | D. | Z.D. | | 20 | Log. 80 | D. | $\frac{d\delta\theta}{d\tau}$ | Z.D. | - | 8 | Log. 30 | Diff. | $\frac{d\delta\theta}{d\tau}$ | $\frac{d\delta t}{dp}$ |
| 0/ | 1 | " | 40 1 | | 01 | 1 | 11 | 1.00 | | 111 | 01 | 1 | " | | 7.1 | | |
| 60 0 | 1 | 40.85 | 2.00368 | 290 | 70 0 | 2 | 39.16 | 2.20185 | 388 | or State | 80.0 | 5 | 20.19 | 2.50541 | 696 | 0.030 | 0.0 |
| 10 | | 41.52 | 2.00658 | 291 | 10 | | 40.59 | 2.20573 | 390 | 0.00 | 10 | | 25.36 | 2.51237 | 707 | 0.031 | 0.0 |
| 20 | | 42.21 | 2.00949 | 292 | 20 | - | 42.04 | 2.20963 | 393 | 1.05 | 20 | | 30.70 | 2.51944 | | 0.033 | |
| .30 | | 42.90 | 2.01241 | 293 | 30 | | 43.52 | 2,21356 | 396 | 225 | 30 | | 36.20 | 2.52660 | | 0.034 | |
| 40 | | 43.59 | 2.01535 | 294 | 40 | | 45.02 | 2.2175? | 398 | 000 | 40 | | 41.88 | 2.53387 | | 0.036 | |
| 50 | | 44.30 | 2.01829 | 295 | 50 | 1 | 46.53 | 2.22150 | 402 | 420 | 50 | | 47.74 | 2.54125 | 749 | 0.038 | 0.0 |
| 1 0 | 1 | 45.01 | 2.02124 | 296 | 71 0 | 2 | 48 08 | 2.22552 | 404 | | 81 0 | 5 | 53 70 | 2.54874 | | 0.010 | |
| 10 | î | | 2.02420 | | 10 | ~ | | 2.22956 | | - 1 | 10 | 6 | | 2.55635 | | 0.042 | |
| 20 | | | 2.02718 | | 20 | | | 2.23363 | | ALC: YOR | 2.0 | | | 2.56407 | | 0.044 | |
| 30 | | | 2.03016 | | 30 | | | 2.23773 | | aCCA1 | 30 | | | 2.57192 | | 0.046 | |
| 40 | | | 2.03316 | | 40 | | | 2.24186 | | | 40 | | | 2.57989 | | 0.049 | |
| 50 | | | 2.03617 | | 50 | | | 2.24603 | | | 50 | | | 2.58800 | | 0.051 | 1 |
| | 1 | | 2.03918 | - | | - | | 2.25022 | - | · | - | - | | | _ | 0.053 | .1 |
| 12 0 | 1 | | | | | 2 | | | | | 82 0 | 0 | - | 2.59624 | 1 | | 1000 |
| 10 | | | 2.04221 | | 10 | 0 | | 2.25445 | | 5.00 | 10 | | | 2.60462 | | 0.057 | |
| 20 | | | 2.04525 | | 20 | 3 | | 2.25870 | | 100 | 20 | | | 2.61313 | | 0.060 | |
| 30 | | | 2.04830 | | 30 | | | 2.26299 | | 100 | 30 | | | 2.62179 | | 0.063 | |
| 40 | | | 2.05137 | | 40 | | | 2.26732 | | | 40 | 7 | | 2.63062 | | 0 067 | |
| 50 | _ | | 2.05445 | - | 50 | _ | | 2.27168 | | | 50 | | | 2.63961 | | 0.071 | |
| 3 0 | 1 | | 2.05754 | | | 3 | | 2.27608 | | - | 83 0 | 7 | | 2.64875 | 1 | 0.074 | 1 - |
| 10 | | | 2.06064 | - | 10 | | | 2.28051 | | | 10 | | | 2.65806 | | 0.079 | |
| 50 | | 55.81 | 2.06376 | 312 | 20 | | 12.74 | 2.28498 | 450 | 0.003 | 20 | | 45.10 | 2.66755 | 967 | 0.084 | 0. |
| 30 | | 56.66 | 2.06688 | 315 | 30 | | 14.75 | 2.28948 | 454 | 0.004 | 30 | | 55.58 | 2.67722 | 986 | 0.089 | 0. |
| 40 | | 57.50 | 2.07003 | 315 | 40 | | 16.80 | 2.29402 | 458 | 0 004 | 40 | 8 | 6.50 | 2.68708 | 1006 | 0.095 | 0. |
| 50 | | 58.36 | 2.07318 | 317 | 50 | | 18.88 | 2.29860 | 462 | 0.005 | 50 | | 17.90 | 2.69714 | 1026 | 0.101 | 0. |
| 1 0 | ī | 59.99 | 2.07635 | 218 | 74 0 | 3 | 91.01 | 2.30322 | 167 | 0.005 | 84. 0 | 8 | 90 80 | 2.70740 | 1017 | 0.107 | 0 |
| 10 | 2 | | 2.07953 | | 10 | | | 2.30789 | | | | 0 | | 2.71787 | | | 1 |
| 20 | ~ | | 2.08273 | | 20 | | | 2.31259 | | | | | | 2.72856 | | | |
| 30 | , | | 2.08594 | | | | | 2.31734 | | | 30 | 9 | | 2.73948 | | | |
| 40 | | | 2.08917 | | | | | | | | | 1 | | 2.75063 | | | |
| 50 | | | 2.09911 | | 40 | | | 2.32213 | | | | | | 2.76202 | | | |
| | _ | | | | 50 | - | | 2.32696 | - | | | - | | | | | |
| 35 () | 2 | | 2.09567 | | | 1- | | 2.33184 | | | | | 53.84 | | | | |
| 10 | | | 2.09894 | | | | | 2.33677 | | | | | | 2.78558 | | | |
| 20 | | | 2.10224 | | | | | 2.34174 | | | | | | 2.79777 | | | |
| 30 | | | 2.10554 | | | | | 2.34676 | | | | | | 2.81025 | | | |
| 4.0 | 1 | | 2.10886 | | | | | 2.35183 | | | | 11 | | 2.82302 | | | |
| 50 | | 9.48 | 2.11220 | 335 | 50 | | 47.48 | 2.35695 | 517 | 0.011 | 50 | | 25.66 | 2.83611 | 1340 | 0.229 | 0 3 |
| 56 O | 2 | 10.48 | 2.11555 | 337 | 76 U | 3 | 50.21 | 2.36212 | 523 | 0.012 | 86 0 | 11 | 47.15 | 2.84951 | 1374 | 0.248 | 0 3 |
| 10 | | 11.50 | 2.11892 | 339 | 10 | | 53.00 | 2.36735 | 528 | 0.012 | 10 | 12 | 9.88 | 2.86325 | 1410 | 0.269 | 0.4 |
| 20 | 1 | 12.52 | 2.12231 | 340 | 20 | 1 | 55.85 | 2.37263 | 533 | 0.013 | 20 | | 33.97 | 2.87735 | 1447 | 0.299 | 0.4 |
| 30 | П | 13.57 | 2.12571 | 342 | 30 | | 58.76 | 2.37796 | 538 | 0.013 | 30 | 1 | 59.51 | 2.89182 | 1484 | 0.317 | 0. |
| 40 | | 14.62 | 2.12913 | 345 | | 1 | | 2.38334 | | | | | 26.61 | 2.90666 | 1523 | 0.345 | 0. |
| 50 | | 15.70 | 2.13258 | 345 | | | | 2.38879 | | | | | | 2.92189 | | | |
| 57 () | 2 | | 2.13603 | | | | | 2 39430 | | | | - | | 2.93751 | - | | - |
| 10 | | | 2.13951 | | | | | 2.39430 | | | | 1 | | 2.95362 | | | |
| 20 | | | 2.14300 | | | | | 2.39987 | | | | | | 2.95302 | | | |
| 30 | | | 2.14652 | | 5 | 3 | | | | | | 15 | | 2.98717 | | | |
| | | | 1 | | | 4 | | 2 41119 | | | | | | 3.00466 | | | |
| 40 | | | 2.15006 | | | | | 2.41695 | | | | | 50.8 | | | | |
| 50 | | | 2.15361 | - | 10.00 | 1 | | 2.43278 | | - | | 17 | | 3.02267 | | | - |
| 68 (| 100 | | | | 35 | | | 2.42867 | | | | | 19.6 | 3.0412 | | 0.722 | |
| 10 | | | 2.16078 | | | | | 2.43463 | | | | 19 | 9.0 | 3.06031 | | | |
| 20 | | | 2.16440 | | | | | 2.44066 | | | | 20 | 2.2 | 3.07998 | | | |
| 30 | | | 2.16804 | | | | | 2.44677 | | | | | 59.6 | 3.10024 | 2089 | 0.987 | 71. |
| 4(| | | 2.17171 | | |) | | 2.45295 | | | | 22 | | 3.12113 | 2155 | 1.101 | 12. |
| 50 | | 29.76 | 2.17539 | 371 | 50 | | | 2.45921 | | | | 23 | 8.9 | 3.14268 | | | |
| 69 (| 12 | | 2.17910 | | | | | 2.46556 | | - Indiana | - | minutes of | - | 3.16489 | | | |
| 10 | - | 39.3 | 2.18283 | 3375 | 10 | | | 2.47198 | | | | | 40.9 | 3.18779 | 2361 | 1.551 | 19 |
| | | | 7 2.1865 | | |) 5 | | 2.47196 | | | | 27 | | 3.21140 | 2431 | 1.740 | 3 |
| 90 | | | 2.1903 | | | | | | | | | | | 3.23574 | | | |
| 20 |) | | 160 1371.30 | 21.525 | 8 %(| 24 | 5.54 | 2.48507 | 1008 | 10.026 | | | 40.8 | | | | |
| 30 | | | | | | | 10.00 | 0 40000 | 1000- | 0 000 | 40 | | | | | | |
| 30 | | 36.33 | 2.1941 | 7 383 | 3 40 |) | | 2.49176 | | | | | 23.2 | 3.26083 | | | |
| 30 | | 36.33 | | 7 383 0 383 | 3 40 | | 15.16 | 2.49176 2.49853 2.50541 | 688 | 0.028 | 50 | 32 | 15.0 | 3.26083 3.28667 3.3133 | 2667 | | 9 5. |

| | | TABLE | XV | III | | | | 89 | , | TAB | . XX | Therr | nometer. |
|----------|-----|---------|----------|------|---------|------------|-----|------|----------|-----|-------------|----------|--------------------|
| | | | | Sec. | | | | | | Th. | Log. | Th. | Log. |
| 11.0 | | Therm | omet | er. | 100 | | | | - | 100 | 0.00173 | 50° | 0.00000 |
| | | | | | | TYA | DI | T | XIX. | 11 | 0.00169 | 51 | 9.99996 |
| P. P. | Th. | Log. | P. P. | Th. | Log. | LA | DL | ı.P. | AIA. | 12 | 0.00164 | 52 | 9.99991 |
| - | 100 | 0.03779 | - | 50° | 0.00000 | 100 | | 13 | 733 0.34 | 13 | 0.00160 | 53 | 9.99987 |
| 10 | 1 | 0.03680 | 9 | 1 | 9.99910 |] | Bar | om | eter. | 14 | 0.00156 | 54 | 9.99983 |
| 20 | 2. | 0.03582 | 18 | 2 | 9.99820 | 10. | | | / | 15 | 0.00151 | 55 | 9.99978 |
| 29 | 3 | 0.03484 | 27 | 3 | 9.99730 | 11 | | | | 16 | 0.00147 | 56 | 9.99974 |
| 39 | 4 | 0 03386 | 36 | 4 | 9.99640 | P. P. | Ba | ır. | Log. | 17 | 0.00143 | 57 | 9.99970 |
| 49 | 5 | 0.03288 | 45 | 5 | 9.99550 | | 27 | .5 | 9.96221 | 18 | 0.00138 | 58 | 9.99965 |
| 59 | 6 | 0.03191 | 54 | 6 | 9.99460 | | | 6 | 9.96379 | 19 | 0.00134 | 59 | 9.99961 |
| 69 | 7 | 0.03094 | 63 | 7 | 9.99371 | | | 7 | 9.96536 | 20 | 0.00130 | 60 | 9.99957 |
| 78 | 8 | 0.02997 | 72 | 8 | 9.99282 | | 11 | 8 | 9.96692 | 21 | 0.00126 | 61 | 9.99953 |
| 88 | 9 | 0.02900 | 81 | 9 | 9.99193 | | | 9 | 9.96848 | 22 | 0.00121 | 65 | 9.99948 |
| 3.7 | 20 | 0.02803 | 30 | 60 | 9.99104 | + | 28 | .0 | 9.97004 | 23 | 0.00117 | 63 | 9.99944 |
| 10 | 1 | 0.02706 | 9 | 1 | 9.99016 | 15 | | 1 | 9.97158 | 24 | 0.00113 | 64 | 9.99940 |
| 19 | 2 | 0.02609 | 18 | 2 | 9.98927 | 30 | | 2 | 9.97313 | 25 | 0.00108 | 65 | 9.99935 |
| 29 | 3 | 0.02514 | 26 | 3 | 9.98839 | 46 | | 3 | 9.97466 | 26 | 0.00104 | | 9.99931 |
| 38 | 4 | 0.02418 | 35 | 4 | 9.98751 | 61 | | 4 | 9.97620 | 27 | 0.00100 | 67 | 9.99927 |
| 48 | 5 | 0.02323 | 44 | 5 | 9.98663 | 76 | - | 5 | 9.97772 | 28 | 0.00095 | 68 | 9.99922 |
| 58 | 6 | 0.02227 | 53 | 6 | 9.98575 | 91 | | 6 | 9.97924 | 29 | 0.00091 | 69 | 9.99918 |
| 67 | 7 | 0.02132 | 62 | 7 | 9.98488 | 106 | 0 4 | 7 | 9.98076 | 30 | 0.00087 | 70 | 9.99913 |
| 77 | 8 | 0.02037 | 70 | 8 | 9.98401 | 122 | | 8 | 9.98227 | 31 | 0.00083 | 71 | 9.99909 |
| 86 | 9 | 0.01942 | 79 | 9 | 9.98314 | 137 | | 9 | 9.98378 | 32 | 0.00078 | 72 | 9.99904 |
| 3 - | 30 | 0.01848 | 1 | 70 | 9.98227 | 111 | 29 | .0 | 9.98528 | 33 | 0.00074 | 73 | 9.99900 |
| . 9 | 1. | 0.01751 | 9 | 1 | 9.98140 | 15 | | 1 | 9.98677 | 34 | 0.00070 | 74 | 9.99896 |
| 19 | 2 | 0.01660 | 17 | 2 | 9.98054 | 29 | | 2 | 9.98826 | 35 | 0.00065 | 75 | 9.99891 |
| 28 | 3 | 0.01566 | 26 | 3 | 9.97967 | 44 | | 3 | 9.98975 | 36 | 0.00061 | 76 | 9.99887 |
| 38 | 4 | 0.01472 | 34 | 4 | 9.97881 | 59 | | 4 | 9.99123 | 37 | 0.00057 | 77. | 9.99883 |
| 47 | 5 | 0.01379 | 43 | 5 | 9.97795 | 73 | | 5 | 9.99270 | 38 | 0.00052 | 78 | 9.99878 |
| 56 | 6 | 0.01285 | 52 | 6 | 9.97709 | 88 | | 6 | 9.99417 | 39 | 0.00048 | 79 | 9.99874 |
| 66 | 8 | 0.01192 | 60 | 7- | 9.97623 | 103 | | 7 | 9.99563 | 40 | 0.00043 | 80 | 9.99870 |
| 75 85 | 9 | 0.01099 | 69 | 8 9 | 9.97537 | 118 | | 8 | 9.99709 | 41 | 0.00039 | 81 | 9.99866 |
| 03 | - | 0.01006 | 11 | | 9.97452 | 133 | | 9 | 9.99855 | 42 | 0.00034 | 82 | 9.99861 |
| | 40 | 0.00914 | | 80 | 9.97367 | | 30 | | 0.00000 | 43 | 0.00030 | 83 | 9.99857 |
| 9 | 1 | 0.00822 | 8 | 1 | 9.97282 | 14 | | 1 | 0.00145 | 44 | 0.00026 | 84 | 9.99853 9.99848 |
| 18 | 2 | 0.00730 | 17 | 2 | 9.97197 | 29 | | 2 | 0.00289 | 45 | 0.00021 | 85 86 | 9.99848 |
| 28 | 3 | 0.00638 | 25 | 3 | 9.97112 | 43 | | 3 | 0.00432 | 4.7 | 0.00017 | 87 | 9.99844 |
| 37 | 4 5 | 0.00546 | 34 | 4 5 | 9.97027 | 57 | | 4 | 0.00575 | 48 | 0.000013 | 88 | 9.99835 |
| 55 | 6 | 0.00455 | 42 50 | 6 | 9.96943 | 71 | | 5 | 0.00718 | 49 | 0.00008 | 89 | 9.99831 |
| 64 | 7 | 0.00363 | 59 | 7 | 9.96859 | 86 | | 6 | 0.00860 | 50 | 0.00000 | | 9.99827 |
| 74 | 8 | 0.00272 | 67 | 8 | 9.96775 | 100 114 | | 8 | 0.01002 | | P. to tenth | | 1 |
| 83 | 9 | 0.00090 | 76 | 9 | 9.96691 | 129 | | 9 | 0.01143 | P. | .2 .3 .4 | | .7 .8 .9 |
| 00 | 50 | 0.00000 | 10 | 90 | 9.96524 | | 31 | | 0.01284 | -0 | 1 1 2 | | 3 3 4 |
| - | 00 | 0.00000 | - | 30 | 3.30324 | | 31 | .0 | 17.01424 | | 1 1 2 | ~ 3 | 3 3 4 |

EXPLANATION.

The true refraction is computed by the following formula, viz. $r=\frac{1}{1+\beta\left(\tau-50\right)}\times\frac{p}{30}\times\delta\theta+\frac{d\,\delta\theta}{d\tau}\left(\tau-50^{\circ}\right)-\frac{d\,\delta\theta}{dp}\left(30-p\right);$ in which r denotes the true refraction, $\beta=0.00375$ the expansion of a given volume of air at the surface of the earth for one degree of the centigrade thermometer, p the height of the English barometer, τ the temperature in the open air by Fahrenheit's thermometer, $\delta\theta$ the mean refraction for 30 inches and $\delta\theta$; and $\delta\theta$ are expressions for determining the effects of changes in the temperature and barometric pressure respectively.

Table XVII. contains $\delta\theta$, the mean refractions, and the expressions for $\frac{d\delta\theta}{d\tau}$ and $\frac{d\delta\theta}{dp}$. Table XVIII. contains the logarithms of $\frac{1}{1+\beta(\tau-50^\circ)}$; Table XIX. the logarithms of $\frac{p}{30}$; and Table XX. the logarithms of $-\frac{\tau-50}{10000}\times.431$.

TABLE XXI. TABLE XXII. 90 Augmentation of the Moon's Semi-Reduction of the Moon's Parallax in the diameter in Altitude and Zenith Dist. Spheroid. 111 1 " 61' Lat. 54' 55' 56' 58' 59 60 57' 0 15 30 16 0 16 30 17 0 14 30 15 18 11 11 10 11 11 " 11 11 11 0 90 0.00 0.00 00 0.00 0.00 0.00 0.00 0 0.0 0 0 0.0 0.0 0.0 0.0 0.0 1 89 0 24 0.25 0.27 0.29 0.31 0.33 1 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 2 88 0.48 0.50 0.54 0.58 0.62 0.65 2 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 387 0.71 0.75 0.80 0.86 0.92 0.97 3 0.0 0.0 0.0 0.0 0.0 00 0.0 00 4 86 1.15 4 0.95 1.00 1.07 1.23 1.30 0.0 0.0 0.0 0.0 0.1 0.1 0.1 01 5 85 1.18 1.34 1.43 5 1.25 1.53 1.62 0.1 0.1 0.1 0.1 0.1 0.1 0.1 0.1 1.94 684 1.41 1.60 1.71 1.83 6 1.50 0.1 0.1 0.1 0.1 0.1 0.1 01 0.1 7 83 1.65 1.75 1.87 2.00 2.13 2.26 7 0.2 0.2 0.2 0.2 0.2 0.2 0.2 0.2 8 82 1.88 2.00 2.14 2.28 2.43 2.58 8 0.2 0.2 0.2 0.2 0.2 0.2 0.2 0.2 981 2.11 2.25 2.40 2.56 2.73 2.90 9 0.3 0.3 0.3 0.3 0.3 0.3 0.3 0.3 10 80 2.35 2.50 2.67 2.85 3.03 3.22 10 0.3 0.3 0.3 0.3 0.3 0.3 0.3 0.4 11 79 2.58 2.75 2.94 3.13 3.33 3.54 11 0.4 0.4 0.4 0.4 0.4 0.4 0.4 0.4 12 78 2.81 3.00 3.20 3.41 3 63 3.86 12 0.4 0.5 0.5 0.5 0.5 0.5 0.5 0.5 13 77 3.04 3.25 3.47 3.69 3.93 4.18 13 0.6 0.5 0.5 0.5 0.6 0.6 0.6 0.6 14 76 3.27 3.50 3.73 3.97 4.23 4.19 14 0.6 0.6 0.6 0.6 0.6 0.7 0.7 0.7 15 75 3.50 3.74 3.99 4.25 4.52 4.80 15 0.7 0.7 0.7 0.7 0.7 0.8 0.8 0.8 16 74 3.73 3.98 4.25 4.53 4.81 5.11 16 0.8 0.8 0.8 0.8 0.8 0.9 0.9 0.9 17 73 3.95 4.22 4.51 4.80 5.10 5.42 17 0.9 0.9 0.9 0.9 1.0 1.0 1.0 1.0 18 72 4.17 1.1 4.46 4.76 5.07 5.39 5.73 18 1.0 1.0 1.0 1.0 1.1 1.1 1.1 19 71 4.40 4.70 5.02 5.35 5.68 6.04 19 1.1 1.1 1.1 1.2 1.2 1.2 1.2 1.2 20 70 4.62 5.62 5.97 1.3 1.3 4.94 5.27 6.35 20 1.2 1.2 1.3 1.3 1.4 1.4 21 69 4.84 5.18 5.89 6.26 6.65 5.52 21 1.3 1.4 1.4 1.4 1.5 1.5 1.4 1.5 22 68 5.06 5.42 6.16 6.95 22 5.77 6.55 1.5 1.5 1.5 1.6 1.6 1.7 1.5 1.6 23 67 5 28 7.25 5.65 6.02 6.42 6.83 23 1.6 1.6 1.6 1.7 1.7 1.7 1.8 1.8 21 66 5.49 24 5.88 6.27 6.68 7.11 7.54 1.7 1.7 1.8 1.8 1.8 1.9 1.9 1.9 25 65 25 5.71 7.39 6.11 6.52 6.94 7.84 1.9 1.9 1.9 2.0 2.0 2.0 2.1 2.1 26 64 5.92 6.34 6.76 7.20 7.66 26 2.0 8.13 2.0 2.1 2.1 2.1 2.2 2.3 2.3 27 63 2.2 6.13 6.56 7.00 7.46 7.93 8.42 27 2.1 2.2 2.3 2.3 2.4 2.3 2.4 28 62 6.34 6.79 7.24 7.72 8.20 8.71 28 2.3 2.3 2.4 2.4 2.5 2.6 2.5 2.5 29 61 6.55 7.01 7.48 7.97 8.47 9.00 29 2.4 2.5 2.5 2.6 26 2.7 2.7 2.8 30 60 6.75 7.23 7.71 8.22 8.74 9.28 2.6 2.7 2.8 3.0 30 2.6 2.7 2.8 2.9 32 58 7.15 7.67 8.17 8.72 9.26 9.84 32 2.9 3.0 3.0 3.1 3.1 3.2 3.2 3.3 34 56 7.55 8.09 8.63 9.20 9.78 10.39 34 3.3 3.3 3.4 3.4 3.5 3.6 3.6 3.7 36 54 7.93 8.50 9.07 9.67 10.28 10.92 36 3.6 3.7 3.7 3.8 3.9 3.9 4.0 4.1 38 52 8.31 8.90 9.51 10.13 10.78 38 3.9 4.2 4.2 4.0 4.1 4.3 4.4 4 6 40 50 8.67 9.30 9.93 10.58 11.26 40 4.3 4.4 4.5 4.8 4.9 4.6 4.6 4.7 12 48 9.03 9.68 10.34 11.02 11.72 12.44 42 4.9 5.2 4.7 4.8 4.8 5.0 5.3 5.1 44 46 9.38 10.05 10.74 11.44 12.17 12.92 44 5.0 5.1 5.2 5.3 5.4 5.5 5.7 5.6 46 44 9.72 10.41 11.12 11.85 12.61 13.38 46 5.7 5.4 5.5 5.6 5.8 5.9 6.0 6.1 48|42|10.05|10.76|11.49|12.25|13.03|13.83 48 5.8 5.9 6.0 6.1 6.2 6.3 6.4 6.5 50 40 10.37 11.10 11.85 12.63 13.43 14 25 50 6.1 6.3 6.4 6.5 6.6 6.7 6.8 6.9 52 38 10.67 11.42 12.19 12.99 13.82 14.66 52 6.5 6.6 6.7 6.9 7.0 7.1 7.2 7.3 54 36 10.95 11.72 12.52 13.34 14.19 15.06 54 6.9 7.0 7.1 7.2 7.4 7.5 7.6 7.7 56 34 11.22 12.01 12.83 13.67 14.55 15.44 56 7.2 7.6 7.3 7.5 7.7 7.9 8.0 8.1 58 32 11.48 12.29 13.12 13.99 14.88 15.79 58 7.5 7.7 7.8 7.9 8.1 8.2 8.4 8.5 60 30 11.72 12.55 13.40 14.29 15.20 16.13 60 7.9 8.2 8.3 8.0 8.4 8.6 8.7 8.9 62 28 11.95 12.79 13.66 14.57 15.50 16.45 8.5 62 8.2 8.3 8.6 8.8 8.9 9.1 9.2 64 26 12.17 13.02 13.91 14.83 15.78 16.75 64 8.5 8.8 8.9 9.1 9.3 9.6 8.6 9.4 66 24 12.37 13.24 14. 14 15.08 16.04 17.03 9.1 66 8.8 8.9 9.2 9.4 9.6 9.7 99 68 22 12.55 13.44 14.36 15.30 16.28 17.28 68 9.0 9.2 9.4 9.5 9.7 9.9 10.0 10.2 70 20 12.72 13.62 14.55 15.51 16.50 17.51 9.8 10.0 10.1 10.3 10.5 70 9.3 9.4 9.6 72 18 12.88 13.79 14.73 15.70 16.70 17.73 72 10.0 10.2 10.4 10.6 10.7 9.5 97 9.9 74 16 13.02 13.94 14.89 15.87 16.88 17.92 74 10.6 10.8 11.0 9.7 9.9 10.1 10.2 10.4 76 14 13.14 14.07 15 03 16.02 17.04 18.09 76 9.9 10.1 10.3 10.4 10.6 10.8 11.0 11.2 78 12 13.24 14 18 15.15 16.15 17.18 18.24 78 10.0 10.2 10.4 10.6 10.8 11.0 11.2 11.4 80 10 13.33 14.28 15.25 16.26 17.30 18.36 80 10.2 10.4 10.6 10.7 10.9 11.1 11.3 11.5 8 13.40 14-36 15.34 16.35 17.39 18.47 10.3 10.5 10.7 10.9 11.1 11.3 11.4 11.6 82 82 84 6 13.46 14.42 15.41 16.42 17.47 18.55 84 10.4 10.6 10.8 11.0 11.2 11.4 11.5 11.7 86 4 13.50 14.46 15.45 16.47 17.52 18.60 10.5 10.6 10.8 11.0 11.2 11.4 11.6 11.8 86 88 2 13.53 14.49 15.48 16.50 17.55 18.63 10.5 10.7 10.9 11.1 11.3 11.5 11.7 11.9 88 0 13.54 14.50 15.49 16.51 17.57 18.65 90 10.5 10.7 10.9 11.1 11.3 11.5 11.7 11.9

TABLE XXIV.

TABLE XXIII.

Logarithms of the Earth's Radii, in each Parallel of Latitude; the Equatorial Radius being Unity, and Compression 350.

Angles of the Vertical with the Radius; or Reduction of the Latitude, in each Parallel, the Compression being 300.

| Lat. Log. R C C C C C C C C C C C C C C C C C C | | | - 80 | | | | 1.0 | | | | | | 1/2 | | K-9-10 | | |
|---|------|--------------|-------------------|------|--------|-----|------|-----|-------|------|-----|-------|---------|--------|--------|------|-----|
| 0° 0.0000000 30° 9.9996402 60° 9.9989151 0 0 0.0 30 9.55.4 60 9.57.4 1 9.99999953 31 96181 61 88932 1 0 24.0 31 10 7.2 61 9.45.1 2 9982 32 95957 62 88720 2 0 47.9 32 10 18.1 62 932.0 3 9960 33 95728 63 88512 3 11.18 33 10 28.3 63 918.3 4 9930 34 95496 64 88308 4 1 35.5 34 10 37.8 64 9 3.8 6 9843 36 95023 66 89118 5 15.92 35 10 46.4 65 48.7 7 9786 37 94781 67 87732 7 24.61 37 </td <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td>4.7</td> <td>100</td> <td>Lat.</td> <td>Re</td> <td>educ.</td> <td>Lat.</td> <td>Reduc.</td> <td>Lat.</td> <td>Redu</td> <td>c.</td> | | | | | | | | 4.7 | 100 | Lat. | Re | educ. | Lat. | Reduc. | Lat. | Redu | c. |
| 0° 0.0000000 30° 9.9996402 60° 9.9999151 0 0 0.0 30 9.55.4 60 9.57.4 1 9.9999995 31 96181 61 88932 1 0.24.0 31 10 7.2 61 9.45.1 2 9.982 32 95957 62 88720 2 0.47.9 32 10 18.1 62 9.32.0 3 9.960 33 95728 63 88512 3 1 1.18.3 10 28.3 918.3 9.2 3 11.18.3 10 28.3 918.3 9.2 3 11.18.3 10 28.3 9.2 3 11.18.4 64 9.3.8 1 7.7 86 6 9.2 2.7 36 10 54.3 66 82.9 7 9.766 37 9.4781 67 87.752 8 3 9.2 38 11 7.7 68 7.596 6 | Lat. | Log. | R | Lat. | Log. | R | Lat. | Lo | g. R | | | - 1 | Union - | | 1 | - | |
| 1 9.9999995 31 96181 61 \$8932 1 0 24.0 31 10 7.2 61 9 45.1 2 9982 32 95957 62 88720 2 0 47.9 32 10 18.1 62 9 32.0 3 9960 33 95786 63 88512 3 1 1.8 33 10 28.3 63 9 3.8 6 9890 35 955261 65 88111 5 159.2 35 10 46.4 65 848.7 6 9843 36 95023 66 87918 6 2 22.7 36 10 54.3 66 832.9 7 9766 37 947811 67 87732 7 2 46.1 37 11 1.4 67 81.6 6 2 22.7 36 10 54.3 66 832.9 | | | | | - | | - | | 110 | 0 | 1 | " | 0 | , " | 0 | | |
| 2 9982 32 95957 62 88720 2 0 47.9 32 10 18.1 62 9 32.0 3 9960 33 95728 63 88512 3 1 11.8 33 10 28.3 63 9 18.3 4 9930 34 95196 64 88305 4 1 35.5 34 10 37.8 64 9 3.8 6 9890 35 95261 65 88111 5 1 59.2 35 10 46.4 65 48.7 6 9943 36 95023 66 87918 6 2 22.7 36 10 54.3 66 832.9 7 9786 37 94781 67 87732 7 2 46.1 37 11 1.4 67 8 16.6 8 9721 38 94537 68 87552 8 3 9.2 38 11 7.7 68 7 59.6 9 9648 39 94291 | 00 | 0.0000 | 0000 | 30° | 9.9996 | 102 | | | | | 0 | 0.0 | | | | | |
| 3 9960 33 95728 63 88512 3 1 11.8 33 10 28.3 63 9 18.3 4 9930 34 95496 64 88308 4 1 35.5 34 10 37.8 64 9 3.8 65 9890 35 95261 65 88111 5 1 59.2 35 10 46.4 65 8 48.7 7 9786 37 94781 67 87732 7 2 46.1 37 11 1.4 67 8 16.6 8 9721 38 94537 68 87552 8 3 9.2 38 11 7.7 68 7 59.6 9 9648 39 94291 69 87378 9 3 32.1 39 11 13.2 69 7 42.0 10 9566 40 94044 70 87210 10 3 54.8 40 11 17.9 70 7 23.8 11 9.999747 41 9.9993794 71 9.9987050 11 4 17.2 41 11 21.7 71 7 5.1 12 9379 42 93543 72 86896 12 4 39.3 42 11 24.7 72 6 45.9 13 9273 43 93291 73 86750 13 5 1.0 43 11 26.9 73 6 26.2 14 9158 44 93038 74 86611 14 5 22.4 44 11 28.2 74 6 6.0 15 9037 45 92786 75 86479 15 5 43.4 45 11 28.7 75 5 45.4 16 8908 46 92533 76 86356 16 6 3.9 46 11 28.4 76 5 24.3 17 8771 47 92280 77 86240 17 6 24.1 47 11 27.3 77 5 2.8 18 8627 48 92028 78 86131 18 6 43.7 48 11 25.2 78 4 41.0 19 8476 49 91776 79 86031 19 7 2.9 49 11 22.3 79 4 18.8 20 8318 50 91525 80 85940 20 7 21.6 50 11 18.6 80 3 56.3 21 9.9998153 51 9.9991277 81 9.9985857 21 7 39.7 51 11 14.1 81 3 33.5 22 7983 52 91030 82 85782 22 7 57.3 52 11 8.8 82 3 10.4 23 7805 53 90785 83 85716 25 846.4 55 10 47.9 85 2 0.0 26 7236 56 90065 86 85500 25 846.4 55 10 47.9 85 2 0.0 26 7236 56 90065 86 85570 26 9 1.6 56 10 39.4 86 1 36.2 27 7035 57 89831 87 85539 27 9 16.1 57 10 30.0 87 1 12.8 28 6629 58 89600 88 85517 28 9 29.9 58 10 19.9 88 0 48.2 29 6618 59 89374 89 85504 29 9 43.0 59 10 9.0 89 0 24.1 | 1 | 9.9999 | 995 | 31 | 96 | 181 | | 1 | 88932 | 1 | 0 | 24.0 | | | | | |
| 4 9930 34 95496 64 8830S 4 1 35.5 34 10 37.8 64 9 3.8 6 9890 35 95261 65 88111 5 1 59.2 35 10 46.4 65 8 48.7 7 9786 37 94781 67 87732 7 2 46.1 37 11 1.4 67 816.6 8 9721 38 94537 68 87552 8 3 9.2 38 11 7.7 68 7 59.6 9 9648 39 94291 69 87378 9 3 32.1 39 11 13.2 69 7 42.0 10 9566 40 94044 70 87210 10 3 54.8 40 11 17.9 70 7 23.8 11 9.9999477 41 9. | | 9 | 982 | | 1 | | | | | | 0 | | | | | | |
| 6 9890 35 95261 65 88111 5 1 59.2 35 10 46.4 65 8 48.7 6 9843 36 95023 66 87918 6 2 22.7 36 10 54.3 66 8 32.9 7 9766 37 94781 67 87732 7 2 46.1 37 11 1.4 67 8 16.6 8 9721 38 94537 68 87552 8 3 9.2 38 11 7.7 68 7 59.6 9 9648 39 94291 69 87378 9 3 32.1 39 11 1.3.2 69 7 42.0 10 9566 40 94044 70 87210 10 3 54.8 40 11 17.9 70 7 23.8 11 9.9999477 41 9.9987050 11 4 1 | 3 | 9 | 960 | 33 | | | | | | 3 | 1 | | | | | | - |
| 6 9843 36 95023 66 87918 6 2 22.7 36 10 54.3 66 8 32.9 7 9786 37 94781 67 87732 7 2 46.1 37 11 1.4 67 8 16.6 8 9721 38 94537 68 87552 8 3 9.2 38 11 7.7 68 7 59.6 10 9566 40 94044 70 87210 10 3 54.8 40 11 17.9 70 7 23.8 11 9.9999477 41 9.9993794 71 9.9987050 11 4 17.2 41 11 21.7 71 7 5.1 12 9379 42 93543 72 86896 12 4 39.3 42 11 24.7 72 6 45.9 13 9273 43 93291 73 86750 13 5 1.0 43 11 26.9 73 6 26.2 14 9158 44 93036 74 86611 14 5 22.4 44 11 28.2 74 6 6.0 15 9037 45 92786 75 86479 15 5 43.4 45 11 28.7 75 5 45.4 16 8909 46 92533 76 86356 16 6 3.9 46 11 28.4 76 5 24.3 17 8171 47 92280 77 86240 17 6 24.1 47 11 27.3 77 5 2 24.3 17 8171 47 92280 77 86240 17 6 24.1 47 11 27.3 77 5 2 24.3 19 8476 49 91776 79 86031 19 7 2.9 49 11 22.3 79 4 18.8 20 8318 50 91525 80 85940 20 7 21.6 50 11 18.6 80 3 56.3 21 9.9998153 51 9.9991277 81 9.9985857 21 7 39.7 51 11 14.1 81 3 33.5 22 7983 52 91030 82 85782 22 757.3 52 11 8.8 82 3 10.4 24 7621 54 90542 84 85659 24 8 30.7 54 10.6 56 10 39.4 86 1 36.2 27 7035 57 89831 87 85539 27 9 16.1 57 10 30.0 87 1 12.8 6829 58 89600 88 85510 29 9 43.0 59 10 9.0 89 0 24.1 29 6618 59 89374 89 85504 29 9 43.0 59 10 9.0 89 0 24.1 | | | - | | | | - | | | | - | | | | | - | |
| 7 9786 37 94781 67 87732 7 2 46.1 37 11 1.4 67 8 16.6 8 9721 38 94537 68 87552 8 3 9.2 38 11 7.7 68 7 59.6 9 9648 39 94291 69 87378 9 3 32.1 39 11 13.2 69 7 42.0 10 9566 40 94044 70 87210 10 3 54.8 40 11 17.9 70 7 23.8 11 9.9999477 41 9.9993704 71 9.9987050 11 4 17.2 41 11 21.7 71 7 5.1 12 9379 42 93543 72 86896 12 4 39.3 42 11 24.7 72 6 45.9 13 9273 43 93291 73 86750 13 5 1.0 43 11 26.9 73 6 26.2 14 9158 44 93038 74 86611 14 5 22.4 44 11 28.2 74 6 6.0 15 9037 45 92786 75 86479 15 5 43.4 45 11 28.7 75 5 45.4 16 8908 46 92533 76 86356 16 6 3.9 46 11 28.4 76 5 24.3 17 8771 47 92280 77 86240 17 6 24.1 47 11 27.3 77 5 2.8 18 8627 48 92028 78 86131 18 6 43.7 48 11 25.2 78 4 41.0 19 8476 49 91776 79 86031 19 7 2.9 49 11 22.3 79 4 18.8 20 8318 50 91525 80 85940 20 7 21.6 50 11 18.6 80 3 56.3 24 9.9998153 51 9.9991277 81 9.99885857 21 7 39.7 51 11 14.1 81 3 33.5 22 7983 52 91030 82 85782 22 7 57.3 52 11 8.8 82 3 10.4 23 7805 53 90785 83 85716 23 8 14.2 53 11 2.6 83 2 47.2 24 7621 54 90542 84 86569 24 8 30.7 54 10 55.7 84 2 23.7 24 7621 54 90542 84 86569 24 8 30.7 54 10 55.7 84 2 23.7 7035 57 89831 87 85539 27 9 16.1 57 10 30.0 87 1 12.8 28 6629 58 89600 88 85517 28 9 9.9 43.0 59 10 9.0 89 0 24.1 29 6618 59 89374 89 85504 29 9 43.0 59 10 9.0 89 0 24.1 | | | | | 7 | | | 1 | | | | | | | | | |
| 6 9721 38 94537 68 87552 8 3 9.2 38 11 7.7 68 7 59.6 9 9648 39 94291 69 87378 9 3 32.1 39 11 13.2 69 7 42.0 10 95666 40 94044 70 87210 10 3 54.8 40 11 17.9 70 7 23.8 11 9.9999477 41 9.9993794 71 9.9987050 11 4 17.2 41 11 21.7 71 7 7.1 12 9379 42 93543 72 868960 12 4 39.3 42 11 24.7 72 6 45.9 13 9273 43 93291 73 86750 13 5 1.0 43 11 26.7 72 6 45.9 14 9158 | | | | | | | | | | | | | | | | | - 1 |
| 9 9648 39 94291 69 87378 9 3 32.1 39 11 13.2 69 7 42.0 10 9566 40 94044 70 87210 10 3 54.8 40 11 17.9 70 7 23.8 11 9.9999477 41 9.9993794 71 9.9987050 11 4 17.2 41 11 21.7 71 7 5.1 12 9379 42 93543 72 86896 12 4 39.3 42 11 24.7 72 6 45.9 13 9273 43 93291 73 86750 13 5 1.0 43 11 26.9 73 6 26.2 14 9158 44 93038 74 86611 14 5 22.4 44 11 28.2 74 6 6.0 15 9037 45 92786 75 86479 15 5 43.4 45 11 28.7 75 5 45.4 16 8909 46 92533 76 86356 16 6 3.9 46 11 28.7 75 5 45.4 16 8909 46 92533 76 86356 16 6 3.9 46 11 28.4 76 5 24.3 17 8771 47 92280 77 86240 17 6 24.1 47 11 27.3 77 5 2.8 18 8627 48 92028 78 86131 18 6 43.7 48 11 25.2 78 4 41.0 19 8476 49 91776 79 86031 19 7 2.9 49 11 22.3 79 4 18.8 19 8476 49 91776 79 86031 19 7 2.9 49 11 22.3 79 4 18.8 19 9.998153 51 9.9991277 81 9.9985557 21 7 39.7 51 11 14.1 81 3 33.5 22 7983 52 91030 82 85782 22 757.3 52 11 8.8 82 3 10.4 24 7621 54 90542 84 85659 24 8 30.7 54 10 55.7 84 2 23.7 24 7621 54 90542 84 85659 24 8 30.7 54 10 55.7 84 2 23.7 7035 57 89831 87 85539 27 9 16.1 57 10 30.0 87 1 12.2 86 6829 58 89600 88 85517 28 9 29.9 58 10 19.9 88 0 48.2 9 6618 59 89374 89 85504 29 9 43.0 59 10 9.0 89 0 24.1 | | CANAL STREET | COLUMN TWO IS NOT | | | | - | | | | | | | | | | |
| 10 9566 40 94044 70 87210 10 3 54.8 40 11 17.9 70 7 23.8 11 9.9999477 41 9.9993794 71 9.9987050 11 4 17.2 41 11 21.7 71 7 5.1 12 9379 42 93543 72 86896 12 4 39.3 42 11 24.7 72 6 45.9 13 9273 43 93291 73 86750 13 5 1.0 43 11 26.9 73 6 26.2 14 9158 44 9303s 74 86611 14 5 22.4 44 11 28.7 75 6 6.0 15 9037 45 92786 75 86479 15 5 43.4 45 11 28.7 75 5 45.4 16 8909 46 92533 76 86346 16 6 3.9 46 11 28.4 76 5 24.3 17 8771 47 92298 | | | | | | | - | | | | _ | | | | | | |
| 11 9.9999477 41 9.9993794 71 9.9987050 11 4 17.2 41 11 21.7 71 7 5.1 12 9379 42 93543 72 86896 12 4 39.3 42 11 24.7 72 6 45.9 13 9273 43 93291 73 86750 13 5 1.0 43 11 26.9 73 6 26.2 14 9158 44 93038 74 86611 14 5 22.4 44 11 28.7 75 5 45.4 44 11 28.7 75 5 45.4 44 11 28.7 75 5 45.4 44 11 28.7 75 5 45.4 44 11 28.7 75 5 45.4 14 11 28.7 75 5 45.4 11 12.7 71 5 24.3 | | _ | - | _ | | | - | | | | _ | | | | | | |
| 12 9379 42 93543 72 86896 12 4 39.3 42 11 24.7 72 6 45.9 13 9273 43 93291 73 86750 13 5 1.0 43 11 24.7 72 6 45.9 14 9158 44 93036 74 86611 14 5 22.4 44 11 28.2 74 6 60.2 15 9037 45 92786 75 86479 15 5 43.4 45 11 28.7 75 5 45.4 16 8908 46 92533 76 86356 16 6 3.9 46 11 28.4 76 5 24.3 17 8771 47 92280 77 86240 17 6 24.1 47 11 27.3 77 5 28.3 19 9476 49 91776 79 86031 18 6 43.7 48 11 25.2 78 4 41.0 20 8318 50 915 | 10 | _ 9 | 566 | 40 | | | | - | | 10 | 3 | - | 40 | | | | _ |
| 13 9273 43 93291 73 86750 13 5 1.0 43 11 26.9 73 6 26.2 14 9158 44 93035 74 86611 14 5 22.4 44 11 28.2 74 6 6.0 15 9037 45 92786 75 86479 15 5 43.4 45 11 28.7 75 5 45.4 16 8908 46 92533 76 86356 16 6 3.9 44 11 28.4 76 5 24.3 17 8771 47 92280 77 86240 17 6 24.1 47 11 27.3 77 5 2.8 18 8627 48 92028 78 86131 18 6 43.7 48 11 25.2 78 4 41.0 19 8476 <td< td=""><td></td><td>9.9999</td><td>1477</td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td>4</td><td></td><td></td><td></td><td></td><td></td><td></td></td<> | | 9.9999 | 1477 | | | | | | | | 4 | | | | | | |
| 14 9158 44 93036 74 86611 14 5 22.4 44 11 28.2 74 6 6.0 15 9037 45 92786 75 86479 15 5 43.4 45 11 28.7 75 5 45.4 16 890% 46 92533 76 86356 16 6 3.9 46 11 28.4 76 5 24.3 17 8771 47 92290 77 86240 17 6 24.1 47 11 27.3 77 5 28.3 18 8627 48 92028 78 86131 18 6 43.7 48 11 25.2 78 4 41.0 19 8476 49 91776 79 86031 19 7 2.9 49 11 22.3 79 4 18.8 20 8318 50 91525 80 85940 20 7 21.6 50 11 18.6 80 3 56.3 21 7.993153 51 | | 9 | 379 | | | | | | | - 10 | 4 | | | | | | |
| 15 9037 45 92786 75 86479 15 5 43.4 48 11 28.7 75 5 45.4 16 8909 46 92533 76 86356 16 6 3.9 46 11 28.4 76 5 24.3 17 8771 47 92230 77 86240 17 6 24.1 47 11 27.3 77 5 28.4 18 8627 48 92028 78 86131 18 6 43.7 48 11 27.3 77 5 28.4 19 8476 49 91776 79 86031 19 7 2.9 49 11 22.3 79 4 18.8 20 8318 50 91525 80 85940 20 7 21.6 50 11 18.6 80 3 56.3 21 9.9998153 51 9.9991277 81 9.9985857 21 7 39.7 51 11 14.1 81 3 33.5 22 7983 52 | 13 | 9 | 273 | 43 | | | | 1 | | 13 | | | | | | | |
| 16 8908 46 92533 76 86356 16 6 3.9 46 11 28.4 76 5 24.3 17 8771 47 92230 77 86240 17 6 24.1 47 11 27.3 77 5 2.8 18 8627 48 92028 78 86131 18 6 43.7 48 11 25.2 78 4 41.0 19 8476 49 91776 79 86031 19 7 2.9 49 11 25.2 79 4 41.0 20 8318 50 91525 80 85940 20 7 21.6 50 11 18.6 80 3 56.3 21 9.9998153 51 9.9991277 81 9.9985857 21 7 39.7 51 11 14.1 81 3 35.5 22 7983 52 91030 82 85782 22 7 57.3 52 11 8.8 82 3 10.4 24 7621 54 | | | | - | | | | | | | 1 | | | | | | |
| 17 8771 47 92280 77 86240 17 6 24.1 47 11 27.3 77 5 2.8 18 8627 48 92028 78 86131 18 6 43.7 48 11 25.2 78 4 41.0 19 8476 49 91776 79 86031 19 7 2.9 49 11 22.3 79 4 18.8 20 8318 50 91525 80 85940 2 7 21.6 50 11 18.6 80 3 56.3 21 9.998153 51 9.9991277 81 9.9985857 21 7 39.7 51 11 14.1 81 3 33.5 63.3 22 7983 52 91030 82 85782 22 7 57.3 52 11 8.8 82 3 10.4 23 7805 53 90785 83 85716 23 8 14.2 53 11 2.6 83 2 47.2 24 7621 | | | | | | | | | | | - | | | | | | |
| 18 6627 48 92028 78 86131 18 6 43.7 48 11 25.2 78 4 41.0 19 8476 49 91776 79 86031 19 7 2.9 49 11 22.3 79 4 18.8 20 8318 50 91525 80 85940 20 7 21.6 50 11 18.6 80 3 56.3 21 9.9998153 51 9.9991277 81 9.9985857 21 7 39.7 51 11 14.1 81 3 33.5 22 7983 52 91030 82 85782 22 7 57.3 52 11 18.8 82 3 10.4 23 7805 53 90785 93 85716 23 8 14.2 53 11 2.6 83 2 47.2 24 7621 54 90542 84 85659 24 8 30.7 54 10 55.7 84 2 23.7 25 <t< td=""><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td>_</td><td>1</td><td></td><td></td><td></td><td></td><td></td><td>-</td></t<> | | | | | | | | | | _ | 1 | | | | | | - |
| 19 8476 49 91776 79 86031 19 7 2.9 49 11 22.3 79 4 18.8 20 8318 50 91525 80 85940 20 7 21.6 50 11 18.6 80 3 56.3 21 9.9998153 51 9.9991277 81 9.9985557 21 7 39.7 51 11 14.1 81 3 33.5 22 7983 52 91030 82 85782 22 7 57.3 52 11 8.8 82 3 10.4 23 7805 53 90785 83 85716 23 8 14.2 53 11 2.6 83 2 47.2 24 7621 54 90542 84 85659 24 8 30.7 54 10 55.7 84 2 23.7 25 7431 55 90302 85 85610 </td <td></td> <td>_</td> <td></td> <td>_</td> <td></td> <td></td> <td></td> <td></td> | | | | | | | | | | | _ | | _ | | | | |
| 20 8318 50 91525 80 85940 20 7 21.6 50 11 18.6 80 3 56.3 21 9.9998153 51 9.9991277 81 9.9985857 21 7 39.7 51 11 14.1 81 3 33.5 22 7983 52 91030 82 85782 22 7 57.3 52 11 8.8 82 3 10.4 23 7805 53 90785 93 85716 23 8 14.2 53 11 2.6 83 2 47.2 24 7621 54 90542 84 85659 24 8 30.7 54 10 55.7 84 2 23.7 25 7431 55 90302 85 85610 25 8 46.4 55 10 47.9 85 2 0.0 26 7236 56 90065 86 85570 26 9 1.6 56 10 39.4 86 1 36.2 27 7035 57 | | | | | 1 | | | | | | | | | | | 1 | - |
| 21 9.9998153 51 9.9991277 81 9.9985657 21 7 39.7 51 11 14.1 81 3 33.5 22 7983 52 91030 82 85782 22 7 57.3 52 11 8.8 82 3 10.4 23 7805 53 90785 93 85716 23 8 14.2 53 11 2.6 83 2 47.2 24 7621 54 90542 84 85659 24 8 30.7 54 10 55.7 84 2 23.7 25 7431 55 90302 85 85610 25 8 46.4 55 10 47.9 85 2 0.0 26 7236 56 90065 86 85570 26 9 1.6 56 10 39.4 86 1 36.2 27 7035 57 89831 87 85539 27 9 16.1 57 10 30.0 87 1 12.3 28 6829 58 89600 88 85517 28 9 29.9 58 10 19.9 89 0 48.2 29 6618 59 89374 89 85504 29 9 43.0 59 10 9.0 89 | | | | _ | | | - | | | | | | | | | | |
| 22 7983 52 91030 82 85782 22 7 57.3 52 11 8.8 82 3 10.4 23 7805 53 90785 93 85716 23 8 14.2 53 11 2.6 83 2 47.2 24 7621 54 90542 84 85659 24 8 30.7 54 10 55.7 84 2 23.7 25 7431 55 90302 85 85610 25 8 46.4 55 10 47.9 85 2 0.0 26 7236 56 90065 86 85570 26 9 1.6 56 10 39.4 86 1 36.2 27 7035 57 89831 87 85539 27 9 16.1 57 10 30.0 87 1 12.3 28 6829 58 89600 88 85517 28 9 29.9 58 10 19.9 88 0 48.2 29 6618 59 89374 89 85504 29 9 43.0 59 10 9.0 89 0 24.1 | 50 | - | - | | | - | | | | | 7 | | | | | | - |
| 23 7805 53 90785 83 85716 23 8 14.2 53 11 2.6 83 2 47.2 24 7621 54 90542 84 85659 24 8 30.7 54 10 55.7 84 2 23.7 25 7431 55 90302 85 85610 25 8 46.4 55 10 47.9 85 2 0.0 26 7236 56 90065 86 85570 26 9 1.6 56 10 39.4 86 1 36.2 27 7035 57 89831 87 85539 27 9 16.1 57 10 30.0 87 1 12.3 28 6829 58 89600 88 85517 28 9 29.9 58 10 19.9 88 0 48.2 29 6618 59 89374 89 85504 29 9 43.0 59 10 9.0 89 0 24.1 | | | | | 1 | | | | | | | | | | | | |
| 24 7621 54 90542 84 85659 24 8 30.7 54 10 55.7 84 2 23.7 25 7431 55 90302 85 85610 25 8 46.4 55 10 47.9 85 2 0.0 26 7236 56 90065 86 85570 26 9 1.6 56 10 39.4 86 1 36.2 27 7035 57 89831 87 85539 27 9 16.1 57 10 30.0 87 1 12.3 28 6629 58 89600 88 85517 28 9 29.9 58 10 19.9 88 0 48.2 29 6618 59 89374 89 85504 29 9 43.0 59 10 9.0 89 0 24.1 | | | | | | | - | | | | | | | | | | |
| 25 7431 55 90302 85 85610 25 8 46.4 55 10 47.9 85 2 0.0 26 7236 56 90065 86 85570 26 9 1.6 56 10 39.4 86 1 36.2 27 7035 57 89831 87 85539 27 9 16.1 57 10 30.0 87 1 12.3 28 6829 58 89600 88 85517 28 9 29.9 58 10 19.9 88 0 48.2 29 6618 59 89374 89 85504 29 9 43.0 59 10 9.0 89 0 24.1 | | | | | | | | | | | - | | | | | 1 | |
| 26 7236 56 90065 86 85570 26 9 1.6 56 10 39.4 86 1 36.2 27 7035 57 89831 87 85539 27 9 16.1 57 10 30.0 87 1 12.3 28 6829 58 89600 88 85517 28 9 29.9 58 10 19.9 88 0 48.2 29 6618 59 89374 89 85504 29 9 43.0 59 10 9.0 89 0 24.1 | | | | | | | | | | | 1 | | | | 4 | | |
| 27 7035 57 89831 87 85539 27 9 16.1 57 10 30.0 87 1 12.3 28 6829 58 89600 88 85517 28 9 29.9 58 10 19.9 88 0 48.2 29 6618 59 89374 89 85504 29 9 43.0 59 10 9.0 89 0 24.1 | | | | | | | | | | | _ | | | | | | |
| 28 6829 58 89600 88 85517 28 9 29.9 58 10 19.9 88 0 48.2 29 6618 59 89374 89 85504 29 9 43.0 59 10 9.0 89 0 24.1 | | | | | | | | | | | 1 - | | | | | | |
| 29 6618 59 89374 89 85504 29 9 43.0 59 10 9.0 89 0 24.1 | | | | | | | | | | | - | | | | | | _ |
| | | | | - | | | | | | | 1 - | | | | | | |
| 30 0402 00 89151 90 85499 30 9 55 4 00 9 57.4 90 0 0.0 | | | | | | | | | | | 1 - | | | | | | |
| | 30 | 1 6 | 102 | 00 | 89 | 191 | 90 | | 00199 | 30 | 9 | 00 4 | 00 | 9 51.4 | 1 90 | 10 0 | 1.0 |

TABLE XXV.

For determining the Latitude, at any time, by the Pole Star.

| 0 | M | N | 0 | M | N | 0 | M | N | 0 | M | N | 0 | M | N | 0 | M | N |
|------|------|------|------|-------|------|------|-------|------|------|-------|------|------|-------|------|------|-------|------|
| h.m. | " | " | h.m. | " | " | h.m. | 11 | 11 | h.m. | 11 | " | h.m. | " | 11 | h.m. | 11 | " |
| 0 0 | 0.00 | 0.00 | 1 0 | 5.85 | 0.11 | 5 0 | 21.82 | 0.37 | 3 0 | 43.63 | 0.60 | 4 0 | 65.45 | 0.63 | 5 0 | 81.42 | 0.41 |
| 10 | 0.17 | 0.00 | 10 | 7.89 | 0.14 | 10 | 25.19 | 0.41 | 10 | 47.44 | 0.62 | 10 | 68.66 | 0.61 | 10 | 83.18 | 0.35 |
| 20 | 0.66 | 0 01 | 20 | 10.20 | 0.19 | 20 | 28.71 | 0.46 | 20 | 51.21 | 0.64 | 20 | 71.68 | 0.59 | 20 | 84.64 | 0.28 |
| 30 | 1.49 | 0 03 | 30 | 12.78 | 0.23 | 30 | 32.34 | 0.50 | 30 | 54.93 | 0.65 | 30 | 74.49 | 0.55 | 30 | 85.78 | 0.22 |
| 40 | 2.63 | 0.05 | 40 | 15.59 | 0.27 | 40 | 36.06 | 0.53 | 40 | 58.56 | 0.65 | 40 | 77.06 | 0.51 | 40 | 86.60 | 0.15 |
| 50 | 4.09 | 0.08 | 50 | 18.61 | 0.32 | 50 | 39.83 | 0.57 | 50 | 62.07 | 0.64 | 50 | 79.38 | 0.46 | 50 | 87.10 | 0.07 |
| 1 0 | 5.85 | 0.11 | 3 0 | 21.82 | 0.37 | 3 0 | 43.63 | 0.60 | 4 0 | 65 45 | 0.63 | 5 0 | 81.42 | 0.41 | 6 0 | 87.26 | 0.00 |

 $\psi=Z+p\cos t-M$ cotan. Z+N; where ψ is = the Latitude; Z= the Zenith Distance; $p=1^{\circ}40'$, or 100'; t= the Horary Angle; $\theta=t$ in the first Quadrant; $=12^{\circ}-t$ in the second; $=t-12^{\circ}$ in the third; and $=24^{\circ}-t$ in the fourth; M and N being the Tabular Quantities. The quantity M is $=\frac{1}{2}p^2\sin^2 t$, and is always positive; but the quantity $N=\frac{1}{3}p^3\sin^2 t$, exceed and third Quadrants of t. When p (the Polar Distance) augments or diminishes 1', the Tabular Quantity must also be augmented or diminished by 0.02M; and for any other quantity of variation in the same proportion.

TABLE XXVI.

To find the Augmentation of the Moon's Semidiameter by the Altitude of the Nonagesimal, and the Apparent Distance of the Moon therefrom.

| | | ART I. | | | PART | r II. | PART III. | | | | | | | | |
|------------|--------------|--------------|--------------|-----------|--|----------------|---|---------|---------------------|----------------|------|------|------|------|--|
| Alt. nor | a. + ap | p. dis. N | foon fr. | nona. | Aggre- gate of | Cor. | True Lat. of Parallax of the Moon in Lat. | | | | | | | it. | |
| Alt. noi | 0. VI. | p. dis. M | II. VIII. | nona. | No from | Cor. | the | 0' | 10' | 20' | 30' | 40' | 50' | 60' | |
| | + - | + - | + - | | Part I. | + | Moon. | | _ | _ | | _ | _ | - | |
| 00 | 0".00 | 4".10 | 7".10 | 30° 29 | 1" | 0".00 | S. Lat. | " | " | " | " | 11 | " | 11- | |
| 1 2 | 0.14 | 4.22 | 7.23 | 28 | 3 | 0.00 | 6° 0′ | 0.00 | 0.29 | 0.59 | 0.90 | 1.22 | 1.54 | 1.88 | |
| 3 | 0.43 | 4.46 | 7.30 | 27. | 4 | 0.02 | 5 40 | 0.00 | 0.27 | 0.56 | 0.85 | 1.16 | 1.46 | 1.78 | |
| 4 . | 0.57 | 4.58 | 7.36 | 26 | 5 | 0.03 | 5 20 | 0 00 | 0.26 | 0.53 | 0.80 | 1.09 | 1.38 | 1.69 | |
| 5 | 0.72 | 4.70 | 7.42 | 25 24 | 6 | 0.04 | 5 0 | 0.00 | 0.24 | 0.49 | 0.76 | 1.02 | 1.30 | 1.59 | |
| 7 | 1.00 | 4.93 | 7.54 | 23 | 8 | 0.06 | 4 40 | | | 0.46 | | | | | |
| 8 | 1.14 | 5.01 | 7.59 | 55 | 8.5 | 0.07 | 4 20 4 0 | | | 0.43 0.40 | | | | 1.40 | |
| 9 | 1.28 | 5.16 | 7.65 | 21 | 9.0 | 0.08 | | | | | | | _ | - | |
| 10 11 | 1.42 | 5.27 5.38 | 7.70 7.74 | 20 | 9.5 | 0.09 | 3 40 | | | 0.37 0.33 | | | | | |
| 12 | 1.70 | 5.49 | 7.79 | 18 | 10.5 | 0.10 | 3 0 | 0.00 | | | | | | | |
| 13 | 1.84 | 5.59 | 7.83 | 17 | 11.0 | 0.12 | 2 40 | 0.00 | 0.13 | 0.27 | 0.42 | 0.58 | 0.74 | 0.91 | |
| 14 15 | 1.98 2.12 | 5.70 | 7.87 | 16 15 | 11.5 | 0.13 | 2 20 | | | 0.24 | | | | | |
| 16 | 2.12 | 5.80 | 7.92 | 15 | 12.0 | 0.14 | 2 0 | | $\frac{0.10}{0.08}$ | 0.21 | 0.33 | 0.45 | 0.58 | 0.72 | |
| 17 | 2.39 | 5.99 | 7.98 | 13 | 12.7 | 0.16 | 1 40 | | | 0.17 | | | | | |
| 18 | 2.53 | 6.09 | 8.02 | 12 | 13.0 | 0.17 | 1 20 | | | 0.14 | | | | | |
| 19 | 2.67 | 6.18 | 8.04 | 11 | 13.3 | 0.18 | 1 0 | | | 0.11 | | - | | - | |
| 20 21 | 2.80 2.94 | 6.27 | 8.06 | 10 | 13.7 | 0.19 | 0 50 | | | 0.09 | | | | | |
| 22 | 3.07 | 6.45 | 8.11 | 8 | 14.3 | 0.21 | 0 40 | 0.00 | 0.03 | $0.08 \\ 0.06$ | 0.13 | 0.19 | 0.20 | 0.34 | |
| 23 | 3.20 | 6.54 | 8.13 | 7 | 14.7 | 0.22 | | - | - | | | | | | |
| 24 | 3.33 | 6.63 | 8.15 | 6 | 15.0 | 0.23 | 0 20 | | | 0.05 | | | | | |
| 25 | 3.46 | 6.71 | 8.16 | 5 | 15.3 15.7 | 0.24 | 0 0 | 0.00 | | 0.02 | | | | | |
| 27 | 3.72 | 6.87 | 8.18 | 3 | 16.0 | 0.26 | N. I. | 1 1 1 1 | - | | | 10.1 | | | |
| 28 | 3.85 | 6.95 | 8.19 | 2 | 16.3 | 0.27 | N. Lat. 0 10 | 0.00 | 0.01 | | | 0.09 | 0.06 | 0.10 | |
| 29 30 · | 3.97 | 7.02 | 8.19 | 0 | 16.7 | 0.28 | 0 10 | 0.00 | 0.01 | + | + | 0.03 | 0.00 | 0.10 | |
| - | + - | + - | + - | - | 1110 | 10.20 | 0 20 | 0.00 | 0.02 | 0.02 | 0.01 | + | 0.02 | 0.05 | |
| | XI. V. | | IX. III. | | | | | | | | | | + | | |
| | | PA | RT I | V. | | | 0 30 | | | 0.03 | | | | | |
| Sum of | | Semid | ameter | | Moon. | | 0 40 0 50 | | | 0.05 | | | | 0.05 | |
| preced. | | | word a | 15' | | 16' | | | - | | | - | | | |
| Equa- | 40" 3 | 0" 0" | 10" 2 | 0" 30 | 9" 40" 8 | 50" 0" | 1 0 | | | 0.08 | | | | | |
| " | " | " " | " | , , | - " | " " | 1 40 | | | 0.14 | | | | | |
| 1 | 0.17 0 | 15 0.13 | 0.100. | 08 0.0 | 06 0.04 0 | | 2 0 | 0.00 | 0.10 | 0.18 | 0.25 | 0.32 | 0.38 | 0.44 | |
| 2 | 0.38 0. | 29 0.25 | 0.21 0. | 17 0.1 | 2 0.08 0 | .04 0 | 2 20 | 0.00 | 0.11 | 0.21 | 0.30 | 0.39 | 0.46 | 0.53 | |
| 3 4 | | | | | 19 0.12 0 | | 2 40 | 0.00 | 0.13 | 0.24 | 0.35 | 0.45 | 0.54 | 0.63 | |
| 5 | | | | | 31 0.21 0 | | 3 0 | | | 0.27 | | | | | |
| 6 | | | | | 37 0.25 0 | | 3 20 | | | 0.30 | | | | | |
| 7 | 1.16 1. | 02 0.87 | 0.73 0. | 58 0.4 | 4 0.29 0 | .15 0 | | | | - | | | | | |
| 8 9 | | | | | 0.330 | | 4 0 4 20 | | | 0.37 | | | | | |
| 10 | | | | | $\begin{array}{c} 660.370 \\ 620.420 \end{array}$ | | 4 40 | | | 0.43 | | | | | |
| 11 | | | | | 0.46 0 | | 5 0 | - | | 0.46 | - | | - | | |
| 12 | 2.00 1. | 75 1.50 | 1.25 1. | 00 0.7 | 75 0.50 0 | .25 0 | 5 20 | 0.00 | 0.26 | 0.50 | 0.73 | 0 96 | 1.18 | 1.40 | |
| 13 14 | 2.16 1. | 89 1.62 | 1.35 1. | 08 0.8 | 31 0.54 0 | .27 0 | 5 40 | 0.00 | 0.27 | 0.53 | 0.78 | 1.02 | 1.26 | 1.49 | |
| 15 | 2.50 2 | 18 1.87 | 1.46 1. | 250.0 | $\begin{array}{c c} 37 & 0.58 & 0 \\ 0.62 & 0 \end{array}$ | .29 0 .31 0 | 6 0 | 0.00 | 0.29 | 0.56 | 0.83 | 1.09 | 1.34 | 1.59 | |
| - | | + + | - | + + | | + | | - | + | + | + | + | + | + | |
| | 20" | 10" 0" | | | 1 - 1 | 10" 0" | | 0' | 10' | 20' | 30' | 40' | 50' | 60' | |
| - | 1 | 7' | | | Pa | ralla | x of | the N | 100n | in La | at. | | | | |
| | | | | | - | | | | | | | | | | |

| ī | TABLE XXVII.—Equations of Second Differences for Twelve Hours. 93 | | | | | | | | | | | | | | | | | | | | |
|--------------------|---|------|---------------------------|---|-------|--------------|------------------|---------------------|-------|----------------|------------|---------|--------------------|--------------|------|--|--------------|-------|-------------------|----------|--------------|
| Time after Noon or | | | | | | | | Second Difference. | | | | | | | | | | | | | 1 |
| L | Mid | nigh | t. | 10' | _ | 20' | 30' | 1' | 2' | , , | 3' | 4' | , , | 5' | 6' | , , | 7' | 8 | // | - ! | 9' |
| h. | m. | h. | m. 0 | | 1 | 0.0 | | | | 0.00 | 0.0 | | 0.00 | 0.0 | | .00 | 0.0 | | 0.0 | 0 | 0.0 |
| 0 | 10 | 11 | 50 | | | | 0 12.3 | 0 0.4 | | .80 | 1.2 | | .60 | | | .50 | 2.9 | | 3.3 | | 3.7 |
| 0 | 20 | 11 | 40 | | | 16.2 | | | | .60 | 2.4 | | .20 | | | .90 | | | 5.5 | | 7.3 |
| 0 | 30 | 11 | 30 | | | 24.0 31.5 | - | $0 \ 1.2$ $0 \ 1.6$ | | .40 | 3.6 | | 80 | | | .20 | 8.4 | | 9.6 | | 10.8 14.2 |
| 0 | 50 | | 10 | | | 38.8 | | | | .90 | 5.8 | | .80 | 9.7 | 0 11 | - | 12 11 11 | | - | | 17.4 |
| Ī | 0 | 11 | 0 | 0 22. | 90 | 45.8 | 1 8.7 | 0 2.3 | | .60 | 6.9 | 0 9 | .20 | 11.5 | 0 13 | .80 | 16.0 | 0 18 | 3.3 | 0 | 20.6 |
| I | 10 | 10 | 50 | | | 52.7 | 1 19.0 | 0 2.6 | | 30 | 7.9 | 4000 | 1 - 1 - | 13.2 | 0 15 | 100 | 18.4 | | | | 23.7 |
| Ļ | 2 0 | 10 | 30 | 100 100 100 100 100 100 100 100 100 100 | | 59.3 5.6 | 1 28 9 1 38.4 | | | 0.60 | 8.9 9.8 | | .90 | 14.8 16.4 | | .80 | 20.7 | | | | 26.7 29.5 |
| î | 40 | 10 | 20 | | | 11.8 | 1 47.6 | 0 3.6 | 0 7 | .20 | 10.8 | | | 17.9 | | | 25.1 | 1 | | | 32.3 |
| 1 | 50 | 10 | 10 | | _ | 17.7 | 1 56.5 | - | | .80 | 11.6 | | 50 | 19.4 | - | 3.30 | 27.2 | - | - | - | 34.9 |
| 2 | 0 | 10 | | 0 41. | 100 | 23.3 | | | | .30 | 12.5 | | | 20.8 | | | 29.2 | 1 | | | 37.5 |
| 5 5 | 20 | 9 | 5 0 | | | 28.8 | | | | 3.9°0 0.4°0 | 13.3 | | .80 | 22.2 23.5 | | $\begin{array}{c c} .60 \\ .20 \\ \end{array}$ | 31.1 | | | | 39.9 42.3 |
| 5 | 30 | 9 | | 0 49. | . 1 - | 39.0 | 2 28.4 | 5 | | 0.90 | 14.8 | 1 1 1 1 | .80 | 24.7 | 0 29 | | 34.6 | | 9.6 | | 44.5 |
| 5 | 40 | 9 | 20 | | | 43.7 | | | | | 15.6 | | 0.70 | 25.9 | | | 36.3 | | | | 46.7 |
| 5 | 50 | 9 | 10 | | _ | 48.2 | | - | - | 30 | 16.2 | - | $\frac{.60}{0.50}$ | | 0 32 | - | 37.9 | - | | | 48.7 |
| 3 | 10 | 9 8 | 50 | | | 52.5 56.6 | | | 1 | .30 | 16.9 | | - | 28.1 | 0 33 | .80 | 39.4 | | | | 50.6 52.4 |
| 3 | 20 | 8 | | 1 0. | 55 | 0.4 | | 0 6.0 | 0 12 | 0,0.5 | 18.1 | 0 24 | .10 | 30.1 | 0 36 | .10 | | | | | 54.2 |
| 3 | 30 | 8 | 30 | | 0 2 | 4.0 | 3 5.9 | | | 2.4 0 | 18.6 | | | 31.0 | | | 43.4 | | 9.6 | | 55.8 |
| 3 | 40 50 | 8 | 20 | | 722 | 7.3 10.4 | | | | 2.7 0 3.0 0 | 19.1 | | | 31.8 | | .10 | 44.6 | | 0.9 | | 57.3 58.7 |
| 14 | 0 | 8 | 0 | | 72 | 13.3 | - | - | - | 3.3.0 | 20.0 | - | .70 | 33.3 | | 0.00 | 46.7 | - | 3.3 | - | 0.0 |
| 4 | 50 | 7 | 40 | 1 9. | 22 | 18.4 | 3 27.6 | 0 6.9 | 0 13 | 3.8,0 | 20.8 | 0 27 | .70 | 34.6 | 0 41 | .50 | 48.4 | 1 | 5.4 | | 2.3 |
| 1 | 40 | 7 | 20 | | 32 | 22.6 | | | 1 | | 21.4 | | | | | | 49.9 | | 7.0 | | 4.9 |
| 5 | 20 | 7 6 | 40 | 1 14 | | 25.8 28.2 | | | | | 21.9 | | - 1 | 36.5 | 1 | | 51.0 51.9 | 1 . | $\frac{8.3}{9.3}$ | 100 | 5.6 |
| 5 | 40 | 6 | | | 82 | 29.5 | | 0.7.5 | | | | | | | | | 15 | | 9.8 | | 7.3 |
| 6 | 0 | | 0 | 1 15 | 02 | 30.0 | 3 45 0 | 4 | | | 22.5 | | 0.0 | 37.5 | 0 45 | .00 | 52.5 | | 0.0 | | 7.5 |
| a | fter Mid | | n or | 10" | 20' | 1 30 | " 40" | 50" | Secon | d Di | fferen | ce. | 5" | 1 6" | 1 7" | 8" | 9" | 24 | h. ter | Ti | me |
| h | mid. | h. | m. | " | " | 11 | " | " | " | " | " | " | 11 | " | " | " | 11 | h. | m. | - | m. |
| 0 | 0 | | 0 | 0.0 | 0.0 | | | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0 | 0 | 24 | 0 |
| 0 | 20 | 11 | 50 40 | 0.1 | 0.5 | | | 0.3 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.1 | 0.1 | 0 | | 23 23 | |
| 0 | 30 | | 30 | 0.1 | 0.4 | | | 1.0 | 0.0 | 0.0 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 0.1 | 1 | 0 | 1 | |
| 0 | 40 | | 20 | 0.3 | 0.8 | | | 1.3 | 0.0 | 0.1 | 0.1 | 0.1 | 0.1 | 0.2 | 0.2 | 0.2 | 1 | 1 | | 22 | |
| 0 | 50 | 11 | 10 | 03 | 0.6 | - | _ | 1.6 | 0.0 | 0.1 | 0.1 | 0.1 | 0.2 | 0.2 | 0.2 | 0.3 | - | 1 | | 22 | |
| li | 10 | 11 | 50 | 0.4 | 0.8 | | 1 | 1.9 | 0.0 | 0.1 | 0.1 | 0.1 | 0.2 | 0.3 | 0.3 | 0.3 | | 2 2 | 90 | 22 | |
| i | 20 | | 40 | 0.5 | 1.0 | | | 2.5 | 0.0 | 0.1 | 0.1 | 0.2 | 0.2 | 0.3 | 0.3 | 0.4 | | 2 | | 21 | |
| 1 | 30 | | 30 | 0.5 | 1. | | | 2.7 | 0.0 | 0.1 | 0.2 | 0.2 | 0.3 | 0.3 | 0.4 | 0.4 | 1 | 3 | 0 | 21 | 0 |
| 1 | 40 50 | | 20 | 0.6 | 1.5 | | 1 | 3.0 | 0.1 | 0.1 | 0.2 | 0.2 | 0.3 | 0.4 | 0.4 | 0.5 | 1 . | 3 | | 20 | |
| 1 2 | 0 | 10 | 0 | 0.7 | 1.4 | | | 3.5 | 0.1 | 0.1 | 0.2 | 0.3 | 0.3 | 0.4 | 0.4 | 0.6 | - | 4 | - | 20 | |
| 2 | 10 | 9 | 50 | 0.7 | 1 | 5 2. | 2 3.0 | 3.7 | 0.1 | 0.1 | 0.2 | 0.3 | 0.4 | 0.4 | 0.5 | 0.6 | | 4 | 20 | 19 | 40 |
| 12 | 20 | 9 | 40 | 0.8 | 1.6 | _ | | 3.9 | 0.1 | 0.2 | 0.2 | 0.3 | 0.4 | 0.5 | 0.5 | 0.6 | 0.7 | 4 | - | 19 | |
| 2 | 30 | 9 9 | 20 | | 1.0 | | | 4.1 | 0.1 | 0.2 | | 0.3 | 0.4 | 0.5 | 0.6 | 0.7 | 0.7 | 5 | | 19 | 40 |
| 5 | 50 | 9 | | | 1.8 | | | 4.5 | 0.1 | 0.2 | | 0.3 | 0.4 | 0.5 | 0.6 | 0.7 | 0.8 | | 40 | | |
| 3 | 0 | 9 | 0 | 0.9 | 1.5 | 2. | 8 3.8 | 4.7 | 0.1 | 0.2 | | 0.4 | 0.5 | 0.6 | 0.7 | 0.7 | 0.8 | 6 | - | 18 | |
| 3 | 10 | | 50 | | 1.9 | | | 4.9 | 0.1 | 0.2 | | 0.4 | 0.5 | 0.6 | 0.7 | 0.8 | 0.9 | | | | 40 |
| 333 | 20 30 | | 40 30 | | 2.0 | | | 5.0 | 0.1 | 0.2 | | 0.4 | 0.5 | 0.6 | 0.7 | 0.8 | | 6 | 40 | 17 | |
| 3 | 40 | 8 | 20 | 1.1 | 2. | 1 3. | 2 4.2 | 5.3 | 0.1 | 0.2 | | 0.4 | 0.5 | 0.6 | 0.7 | 0.8 | 1.0 | 7 | 20 | 16 | 40 |
| 3 | 50 | - | and the local division in | - Western Street, | 2.5 | | | 5.4 | 0.1 | 0.2 | 0.3 | 0.4 | 0.5 | 0.6 | 0.8 | 0.9 | 1.0 | 7 | 40 | 16 | 20 |
| 4 | 0 | 8 | () | 1.1 | 2.5 | | | 5.6 | 0.1 | 0.2 | 0.3 | 0.4 | 0.6 | 0.7 | 0.8 | 0.9 | 1.0 | 8 | | 16 | |
| 44 | | | | | 2.3 | | | 5.8 | 0.1 | 0.2 | 0.3 | 0.5 | 0.6 | 0.7 | 0.8 | 0.9 | 1.0 | | | | 20 |
| 5 | 0 | 7 | 0 | 1.2 | 2. | 1 3. | 7 4.9 | 6.1 | 0.1 | 0.2 | 0.4 | 0.5 | 0.6 | 0.7 | 0.9 | 1.0 | 1.1 | 10 | 0 | 14 | 0 |
| 5 | 20 | | 40 | | 2. | | | 6.2 | 0.1 | 0.2 | 0.4 | 0.5 | 0.6 | 0.7 | 0.9 | 1.0 | 1.1 | | | | 20 |
| 5 | 40 | | 20 | | 2. | | | 6.2 | 0.1 | 0.2 | 0.4 | 0.5 | 0.6 | 0.7 | 0.9 | 1.0 | 1.1 | 11 12 | 20 | 12 | |
| 5 | U | 0 | U | 1.2 | 2.0 | 1 3. | 1 5.0 | 0.2 | U. I | 10.2 | 10.4 | 0.5 | 0.6 | 10.7 | 0.9 | 1.0 | 1.1 | 12 | U | 12 | U |

Reduction to the Meridian. PART I.

| ŧ | | | | 34 | | | - | | | - | | | | |
|----|----------|------|--------------|-------|-------|--------|----------------|-------|--------|------------------|---------|--------|---------|------------------|
| ł. | 8 | 0m | lm. | 2m | 3m | 4m. | 5 ^m | 6m | 7m | Sm | 9m | 10m | 11m | 12m |
| ı | 15.00 | " | " | " | " | " | " | " | " | 10000 | 1 50 00 | " | 000 14 | 200 00 |
| ı | 0 | 0 00 | 1.96 | | | | 49.09 49.41 | | | 125.65 126.17 | | | | |
| ı | 1 2 | 0.00 | 2.03 | | | | 49.74 | | | 126.70 | | | | |
| ı | 3 | 0.00 | 2.16 | | | | 50.07 | | | 127.23 | | | | |
| ı | 4 | 0.01 | 2.23 | | | | 50.40 | | | 127.75 | | | | |
| ı | 5 | 0.01 | 2.30 | | | | 50.74 | | | 128.28 | | | | |
| 1 | 6 | 0.02 | 2.38 | 8.66 | 18.87 | 33.01 | 51.07 | 73.06 | 98.97 | 128.81 | 162.58 | 200.26 | 241.87 | 287.41 |
| ĺ | 7 | 0.03 | 2.45 | 8.80 | 19.07 | 33.27 | 51.40 | 73.46 | | 129.34 | | | | |
| ı | 8 | 0.03 | 2.52 | | | | 51.74 | | | 129.87 | | | | |
| I. | 9 | 0.01 | 2.60 | - | - | - | - | | | 130.41 | | | | |
| I | 10 | 0.05 | 2.67 | 9.22 | 19.69 | 34.09 | 52.41 | 74.66 | 100.84 | 130.94 | 164.97 | 202.92 | 244.79 | 290.58 |
| l | 11 | 0.07 | 2.75 | 9.36 | 19.90 | 34.36 | 52.75 | 75.07 | 101.31 | 131.48 | 165.57 | 203.58 | 245.52 | 291.38 |
| I | 12 | 0.08 | 2.83 | 9.50 | 20.11 | 34.01 | 53.09 | 75.47 | 101.78 | 132.01 132.55 | 166 27 | 904.23 | 246.20 | 292.18 |
| ı | 13 14 | 0.09 | 2.91 2.99 | 0.70 | 20.32 | 95 10 | 53,43 | 76.90 | 102.23 | 133.09 | 167.37 | 905.50 | 917 79 | 993 78 |
| ۱ | 15 | 0.12 | 3.07 | 9.13 | 20.74 | 35.46 | 54 19 | 76.70 | 103.20 | 133.63 | 167.98 | 206.26 | 248.46 | 294.58 |
| ł | 16 | 0.14 | 3.15 | 10.09 | 20.95 | 35.74 | 54.46 | 77.10 | 103-67 | 134.17 | 168.58 | 206.93 | 249.19 | 295.38 |
| ı | 17 | 0.16 | 3.23 | | | | | | | 134.71 | | | | |
| ŀ | 18 | 0.18 | 3.32 | 10.39 | 21.38 | 36.30 | 55.15 | 77.92 | 104.63 | 135.25 | 169.80 | 208.27 | 250.67 | 296.99 |
| Ł | 19 | 0.20 | 3.40 | 10.54 | 21.60 | 36.59 | 55.50 | 78.34 | 105.10 | 135.79 | 170.41 | 208.95 | 251.41 | 297.79 |
| ľ | 20 | 0.22 | 3.49 | 10 69 | 21.82 | 36.87 | 55.85 | 78.75 | 105.58 | 136.34 | 171.02 | 209.62 | 252.15 | 298.60 |
| ı | 21 | 0.24 | 3.58 | 10.84 | 22.03 | 37.15 | 56.20 | 79.17 | 106.06 | 136.88 | 171.63 | 210.30 | 252.89 | 299.40 |
| I | 22 | 0.26 | 3.67 | | | | | | | | | | | 300.21 |
| ł | 23 | 0.29 | 3.76 | | | | | | | | | | | 301.02 |
| ı | 24 | 0.31 | 3.85 | 11.31 | 22.70 | 38.01 | 57.25 | 20.42 | 108.00 | 130.03 | 174.00 | 912 09 | 1955 87 | 301.83 |
| ı | 25 26 | 0.37 | | | | | | | | | | | | 303.46 |
| ı | 27 | 0.40 | 4.13 | | | | | | | | | | | 304.27 |
| ۱ | 28 | 0.43 | 4.22 | | | | | | | | | | | 305.09 |
| 1 | 29 | 0.46 | 4.32 | 12.11 | 23.82 | 39.47 | 59.03 | 82.53 | 109.95 | 141.29 | 176.56 | 215.75 | 258.87 | 305 90 |
| t | 30 | 0.49 | 4.42 | 12.27 | 24.05 | 39.76 | 59.39 | 82.95 | 110.44 | 141.85 | 177.18 | 216.44 | 259.62 | 306.72 |
| ı | 31 | 0.52 | 4.52 | | | | | | | | | | | 307.54 |
| ۱ | 32 | 0.56 | 4.62 | | | | | | | | | | | 308.36 |
| ŧ | 33 | 0.59 | 4.72 | | | | | | | | | | | 309.18 |
| ۱ | 34 | 0.63 | 4.82 | | | | | | | | | | | 310.00 |
| ı | 35 36 | 0.67 | 4.92 | | | | | | | | | | | 311.65 |
| 1 | 37 | 0.75 | 5.13 | | | | | | | | | | | 312.47 |
| ı | 38 | 0.79 | 5.24 | | | | | | | | | | | 313.30 |
| 1 | 39 | 0.83 | 5.35 | | | | | | | | | | | 314.12 |
| ł | 40 | 0.87 | 5.45 | 13.96 | 26.40 | 42.70 | 63.05 | 87.26 | 115.40 | 147.46 | 183.45 | 223.36 | 267.20 | 314.95 |
| ı | 41 | 0.92 | 5.56 | | | | | | | | | | | 315.78 |
| ā | 42 | 0.96 | 5.67 | | | | | | | 148.60 | | | | |
| 1 | 43 | 1.01 | 5.79 | | | | | | | | | | | 317.44 |
| 1 | 44 | 1.06 | 5.90 | | | | | | | 150.31 | | | | 318.27 |
| 1 | 45 46 | 1.10 | 6.01 | | | | | | | | | | | 319.11 |
| 1 | 47 | 1.20 | 6.24 | | | | | | | | | | | 320.78 |
| 1 | 48 | 1.26 | 6.36 | | | | | | | | | | | 321.62 |
| 1 | 49 | 1.31 | 6.48 | | | | | | | | | | | 322 45 |
| I | 50 | 1.36 | 6.60 | 15.76 | 28,85 | 45.87 | 66.81 | 91.68 | 120.47 | 153.19 | 189.83 | 230.40 | 274.88 | 323.29 |
| 1 | 51 | 1.42 | 6.72 | 15.95 | 29.10 | 46.18 | 67.19 | 92.13 | 120.98 | 153.77 | 190.47 | 231.11 | 275.66 | 324.13 |
| 1 | 52- | 1.48 | 6.84 | | | | | | | | | | | 324 97 |
| 1 | 53 | 1.53 | 6.96 | 16.32 | 29.61 | 46.82 | 67.96 | 93.02 | 155.01 | 154.93 | 191.76 | 232.53 | 277.21 | 325.82 |
| 1 | 54 | 1.59 | 7.09 | 16 51 | 29.86 | 47.14 | 60.70 | 93.47 | 122.53 | 155.51 | 192.41 | 233.24 | 271.99 | 326.66 327.50 |
| 1 | 55 56 | 1.65 | 7.21 | 16.70 | 30.12 | 47.10 | 69 19 | 94 48 | 199 57 | 156.69 | 193.71 | 234.67 | 279.55 | 328.35 |
| I | 57 | 1.77 | 7.4.7 | 17.09 | 30.61 | 48.11 | 69.51 | 94.83 | 121.09 | 157.26 | 194.36 | 235.38 | 280.33 | 329.20 |
| 1 | 58- | 1.83 | 7.59 | 17.28 | 30.89 | 48.43 | 69.90 | 95.29 | 124.61 | 157.85 | 195.02 | 236.10 | 281.11 | 330.01 |
| I | 59 | 1.90 | 7.72 | 17.48 | 31.15 | 148.76 | 70.29 | 95.75 | 125.13 | 158.43 | 195.67 | 236.82 | 281.89 | 330.89 |
| 1 | .2 | 0.01 | 0.02 | 0.03 | 0.05 | 0.06 | 0.07 | 0.09 | 0.10 | 0.11 | 0.12 | 0.14 | 0.15 | 0.16 |
| I | .4 | 0.01 | | 0.06 | | | | 0.17 | 0.20 | 0.22 | 0.25 | 0.28 | 0.30 | 0.33 |
| 1 | .6 | 0.02 | | | | 0.18 | | 0.26 | 0.30 | 0.34 | 0.37 | 0.41 | 0.45 | 0.49 |
| 1 | .8 | 0.02 | 0.08 | 0.13 | 0.18 | 0.24 | 0.28 | 0.34 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 | 0.66 |

| 1 | | | VIII. | | | 77.7 | TA | | | | .—Red | | | | | lstice. | | | 95 |
|---|-----|----------|-------|-----|----------|--------|--------|---|----------|---------|--------------------|--------|---|----------|----------|---------------|------|-------|---|
| ı | PA | ART | II. | 1 | | 1 | | | qui | ty o | f the Ec | liptic | | 40 | ″·. | | | NOT I | |
| ı | | | 1- | A | rg. | Reduc | Diff. | Variation in 100" change of obliquity. | Aı | g. | Reduc. | Diff | Variation in 100" ehange of obliquity. | A | rg. | Redu | 1C. | Diff: | Variation in 100" change of obliquity. |
| ı | | | + | m. | s. 0 | 0 00 | 00.02 | 0.0000 | m. 10 | s. 0 | 1 11.71 | 2.41 | 0.0651 | m. 20 | s. 0 | AY4 | .83 | 4.80 | 0.2606 |
| ı | m. | 8. | " | | 10 | | | 0.0000 | | 10 | | | 0.0673 | | 10 | | .63 | 4.81 | 0.2650 |
| ı | 0 | 0 | .0.00 | , | 50 | | | 0.0001 | 1 | 20 | | | 0 0695 | 16 | 20 | | | | 0.2694 |
| ı | 0: | 30 | 0.00 | | | | | 0.0002 | | 30 | | | 0.0717 | | 30 | | | | 0.2738 |
| ı | - | 30 | 0.00 | 10 | 50 | | | 0.0005 | | 50 | | | 0.0763 | О | 50 | 1 - | | | 0.2828 |
| ı | 2 | 0 | 0.00 | 1 | 0 | | | 0.0007 | 11 | 0 | | | 0.0787 | 21 | 0 | - | - | - | 0.2873 |
| ı | | 30 | 0.00 | | 10 | 0 0.9 | 8 0.29 | 0.0009 | | 10 | | | 0.0811 | | 10 | | | | 0.2919 |
| ı | 3 5 | 0 | 0.00 | | 20 | | | 0.0011 | | 30 | | | 0.0836 | | 30 | | | | 0.2965 |
| ı | 4 | 30 | 0.00 | | 30 40 | | | 0.0014 | | 40 | | | 0.0860 | 1 | 40 | 110 | | | 0.3012 |
| ı | | 30 | 0.01 | | 50 | | | 0.0022 | | 50 | | | 0.0911 | | 50 | 115 | | | 0.3106 |
| ı | 5 | 0 | 0.01 | 2 | 0 | 0 2.8 | 7 0.50 | 0.0026 | 12 | 0 | 1, 43.26 | 2.89 | 0.0937 | 22 | 0 | 5 47 | 7.06 | 5.25 | 0.3154 |
| | | 10 | 0.01 | | 10 | 0 3.3 | 7 0.54 | 0.0031 | | 10 | | | 0.0963 | | 10 | | | | 0.3202 |
| | | 20 30 | 0.01 | | 20 30 | | | 0.0036 | | 30 | | | 0.0990 | | 30 | | | 1 | 0.3250 |
| | | 40 | 0.01 | | 40 | | | 0.0041 | | 40 | | | 0.1044 | | 40 | | | 1 | 0.3349 |
| 4 | | 50 | 0.01 | | 50 | | | 0.0053 | | 50 | | | 0.1072 | | 50 | 1 | | | 0.3398 |
| | 6 | 0 | 0.01 | 3 | 0 | 0 6.4 | 5 0.74 | 0.0059 | 13 | 0 | | 1 | 0.1100 | 53 | | 1 | - | | 0.3448 |
| ı | | 10 | 0.01 | н | 10 | | | 0.0066 | | 10 | | | 0.1128 | | 10 | 1 | | | 0.3498 |
| ı | | 20 30 | 0.01 | | 20 | | | 0.0073 | | 20 | 2 7.48 2 10.69 | | 0.1157 | | 20 30 | | | | 0.3549 |
| ı | | 40 | 0.02 | | 40 | | | 0.0088 | | | 2 13.94 | | | U | 40 | | | | 0.3651 |
| ı | | 50 | 0.02 | - | 50 | | | 0.0096 | | 50 | | | 0.1246 | | 50 | | | | 0.3703 |
| ı | 7 | 0 | 0.02 | 4 | 0 | 0 11.4 | 7 0.97 | 0.0104 | 14 | 0 | | | 0.1276 | 24 | 0 | | | | 0.3755 |
| ı | | 10 | 0.02 | | 10 | | | 0.0113 | | 10 | | | 0.1307 | | 10 | | | | 0.3807 |
| | | 20 30 | 0.03 | | 20 30 | | | 0.0122 | | 30 | | | 0.1338 | | 30 | | | | 0.3860 0.3913 |
| ı | | 40 | 0.03 | | 40 | | | 0.0132 | | 40 | | | 0.1401 | | 40 | | | | 0.3913 |
| | - 4 | 50 | 0.04 | | 50 | | | 0.0152 | | 50 | | | 0.1433 | | 50 | | | | 0.4021 |
| ١ | 8 | 0 | 0 04 | 5 | 0 | | | 0.0163 | 15 | 0 | | | 0.1465 | 25 | 0 | | | | 0.4075 |
| ١ | | 10 | 0.04 | | 10 | | | 0.0174 | | 10 | | | 0.1498 | | 10 | | _ | | 0.4130 |
| ı | | 20 30 | 0.05 | ١. | 30 | | | 0.0185 | | | | | 0.1531 0.1564 | H | 20 30 | | | | 0.4185 |
| ı | | 40 | 0.05 | н | 40 | | | 0.0209 | | 40 | | | 0.1598 | 1 | 40 | | | | 0.4296 |
| ı | | 50 | 0.06 | | 50 | 0 24.4 | 0 1.42 | 0.0221 | | 50 | | | 0.163? | | 50 | 7 58 | 3.53 | 6.20 | 0.4352 |
| ı | 9 | 0 | 0.06 | 6 | 0 | | | 0.0234 | 16 | 0 | | | 0.1667 | 26 | 0 | | | | 0.4408 |
| ı | | 10 20 | 0.07 | в | 10 | | | 0.0247 | | 10 | | | 0.1702 | | 10 | | | | 0.4465 |
| ı | | 30 | 0.01 | н | 20 30 | | | 0.0261 | | 30 | | | 0.1773 | | 30 | | | | 0.4579 |
| | | 40 | 0.08 | | 40 | | | 0.0289 | | | | | 0.1809 | | 40 | | | | 0.4637 |
| | | 50 | 0.09 | | 50 | | | 0.0303 | | - | | - | 0.1845 | 1 | 50 | - | - | | 0.4695 |
| | 10 | 0 | 0.09 | 7 | | | | 0.0318 | 17 | 0 | | | 0.1882 | 27 | 0 | | | | 0.4754 |
| | | 10 20 | 0.10 | | 10 | | | 0.0333 | | 10 | | | 0.1919 | | 10 | | | | 0.4813 |
| | | 30 | 0.11 | | 30 | | | 0.0345 | | _ | | | 0.1994 | 1 | 30 | | | | 0.4932 |
| 1 | | 40 | 0.12 | | 40 | 0 42.1 | 5 1.85 | 0.0381 | | | 3 43.81 | 4.21 | 0.2033 | 1 | 40 | 9 8 | .86 | 6.63 | 0.4993 |
| | - | 50 | 0.13 | _ | 50 | - | | 0.0399 | | | 3 48.05 | | | | 50 | - | | - | 0.5053 |
| | 11 | 0 | 0.14 | 8 | | | | 0.0416 | 18 | | 3 52.33 | | | 58 | 10 | | | | 0.5114 0.5175 |
| | | 10 20 | 0.15 | 1 | | | | 0.0452 | | 20 | 3 56.66 4 1.02 | | 0.2149 | 1 | 10 20 | | | | 0.5175 |
| | | 30 | 0.16 | | 30 | 0 51.8 | 1 2.05 | 0.0470 | | 30 | 4 5.42 | 1.44 | 0.2229 | 1 | 30 | 9 42 | .42 | 6.83 | 0.5299 |
| | | 40 | 0 17 | - | 40 | 0 53.8 | 6 2.09 | 0.0489 | | 40 | | | 0.2269 | | 40 | | | | 0.5361 |
| | | 50 | 0.18 | - | | | | 0.0508 | 10 | - | 4 14.34 | - | - | 200 | 50 | | | | 0.5424 |
| | 12 | 0 10 | 0.19 | 9 | 10 | | | 0.0527 | 19 | | 4 18.87 4 23.43 | | | 29 | | | | | 0.5487 0.5550 |
| | | 20 | 0.21 | | 20 | | | 0.0567 | | | 4 28.03 | | | | | | | | 0.5614 |
| | | 30 | 0.23 | | 30 | 1 4.7 | 2 2.29 | 0.0587 | | 30 | 4 32.67 | 4.68 | 0.2477 | | 30 | 10 24 | .01 | 7.07 | 0.5678 |
| | | 40 | 0.24 | | 40 | | | 0.0608 | | | 4 37.35 | | | | | | | | 0.5743 |
| - | 13 | 50 | 0.25 | 10 | 50 | | | 0.0629 | 20 | | 4 42.07 4 46.83 | | 0.2563 | 30 | | 10 38 $10 45$ | | | 0.5808 |
| - | -17 | 47 | 17121 | 110 | () | 11.1 | | lawar. | - () | (/ | E 20000 | | 0.0000 | 17(1 | - | TO 20 | TU | | 171170117 |

TABLE XXXI. TABLE XXX. 96 To change mean Solar into Sidereal Time. To change Sidereal into mean Solar Time. Sidereal Sider. Min. Subtract Seconds. Add Seconds. Soar Add Parts Sider. Subtr. Pts. Solar Min. Subtract Add Days. Sec. of a Sec. of a Sec. 3 55.908 0.164 3 56.556 0.164 0.003 1 0.003 1 2 2 51.816 2 0.328 2 0.005 7 53.112 2 0.329 0.006 2 3 11 47.724 3 3 11 49.668 3 0.493 3 0.008 0.491 0.008 3 4 15 43.632 46.224 4 0.658 0.011 4 0.655 4 0.011 4 0 15 5 19 39.540 5 0 5 0.8195 0.014 5 19 42.780 5 0822 0.014 0 23 35.448 6 6 6 6 0.017 0.983 6 0.016 6 0 23 39.336 0.986 7 27 31.356 7 0 7 1.147 7 0.019 7 0 27 35.892 7 1.150 0.019 27.264 8 0 31 8 0 31 32.448 8 1.315 8 0.022 8 1.311 8 0.022 23.172 9 0 35 1.474 9 0 35 29.001 9 1.479 9 0.025 9 9 0.025 39 10 1.643 10 10 0 39 19.080 10 1.636 10 0.027 25 560 0.027 11 43 43 0 14.988 11 1.802 11 11 22.116 11 1.807 11 0.030 0 030 12 0 4.7 10.896 1.966 12 12 12 47 18.672 12 1.972 12 0.033 0.032 13 0 51 6.804 13 2.130 13 13 0 51 15.228 13 2.136 13 0.036 0.035 14 0 55 2.712 2.294 14 55 11.784 14 2.300 14 0.038 14 14 0.038 15 0 58 15 15 0 59 8.340 15 2.464 15 0 041 58.620 15 2.457 0.041 16 54.528 16 16 3 16 2.621 16 4.896 16 2.629 0.044 0.014 17 6 50.436 17 2.785 17 17 0.046 17 7 1.452 17 2.893 0.047 18 10 46.344 18 10 58 008 18 2.949 18 0.049 18 18 3.057 0.050 19 14 42.252 19 3.113 19 19 14 54.564 19 3.221 19 0.053 0.052 20 18 38.160 20 3.277 20 18 51.120 20 3.286 20 0.055 20 0.055 22 47.676 21 99 34.068 21 3.440 21 21 21 3.450 91 0.058 1 22 22 26 44.232 22 22 26 29.976 22 3.604 22 0.060 0.061 3.614 23 23 23 30 25.884 23 3.768 23 23 1 30 40.788 0.063 3.779 0.064 24 34 94 34 37.344 24 3.943 24 0.066 21.792 24 3.932 24 0.066 38 33.900 25 25 25 38 17.700 25 4.096 25 0.068 25 4.108 0.069 26 13.608 26 1 42 30.456 26 4.272 26 0.072 42 26 4.259 26 0.071 27 46 9.516 27 46 27.012 27 4.436 27 27 4.423 27 0.074 0.075 28 28 50 23.568 28 4.600 28 0.077 1 50 5.424 28 4.587 28 0.076 29 54 1.332 29 29 1 54 20.124 29 4.764 29 0.080 4.751 29 0.079 4.928 30 57 30 58 16.680 30 30 0.082 57.240 30 4 915 30 0.082 31 3 1 53.148 31 2 2 13 236 31 5.092 31 0.085 31 5 079 0.085 32 2 32 2 6 9.792 5 49.056 32 32 5.257 32 0.088 5.242 32 0.037 33 2 44.964 33 2 10 6.348 33 5.421 33 0.091 9 33 5.406 33 0.090 2 34 34 2 14 2.904 34 13 40.872 34 34 5.585 0.094 5.570 34 0.093 35 5 17 36.780 2 35 17 59.460 35 5.750 35 0 097 35 5.734 35 0.096 36 5.914 36 0.100 36 5.898 0.098 Sid. Hrs. Sol. Hrs. 9.8565 37 6.078 37 0.103 9.829 6.062 37 0.101 2 2 0 19.713 38 6.212 38 0 106 19.659 38 6.225 38 0.104 3 3 29.569 39 6.407 39 0.108 29.488 39 6.389 39 0.106 4. 4 0 39.426 40 6.571 40 0.111 0 39.318 40 6.553 40 0.109 5 49.282 41 6.735 41 0.114 5 49.147 41 6.717 41 0.112 6 59.139 42 6.900 42 0.116 6 58.977 42 6.881 42 0.115 7 43 7.064 0.119 7 8.806 43 1 8.995 43 7.014 43 0.117 8 1 18.852 44 7.228 44 0.122 8 18.636 44 7.208 44 0.120 9 28.708 45 7.393 0.125 9 28.465 1 4.5 45 7.372 45 0.123 10 1 38.565 46 7.557 46 0.128 10 38.295 46 7.536 46 0.126 7.722 11 1 48.421 47 0.131 11 48.124 47 47 7.699 4.7 0.128 12 1 58.278 48 7.886 48 0.133 12 57.954 48 7.864 48 0.131 13 2 8.134 49 8.050 13 2 49 0.136 7.783 4.9 8.027 4.9 0.134 2 14 17.991 50 8.214 50 0 138 14 2 17.613 50 8.191 50 15 2 27.847 51 8.378 51 0.141 15 2 27.442 8.355 51 16 9 37.704 52 8.543 52 0.144 16 2 37.272 52 8.519 0.142 17 47.560 53 8.707 53 0.147 47.101 17 2 53 8,683 0.145 57.417 54 18 8.872 54 0.150 18 2 56.931 54 8.616 0 147 54 19 3 7.273 55 9.036 0.152 3 55 19 6.760 55 9.010 55 0.150 20 3 17.130 56 9.200 56 0.155 20 3 16.590 56 9.174 56 0.153 21 3 26.987 57 9.364 57 0.157 21 3 57 9 338 0.156 26.419 57 22 3 36.844 58 9.528 0.159 22 3 36.249 58 58 9.502 58 0.158 23 3 46,700 0.162 59 59 9.692 59 23 3 9.666 59 0.161 46.078 24 3 56.556 60 9.856 60 0.164 24 3 60 9.829 60 0.161 55.908 This Table may be used to shew the Sun's Right

Ascension also, in Sidereal Time.

TABLE XXXII.

To convert Mean Time into Parts of the Equator.

TAB. XXXIII. 97 Lengths of Circular Arcs.

| 200 | | 100 | | 1 | A Vancous | | Arcs. |
|------------------------------|-----------------|-------|--------------|-------|--|------|-------------|
| Mean | Parts of the | Mean | Parts of the | Mean | Parts of the | | Arc. |
| Time. | Equator. | Time. | Equator. | Time. | Equator. | | 22.20 |
| h. | 0 1 " | m. | 0 / // | 8. | , " | | |
| 1 | 15 2 27.847 | 1 | 0 15 2.464 | 1 | 0 15.041 | 1° | 0.01745329 |
| 2 > | 30 4 55.694 | 2 | 0 30 4.928 | 2 | 0 30.082 | 2 | 0.03490659 |
| 3 | 45 7 23.541 | 3 | 0 45 7.392 | 3 | 0 45.123 | 3 | 0.05235988 |
| 4 | 60 9 51.388 | 4 | 1 0 9.856 | , 4 | 1 0.164 | 4 | 0.06981317 |
| 5 | 75 12 19.235 | 5 | 1 15 12.321 | 5 | 1 15.205 | 5 | 0.08726646 |
| 6 | 90 14 47.081 | 6 | 1 30 14.785 | 6 | 1 30.246 | 6 | 0.10471976 |
| 7 | 105 17 14.928 | 7 | 1 45 17.249 | 7 | 1 45.287 | 7 | 0.12217: 05 |
| 8 | 120 19 42.775 | 8 | 2 0 19.713 | 8 | 2 0.328 | 8 | 0.13962634 |
| 9 | 135 22 10.622 | * 9 | 2 15 22.177 | 9 | 2 15.369 | 9 | 0.15707963 |
| 10 | 150 24 38.469 | 10 | 2 30 24.641 | 10 | 2 30.411 | 10 | 0.17453993 |
| 11 | 165 27 6.316 | 11 | 2 45 27.105 | 11 | 2 45.452 | 20 | 0.34906585 |
| 12 | 180 29 34.163 | 12 | 3 0 29.569 | 12 | 3 0.493 | 30 | 0.52359878 |
| 13 | 195 32 2.010 | 13 | 3 15 32.033 | 13 | 3 15.534 | 40 | 0,69813170 |
| 14 | 210 34 29.857 | _14 | 3 30 34.497 | 14 | 3 30.575 | 50 | 0.87266463 |
| 15 | 225 36 57.703 | 15 | 3 45 36.962 | 15 | 3 45.616 | 60 | 1.04719755 |
| 16 | 240 39 25.550 | 16 | 4 0 39.426 | 16 | 4 0.657 | 70 | 1.22173048 |
| 17 | 255 41 53.397 | 17 | 4 15 41.890 | 17 | 4 15.698 | 80 | 1.39626340 |
| 18 | 270 44 21.244 | 18 | 4 30 44.354 | 18 | 4 30.739 | 90 | 1.57079633 |
| 19 | 285 46 49.091 | 19 | 4 45 46.818 | 19 | 4 45.780 | 100 | 1.74532925 |
| 20 | 300 49 16.938 | 20 | 5 0 49.282 | 20 | 5 0.821 | 110 | 1.91936218 |
| 21 | 315 51 44.784 | 21 | 5 15 51.746 | 21 | 5 15.862 | 120 | 2.09439510 |
| 22 | 330 54 12.631 | 22 | 5 30 54.210 | 22 | 5 30.903 | 130 | 2.26892803 |
| 23 | 345 56 40.478 | 23 | 5 45 56.674 | 23 | 5 45.944 | 140 | 2.44346095 |
| 24 | 360 59 8.325 | 24 | 6 0 59.138 | 24 | 6 0.985 | 150 | 2.61799388 |
| | | 25 | 6 16 1.603 | 25 | 6 16.027 | 160 | 2.79252680 |
| | | 26 | 6 31 4.067 | 26 | 6 31.058 | 170 | 2.96705973 |
| Decimals | 1 2 2 2 2 2 2 3 | 27 | 6 46 6.531 | 27 | 6 46.109 | 180 | 3.14159265 |
| of Mean | Parts of the | 28 | 7 1 8.995 | 28 | 7 1.150 | 210 | 3.66519143 |
| Time. | Equator. | 29 | 7 16 11.459 | 29 | 7 16.191 | 240 | 4.18879020 |
| | 1 72 | 30 | 7 31 13.923 | 30 | 7 31.232 | 270 | 4.71238898 |
| S. | " | 31 | 7 46 16.387 | 31 | 7 46.273 | . 1' | 0 00029089 |
| 0.1 | 1.504 | 32 | 8 1 18.851 | 32 | 8 1.314 | 2 | 0.00058178 |
| 0.1 | 3.008 | 33 | 8 16 21.315 | 33 | 8 16.355 | 3 | 0.00038178 |
| 0.3 | 4.512 | 34 | 8 31 23.779 | 34 | 8 31.396 | 4 | 0.00116355 |
| 0.4 | 6.016 | 35 | 8 46 26.244 | 35 | 8 46.437 | 5 | 0.00145444 |
| 0.5 | 7.521 | 36 | 9 1 28.708 | 36 | 9 1.478 | 6 | 0.00174533 |
| 0.6 | 9.025 | 37 | 9 16 31.172 | 37 | 9 16.519 | 7 | 0.00174533 |
| 0.7 | 10.529 | 38 | 9 31 33.636 | 38 | 9 31.560 | 8 | 0.00232711 |
| 0.8 | 12.033 | 39 | 9 46 36.100 | 39 | 9 46.601 | 9 | 0.00261799 |
| 0.9 | 13.537 | 40 | 10 1 38.565 | 40 | 10 1.643 | 10 | 0.00290888 |
| S. | " | 41 | 10 16 41.029 | 41 | 10 16.684 | 20 | 0.03581776 |
| 0.01 | 0.150 | 42 | 10 16 41.029 | 41 | 10 16.084 | 30 | 0.00872665 |
| 0.02 | 0.301 | 43 | 10 46 45.957 | 43 | 10 31.723 | 40 | 0.01163553 |
| 0.02 | 0.451 | 44 | 11 1 48.421 | 44 | 11 1.807 | 50 | 0.01163333 |
| 0.04 | 0.602 | 45 | 11 16 50.885 | 45 | 11 16.848 | 60 | 0.01745329 |
| 0.05 | 0.752 | 46 | 11 31 53.349 | 46 | 11 31.889 | 1" 1 | 0.00000485 |
| 0.05 | 0.903 | 47 | 11 31 53.349 | 40 | 11 31.889 | 2 | 0.00000485 |
| 0.07 | 1.053 | 48 | 12 1 58.277 | 48 | 12 1.971 | 3 | 0.00000970 |
| 0.03 | 1.203 | 49 | 12 17 0.741 | 4.5 | 12 1.971 | 4 | 0.00001454 |
| 0.09 | 1.354 | 50 | 12 32 3.206 | 50 | 12 32.053 | 5 | 0.00001939 |
| 8. | " | 51 | 12 47 5.670 | 51 | 12 47.094 | | 0.00002909 |
| 0.001 | 0.015 | 52 | 13 2 8.134 | 52 | 12 47.094 | 7 | 0.00002909 |
| 0.002 | 0.030 | 53 | 13 17 10.598 | 53 | 13 17.176 | 8 | 0.00003394 |
| 0.002 | 0.045 | 54 | 13 32 13.062 | 54 | 13 32.217 | 9 | 0.00003879 |
| 0.001 | 0.060 | 55 | 13 47 15.526 | 55 | 13 47.259 | 10 | 0.00004363 |
| 0.005 | 0.075 | 56 | 14 2 17.990 | 56 | 14 2.300 | 20 | 0.00004848 |
| 0.006 | 0.075 | 57 | 14 17 20.451 | 57 | 14 2.300 | 30 | 0.00009696 |
| 0.007 | .0.105 | 58 | 14 32 22.918 | 58 | 14 32.382 | 40 | 0.00014544 |
| 0.008 | 0.120 | 59 | 14 47 25.382 | 59 | 14 47.423 | 50 | 0.00019393 |
| 0.009 | 0.135 | 60 | 15 2 27.847 | 60. | 15 2.464 | 60 | 0.00029089 |
| Anna Printers and Publishers | | - | C | - | Commence of the last of the la | 777 | |

G

Annual Precession of a Star in R. A. in Time.

Argument, R. A. of the Star in Time.

| S. | _ | + | | + | | + | | + | - | + | _ | + | S. |
|-------|-----|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|----|
| | 0h | 12h | 1h | 13h | 2h | 14h | 3h | 15h | 4h | 16h | 5h | 17h | |
| N. | + | _ | + | - | + | _ | + | | + | - | + | | N. |
| P. P. | m. | S. | P. P. | S. | m. |
| + | 0 | 0.000 | + | 0.346 | + | 0.668 | + | 0.945 | + | 1.157 | + | 1.291 | 60 |
| 6 | 10 | 0.058 | 5 | 0.402 | 5 | 0.718 | 3 | 0.985 | 2 | 1.185 | 1 | 1.305 | 50 |
| 12 | 20 | 0.117 | 11 | 0.457 | 9 | 0.766 | 7 | 1.024 | 4 | 1.211 | 1 | 1.316 | 40 |
| 17 | 30 | 0.174 | 16 | 0.511 | 14 | 0.813 | 10 | 1.060 | 6 | 1.235 | 2 | 1.325 | 30 |
| 23 | 40 | 0.232 | 22 | 0.565 | 18 | 0.859 | 14 | 1.095 | 8 | 1.256 | 2 | 1.331 | 20 |
| 29 | 50 | 0.289 | 27 | 0.617 | 23 | 0.903 | 17 | 1.127 | 11 | 1.274 | 3 | 1.335 | 10 |
| 35 | 60 | 0.346 | 32 | 0.668 | 28 | 0.945 | 21 | 1.157 | 13 | 1.291 | 4 | 1.336 | 0 |
| N. | + | | + | _ | + | _ | + | _ | + | _ | + | _ | N. |
| | 11h | 23h | 10h | 22h | 9h | 21h | Sh | 20h | 7h | 19h | 6h | 18h | |
| S. | _ | + | _ | + | - | + | - | + | - | + | - | + | S. |
| 9 | | | | | | | | | | 11.1 | | 11.0 | |

Multiply the number found from the Table, with its proper sign, by the natural tangent of the Star's declination, to which add the constant quantity $3^{\circ}.068$ for the annual precession, = a in the Synopsis.

TABLE XXXV.

Argument, R. A. of the Star in Time.

| 1- | | | | | | | | | | | | | | |
|------|-----|-----|----------|-------|----------|-------|----------------------|-------|----------|-------|----------|-------|----------|----|
| | 1 | Oh | + 12h | 1h | + 13h | 2h | + 14 ^h | 3h | + 15h | 4h | + 16h | 5h | + 17h | |
| P. 1 | P. | m. | S. | P. P. | S. | P. P. | S. | P. P. | ·S• | P. P. | S- | P. P. | 8. | m. |
| + | - 1 | 0 | 0.000 | + | 0.349 | + | 0.675 | + | 0.954 | + | 1.168 | + | 1.304 | 60 |
| 6 | 3 | 10 | 0.059 | 5 | 0.406 | 5 | 0.725 | 3 | 0.995 | 2 | 1.197 | 1 | 1.318 | 50 |
| 12 | 2 | 20 | 0.118 | 11 | 0.462 | 9 | 0.774 | 7 | 1.034 | 4 | 1.222 | 2 | 1.329 | 40 |
| 18 | 3 | 30 | 0.176 | 16 | 0.516 | 14 | 0.821 | .10 | 1.071 | 7 | 1.247 | 2 | 1.339 | 30 |
| 24 | 6 | 40 | 0.234 | 22 | 0.571 | 19 | 0.868 | 14 | 1.106 | 9 | 1.269 | 3 | 1.345 | 20 |
| 30 | | 50 | 0.292 | 27 | 0.623 | 24 | 0.912 | 17 | 1.138 | 11 | 1.287 | 4 | 1.349 | 10 |
| 36 | 3 | 60 | 0.349 | 33 | 0.675 | 28 | 0.954 | 21 | 1.168 | 13 | 1.304 | 5 | 1.350 | 0 |
| | | 11h | 23h | 10h | 22h | 9h | 21h | gh | 20h | 7h | 19h | 6h | 18h | |
| | | | + | _ | + | - | + | _ | 1+ | _ | + | _ | + 0 | |

The number from the Table = p, and $p \times \sec$ dec. = b.

TABLE XXXVI.

Argument, R. A. of the Star in Time.

| | | | | 8 | | , | | | | - 65 | | | |
|-------|-----|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|----|
| | - | + | - | + | | + | | + | - | + | - | + | |
| | 0h | 12h | 1h | 13h . | 2h | 14h | 3h | 15h | 4,h | 16h | 5h | 17h | - |
| P. P. | m. | S. | P. P. | S. | m. |
| - | 0 | 1.239 | _ | 1.196 | | 1.073 | | 0.876 | | 0.619 | | 0.321 | 60 |
| 0 | 10 | 1.237 | 2 | 1.181 | 3 | 1.045 | 4 | 0.837 | 5 | 0.572 | 5 | 0.268 | 50 |
| 0 | 20 | 1.234 | 4 | 1.164 | 7 | 1.015 | 9 | 0.796 | 10 | 0.523 | 11 | 0.215 | 40 |
| 1 | 30 | 1.228 | 6 | 1.144 | 10 | 0.983 | _13 | 0.751 | 15 | 0.474 | 16 | 0.162 | 30 |
| 1 | 40 | 1.220 | 8 | 1.123 | 14 | 0.949 | 18 | 0.710 | 20 | 0.424 | 22 | 0.108 | 20 |
| 1 1 | 50 | 1.209 | 10 | 1.099 | 17 | 0.913 | 22 | 0.666 | 25 | 0.373 | 27 | 0.054 | 10 |
| 1 1 | 60 | 1.196 | 13 | 1.073 | 20 | 0.876 | 26 | 0.619 | -30 | 0.321 | 32 | 0.000 | 0 |
| | 11h | 23h | 10h | 22h | 9h | 21h | gh | 20h | 7 h | 19h | 6h | 18h | |
| | + | | + | - | + | - | + | _ | + | | ,+ | - | |

The number from the Table =q, and $q \times \sec$ dec. =c.

| Argument, | R. | A. | of | the | Star | in | Time. |
|-----------|----|----|----|-----|------|----|-------|
|-----------|----|----|----|-----|------|----|-------|

| S. 1 | + | | + | _ | + | _ | + | _ | + | | + | - | S. |
|--------|-----|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------------|-------|----|
| true . | Oh | 12h | 1h | 13h | 2h | 14h | 3h | 15h | 4.h | 16h | 5 ^h | 17h | |
| N. | - | + | _ | + | - | + | - | + | - | + | - | + | N. |
| P. P. | m. | S. | P. P. | S. | m. |
| - | 0 | 0.643 | | 0.621 | - | 0.557 | _ | 0.455 | _ | 0.322 | _ | 0.166 | 60 |
| 0 | 10 | 0.643 | 1 | 0.613 | 2 | 0.542 | 2 | 0.435 | 3 | 0.297 | 3 | 0.139 | 50 |
| 1 | 20 | 0.641 | 2 | 0.604 | -4 | 0.527 | 5 | 0.413 | 5 | 0.272 | 6 | 0.112 | 40 |
| 1 | 30 | 0.638 | 3 | 0.594 | 6 | 0.510 | 7 | 0.392 | 8 | 0.246 | 8 | 0.084 | 30 |
| 2 | 40 | 0.633 | 4 | 0.583 | 8 | 0.493 | 9 | 0.369 | 10 | 0.220 | 11 | 0.056 | 20 |
| 2 | 50 | 0.628 | 5 | 0.571 | 10 | 0.474 | 11 | 0.346 | 13 | 0.193 | 14 | 0.028 | 10 |
| 3 | 60 | 0.621 | 7 | 0.557 | 12 | 0.455 | 14 | 0.322 | 16 | 0.166 | 17 | 0.000 | 0 |
| N. | + | _ | + | _ | + | _ | + | | + | _ | + | | N. |
| 13 | 11h | 23h | 10h | 22h | 9h | 21h | 8h | 20h | 7h | 19h | 6h | 18h | |
| S. | _ | + | _ | + | - | + | - | + | - | + | - | + | S. |

The number from the Table gives s, and $s \times \text{tang. dec.} = d$.

TABLE XXXVIII.

Annual Precession of a Star in N. P. D.

Argument, R. A. of the Star in Time.

| - | | | | | | | | | | | | | |
|-------|-----|--------|-------|--------|-------|--------|-------|--------|-------|--------|-------|-------|-----|
| S. | - | + | | + | - | + | - | + 4 | _ | + | - | + | S. |
| | Oh | 12h | [h | 13h | 2h | 14h | 3h | 1.5h | 4h | 16h | 5h | 17h | * |
| N. | + | _ | + | | 1 | | + | 1 | 1 | | 1 | | N. |
| | | | - | | - | | | | | | | | 41. |
| P. P. | m. | " | P. P. | // - | P. P. | " | m. |
| - | 0 | 20.044 | - | 19.361 | - | 17.358 | | 14.173 | - | 10.022 | - | 5.188 | 60 |
| 13 | 10 | 20.025 | 35 | 19.116 | 55 | 16.904 | 70 | 13.542 | 81 | 9.255 | 87 | 4.338 | 50 |
| 27 | 20 | 19.968 | 71 | 18.835 | 110 | 16.419 | 140 | 12.884 | 162 | 8.471 | 174 | 3.481 | 40 |
| 40 | 30 | 19.872 | 106 | 18.518 | 164 | 15.902 | 210 | 12.202 | 243 | 7.670 | 261 | 2.616 | 30 |
| 53 | 40 | 19.739 | 141 | 18.165 | 219 | 15.354 | 280 | 11.497 | 324 | 6.855 | 348 | 1.747 | 20 |
| 66 | 50 | 19.569 | 176 | 17.779 | 274 | 14.778 | 350 | 10.769 | 405 | 6.027 | 435 | 0.874 | 10 |
| 80 | 60 | 19.361 | 212 | 17.358 | 329 | 14.173 | 420 | 10.022 | 486 | 5.188 | 522 | 0.000 | 0 |
| N. | - | + | - | + | _ | . + | _ | + | _ | + | _ | + | N. |
| W-P | 11h | 23h | 10h | 22h | 9h | 21h | 8h | 20h | 7h | 19h | 6h | 18h | |
| S. | + | - | + | | + | | + | | + | | + | - | S. |

The number from the Table = a'.

TABLE XXXIX.

Aberration in N. P. D. to find p'.

Argument, R. A. of the Star in Time.

| | _0h | 12h | 1h | 13h | 2h | 14h | 3h | 15h - | 4.h | 16h | 5h | 17h | |
|-------|-----|--------|-------|--------|-------|-----------|-------|--------|-------|--------|-------|-------|----|
| | - | + | - | + | _ | + | - | + + | - | + | - | + | |
| P. P. | m. | " | P. P. | // | P. P. | " | P. P. | 11 | P. P. | // | P. P. | " | m. |
| - | 0 | 20.255 | - | 19.565 | - | 17.541 | - | 14.322 | 4 | 10.128 | | 5.243 | 60 |
| 12 | 10 | 20.236 | 34 | 19.318 | 54 | 17.083 | 7.0 | 13.684 | 82 | 9.353 | 88 | 4.384 | 50 |
| 24 | 20 | 20.178 | 68 | 19.033 | 108 | 16.592 | 140 | 13:019 | 164 | 8.560 | 176 | 3.517 | 40 |
| 36 | 30 | 20.082 | 102 | 18.713 | 162 | 16.069 | 210 | 12.330 | 246 | 7.751 | 264 | 2.644 | 30 |
| 48 | 40 | 19.947 | 136 | 18.357 | 216 | 15.516 | 280 | 11.618 | 328 | 6.928 | 352 | 1.764 | 20 |
| 60 | 50 | 19.775 | 170 | 17.966 | 270 | 14.934 | 350 | 10.884 | 410 | 6.091 | 440 | 0.883 | 10 |
| 72 | 60 | 19.565 | 224 | 17.541 | 324 | 14.322 | 420 | 10.128 | 492 | 5.243 | 528 | 0.000 | 0 |
| 775 | + | 1 | + | | + | Married . | + | _ | +11 | | + | | - |
| | 111 | 23h | 10h | 22h | 9h | 21h | 8h | 20h | 7h | 19h | 6h | 18h | |

Multiply the number found in the Table by the natural sine of the Star's declination; the result will give V.

TABLE XL.

Aberration in N. P. D. to find q'.

| Argument, R. A. of the Star in T | ı ime. |
|----------------------------------|--------|
|----------------------------------|--------|

| | Oh | 12h | 1h | 13h | 2h | 14h | 3h | 15h | 4.h | 16h | 5h | 17h | |
|-------|-----|-------|-------|-------|-------|--------|-------|--------|-------|--------|-------|--------|----|
| | + | _ | + | - | + | - | + | _ | + | | + | - | _ |
| P. P. | m. | " | P. P. | " | P. P. | " | P. P. | " | P. P. | " | P. P. | " | m. |
| + | 0 | 0.000 | + | 4.809 | + | 9.290 | + | 13.138 | + | 16.090 | + | 17.947 | 60 |
| 80 | 10 | 0.810 | 75 | 5.588 | 64 | 9.984 | 50 | 13.700 | 30 | 16.480 | 10 | 18.140 | 50 |
| 160 | 20 | 1.619 | 150 | 6.355 | 128 | 10.657 | 100 | 14.233 | 60 | 16.839 | 20 | 18.298 | 40 |
| 240 | 30 | 2.426 | 225 | 7.110 | 192 | 11.311 | 150 | 14-740 | 90 | 17.166 | 30 | 18.420 | 30 |
| 320 | 40 | 3.226 | 300 | 7.852 | 256 | 11.943 | 200 | 15.220 | 120 | 17.460 | 40 | 18.509 | 20 |
| 400 | 50 | 4.022 | 375 | 8.579 | 320 | 12.552 | 250 | 15.669 | 150 | 17.720 | 50 | 18.562 | 10 |
| 480 | 60 | 4.809 | 450 | 9.290 | 384 | 13.138 | 300 | 16.090 | 180 | 17.947 | 60 | 18.580 | 0 |
| | + | | + | | + | _ | + | | + | | + | _ | |
| | 11h | 23h | 10h | 22h | 9h | 21h | 8h | 20h | 7h | 19h | 6h | 18h | |

The number from this Table, multiplied by the natural sine of the Star's declination, gives a product, to which r' being added, the result will be c'.

TABLE XLI.

| Argument, D | eclination | of | the | Star. |
|-------------|------------|----|-----|-------|
|-------------|------------|----|-----|-------|

| ; | 5 | | | 0820 | ~ |
|---|---|---|------|----------|---|
| _ | - | - | | | |

| -0 | Dec. North — South + | | | | | | | | | | | | | | | | |
|----|---|----|-------|----|-------|----|-------|----|-------|----|-------|----|-------|----|-------|----|-------|
| D. | D. No. No. | | | | | | | | | | | | | | | | |
| 0 | " | 0 | // | 0 | 11 | 0 | " | 0 | " | 0 | " | 0 | 11 | 0 | " | 0 | " |
| 0 | 8.066 | 10 | 7.944 | 20 | 7.579 | 30 | 6.985 | 40 | 6.179 | 50 | 5.185 | 60 | 4.033 | 70 | 2.759 | 80 | 1.401 |
| 1 | 8.065 | 11 | 7.918 | 21 | 7.530 | 31 | 6.913 | 41 | 6.087 | 51 | 5.076 | 61 | 3.910 | 71 | 2.626 | 81 | 1.262 |
| 2 | 2 8.061 12 7.890 22 7.479 32 6.840 42 5.994 52 4.966 62 3.787 72 2.493 82 1.123 3 8.055 13 7.859 23 7.425 33 6.765 43 5.900 53 4.854 63 3.662 73 2.358 83 0.983 | | | | | | | | | | | | | | | | |
| 3 | 8.055 | 13 | 7.859 | 23 | 7.425 | 33 | 6.765 | 43 | 5.900 | 53 | 4.854 | 63 | 3.662 | 73 | 2.358 | 83 | 0.983 |
| | | | | | | | 6.687 | | | | | | | | | | |
| 5 | 8.035 | 15 | 7.791 | 25 | 7.311 | 35 | 6.607 | 45 | 5.703 | 55 | 4.626 | 65 | 3.409 | 75 | 2.088 | 85 | 0.703 |
| 6 | 8.021 | 16 | 7.753 | 26 | 7.250 | 36 | 6.526 | 46 | 5.603 | 56 | 4.510 | 66 | 3.281 | 76 | 1.951 | 86 | 0.563 |
| | | | | | | | 6.442 | | | | | | | | | | |
| | | | | | | | 6.356 | | | | | | | | | | |
| 9 | 7.967 | 19 | 7.626 | 29 | 7.055 | 39 | 6.268 | 49 | 5.292 | 59 | 4.154 | 69 | 2.891 | 79 | 1.539 | 89 | 0.141 |

The number from this Table is r'.

TABLE XLII.

Lunar Nutation in R. A. to find s' = d'.

| Argument. | R. | A. of | f the | Star | in ' | Time |
|-----------|----|-------|-------|------|------|----------|
| Algument | LL | AL U | une | Star | 111 | I IIIIe. |

| C | | | 4 | | | | | | | | | | |
|------|------|-------|-------|--------|-------|-------|-------|-------|-------|-------|-------|-------|----|
| S. | - | + | - | + | - | + | - | + | - | + | - | + | S. |
| | Op | 12h | 1h | 13h | 2h | 14h | 3h | 15h | 4,h | 16h | 5h | 17h | |
| N. | + | _ | + | _ | + | - | + | _ | + | | + | | N. |
| P. P | 1 m. | " | P. P. | " | P. P. | // | P. P. | " | P. P. | " | P. P. | " | m. |
| + | 0 | 0.000 | + | 2.497 | + | 4.824 | + | 6.823 | + | 8.355 | + | 9.319 | 60 |
| 42 | | 0.421 | 40 | 2.901 | 34 | 5.185 | 26 | 7.113 | 17 | 8.558 | 4 | 9.419 | 50 |
| 84 | | 0.841 | 80 | 3.300 | 68 | 5.534 | 52 | 7.391 | 34 | 8.744 | 9 | 9.501 | 40 |
| 126 | | 1.260 | 120 | 3.693 | 102 | 5.874 | 78 | 7.655 | 51 | 8.914 | 14 | 9.566 | 30 |
| 168 | | 1.675 | 160 | 4.077 | 136 | 6.202 | 104 | 7.903 | 68 | 9.066 | 18 | 9.611 | 20 |
| 210 | | 2.088 | 200 | 4.4.55 | 170 | 6.518 | 130 | 8.137 | 85 | 9.202 | 22 | 9.639 | 10 |
| 252 | 60 | 2.497 | 240 | 4.824 | 204 | 6.823 | 156 | 8.355 | 102 | 9.319 | 27 | 9.648 | 0 |
| N. | 1 + | - | + | - | + | _ | + | _ | + | _ | + | | N. |
| | 111 | 1 23h | 10h | 22h | 9h | 21h | gh | 20h | 7h | 19h | 6h | 18h | |
| S. | | + | - | + | - | + | - | + | - | + | - | + | S. |

TABLES

FOR COMPUTING THE NUTATION OF A STAR IN RIGHT ASCENSION AND DECLINATION.

| TAI | | OF NU | LIII. | ٧. | TAB | | LE X or of N | LIV. | N. | | JATION | | LV. QUINOX ENSION | |
|--|--|--|--|--|--|--|--|--|--|--|--|--|---|---|
| R.A. | the Notar.—the Notar.—Star- | Lon- I | n in R. A Moon's N in Decl gns — L | Vode. lin. | R.A. For | the N Star— the N | Lon. Nutation | n in R. A Moon's N n in Dec | lode. | L | 0 | RGUME le of th Node | e Moon' | S |
| | | | S. S. II VIII — + | | | | | S. S. IIVIII — + | | | | | | |
| 0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 28 29 29 20 20 20 20 20 20 20 20 20 20 20 20 20 | 8.77 8.77 8.77 8.76 8.75 8.74 8.72 8.69 8.66 8.64 8.61 8.55 8.51 8.43 8.39 8.34 8.13 8.13 8.77 8.13 8.77 8.13 | 7.27 7.18 7.10 7.00 6.91 6.82 6.52 6.62 6.41 6.31 6.20 6.09 5.98 5.87 5.75 5.64 5.52 5.39 4.90 4.78 4.65 4.65 6.52 6.52 6.52 6.52 6.52 6.52 6.53 6.54 6.54 6.54 6.55 6.55 6.55 6.55 6.55 | 3.84 3.71 3.57 3,43 3.29 3.14 3.00 2.86 2.71 2.56 2.42 2.27 2.12 1.97 1.82 1.67 0.92 0.76 0.46 0.46 0.41 0.01 0.01 0.01 0.01 0.01 0.01 0.01 | 30 29 28 27 26 25 24 23 22 21 20 19 18 17 16 15 14 13 12 11 10 9 8 7 6 5 4 4 3 2 2 | 0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 26 27 28 28 28 29 29 20 20 20 20 20 20 20 20 20 20 20 20 20 | 1.29 1.28 1.28 1.28 1.28 1.28 1.29 1.27 1.27 1.27 1.26 1.25 1.24 1.24 1.21 1.20 1.19 1.18 1.17 1.16 1.15 1.14 1.13 1.12 1.11 | 1.09 1.08 1.07 1.06 1.07 1.00 0.98 0.97 0.95 0.94 0.92 0.88 0.86 0.84 0.79 0.77 0.76 0.74 0.72 0.70 0.68 0.66 0.64 | 0.48 0.46 0.44 0.42 0.40 0.38 0.35 0.27 0.25 0.22 0.20 0.18 0.16 0.13 0.11 0.09 0.07 0.04 | 30 29 28 27 26 25 24 22 21 20 19 18 11 16 15 14 13 12 11 | 0 1 2 3 4 4 5 6 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 26 27 28 28 28 29 29 20 20 20 20 20 20 20 20 20 20 20 20 20 | 2.40 2.70 2.99 3.29 3.59 3.88 4.17 4.46 4.75 5.04 5.33 5.61 5.90 6.18 6.46 6.74 7.01 7.29 7.56 7.83 8.10 8.36 | 8.62 8.88 9.14 9.39 9.64 9.89 10.14 10.38 10.62 11.08 11.31 11.76 11.98 12.19 12.40 12.61 12.81 13.01 13.59 14.13 14.30 14.46 14.62 14.78 14.78 14.78 | " 14.93 15.08 15.23 15.36 15.50 15.63 15.75 15.87 15.99 16.10 16.20 16.30 16.49 16.58 16.68 16.67 16.88 17.03 17.18 17.15 17.18 17.20 17.22 17.23 17.24 17.24 | 30 29 28 27 26 25 24 23 22 21 20 19 18 17 16 15 14 13 12 11 10 9 8 7 6 5 |
| | S. S. | S. S. | | | | S. S. | S. S. | | | | S. S. | S. S. | S. S. IX III | |

To find the Nutation of a Star in Right Ascension.

To the log of the sum or difference of the equations from Tables XLIII. XLIV. answering to their proper arguments, add the log. tangent of the Star's declination; the sum will be the log. of part first of nutation, and if the declination is south, change the sign-to which apply the equation from Table XLV. answering to the longitude of the Moon's node, and the sum or difference will be the nutation in right ascension.

To find the Nutation of a Star in Declination.

Increase the arguments of Tables XLIII. and XLIV. each by the three signs, and the sum or difference of the corresponding equations will be the nutation in declination. If the declination is south change the sign of the second equation.

FOR COMPUTING THE ABERRATION OF A STAR IN RIGHT ASCENSION AND DECLINATION.

| TABLE XLVI. | TABLE XLVII. | TABLE XLVIII. |
|--|--|---|
| OR | OR | OR |
| | TABLE II. OF ABERRATION. | TABLE III. OF ABERRATION. |
| TABLE I. OF ABERRATION. | TABLE II. OF ABERRATION. | |
| ARGUMENT. | ARGUMENT. | ARGUMENT. |
| For the Aberration of R.A. | For the Aberration in R.A. | |
| A Lawrence . | | For part 2d of Aber. in Decl. |
| R.A. Star-Lon. Sun. | R.A. Star+Sun's Lon. | Sun's Lon.+Star's Decl. |
| | For the Aberration in Decl. | For part 3d Aber. in Decl. |
| R. Ascen. Star + 3 signs - Sun's | R. Ascen. Star+3 signs+Sun's | |
| Lon. | · Decl. | Sun's Lon.+Star's Decl. |
| S. S. S. S. S. S. | S. S. S. S. S. S. | S. S. IS. S. S. S. F. |
| O VI I VII II VIII | O VI IV II II VIII | O VI IVII II VIII |
| -+-+-+ | +-+-+- | -+-+-+ |
| 0 // // // 0 | 0 / // // 0 | , 0 // // // 0 |
| 0 19.42 16.82 9.71 30 | 0 0.84 0.73 0.42 30 | 0 4.03 3.49 2.02 30 |
| 1 19.41 16.64 9.41 29 2 19.40 16.47 9.12 28 | 1 0.84 0.72 0.41 29 2 0.84 0.71 0.39 28 | 1 4.03 3.46 1.96 29 2 4.03 3.42 1.89 28 |
| 3 19.39 16.29 8.82 27 | 2 0.84 0.71 0.39 28 3 0.84 0.70 0.38 27 | 2 4.03 3.42 1.89 28 3 4.03 3.38 1.83 27 |
| 4 19.37 16.10 8.51 26 | 4 0.84 0.69 0.37 26 | 4 4.02 3.34 1.77 26 |
| 5 19.34 15.91 8.21 25 | 5 0.83 0.69 0.35 25 | 5 4.02 3.30 1.70 25 |
| 6 19.31 15.71 7.90 24 | 6 0.83 0.68 0.34 24 | 6 4.01 3.26 1.64 24 |
| 7 19.27 15.51 7.59 23 8 19.23 15.30 7.27 22 | 7 0 83 0.67 0.33 23 8 0.83 0.66 0.31 22 | 7 4.00 3.22 1.58 23 |
| 8 19.23 15.30 7.27 22 9 19.18 15.09 6.96 21 | 8 0.83 0.66 0.31 22 9 0.83 0.65 0.30 21 | 8 3.99 3.18 1.51 22 9 3.98 3.13 1.45 21 |
| 10 19.12 14.88 6.64 20 | 10 0.83 0.64 0.29 20 | 10 3.97 3.09 1.38 20 |
| 11 19.06 14.66 6.32 19 | 11 0.82 0.63 0.27 19 | 11 3.96 3.04 1.31 19 |
| 12 13.99 14.43 6.00 18 | 12 0.82 0.62 0.26 18 | 12 3.95 3.00 1.25 18 |
| 13 18.92 14.20 5.68 17 | 13 0.82 0.61 0.25 17 | 13 3.93 2.95 1.18 17 |
| 14 18.84 13.97 5.35 16 | 14 0.81 0.60 0.23 16 | 14 3.91 2.90 1.11 16 |
| 15 18.76 13.73 5.03 15 16 18.67 13.49 4.70 14 | 15 0.81 0.59 0.22 15 16 0.81 0.58 0.20 14 | 15 3.90 2.85 1.04 15 16 3.88 2.80 0.98 14 |
| 17 18.57 13.24 4.37 13 | 17 0.80 0.57 0.19 13 | 16 3.88 2.80 0.98 14 17 3.86 2.75 0.91 13 |
| 18 18.47 12.99 4.04 12 | 18 0.80 0.56 0.17 12 | 18 3.84 2.70 0.84 12 |
| 19 18 36 12.74 3.71 11 | 19 0.79 0.55 0.16 11 | 19 3.81 2.65 0.77 11 |
| 20 18.25 12.48 3.37 10 | 20 0.79 0.54 0.15 10 | 20 3.79 2.59 0.70 10 |
| 21 18.13 12.22 3 04 9 | 21 0.78 0.53 0.13 9 | 21 3.77 2.54 0.63 9 |
| 22 18.00 11.96 2.70 8 23 17.87 11.69 2.37 7 | 22 0.78 0.52 0.12 8 23 0.77 0.50 0.10 7 | 22 3.74 2.48 0.56 8 23 3.71 2.43 0.49 7 |
| 23 17.87 11.69 2.37 7 24 17.74 11.41 2.03 6 | 23 0.77 0.50 0.10 7 24 0.77 0.49 0.09 6 | 23 3.71 2.43 0.49 7 24 3.68 2.37 0.42 6 |
| 25 17.60 11.14 1.69 5 | 25 0.76 0.48 0.07 5 | 25 3.66 2.31 0.35 5 |
| 26 17.45 10.86 1.35 4 | 26 0.75 0.47 0.06 4 | 26 3.63 2.26 0.28 4 |
| 27 17.30 10.58 1.02 3 | 27 0.75 0.46 0.04 3 | 27 3.59 2.20 0.21 3 |
| 28 17·15 10.29 0.68 2 29 16·98 10.00 0.31 1 | 28 0.74 0.44 0.03 2 | 28 3.56 2.14 0.14 2 |
| 29 16.98 10.00 0.31 1 30 16.82 9.71 0.00 0 | 29 0.73 0.43 0 02 1 1 1 1 1 1 1 1 1 | 29 3.53 2.08 0.07 1 30 3.49 2.02 0.00 0 |
| -+-+-+ | + - + - + - | -+-+-+ |
| S. S. S. S. S. | S. S. S. S. S. | S. S. S. S. S. |
| XIV XIV IX III | XI V X IV IX III | XI V X IV IX III |
| | | |

To find the Aberration of a Star in Right Ascension.

To the log. of the sum or difference of the equations from Tables XLVI. XLVII. answering to their arguments, add the log. secant of the Star's declination, the sum will be the log. of the aberration in right ascension.

To find the Aberration of a Star in Declination.

Find the sum or difference of the equations answering to the former arguments, increased by 111 signs, to the log. of which, add the log. sine of the Star's declination; the sum will be the log of part 1st of the aberration. Take parts second and third of aberration from Table XLVIII. which, applied to the former, will give the aberration in declination. If the Star's declination is south, change the sign of parts 2d and 3d.

| _ | | | | | | - | | _ | | | | _ | | | - | | 103 |
|-----|----------------|------------|--------|---------------------|-----------------------|-------|------|-----------------|----------|----------|-----------------|------|-----------------|--------------|----------------|-------------|----------|
| - | | | | | | | | | | | | - | | TAI | BLE I | II. | 103 |
| L | TAE | BLE | XLIX | ζ. | - | | | | | | 1 | | Lun | Nut. | | | noxes |
| Ī | Mean | Obliqu | ity of | the | 12. | | | | | | | 4 | | | R.A | | |
| X | ear ' | o / | . 6. | | | | TA | BL | EL | III. | | 3 | Long. Moon's | o vi | T VII | | Moon's |
| | 800 2 | | | 6.24 | - 3 | | | | | | | | Node. | | 11 | - | Node. |
| | 810 2 820 2 | | | $\frac{1.83}{7.41}$ | Sol N | Just | of t | he | Equi | noxe | s in R. | Ā. | 0 | s 0.00 | s 0.55 | s 0.97 | 30 |
| | 830 2 | | | 3.00 | | 1, | | | <u>-</u> | - | 1 | | 2 | 0.04 | 0.59 | 0.98 | 28 |
| Γ | Annu | ial Dir | ninuti | on. | Sun | 0 | C | VI | 1- | VII | Sun's | 8 | 6 | 0.08 | 0.62 | 1.00 | 26 |
| ı, | 16 | 0.44 | 13 | 12/ | Lon | - 111 | | III | 1 | IV + | Long | - 3 | 8 | 0.11 | 0.69 | 1.02 | 22 |
| | - | hly Di | - | the same | 0 | - | + s | + | + | + | | - | 10 | 0.19 | 0.71 | 1.04 | 20 |
| • | an. | 1 | 0.0 | | 0 | | | 00 | 0 | .06 | 30 | 1 | 12 14 | 0.23 | $0.75 \\ 0.78$ | 1.05 | 18 |
| 100 | March | 1 | 0.0 | | 5 | | | 02 | | .07 | 25 | | 16 | 0.30 | 0.81 | 1.07 | 14 |
| | April | $^{1}_{1}$ | 0. | | 10 15 | -6 | | 03 | | .07 | 20 15 | | 18 | 0.34 | 0.83 | 1.08 | 12 |
| | May | i | 0. | | 20 | -3 | 0. | 05 | . 1 | .07 | 10 | | 20 | 0.37 | 0.86 | 1.09 1.09 | 10 |
| J | luly | 1 | 0.9 | 22 | 25 | -1 | | 06 | | .06 | 5 | | 24 | 0.44 | 0.90 | 1.10 | 6 |
| | Augusept. | st 1 | 0.5 | - | 30 | 1 | | 00 | -0 | 0.06 | 0 | | 26 28 | 0.48 | 0.92 | 1.10 1.10 | 4 2 |
| | Oct. | 1 | 0.5 | | | - | 11 V | III | | | | | 30 | 0.56 | 0.93 | 1.10 | 1 |
| | Nov. | 1 | 0.5 | | | | ΧI | V | | - | | | | XI V | XIV | IXI | |
| F | Dec. | 1 | 0.4 | | 100 - | 1 | + | + | 1 1 1 | ** | {o | | - | + - | | - + - | |
| 1 | | Sal. | n El | | ABLE | - | - | | 1 | | 41 19 | | 7 | ABL | E'LI. | | |
| 1 | Mo | on's t | | 1 | on of t | | | - | ndin | œ. | 7 | J | Lunar | Equa | ion of | the | |
| ۱ | | Long. | | Equ | ation. | | | | e Mo | | 6 04 | | | Obliqu | | 100 | 7 9 9 |
| 1 | 8 | 1 5 | S | | - 1 | - | | 1 | 1.71 | | - | 64 | 8 cosi | n Long | g. Moc | | |
| ı | 0 | 0 | VI | 1 | 0.43 | 3.5 | | 01 | 7 | 00 | Long. Moon's | 0 | VI | I VII | IIVI | | Long. |
| | 0 | 0 5 | VI | | 0.43 | Ma | | 26 | Sept. | 23 | Node. | + | - | + | + - | - | Node. |
| 1 | | 10 | 9:1 | | 0.41 | | | 31 | Oct. | 3 | 0 | | " | " | " | 7 | H |
| ı | | 15 20 | | | 0.37° 0.33 | Apı | | 5 10 | | 9 14 | 0 | 1 | 0.65 | 8.34 | 4.8 | | 30 |
| ۱ | | 25 | | | 0.29 | 10 | | 15 | | 19 | 1 2 | | 0.64 | 8.25 8.16 | 4.5 | | 29 28 |
| ı | 1 | 0 | VII | | 0.22 | | | 20 | | 24 | 3 | 9 | .62 | 8.08 | 43 | | 27 |
| ı | | 5 10 | | | $0.15 \\ 0.08$ | Ma | | 25 1 | Nov. | 29 | 4 5 | 1 10 | 0.61 | 7.94 | 4.2 | | 26 25 |
| 1 | | 15 | | | 0.00 | £., | | 6 | | 8 | .6 | - | 0.58 | 7.79 | 3.9 | 2 | 24 |
| ı | | 20 25 | | | 0.08 0.22 | 6 | | 11 16 | | 13 18 | 7 | | 0.56 | 7.69 | 3.7 | | 23 |
| 1 | II | 0 | VIII | | 0.29 | | | $\frac{10}{21}$ | | 22 | 8 9 | 100 | 0.54 | 7.59 | 3.6 | | 22 21 |
| ı | | 5 | , 111 | | 0.33 | | | 27 | 21 | 27 | 10 | 3. | 0.50 | .7.38 | 3 3 | 9 | 20 |
| 1 | | 10 | | | 0.37 | Jur | ne | 1 6 | Dec. | 2 | 11 | | 0.46 | 7.27 | 3.1 | | 19 18 |
| | | 20 | | 1 | 0.43 | | 1-7 | 11 | | .12 | 13 | 9 | .39 | 7.04 | 2.8 | | 17 |
| | | 25 | 777 | | 0.43 | | | 16 | | 17 | 14 | | 35 | 6.93 | 2.6 | | 16 |
| | III | 0 5 | IX | | 0.43 | 1 | | 22 | | 22 | 15 16 | 1 | 0.31 | 6.81 | 2.4 | | 15 14 |
| Į | 11 | 10 | | 1 | 0.37 | Jul | | 2. | Jan. | 1 | 17 | 9 | .21 | 6.57 | 2.1 | 7 | 13 |
| | | 15 20 | | | 0.33 | | | 7 | | 6 | 18 | |).16 | 6.45 | 2.0 1.8 | | 12 11 |
| | | 25 | | | $0.29 \\ 0.22$ | 100 | | 13 18 | | 16 | 20 | | 0.06 | 6.32 | 1.6 | | 10 |
| | īV | 0 | X | | 0.15 | - | | 23 | | 20 | 21 | | 3.99 | 6.06 | 1.5 | 1 | 9 |
| | | 5 | 110 | | 0.08 | 1 | | 28 | | 25 | 22 23 | | 3.93 | 5.93 5.80 | 1.3 | | 8 7 |
| 1 | - | 10 15 | | | 0.00 | Au | g. | 8 | Feb. | 30 | 24 | 8 | 3.80 | 5.66 | 1.0 | 1 | 6 |
| 1 | | 20 | | | 0.15 | | | 13 | | 9 | 25 | | 3.73 3.65 | 5.53 | 0.8 | | 5 |
| | v | 25 0 | XI | | 0.22 | | | 18 | | 14 | 26 27 | | 3.57 | 5.38 5.25 | 0.6 | | 4 3 |
| | - | 5 | AI | | 0.33 | | | 29 | | 24 | 23 | 8 | 3.50 | 5.11 | 0.3 | 3 | 2 |
| | 1 | 10 | | - | 0.38 | Ser | | 3 | Mar. | _ 1 | 30 | | 3.43 | 4.96 | 0.1 | | 1 0 |
| | | 15 20 | | | $0.41 \\ 0.43$ | | | 13 | | 6 11 | - 50 | + | | + - | + - | _ | |
| | | 25 | -,- | | 0.43 | | | 18 | | 16 | | | | X IV | | II | |
| | VI | 0 | XII | 10 | 0.43 | - | - | 23 | | 21 | | | -44- | 141 | (10) | 2000 | S-111 |

| 104 | Cha- Constellations Pr. Name, Mag. Right Annual Declination Annual | | | | | | | | | | | | | | |
|------------------|---|------------|---|----|----|------|---|------|----|----|------|---------------|--|--|--|
| Cha- racters. | Characters. Constellations. Pr. Name. Mag. Right Ascension. Var. Declination. Var. Var. k m s s s '' '' | | | | | | | | | | | | | | |
| | | | | | | | | | | , | | | | | |
| α | Ursæ Minoris | Pole Star | 2 | 0 | | | | | | | 29 N | | | | |
| 06 | Eridani | Achernar | 1 | 1 | 31 | 18.0 | | 2.24 | | 19 | | -18.52 | | | |
| æ | ARIETIS | | 2 | 1 | 57 | 29.9 | | 3.36 | | 38 | 42 N | | | | |
| α | TAURI | Aldebaran | 1 | 4 | | | + | 3.43 | | 9 | 21 N | | | | |
| α | Aurigæ | Capella | 1 | 5 | | 0.0 | | 4.41 | | 48 | 45 N | + 4.54 | | | |
| β | Orionis | Rigel | 1 | 5 | | 16.6 | | 2.88 | | 24 | | | | | |
| 2 | Orionis | Bellatrix | 2 | 5 | 15 | 54.6 | | 3.22 | | 11 | 11 N | + 4.01 | | | |
| α | Orionis | Betelguese | 1 | 5 | 45 | 51.9 | | 3.25 | | 22 | | + 1.36 | | | |
| α | Navis | Canopus | 1 | 6 | 20 | 8.2 | | 1.33 | | 36 | | + 1.68 | | | |
| Œ | Canis Majoris | Sirius | 1 | 6 | 37 | 34.1 | + | 2.64 | 16 | 29 | | + 4.41 | | | |
| α | Geminorum | Castor | 1 | 7 | 23 | 36.9 | + | 3.85 | 32 | 15 | 26 N | _ 7.12 | | | |
| α | Canis Minoris | Procyon | 1 | 7 | | 18.0 | | 3.17 | | 39 | 32 N | | | | |
| β | GEMINORUM | Pollux | 1 | 7 | - | 47.0 | | 3.69 | | 26 | 3 N | | | | |
| β | Navis | 1000 | 1 | 9 | 11 | | | 0.75 | | 0 | | + 14.85 | | | |
| α | Leonis | Regulus | 1 | 9 | 59 | 12.4 | + | 3.21 | 12 | 48 | 18 N | —17.23 | | | |
| OS. | Ursæ Majoris | Dubhe | 2 | 10 | 53 | 2.5 | + | 3.83 | 62 | 40 | 40 N | -19.26 | | | |
| | Crucis | 11/2 | 1 | 12 | 17 | 7.7 | + | 3.25 | 62 | 7 | | + 20.02 | | | |
| a | Virginis | Spica | 1 | 13 | 16 | 8.8 | + | 3.14 | - | 15 | 35 S | +18.94 | | | |
| β | Centauri | 11 | 1 | 13 | 51 | | | 4.12 | | 32 | 11 S | | | | |
| α | Draconis | 31 | 2 | 13 | 59 | 44.2 | + | 1.64 | 65 | 12 | 2 N | 17.42 | | | |
| α | Bootis | Arcturus | 1 | 14 | 7 | 49.3 | + | 2.73 | 20 | 4 | 56 N | -18.97 | | | |
| α | Centauri | | 1 | 14 | 28 | 36.6 | + | 4.45 | 60 | 8 | | + 16.12 | | | |
| a | 2 Libræ | Zubenesch | 2 | 14 | 41 | 22.9 | + | 3.30 | | 19 | | + 15.25 | | | |
| | Scorpionis | Antares | 1 | 16 | 18 | 52.5 | | 3.66 | | 2 | 27 S | | | | |
| α | Draconis | Rastaban | 3 | 17 | 52 | 37.1 | + | 1.38 | 51 | 30 | 46 N | 0.67 | | | |
| æ | Lyræ | Vega | 1 | 18 | 31 | 7.2 | + | 2.03 | 38 | 37 | 44 N | + 3.02 | | | |
| | AQUILE | Altair | 1 | 19 | 42 | 23.6 | + | 2.93 | 8 | 25 | 15 N | + 9.06 | | | |
| | Aquarii | 7 11 20 11 | 3 | 21 | 56 | 57.0 | + | 3.09 | | 9 | 6 S | | | | |
| | Gruis | | 2 | 21 | 56 | 57.9 | + | 3.85 | | 48 | | -17,18 | | | |
| | Pis. Austr. | Fomalhaut | 1 | 22 | 43 | 7.7 | + | 3.34 | | | | -18.86 | | | |
| α | PEGASI | Marcab | 2 | 22 | 56 | 12.1 | + | 2.98 | 14 | 16 | 53 N | + 19.3 | | | |

TABLE LIV.—Decimal Numbers for each Day in the Year.

| | | | 0 | | 7 | f 2 | Mot | nths. | 13 | 12.4 | | | | |
|---|-----|-------|-------|-------|--------|-------|-------|-------|-------|----------|-------|-------|-------|---|
| ė | D. | Jan. | Feb. | March | April. | May. | June. | July. | Aug. | Sept. | Oct. | Nov. | Dec. | |
| | | | 0.085 | | | | | | | | | 0.832 | | |
| | 2 | 0.003 | 0.088 | 0.164 | 0.249 | 0.331 | 0.416 | 0.499 | 0.583 | | | 0.835 | | |
| | | | 0.091 | | | | | | | 0-0 - 00 | | 0.833 | | |
| | | | 0.093 | | | | | | | | | | 0.922 | |
| | 5 | 0.011 | 0.096 | 0.173 | 0.258 | 0.340 | 0.425 | 0.507 | 0.592 | 0.675 | 0.758 | 0.843 | 0.925 | |
| | 6 | 0.014 | 0.099 | 0.175 | 0.260 | 0.342 | 0.427 | 0.509 | 0.594 | 0.678 | 0.760 | 0.845 | 0.928 | |
| | 17 | 0.017 | 0.102 | 0.178 | 0.263 | 0.345 | 0.430 | 0.512 | 0.597 | 0.681 | 0.763 | 0.848 | 0.931 | |
| | 8 | 0.019 | 0.104 | 0.181 | 0.266 | 0.348 | 0.433 | 0.515 | 0.600 | 0.684 | 0.766 | 0.951 | 0.933 | |
| | 9 | 0.022 | 0.107 | 0.184 | 0.269 | 0.351 | 0.436 | 0.518 | 0.602 | 0.687 | 0.769 | 0.854 | 0.936 | |
| | 10 | 0.025 | 0.109 | 0.186 | 0.271 | 0.353 | 0.438 | 0.520 | 0.605 | 0.689 | 0.772 | 0.856 | 0.939 | |
| | 111 | 0.028 | 0.112 | 0.189 | 0.274 | 0.356 | 0.441 | 0.523 | 0.608 | 0.692 | 0.775 | 0.859 | 0.942 | |
| | 12 | 0.030 | 0.115 | 0.192 | 0.277 | 0.359 | 0.444 | 0.526 | 0.610 | 0.695 | 0.777 | 0.862 | 0.944 | |
| | 13 | 0.033 | 0.118 | 0.195 | 0.280 | 0.362 | 0.447 | 0.529 | 0.613 | 0.698 | 0.780 | 0.865 | 0.947 | |
| | 14 | 0.036 | 0.120 | 0.197 | 0.282 | 0.364 | 0.449 | 0.531 | 0.616 | 0.701 | 0.782 | 0.867 | 0.950 | |
| | 15 | 0.039 | 0.123 | 0.200 | 0.285 | 0.367 | 0.452 | 0.534 | 0.619 | 0.703 | 0.785 | 0.870 | 0.953 | |
| | 16 | 0.041 | 0.127 | 0.203 | 0.288 | 0.370 | 0.455 | 0.537 | 0.622 | 0.706 | 0.788 | 0.873 | 0.955 | |
| | 17 | 0.044 | 0.129 | 0.206 | 0.291 | 0.373 | 0.458 | 0.540 | 0.625 | 0.709 | 0.791 | 0.876 | 0.958 | ı |
| | 18 | 0.046 | 0.131 | 0.208 | 0.293 | 0.375 | 0.460 | 0.542 | 0.627 | 0.711 | 0.793 | 0.878 | 0.961 | |
| | 19 | 0.049 | 0.134 | 0.211 | 0.296 | 0.378 | 0.463 | 0.545 | 0.630 | 0.714 | 0.796 | 0.882 | 0.964 | |
| | 20 | 0.052 | 0.137 | 0.214 | 0.299 | 0.381 | 0.466 | 0.548 | 0.633 | 0.717 | 0.799 | 0.884 | 0.966 | |
| | 21 | 0.056 | 0.140 | 0.217 | 0.302 | 0.383 | 0.468 | 0.551 | 0.636 | 0.720 | 0.802 | 0.887 | 0.969 | |
| | 22 | 0.057 | 0.142 | 0.219 | 0.304 | 0.386 | 0.471 | 0.553 | 0.638 | 0.722 | 0.804 | 0.890 | 0.971 | |
| | | | | | | | | | | | | 0.893 | | |
| | 24 | 0.063 | 0.148 | 0.225 | 0.309 | 0.392 | 0.476 | 0.559 | 0.644 | 0.728 | 0.810 | 0.895 | 0.977 | |
| | 25 | 0.066 | 0.151 | 0.227 | 0.312 | 0.395 | 0.479 | 0.562 | 0.647 | 0.731 | 0.813 | 0.898 | 0.980 | |
| | 26 | 0.068 | 0.153 | 0.230 | 0.315 | 0.397 | 0.482 | 0.564 | 0.649 | 0.733 | 0.815 | 0.900 | 0.283 | |
| | | | | | | | | | | | | 0.903 | | |
| | | | | | | | | | | | | 0.906 | | |
| | 29 | 0.077 | 0.162 | | | | | | | | | 0.909 | | |
| | 30 | 0.079 | | 0.241 | 0.326 | 0.408 | 0.493 | 0.575 | 0.660 | | | 0.912 | | |
| | 31 | 0.082 | | 0.244 | | 0.411 | | 0.578 | 0.663 | | 0.829 | | 0.997 | |

| | | | | TABLE | | | , 10. |
|---|----------|----------------------|---------------------------|----------------------|----------------------|------------------------|----------------------|
| | 15 (1) | | | March. | ry Day in the Y | | 1-00 |
| | Days. | January. | February. | h m s | April. | May. | June. |
| ľ | -1 | 18 44 5 | 20 56 36 | 22 49 40 | 0 43 11 | 2 34 27 | h m s 4 37 12 |
| ı | 2 | 18 48 30 | 21 0 41 | 22 53 24 | 0 46 49 | 2 38 16 | 4 41 18 |
| | 3 4 | 18 52 55 18 57 19 | 21 4 45 21 8 47 | 22 57 7 23 0 51 | 0 50 27 | 2 42 6 2 45 56 | 4 45 24 4 49 31 |
| | . 5 | 19 1 43 | 21 12 50 | 23 4 33 | 0 57 45 | 2 49 47 | 4 53 38 |
| 1 | 6 | 19 6 7 | 21 16 51 | 23 8 16 | 1 1 24 | 2 53 38 | 4 57 45 |
| | 8 | 19 10 30 19 14 52 | 21 20 51 21 24 51 | 23 11 57 23 15 39 | 1 5 3 | 2 57 30 3 1 23 | 5 1 52 5 6 0 |
| И | - 9 | 19 19 14 | 21 28 50 | 23 19 20 | 1 12 22 | 2 5 16 | 5 10 8 |
| ı | 10 | 19 23 36 | 21 32 45 | 23 23 1 | 1 16 2 | 3 9 10 3 13 4 | 5 14 17 |
| Į | 11 | 19 27 57 | 21 36 45 21 40 42 | 23 26 41 23 30 22 | 1 19 42 1 23 23 | 3 13 4 3 16 59 | 5 18 25 5 22 34 |
| | 13 | 19 36 37 | 21 44 38 | 23 34 1 | 1 27 3 | 3 20 55 | 5 26 43 |
| ı | 14 | 19 40 57 19 45 15 | 21 4, 33 21 52 27 | 23 37 41 23 41 21 | 1 30 45 | 3 24 51 3 28 48 | 5 30 52 |
| ı | 15 16 | 19 45 15 19 49 33 | 21 56 21 | 23 41 21 23 45 0 | 1 34 26 | 3 32 45 | 5 35 2 5 39 11 |
| 1 | 17 | 19 53 50 | 22 0 14 | 23 48 39 | 1 41 50 | 3 36 43 | 5 43 20 |
| ı | 18 | 19 58 7 | 22 4 6 22 7 57 | 23 52 18 23 55 56 | 1 45 33 1 49 16 | 3 40 42 3 44 40 | 5 49 30 |
| ı | 19 20 | 20 2 23 | 22 11 48 | 23 55 56 23 59 35 | 1 49 16 1 52 59 | 3 44 40 3 48 40 | 5 51 39 5 55 49 |
| ı | 21 | 20 10 52 | 22 15 38 | 0 3 13 | 1 56 43 | 3 52 40 | 5 59 59 |
| ı | 22 | 20 15 6 20 19 19 | 22 19 27 22 23 16 | 0 6 51 0 10 29 | 2 0 27 2 4 12 | 3 56 41 4 0 42 | 6 4 8 |
| ı | 23 | 20 23 31 | 22 27 4 | 0 10 29 | 2 7 57 | 4 4 43 | 6 8 18 |
| ı | 25 | 20,27 42 | 22 30 52 | 0 17 45 | 2 11 43 | 4 8 45 | 6 16 36 |
| I | 26 27 | 20 31 52 20 36 1 | 22 34 38 22 38 25 | 0 21 23 | 2 15 29 2 19 15 | 4 12 48 4 16 51 | 6 20 45 6 24 54 |
| ı | 28 | 20 40 10. | 22 42 10 | 0 28 39 | 2 23 2 | 4 20 54 | 6 24 54 6 29 3 |
| ı | 29 | 20 44 18 | 22 45 55 | 0 33 17 | 2 26 50 | 4 24 58 | 6 33 11 |
| 1 | 30 | 20 48 25 20 52 31 | 2.02 | 0 35 55 | 2 30 38 | 4 29 2 4 33 7 | 6 37 20 |
| 1 | Days. | July. | August. | September. | October. | November. | December. |
| ı | 1110 | h m s | h m s | h m s | h m s | h m s | h, -m - s |
| 1 | 1 2 | 6 41 23 6 45 36 | 8 46 14 8 50 6 | 10 42 14 10 45 52 | 12 30 19 12 33 57 | 14 26 39 14 30 35 | 16 30 36 16 34 56 |
| ı | 3 | 6 49 44 | 8 53 58 | 10 49 29 | 12 37 35 | 14 34 32 | 16 39 16 |
| 1 | 4 | 6 53 51 | 8 57 50 | 10 53 6 | 12 41 13 | 14 38 30 | 16 43 37 |
| ı | 5 6 | 6 57 58 | 9 1 41 9 5 31 | 10 56 43 11 0 20 | 12 44 52 12 48 31 | 14 42 28 | 16 47 59 16 52 21 |
| ı | 7 | 7 6 11 | 9 9 21 | 11 3 56 | 12 52 11 | 14 50 27 | 16 56 44 |
| ı | 8 | 7 10 18 | 9 14 10 | 11 7 33 | 12 55 51 | 14 54 28 | 17 1 7 |
| 1 | 9 | 7 14 23 7 13 29 | 9 16 59 9 20 47 | 11 11 9 1 11 14 45 | 12 59 31 13 3 12 | 14 58 30 15 2 33 | 17 5 31 17 9 55 |
| 1 | 11 | 7 22 34 | 9 24 34 | 11 18 21 | 13 3 53 | 15 6 36 | 17 14 20 |
| 1 | 12 | 7 26 38 7 30 42 | 9 28 21 9 32 7 | 11 21 56 11 25 32 | 13 10 35 13 14 17 | 15 10 41 15 14 46 | 17 18 44 17 23 10 |
| 1 | 14 | 7 30 42 7 34 46 | 9 35 53 | 11 29 8 | 13 18 0 | 15 18 52 | 17 23 10 17 27 35 |
| 1 | 15 | 7 38 49 | 9 49 38 | 11 32 43 | 13 21 44 | 15 22 59 | 17 32 1 |
| 1 | 16 | 7 42 51 7 46 53 | 9 43 23 9 47 7 | 11 36 19 11 39 54 | 13 24 28 13 29 12 | 15 27 6 15 31 15 | 17 36 27 17 40 53 |
| 1 | 18 | 7 50 55 | 9 50 51 | 11 43 29 | 13 32 57 | 15 35 24 | 17 45 19 |
| 1 | 19 | 7 54 55 | 9 54 34 | 11 47 5 | 13 36 43 | 15 39 34 | 17 49 45 |
| 1 | 20 21 | 7 58 56 8 2 56 | 9 58 16 10 1 58 | 11 50 40 | 13 40 29 13 44 16 | 15 43 45 15 47 57 | 17 54 12 17 58 38 |
| 1 | 22 | 8 6 55 | 10 5 40 | 11 57 51 | 13 48 3 | 15 52 9 | 18 3 5 |
| I | 23 | 8 10 53 | 10 9 21 | 12 1 27 | 13 51 52 13 55 41 | 15 56 22 16 0 36 | 18 7 31 |
| 1 | 24 25 | 8 14 51 8 18 49 | 10 13 2 10 16 42 | 12 5 3 12 8 39 | 13 55 41 | 16 4 51 | 18 11 58 18 16 25 |
| 1 | 26 | 8 22 45 | 10 20 22 | 12 12 15 | 14' 3 21 | 16 9 7 | 18 20 51 |
| I | 27 | 8 25 42 | 10 24 2 10 27 41 | 12 15 51 12 19 28 | 14 7 12 | 16 13 23 16 17 40 | 18 25 17 18 29 44 |
| 1 | 28 29 | 8 30 37 8 34 32 | 10 27 41 10 31 20 | 12 19 28 | 14 14 56 | 16 21 58 | 18 34 10 |
| | 30 | 8 38 26 | 10 34 58 | 12 26 42 | 14 18 50 | 16 26 17 | 18 38 35 |
| 1 | 31 | 8 42 20 1 | 10 38 36 | | 14 22 44 | Н | 18 43 1 |
| | | - | | | | 14 - 11 - | |

| 10 | 6 | TABLE | LVII.—Sun's | Declination for | r every Day in | the Year 1828 | 3. |
|------|---|-------------------------|----------------------|-----------------------|----------------------|----------------------|----------------------|
| 17 | J | anuary. | February. | March. | April. | May. | June. |
| Da | ys. | South. | South. | South. | North. | North. | North. |
| - | | 0 / .// | 0 . / // | 0/_ // | 0-1 11 | 0-1-11- | - 0 / H |
| 1 | 1 2 2 | | 17 17 44 17 0 43 | 7 28 10 7 5 18 | 4 38 49 5 1 52 | 15 9 11 15 27 8 | 22 5 43 |
| | 2 2 3 2 | - 10.1 | 16 43 23 | 6 42 21 | 5 24 50 | 15 27 8 15 44 50 | 22 13 37 22 21 7 |
| 4 | 4 2 | | 16 25 46 | 6 19 18 | 5 47 43 | 16 2 17 | 22 28 14 |
| | 5 2 | | 16 7 53 | 5 56 9 | 6 10 29 | 16 19 27 | 22 34 57 |
| 10. | 6 2 2 | | 15 49 42 15 31 15 | 5 32 56 5 9 38 | 6 33 9 6 55 43 | 16 36 22 16 53 0 | 22 41 17 22 47 12 |
| 100 | 8 2 | | 15 12 32 | 4 46 15 | 7 18 10 | 17 9 22 | 22 47 12 22 52 44 |
| 1 | 9 2 | | 14 53 34 | 4 22 50 | 7 40 30 | 17 25 26 | 22 57 52 |
| | 0 2 | | 14 34 21 | 3 59 21 3 35 48 | 8 2 42 | 17 41 13 17 56 43 | 23 2 36 |
| | 1 2 2 | | 14 14 53 13 55 10 | 3 35 48 3 12 13 | 8 24 46 8 46 42 | 17 56 43 18 11 54 | 23 6 55 23 10 50 |
| | 3 2 | | 13 35 14 | 2 48 36 | 9 8 29 | 18 26 48 | 23 14 20 |
| | 4 2 | 1 25 59 | 13 15 5 | 2 34 57 | 9 30 6 | 18 41 22 | 23 17 26 |
| | 5 2 | | 12 54 43 12 34 8 | 2 1 16 1 37 35 | 9 51 35 10 12 54 | 18 55 38 19 9 35 | 23 20 7 |
| | 6 2 2 | | 12 34 8 12 13 21 | 1 13 52 | 10 12 54 10 34 2 | 19 9 35 19 23 12 | 23 22 24 23 24 16 |
| 0-1 | 8 2 | | 11 52 22 | 0 50 10 | 10 55 1 | 19 36 29 | 23 25 43 |
| | 9 2 | 7 1 | 11 31 13 | 0 26 27 | 11 15 48 | 19 49 27 | 23 26 45 |
| | 0 2 | | 11 9 52 10 48 22 | 0 2 45 S 0 20 56 N | 11 36 24 | 20 2 4 20 14 20 | 23 27 22 23 27 35 |
| | 2 1 | | 10 26 41 | 0 44 36 | 12 17 1 | 20 26 16 | 23 27 22 |
| 2 | 3 1 | 9 36 29 | 10 4 51 | 1 8 14 | 12 37 2 | 20 37 51 | 22 26 45 |
| | 4 1 | | 9 42 52 | 1 31 50 1 55 24 | 22 56 50 13 16 25 | 20 49 5 | 23 25 44 |
| | 6 1 | | 9 20 44 8 58 28 | 1 55 24 2 18 56 | 13 16 25 13 35 48 | 20 59 57 21 10 28 | 23 24 17 23 22 26 |
| | 7 1 | | 8 36 5 | 2 42 24 | 13 54 56 | 21 20 36 | 23 20 10 |
| | 8 1 | | 8 13 33 | 3 5 49 | 14 13 51 | 21 30 23 | 23 17 30 |
| | 80 1 | | 7 50 55 | 3 29 10 3 52 27 | 14 32 32 14 50 59 | 21 39 47 21 48 49 | 23 14 25 23 20 56 |
| | 80 1 | | 1-0 0 | 4 15 40 | 19 30 39 | 21 57 28 | 23 20 56 |
| - | | July. | August. | September. | October. | November. | December. |
| Da | | North. | North. | North. | South. | South. | South. |
| 100 | 0 | 1.110 | 0 / // | 9 1 " | 0 / . // | 0 / // | 0 / 1" |
| 9 | | | 17 59 28 | 8 13 9 7 51 16 | 3 16 33 3 39 51 | 14 31 39 14 50 44 | 21 52 8 22 1 9 |
| 11.0 | 3 22 | 58 2 | 17 28 33 | 7 29 15 | 4 3 7 | 15 9 35 | 22 9 44 |
| 4 | 1 22 | | 17 12 39 | 7 7 6 | 4 26 20 | 15 28 11 | 22 17 53 |
| 1 4 | 22 22 | | 16 56 29 16 40 2 | 6 44 51 6 22 28 | 4 49 30 5 12 36 | 15 46 32 16 4 37 | 22 25 37 22 32 34 |
| | 22 | the same of the same of | 16 23 19 | 5 59 59 | 5 35 39 | 16 22 26 | 22 32 54 22 39 45 |
| 1 | 3 22 | 28 33 | 16 6 21 | 5 37 25 | 5 58 37 | 16 39 59 | 22 46 9 |
| | 22 | | 15 49 6 | 5 14 44 | 6 21 31 | 16 57 14 | 22 52 6 |
| 10 | | | 15 31 36 15 13 52 | 4 51 59 4 29 8 | 6 44 19 7 7 2 | 17 14 12 17 30 52 | 22 57 36 23 2 38 |
| 1 | | 57 58 | 14 55 53 | 4 6 12 | 7 29 40 | 17 47 14 | 23 7 13 |
| 1: | 3 21 | 49 22 | 14 37 39 | 3 43 13 | 7 52 11 | 18 3 18 | 23 11 21 |
| 1 | | | 14 19 11 14 0 30 | 3 20 9 2 57 2 | 8 14 35 8 36 52 | 18 19 2 18 34 27 | 23 15 0 23 18 12 |
| 1 | | | 13 41 35 | 2 33 51 | 8 59 2 | 18 49 32 | 23 18 12 23 20 56 |
| 1 | 7 21 | 11 16 | 13 22 27 | 2 10 38 | 9 21 4 | 19 4 17 | 23 23 12 |
| 1 | | | 13 3 7 | 1 47 22 | 9 42 58 | 19 18 41 | 24 24 59 |
| 1 2 | | | 12 43 35 12 23 50 | 1 24 4 1 0 43 | 10 4 43 | 19 32 44 19 46 27 | 23 26 19 23 27 10 |
| 2 | | | 12 3 54 | 0 37 22 | 10 47 46 | 19 59 47 | 23 27 33 |
| 2 | 2 20 | 15 36 | 11 43 46 | 0 13 59 N | | 20 12 46 | 23 27 27 |
| | $\begin{array}{c c} 3 & 20 \\ 4 & 19 \end{array}$ | | 11 23 28 11 2 58 | 0 9 25 S 0 32 50 | 11 30 10 11 51 7 | 20 25 22 20 37 35 | 23 26 53 23 25 51 |
| | | 50 57 | 11 2 58 10 42 18 | 0 56 15 | 12 11 53 | 20 37 35 | 23 25 51 23 24 21 |
| 2 | 6 19 | 24 58 | 10 21 28 | 1 19 39 | 12 32 28 | 21 0 53 | 23 22 22 |
| 2 | | 11 30 | 10 0 28 | 1 43 4 | 12 52 51 | 21 11 57 | 23 19 55 |
| 2 2 | | 57 42 43 36 | 9 39 18 9 17 59 | 2 6 28 2 29 51 | 13 13 2 13 33 1 | 21 22 36 21 32 52 | 23 17 0 23 13 37 |
| 3 | | 29 11 | 8 56 31 | 2 63 13 | 13 52 47 | 21 42 43 | 23 9 46 |
| 3 | | 3 14 28 | 8 34 54 | | 14 12 20 | - 1 | 23 5 27 |
| 1 | | | | | | | |

| TABLE LVIII.—Equation | of Time | for every | Day in | the ! | Year 1828. | 107 |
|-----------------------|---------|-----------|--------|-------|------------|-----|
| | | | | | | |

| 1-1 | Jan. | IF | eb. | M | ar. | Ap | ril | Ma | ıy. | Ju | ne. | Ju | ly. | Au | g. | Ser | ot. | 00 | ct. | No | v. | De | c. | |
|-------|-------------------|------|-----|--------------|-----|----|-----|----|-----|-----|-----|-----|-----|----|----|-----|-----|-----|-------|----|----|----|-----|-----|
| Days. | Add | A | dd | A | dd | A | dd | Su | b. | Su | b. | A | ld | Ac | ld | Su | b. | Su | b. | Su | b. | Su | b. | - |
| | m s | n | S | m | S | m | S | m | 8 | m | 8 | m | 8 | m | S | m | S | m | 8 | m | S | m | S | |
| 1 | 3.3 | 5 13 | 52 | 12 | 35 | 3 | 54 | 3 | 5 | 2 | 33 | 3 | 25 | 5 | 57 | 0 | 15 | 10 | 25 | 16 | 17 | 10 | 38 | - |
| 2 | 4 | 1 14 | 0 | 12 | 23 | 3 | 36 | 3 | 13 | 2 | 24 | 3 | 37 | 5 | 53 | 0. | 34 | 10 | 43 | 16 | 17 | 10 | 14 | - |
| 3 | 4 3 | 2 14 | , 7 | 12 | 10 | 3 | 18 | 3 | 19 | 2 | 14 | 3 | 48 | 5 | 49 | 0 | 53 | 11 | 2 | 16 | 17 | 9 | 50 | n |
| 4 | 4 5 | 9 14 | 13 | 11 | 56 | 3 | 0 | 3 | 26 | 2 | 4 | 3 | 58 | 5 | 44 | 1 | 12 | 11 | 20 | 16 | 16 | 9 | 26 | |
| 5 | 5 2 | 114 | 18 | 11 | 42 | 2 | 42 | 3 | 31 | 1 | 54 | 4 | 9 | 5 | 38 | 1 | 32 | 11 | 38 | 16 | 14 | 9 | 1 | |
| 6 | 5 5 | 114 | 23 | 11 | 28 | 2 | 25 | 3 | 37 | 1 | 43 | 4 | 19 | 5 | 32 | 1 | 51 | 11 | 55 | 16 | 11 | 8 | 35 | |
| 7 | 6 2 | 11 | 27 | 11 | 14 | 2 | 7 | 3 | 41 | 1 | 33 | 4 | 29 | 5 | 25 | 2 | 11 | 12 | 12 | 16 | 8 | 8 | . 9 | |
| 8 | 6 4 | 3 14 | 30 | 10 | 59 | 1 | 50 | 3 | 45 | 1 | 21 | 4 | 39 | 5 | 18 | 2 | 32 | 12 | 29 | 16 | 3 | 7. | 43 | |
| 9 | 7 1 | 1 14 | 32 | 10 | 43 | 1 | 33 | 3 | 48 | 1 | 10 | 4 | 48 | 5 | 10 | 2 | 52 | 12 | 45 | 15 | 58 | 7 | 15 | 1 |
| 10 | 7 3 | 3 14 | 34 | 10 | 28 | 1 | 17 | 3 | 51 | 0 | 58 | 4 | 57 | 5 | 1 | 3 | 12 | 13 | 0 | 15 | 52 | 6 | 48 | 141 |
| 11 | 8 | 114 | 35 | 10 | 12 | 1 | 1 | 3 | 53 | 0 | 46 | 5 | 5 | 4 | 52 | 3 | 33 | 13 | 15 | 15 | 45 | 6 | 20 | |
| 12. | 8 2 | 5 14 | 35 | 9 | 55 | 0 | 45 | 3 | 55 | 0 | 34 | 5 | 13 | 4 | 43 | 3 | 54 | 13 | 30 | 15 | 37 | 5 | 52 | |
| 13 | 8 4 | 3 14 | 34 | 9 | 39 | 0 | 29 | 3 | 55 | 0 | 21 | 5 | 20 | 4 | 32 | 4 | 15 | 13 | 44 | 15 | 29 | 5 | 23 | |
| 14 | 9 10 | 14 | 33 | 9 | 22 | 0 | 14 | 3 | 56 | 0 | 9 | 5 | 27 | 4 | 22 | 4 | 36 | 13 | 59 | 15 | 19 | 4 | 55 | |
| | 90000 | 1 | 53 | 1 | 91 | S | ıb. | | п. | Ac | id. | | 12 | - | | | | | | | | | , | |
| 15 | 9 3 | 2 14 | | | 5 | 0 | 1 | 3 | 56 | 0 | 4 | 5 | 34 | 4 | 10 | 4 | 57 | 14 | 31 | 15 | 9 | 4 | 25 | |
| 16 | 9 5 | 114 | 28 | 8 | 47 | 0 | 16 | 3 | 55 | 0 | 17 | 5 | 40 | | 58 | 5 | 18 | 14 | 24 | 14 | 58 | 3 | 56 | |
| 17 | 10 1. | 5 14 | 24 | 8 | 30 | 0 | 30 | 3 | 54 | 0 | 30 | 5 | 4.5 | 3 | 46 | 5 | 35 | 14 | 33 | 14 | 46 | 3 | 27 | |
| | 10 3 | 5 14 | 19 | 8 | 12 | 0 | 44 | 3 | 52 | 0 | 43 | 5 | 50 | 3 | 33 | 6. | 0 | .4 | 47 | 14 | 34 | 2 | ,57 | 1 |
| | 10 5 | 114 | 14 | 7 | 54 | 0 | 58 | 3 | 49 | 0 | 55 | 5 | 51 | 3 | 20 | 6 | 21 | 14 | 53 | 14 | 20 | 2 | 27 | |
| | - | 2 14 | | 7 | 36 | 1 | 11 | 3 | 46 | 1 | 9 | 5 | 53 | 3 | 6 | 6 | 43 | 15 | 3 | 14 | 6 | 1 | 58 | |
| | The last lines in | 14 | | 7 | 18 | 1 | 24 | 3 | 43 | 1 | 25 | 10 | 1 | 2 | 51 | 7 | 3 | | 13 | 13 | 51 | 1 | 28 | |
| | | 13 | | 7 | 0 | 1 | 36 | 3 | 39 | 1 | 35 | 10) | 1 | | 37 | 7 | | 15 | | 13 | 35 | 0 | 58 | |
| 23 | 12 3 | 3 13 | 47 | 6 | 41 | 1 | 48 | 3 | 34 | 1 | 47 | 1.6 | 6 | 2 | 21 | 17 | 45 | 15 | 35 | 13 | 18 | | 28 | 1 |
| 1.10 | | | 20 | | 100 | | 15 | 3. | | 100 | | Ш, | | 6 | | | | | - () | 1 | 7 | A | dd | 1 |
| | 100 | 3 13 | 1 | ALC: UNKNOWN | 23 | | 59 | | 29 | 2 | 0 | | 7 | | 5 | | | 15 | | 13 | 1 | 0 | 2 | |
| | | 3 13 | | | 4 | 2 | 10 | 3 | 24 | 2 | 13 | | 8 | | 49 | | | 15 | | 12 | 42 | 1 | 32 | |
| | | 113 | | | 46 | 2 | 20 | 3 | 18 | 2 | 25 | | 8 | | 33 | | - 1 | 15 | | 12 | 23 | _ | 2 | |
| | | 13 | | 5 | 27 | 2 | 30 | 3 | 12 | 2 | 38 | | 8 | | 16 | 1 | 7 | 1-0 | 1 | 1 | 4 | 1 | 32 | |
| 100 | | 2 12 | - | | 8 | | 40 | 3 | 5 | 2 | 50 | | 7 | | 58 | 1 | 26 | - | - 7 | 11 | 43 | | 1 | |
| | | 3 12 | 47 | 4 | 50 | 2 | 49 | 2 | 57 | 3 | 2 | 6 | 5 | | 41 | | - | | | 11 | 22 | | 30 | |
| | 13 3 | | - | 4 | 31 | 2 | 57 | 2 | 50 | 3 | 14 | 6 | 3 | | 23 | | . 6 | 16 | | 11 | 0 | | 0 | |
| 31 | 13 43 | 3 | | 4 | 13 | | C | 2 | 41 | | 14 | 6 | 0 | 0 | 4 | 1 | 0 | 16 | 15 | | | 3 | 29 | 1 |

TABLE LIX.—Correction of the Longitude by Chronometers.

| Ī | Days. | Log. | Days. | Log. | Days. | Log. | Days. | Log. rec | • |
|---|-------|---------|-------|---------|-------|---------|-------|-----------|---|
| | 1 | 0.00000 | 31 | 2,69548 | 61 | 3.27669 | 91 | 3.62180 | |
| | 2 | 0.47712 | 32 | 2.72263 | 62 | 3.29070 | 92 | 3.63124 | |
| | - 3 | 0.77815 | 33 | 2.74896 | 63 | 3.30449 | 93 | 3.64058 | |
| | 4 | 1.00000 | 34 | 2.77452 | 64 | 3.31806 | 94 | 3.64982 | |
| | 5 | 1.17609 | 35 | 2.79934 | 65 | 3.33143 | 95 | - 3.65896 | |
| ш | 6 | 1.32222 | 36 | 2.82347 | 66 | 3.34459 | 96 | 3.66801 | J |
| П | 7 | 1.44716 | 37 | 2.84696 | 67 | 3.35755 | 97 | 3.67697 | , |
| н | 8 | 1.55630 | 38 | 2.86982 | 68 | 3.37033 | 98 | . 3.68583 | d |
| | 9 | 1.6532 | 39 | 2.89209 | 69 | 3.38292 | 99 | 3.69461 | |
| | 10 | 1 74036 | 40 | 2.91381 | 70 | 3.39533 | 100 ' | - 3.70329 | |
| | 111 | 1.8195+ | 41 | 2.93500 | ×71 | 3.40756 | 101 | 3.71189 | |
| | 12 | 1.89209 | 42 | 2.95569 | 72 | 3.4 963 | 102 | 3.72041 | |
| | 13 | 1.95904 | 43 | 2.97589 | 73 | 3.43152 | 103 | 3.72884 | |
| | 14 | 2.02119 | 44 | 2.99564 | 74 | 3.44326 | 104 | 3.73719 | |
| | 15 | 2.07918 | 45 | 3.01494 | 75 | 3.45484 | 105 | 3.74547 | |
| | 16 | 2.13354 | 46 | 3.03383 | 76 | 3.46627 | 106 | 3.75366 | |
| | 17 | 2.18469 | 47 | 3.05231 | 77 | 3.47756 | 107 | 3.76178 | ķ |
| | 18 | 2.23300 | 48 | 3.07041 | 78 | 3.48869 | 108 | 3.76982 | |
| | 19 | 2.27875 | 49 | 3.08814 | 79 | 3.49969 | 109 | 3.77779 | |
| | 20 | 2.32222 | 50 | 3.1055 | 80 | 3.51055 | 110 | 3.78569 | |
| | 21 | 2.36361 | . 51 | 3.12254 | 81 | 3.52127 | 111 | 3.79351 | |
| | 22 | 2.40312 | 52 | 3.13925 | 82 | 3.53186 | 112 | 3.80127 | |
| | 23 | 2.41091 | 53 | 3.15564 | 83 | 3.54233 | 113 | 3.80895 | |
| | 24 | 2.47712 | 54 | 3.17173 | 84 | 3.55:67 | 114 | 3.81657 | |
| | 25 | 2.51188 | 55 | 3.18752 | 85 | 3.56289 | 115 | 3.82413 | |
| - | 26 | 2.54531 | 56 | 3.20303 | 86 | 3.57299 | 116 | 3.83161 | |
| | 27 | 2.57749 | 57 | 3.21827 | 87 | 3.58297 | 117 | 3.83904 | |
| | 28 | 2.60853 | 58 | 3.233?5 | 88 | 3.59284 | 118 | 3.84640 | |
| | 29 | 2.63×49 | 59 | 3.21797 | 89 | 3.60260 | 119 | 3.85870 | |
| | 30 | 2.66745 | 60 | 3.26245 | 90 | 3.61225 | 120 | 3.86094 | |

| TABLE L | X.—Latitude | s and Longitudes of Places. | 1202 | | | | |
|--------------------------|--------------------------|--|--------------------|--|--|--|--|
| | | Longitude. | High Water. | | | | |
| Names of Places. | Latitude. | In Degrees. In Time. | time Spring Neap | | | | |
| | 0 11 11 | o'' h m s | h m teet feet | | | | |
| Aberdeen · · · | 57 8 50 N | | 0 45 | | | | |
| Amsterdam . | 52 22 17 N | The second secon | 3 0 | | | | |
| Archangel | 64 34 0 N | | 6 0 | | | | |
| Batavia | 6 9 08 | 106 51 45 E 7 7 27 E | 1000 | | | | |
| Berlin | 52 31 45 N | | | | | | |
| Berwick | 55 46 21 N | The state of the s | 2 30 15 | | | | |
| Bombay (Church) | 18 57 44 N | 100 | 10 0 | | | | |
| Bremen | 53 4 38 N 48 23 14 N | The same of the sa | 6 0 | | | | |
| Brighton | 48 23 14 N 50 49 32 N | The second secon | 10 10 18 | | | | |
| Bristol | 51 27 6 | the state of the s | 6 50 42 | | | | |
| Cadiz | 36 32 0 1 | 6 17 22 W 0 25 9 W | 4 20 | | | | |
| Calais | 50 57 32 N | OH WE SE THE PURE THE TAX TO DESCRIPT | 11 40 18 | | | | |
| Calcutta | 22 33 0 N | | 3 10 | | | | |
| Cambridge | 52 12 43 N 23 8 9 N | | 130 1 4 | | | | |
| Coimbra | 40 20 30 N | The party of the p | 1 11 75 | | | | |
| Constantinople | 41 1 27 1 | | 76 (1) 81 | | | | |
| Copenhagen | 55 41 4 N | 1 12 35 8 6 E 0 50 21 E | I GO OF | | | | |
| Cork | 51 51 50 N | | 6 30 | | | | |
| Dantzic | 54 20 48 N 53 23 13 N | 10 00 | 9 20 | | | | |
| Dundee | 56 28 0 N | | 2 10 | | | | |
| Edinburgh (Observatory). | 55 57 21 N | | 2 20 16 8 | | | | |
| Florence | 43 46 41 N | | 1082 90 32 | | | | |
| Genoa | 44 25 0 N | | DOT IN THE | | | | |
| Glasgow | 55 51 32 N | The second secon | 0 0 | | | | |
| Cattingen | 50 56 8 N 51 31 50 N | | [*] | | | | |
| Greenwich | 51 28 38 N | | 1 1 | | | | |
| Heligoland | 54 11 34 N | | 11 0 | | | | |
| Hull . | 53 48 0 N | | 6 0 | | | | |
| Hieres | 43 7 2 N | The state of the s | | | | | |
| Jamaica (Port Royal) . | 17 58 0 N 38 42 24 N | | 2 15 | | | | |
| Liverpool | 53 24 40 N | | | | | | |
| Lizard (Light) | 49 57 44 N | | 5 0 | | | | |
| London | 51 30 49 N | | 2 50 19 | | | | |
| Madras | 13 4 9 N 40 24 57 N | | | | | | |
| Malta | 35 53 0 N | | | | | | |
| May (Light) | 56 11 22 N | | 1 50 | | | | |
| Montpelier | 43 36 16 N | 3 52 40 E 0 15 31 E | 2 Y 30 1 | | | | |
| Moscow | 55 45 45 N | | 7 1 m | | | | |
| Naples | 40 50 15 N 51 45 39 N | | | | | | |
| Palermo | 38 6 44 N | | | | | | |
| Paris | 48 50 14 N | | 1 1 6 8 | | | | |
| Pekin | 2 | 1116 26 45 E 7 45 5 E | 15- 11- | | | | |
| Petersburgh | 59 56 23 N | | 2 20 | | | | |
| Philadelphia | 39 56 55 N 50 22 20 N | | 2 30 | | | | |
| Portsmouth | 50 48 3 N | | 6 0 18 | | | | |
| Rome | 41 53 54 N | | 11 20 10 | | | | |
| Rotterdam | 51 55 22 N | 4 29 11 E 0 17 56 E | 4 1 0 | | | | |
| Slough | 51 30 20 N | | | | | | |
| Stockholm | 59 20 31 N 43 7 9 N | | U 10 | | | | |
| Upsal | 59 51 50 N | | 5. 1. 5 | | | | |
| Venice | 45 25 32 N | 12 20 59 E 0 49 24 E | A | | | | |
| Vienna | 48 12 36 N | 17 22 45 E 1 5 31 E | 9-3 99 6 | | | | |
| Yarmouth | 52 36 40 N | | 8 50 8 | | | | |
| York (New) | 40 42 6 N | 73 59 0 W 4 55 56 W | 3 0 | | | | |

Maria de Laborati

| | | | LXI. | | | TABLE LX11. 109 Time into Space. | | | | | | | | | |
|------------|--------------|----------|--------------|----------|----------------|----------------------------------|-------------------------|----------|-------------|----------|---------------|--|--|--|--|
| To conv | ert Degre | ce inte | Time. | f the | Equator | To con | | | | Degr | ees and | | | | |
| To conv | | | al Time | | Equator | 10 con | | | e Equato | | ees and | | | | |
| 0 1 | h m | / | m s | " | 8 | b I | h ° m ° ' s ' | | | | | | | | |
| 1 | 0 4 | 1 | 0 4 | 1 | 0.066 | 1 | 15 | 1 | 0 15 | 1 | 0 15 | | | | |
| 2 | 0 8 | 2 | 0 8 | 2 | 0.133 | 2 | 30 | 2 | 0 30 | 2 | 0 30 | | | | |
| 3 | 0 12 | 3 | 0 12 | 3 | 0.200 | 3 | 45 | 3 | 0 45 | 3 | 0 45 | | | | |
| 4 5 | 0 16 0 20 | 4 5 | 0 16 0 20 | 4 5 | 0.266 0.333 | 5 | 60 75 | 5 | 1 0 1 15 | 4 5 | 1 0 1 15 | | | | |
| 6 | 0 24 | 6 | 0 24 | 6 | 0.400 | 6 | 90 | 6 | 1 30 | 6 | 1 30 | | | | |
| 7 | 0 28 | 7 | 0 28 | 7 | 0.466 | 7 | 105 | 7 | 1 45 | 7 | 1 45 | | | | |
| 8 | 0 32 | 8 | 0 33 | 8 | 0.533 | 8 | 120 | 8 | 2 0 | 8 | 2 0 | | | | |
| 9 | 0 36 | 9 | 0 36 | 9 | 0.600 | 9 | 135 | 9 | 2 15 | 9 | 2 15 | | | | |
| 10 | 0 40 | 10 | 0 40 | 10 | 0.666 | 10 | 150 | 10 | 2 30 | 10 | 2 30 | | | | |
| 11 | 0 44 0 48 | 11 12 | 0 44 0 48 | 11 | 0.733 | 11 | 165 | 11 12 | 2 45 | 11 12 | 2 45 | | | | |
| 12 13 | 0 52 | 13 | 0 52 | 12 13 | 0.799 0.866 | 12 13 | 180 195 | 13 | 3 0 3 15 | 13 | 3 15 | | | | |
| 14 | 0 56 | 14 | 0 56 | 14 | 0.933 | 14 | 210 | 14 | 3 30 | 14 | 3 30 | | | | |
| 15 . | 1 0 | 15 | 1 0 | 15 | 1.000 | 15 | 225 | 15 | 3 45 | 15 | 3 45 | | | | |
| 16 | 1 4 | 16 | 1 4 | 16 | 1.066 | 16 | 240 | 16 | 4 0 | 16 | 4 0 | | | | |
| 17 18 | 1 8 | 17 18 | 1 8 1 12 | 17 | 1.133 | 17 | 255 | 17 | 4 15 4 30 | 17 | 4 15 4 30 | | | | |
| 19 | 1 16 | 19 | 1 16 | 19 | 1.200 | 18 19 | 270 285 | 19 | 4 45 | 19 | 4 45 | | | | |
| 20 | 1 20 | 20 | 1 20 | 20 | 1.333 | 20 | 300 | 20 | 5 0 | 20 | 5 0 | | | | |
| 25 | 1 40 | 21 | 1 24 | 21 | 1.400 | 21 | 315 | 21 | 5 15 | 21 | 5 15 | | | | |
| 30 | 2 0 | 22 | 1 28 | 22 | 1.466 | 22 | 330 | 22 | 5 30 | 22 | 5 30 | | | | |
| 35 | 2 20 | 23 | 1 32 | 23 | 1.533 | 23 | 345 | 23 | 5 45 | 23 | 5 45 | | | | |
| 40 | 2 40 | 24 25 | 1 36 | 24 | 1.600 | 24 | 360 | 24 | 6 0 | 24 25 | 6 0 | | | | |
| 45 50 | 3 20 | 26 | 1 44 | 25 26 | 1.666 | Tenths. | | 25 26 | 6 15 6 30 | 26 | 6 15 6 30 | | | | |
| 55 | 3 40 | 27 | 1 48 | 27 | 1.799 | S | | 27 | 6 45 | 27 | 6 45 | | | | |
| 60 | 4 0 | 28 | 1 52 | 28 | 1.866 | 0.1 | 1.5 3.0 | 28 | 7 0 | 28 | 7 0 | | | | |
| 65 | 4 20 | 29 | 1 56 | 29 | 1.933 | 0.3 | 4.5 | 29 | 7 15 | 29 | 7 15 | | | | |
| 70 | 4 40 | 30 | 2 0 | 30 | 2.000 | 0.4 | 6.0 | 30 | 7 30 | 30 | 7 30 | | | | |
| 75 | 5 0 | 31 | 2 4 | 31 | 2.066 | 0.5 | 7.5 | 31 | 7 45 | 31 | 7 45 | | | | |
| 80 90 | 5 20 6 0 | 32 | 2 8 2 12 | 32 | 2.133 | 0.6 | 9.0 | 32 | 8 0 8 15 | 32 33 | 8 0 | | | | |
| 100 | 6 40 | 34 | 2 16 | 34 | 2.266 | 0.7 | 10.5 | 34 | 8 30 | 34 | 8 30 | | | | |
| 110 | 7 20 | 35 | 2 20 | 35 | 2.333 | 0.9 | 13.5 | 35 | 8 45 | 35 | 8 45 | | | | |
| 120 | 8 0 | 36 | 2 24 | 36 | 2.400 | 1.0 | 15.0 | 36 | 9 0 | 36 | 9 0 | | | | |
| 130 | 8 40 | 37 | 2 28 | 37 | 2.466 | Hund | redths. | 37 | 9 15 | 37 | 9 15 | | | | |
| 140 150 | 9 20 | 38 | 2 32 2 36 | 38 | 2.533 | S | 1 " | 38 39 | 9 30 9 45 | 38 | 9 30 9 45 | | | | |
| 160 | 10 40 | 40 | 2 40 | 40 | 2.666 | 0.01 | 0.15 | 40 | 10 0 | 40 | 10 0 | | | | |
| 170 | 11 20 | 41 | 2 44 | 41 | 2.733 | 0.02 | 0.30 | 41 | 10 15 | 41 | 10 15 | | | | |
| 180 | 12 0 | 42 | 2 48 | 42 | 2.799 | 0.03 | 0.45 | 42 | 10 30 | 42 | 10 30 | | | | |
| 190 | 12 40 | 43 | 2 52 | 43 | 2.866 | 0.05 | 0.75 | 43 | 10 45 | 43 | 10 45 | | | | |
| 200 | 13 20 | 44 45 | 2 56 | 44 | 2.933 | 0.06 | 0.90 | 44 | 11 0 | 44 | 11 0 | | | | |
| 210 | 14 0 | 46 | 3 0 | 45 | 3.000 | 0.07 | 1.05 | 45 | 11 15 | 45 | 11 15 | | | | |
| 230 | 15 20 | 47 | 3 8 | 47 | 3.133 | 0.08 | 1.20 | 40 | 11 45 | 47 | 11 45 | | | | |
| 240 | 16 0 | 48 | 3 12 | 48 | 3.200 | 0.09 | 1.35 | 48 | 12 0 | 48 | 12 0 | | | | |
| 250 | 16 40 | 49 | 3 16 | 49 | 3.266 | | andths. | 49 | 12 15 | 49 | 12,15 | | | | |
| 260 | 17 20 | 50 | 3 20 | 50 | 3.333 | 8 | 1 " | 50 | 12 30 | 50 | 12 30 | | | | |
| 270 | 18 0 | 51 | 3 24 | 51 | 3.400 | 0.001 | 0.015 | 51 | 12 45 | 51 | 12 45 | | | | |
| 280 | 18 40 19 20 | 52 53 | 3 28 3 32 | 52 53 | 3.466 | 0.002 | 0.030 | 52 53 | 13 0 | 52 53 | 13 0 | | | | |
| 300 | 20 0 | 54 | 3 36 | 54 | 3.533 | 0.003 | 0.045 | 54 | 13 13 | 54 | 13 30 | | | | |
| 310 | 20 40 | 55 | 3 40 | 55 | 3.666 | 0.004 | 0.000 | 55 | 13 45 | 55 | 13 45 | | | | |
| 390 | 21 20 | 56 | 3 44 | 56 | 3.733 | 0.006 | 0.090 | 56 | 14 0 | 56 | 14 0 | | | | |
| 330 | 22 0 | 57 | 3 48 | 57 | 3.799 | 0.007 | 0.105 | | 14 15 | 57 | 14 15 | | | | |
| 340 | 22 40 23 20 | 58 | 3 52 | 58 | 3.866 | 0.008 | 0.120 | | 14 30 | 58 | 14 30 | | | | |
| 360 | 24 0 | 59 60 | 3 56 | 59 60 | 3.933 | 0.009 | 0.135 | | 14 45 | 59 60 | 14 45 15 0 | | | | |
| | convert | | | | of Ter- | | | | into Deg | - | - | | | | |
| 1 3 | restrial L | ongitu | ide into | Tim | e. | 02 10 | | | al Longi | | nd Land | | | | |
| | | | | | | - | 0. 10. | 100011 | | | | | | | |

| 1110 | TABLE LXIII.—U | seful Numbers. | TO DESCRIPTION OF THE PARTY OF |
|--------------|--|------------------------------|---|
| Char. | Numbers. | Logarithms. | Arith. Com. Log. |
| | 3 .14159265 | 0.4971499 | 9.5028501 |
| 7 2 T | 9 .86960440 | 0.9942998 | 9.0057002 |
| | 0 .78539816 | 9.8950899 | 0.1049101 |
| 147 | 0.52359878 | 9.7189986 | 0.2810014 |
| 1 1 DO | 57°.29577951 | 1.7581226 | 8.2418774 |
| A=R° A=R" | 206264".8 | 5.3144251 | 4.6855749 |
| | | 2.2418773 | |
| A=1° | 0 .01745329 | - | 1.7581227 |
| A=1' | 0 .0002908882 . | 4.4637262 | 2.5362738 |
| A=1" | 0 .0000048481368 | 6.6855749 | 5.3144251 |
| | 0.0795775=area of a circle to cir- | 2.9007904 | 1.0992096 |
| | cumference unity . | VI. 0 11 SS(1) | |
| | 1296000=seconds in a circle | 6.1126050 | 3.8873940 |
| | 86400=seconds in 24 hours | 4.9365137 | 5.0634863 |
| | 86164.0908 seconds of time the | 4.9353264 | * OCTORDO |
| | earth takes to perform a rota- | 4.9333204 | 5.0646736 |
| | tion about its axis .) Half 43082.0454 | 4.6342964 | t actiona |
| No. of | (43082.0454) ² | 9.2685928 | 5.3657036 |
| 100 | Length of the tropical year | 3.2003320 | 0.7314072 |
| | =365d 5h 48m 50s= . | 15 (2) 19 56 | |
| | 31556930s | 7.4990948 | 2.5009052 |
| | Metre 39.37079 inches | 1.5951741 | 8.4048259 |
| , | 3.2808992 feet | 0.5159929 | 9.4840071 |
| 0.00 | 1 French toise= 1.065777 fath. | 0.0276664 | 9.9723336 |
| | 1 Myriametre = 6.213856 miles | 0.7933608 | 9.2066392 |
| | 1 Hectare = 2.47117 acres | 0.3929026 | 9.6070974 |
| Stere | 1 Cubic metre =35.31716 feet | 1.5479850 | 8.4520150 |
| Litre | 1 Cu. Decimetre=61.0286 inches | 1.7855291 23 | 8.2144709 77 |
| Little | 1 Kilogramme = 121.33 lb. Troy | 1.0839682 | 8.9160318 |
| | 1 Gramme =15.444 grains T. | 1.1887598 | 8.8112402 |
| 1 | Mean circumference of the earth } | 4.3954312 | 5.6045688 |
| | Diameter 7912 miles . | 3.8982863 | 6.1017137 |
| N. 36 | Radius of Equator 3962.349 miles | 3.5979528 | 6.4020372 |
| | Semipolar axis 3949.669 | 3.5965608 | 6.4034392 |
| | Difference 12.680 | 1.1031193 | 8.8968807 |
| 1250 | Geographical mile=6075.6 feet | 3.7835892 | 6.2164108 |
| 1000 | Circumference of the equator = 24896 miles | 4.3961296 | 5.6038704 |
| 0 | Radius of Eq.=20920000 ft. from | 7.3205617 | 2.6794383 |
| | a Mean of Playfair and Lambton | 1.0403011 | W10104303 |
| - | Mean Velocity of sound 1140 feet \ | 2.0560040 | C 04000** |
| 15.1 | per second | 3.0569049 | 6.9430951 |
| 100 | Modulus of Tabular logs. | | P. Franklin |
| | =0.4342944819 . | Cell - Control | CATE OF MARK |
| 1 | Double 0.8685889638 . | THE STORY OF STREET | THE R. LEWIS CO., LANSING |
| | Reciprocal or hyper. log. 10 | 2.3025851 | 7.6974149 |
| | Log. of this | 0.3622149 | 9.6377851 |
| F | Number of which 1 is the hyp. log.] | 0.4342945 | 9.5657055 |
| 100 | 2.71828183 . 5 | 3,202,00 | 010001000 |
| | its recip. 0.36787944 . | District Co. Street, Sec. 19 | |
| 00, | Length of seconds pendulum | 1 5000700 | 0.40,000 |
| 1 | at London 39.1393 inches . | 1.5926130 | 8.4073870 |
| 1 | at Edinburgh 39.1555 in. | 1.5927928 | 8.4071072 |
| | Force of gravity or g at. | 1 5000000 | 0.4000***0 |
| g | London 32.19084 . | 1.5077222 | 8.4922778 |
| 1 | Edinburgh 32.20415 . | 1.5079109 1.2066922 | 8.4920391 |
| ₹5 | London 16.09542 . | 1.2068809 | 8.7933078 |
| | Edinburgh 16.102075 . | 1.2008809 | 8.7911191 |

 $h = \left\{ 251.5 + \frac{3}{2} (n-1) \right\} n$ in which h is the height in feet, and n the change of temperature.

 $t=97^{\circ}.08 \cos^{\frac{3}{2}} \lambda = \left(10^{\circ}.53 + \frac{h}{251.5 + 0.005h}\right)$ in which t is the temp. and λ the latitude.

 $n = \frac{h}{251.5 + 0.005h}$ very nearly, n being the change of temp. in degrees of Fah.

| 1 | | | T | 'AB | LE | LX | 1V. | | | | | | | | of H | igh \ | Vater. | | | 1 | 11 |
|-----|----------|----------|----------|----------|----------|----------|----------|----------|-------|----------|-------------|----------|----------------|----------|----------|-------|----------|---------------|----------|----------------|----------|
| | on's | | | - 01 | | here! | *01 | | Moor | | Hori Moo | | tal Par | | 201 | | 104 | 501 | | Moo | |
| Tr. | ansit | 54 | 55' | 56' | 57' | 58' | 59' | 60' | Trans | sit. | Tran | nsit. | 54 | 55' | 56' | 57' | 58' | 59' | 60' | Tran | isit |
| h | m | m | m | m | m | m | m | m | | m | h | m | m | m | m | m | m | m | m | h | m |
| 0 | 0 | -4 | 3 | -2 | -0 | | +4 | | 12 | 0 | 6 | 0 | -56 | 58 | -60 | 62 | 65 | 69 | 72 | | 0 |
| ш | 10 | 6 | 5 | 4 | 3 | | | +2 | | 10 | | 10 | 52 | 54 | 56 | 59 | 62 | 65 | 68 | | 10 |
| | 20 | 8 | 7 | 6 | 5 | -0 | 0 | 1 | | 20 | | 20 | 49 | 51 | 53 | 55 | 58 | 60 | 63 | | 20 |
| | 30 | 10 | 10 | 9 | 8 | 10 | 6 | 5 8 | | 30 | | 30 | 46 | 48 | 50 | 51 | 54 49 | 56 | 58 | | 30 |
| п | 40 | 12 | 12 14 | 11 | 13 | 12 | 12 | 11 | | 40 50 | | 40 50 | 43 38 | 39 | 45 40 | 47 | 43 | 51 44 | 53 | | 40 50 |
| | 50 | 15 | | | _ | | | | | - | | - | | | | | | - | 45 | | _ |
| 1 | 0 | 17 | 17 | 16 | 16 | 16 19 | 15 | 15 18 | 13 | 0 | 7 | 0 | 32 | 33 | 33 | 34 | 35 | 36 | 37 | | 0 |
| | 10 | 20 | 20 | 19 22 | 19 | 22 | 19 | 22 | | 10 20 | | 10 20 | 27 22 | 27 22 | 28 | 28 | 29 22 | - 30 22 | 30 | | 10 20 |
| | 20 | 22 24 | 24 | 25 | 25 | 25 | 25 | 25 | | 30 | | 30 | 18 | 18 | 22 17 | 16 | 16 | 15 | 22 14 | | 30 |
| н | 30 | 27 | 27 | 28 | 28 | 28 | 29 | 29 | | 40 | | 40 | 11 | 11 | 10 | 10 | 8 | 7 | 6 | | 40 |
| п | 50 | 29 | 30 | 31 | 31 | 31 | 32 | 33 | | 50 | 0 | 50 | 6 | _ 6 | 5 | _ 4 | 2 | o | + 1 | | 50 |
| 2 | 0 | 31 | 32 | 33 | 33 | 34 | 35 | 36 | | 0 | 8 | 0 | _ 1 | + 1 | + 2 | + 3 | 5 | 7 | 9 | | 0 |
| l ~ | 10 | 34 | 35 | 36 | 36 | 37 | 38 | 39 | 1.2 | 10 | | 10 | + 2 | 4 | 5 | 7 | 9 | 12 | 14 | | 10 |
| | 20 | 36 | 37 | 38 | 39 | 39 | 41 | 43 | | 20 | | 20 | 5 | . 7 | 9 | 11 | 14 | 16 | 19 | | 20 |
| | 30 | 38 | 39 | 40 | 41 | 42 | 44 | 46 | 4 | 30 | | 30 | - 8 | 10 | 12 | 15 | 18 | 21 | 24 | | 30 |
| | 40 | 40 | 41 | 43 | 44 | 46 | 48 | 50 | 1. | 40 | | 40 | 11 | 13 | 16 | 18 | 21 | 25 | 28 | | 40 |
| н | 50 | 42 | 43 | 50 | 46 | 48 | 50 | 52 | | 50 | н | 50 | 13 | 16 | 18 | 20 | 23 | 27 | 30 | | 50 |
| 3 | 0 | 44 | 45 | 47 | 49 | 51 | 53 | 55 | 15 | 0 | 9 | 0 | 14 | 17 | 19 | 21 | 21 | 28 | 32 | 21 | 0 |
| | 10 | 46 | 47 | 49 | 51 | 54 | 56 | 58 | | 10 | | 10 | 15 | 18 | | 23 | 26 | 30 | 34 | | 10 |
| | 20 | 48 | 49 | 51 | 53 | 56 | 58 | 61 | | 20 | | 20 | 17 | 19 | 22 | 25 | 28 | 32 | 36 | | 20 |
| | 30 | 50 | 52 | 54 | 56 | 58 | 61 | 64 | | 30 | | 30 | 16 | 18 | | 24 | | 31 | 35 | | 30 |
| П | 40 | 52 | 54 | 56 | 48 | 61 | 64 | 67 | | 40 | | 40 | 16 | 18 | 21 | 24 | | 31 | 35 | | 49 |
| Ш | 50 | 53 | 55 | 57 | 60 | 63 | 66 | 69 | | 50 | | 50 | 16 | 18 | 21 | 23 | | 30 | 34 | | 50 |
| 4 | 0 | 55 | 57 | 59 | 62 | 65 | 69 | | 16 | 0 | 10 | 0 | 15 | 17 | 20 | 23 | | 30 | | 22 | 0 |
| ш | 10 | 56 | 58 | 61 | 63 | 66 | 70 | 73 | | 10 | 0 | 10 | 14 | 17 | 20 | 22 | | 29 | 32 | | 10 |
| ш | 20 | 57 | 60 | 63 | 65 | 63 | 72 | | | 20 | | 20 | 13 | .16 | | | | 27 | 31 | | 20 |
| ш | 30 | 58 | 61 | 64 | | 69 | 73 74 | | | 30 | | 30 | 12 | 15 | | 19 | | 26 | 30 | | 30 |
| ш | 40 50 | 59 60 | 62 62 | 65 | 67 | 70 | 75 | 78 | | 40 50 | | 40 50 | 11 9 | 13 11 | 16 14 | 18 | | 25 22 | 28 | | 40 |
| Η, | | | | | | 71 | 75 | | 10 | _ | 11 | | 7 | - | | | | | 25 | - | 50 |
| 5 | | 60 | 63 63 | 66 | 68 68 | 72 | 76 | 79 80 | 17 | 10 | 11 | 10 | | 9 8 | 12 10 | 14 | | 20 | | 23 | 0 |
| н | 10 20 | 60 | 63 | 66 | 68 | 71 | 75 | 80 | | 20 | 11 | 20 | 4 | 6 | 7 | 9 | 1 | 17 14 | 20 | | 10 20 |
| ш | 30 | 59 | 62 | 65 | 67 | 70 | 74 | 78 | | 30 | | 30 | + 2 | 4 | 6 | 7 | | 12 | | | 30 |
| | 40 | 58 | 61 | 63 | 65 | 68 | 72 | 76 | | 40 | 8 | 40 | ő | 2 | 4 | 5 | | 9 | 11 | 1 | 40 |
| ш | 50 | 57 | 60 | 62 | 65 | 68 | 71 | 74 | | 50 | 6 | 50 | _ 2 | _ 1 | + 1 | 2 | | 6 | 1 | | 50 |
| 6 | | 56 | 58 | 61 | 64 | 67 | 69 | 72 | 18 | 0 | 12 | 0 | _ 1 | 0 | 0 | + 0 | + 2 | | | 24 | 0 |
| - | | 00 | 00 | 01 | | | | | | | | | g the | | | | ide. | 1 1 2 | 1 + 1 | 123 | - |
| - | _ | | 1 | Mod | n's | Hor | | Moo | | | | | oon's | | 1 | 1 | Tuc. | 1 | - | | - |
| н | Ti | me. | | | ar. | | | | ar. 5 | | | | Par. | | Tir | ne. | Mult. | Tir | ne. | Mul | t. |
| ш | | | F | Mu | ltip | liers. | | Mul | tipl | iers | . | M | ultipl | iers. | | | 576 | 10. | 16.9 | | |
| h | m | h | m | | | | | | | | - | | | -71 | h | m | | h | m | T | - |
| 0 | | 12 | | | | | | | | | | | 95a + (| | | | 1.000 | | | 0.51 | |
| 0 | | 12 | | | | | | | | | | | 4a+(| | | | 0.998 | | | 0.46 | |
| 1 | | 13 | | | | | | | | | | | 1a+(| | | | 0.993 | | | 0.42 | |
| 2 | | | | | | | | | | | | | (4a+(| | | | 0.985 | | | 0.38 | |
| 2 | | | | | | | | | | | | |)5a+(| | | | 0.974 | | | 0.34 | |
| 3 | | | | | | | | | | | | | 76a+(29a+(| | | - | 0.959 | 4 | | $0.31 \\ 0.27$ | |
| 4 | | | | | | | | | | | | | 72a+(| | | | 0.921 | | | 0.27 0.23 | |
| 1 5 | | 17 | 200 | .284 | a+(| 0.959 | 360. | 250 | 2+0 | .75 | 05 | 0.29 | 25a+6 |).527 | | 00 1 | 0.897 | 4 | 20 | 0.20 | |
| | | 18 | | | | | | | | | | | 05a+(| | | | 0.871 | 4 | | 0.17 | |
| | | | | | | | | | | | | | 27a+(| | | | 0.843 | 4. | | 0.14 | - |
| 1 2 | 20 | 19 | 20.0 | .000 |)a+ | 1.27 | 760. | 0000 | 1+1 | .00 | 060 | 0.00 | 00a+0 | 0.703 | 1 | _ | 0.812 | | | 0.11 | |
| 8 | | 20 | 0.0 | .034 | a+) | 1.138 | 360. | 030 | a+0 | .97 | 06 | 0.02 | 27n+0 | 0.682 | 2 | | 0.779 | 5 | | 0.09 | |
| | | | | | | | | | | | | |)5a+(| | | | 0.774 | 5 | | 0.06 | |
| 9 | | | | | | | | | | | | | 25a+0 | | | | 0.708 | 5 | | 0.05 | |
| 10 |) (| 22 | 00 | .460 |)a+(| 0.74 | 96 0. | 4130 | 4+0 | .58 | 76 | 0.37 | 72a+0 | .412 | 2 3 | | 0.670 | 5 | | 0.03 | |
| 10 | | | | | | | | | | | | | 29a+1 | | | | 0.631 | 5 . | _ | 0.02 | |
| 10 | | | | | | | | | | | | | 6a+0 | | | | 0.591 | | | 0.01 | |
| 12 | 3 (| 24 | 0 0 | .995 | a+ | 0.149 | 96 0. | 883 | a+0 | .11 | 760 |).79 | 95a+(| 0.082 | 3 | 0 (| 0.551 | 6 | 05 | 0.00 | 0 |

| | | | | | 0.0 | | | | | | | | | |
|---|-----------------|----------------------|-------------|---------|---|--------|------------|-------------|-------|------------|----------------|----------|-----------------|------------------|
| 112 | - | E LXV | /1.—E | quatio | ons of T | | Diffe | | | Twe | elve I | lour | rs. | _ |
| Tir after No Midni | oon or | 1' 2' | 13'1 | 4/ 1 8 | 5' 6' | 7' | 8' 1 | 9' | 10'1 | 10" | 20" | 30" | 40" | 50" |
| + | - | | | | | ", | | | 1-1 | | | | | -1 |
| h m | h m | 0.0 0. | 0.0 | 16 1 | 0.0 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 0 | 11 30 | 0.2 0. | | | 0.9 1.1 | 1.3 | 1.5 | 1.6 | 1.8 | 0.0 | 0.1 | 0.1 | 0.1 | 0.5 |
| 1 0 | 11 0 | 0.3 0. | 1 3 | | 1.6 1.9 2.1 2.5 | 2.2 | 2.5 3.3 | 2.9 | 3.2 | 0.1 | 0.1 | 0.2 | 0.2 | 0.3 |
| 1 30 | 10 30 | 0.5 0. | | | 2.3 2.8 | | 3.7 | 4.2 | 4.6 | | 0.1 | 0.5 | 0.3 | 0.4 |
| 2 30 | 9 30 | 0.5 1. | | | 2.4 2.9 | - | 3.8 | 4.3 | 4.8 | 0.1 | 0.2 | 0.8 | 0.3 | 0.4 |
| 3 0 | 9 0 8 30 | 0.5 0. | | | 2.3 2.8 2.2 2.6 | | 3.7 | 4.2 3.9 | 4.7 | 0.1 | 0.2 | 0.2 | | 0.4 |
| 3 30 4 0 | 8 0 | 0.4 0. | | 1.5 | 1.9 2.2 | 2.6 | 3.0 | 3.3 | 3.7 | 0.1 | 0.1 | 0.2 | 1 | 0.3 |
| 4 30 | 7 30 | 0.3 0. | | | 1.5 1.8 1.0 1.9 | | 2.3 | 2.6 | 2.9 | | 0.1 | 0.1 | 1 | 0.2 |
| 5 0 5 30 | 6 30 | 0.2 0. | | | 0.5 0.6 | | | 0.9 | 1.0 | | | 0.1 | | 0.1 |
| 6 0 | 6 0 | 0.0 0. | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| + - TABLE LXVII.—Equations of Fourth Differences for Twelve Hours | | | | | | | | | | | | | | |
| Time Fourth Difference. | | | | | | | | | | | | | | |
| Mic | lnight. | 1' | 2' | 3 | 4 | | 5' | 10 | " | 20" | 30 |)" - | 40" | 50" |
| h m | h n | " | " | | , ,, | | " | " | | " | " | , | " | 11: |
| 0 0 | | 0.0 | 0.0 | 1 | | .0 | 0.0 | 0. | - 1 | 0.0 | 0. | | 0.0 | 0.0 |
| 0 30 | 11 3 | 0 0.2 | 1 | | | .6 | 2.0 | 0. | | 0.1 | 0. | - 1 | 0.3 | 0.2 |
| 1 30 | 10 3 | 0 0.6 | 1.2 | | - | .3 | 2.9 | 0. | | 0.2 | 0. | 3 | 0.4 | 0.5 |
| 2 30 | | | | | | .6 | 4.5 | 0. | | 0.3 | 1 | 4 | 0.6 | 0.7 |
| 3 0 | | 0 1.0 | | | 1 | .1 | 5.1 | 0. | | 0.3 | 0. | | 0.7 | 0.9 |
| 3 30 | | $0 1.1 \\ 0 1.2$ | 2.3 | 1 | | .6 | 5.7 | 0. | - 1 | 0.4 | 0. | | 0.8 | 0.9 |
| 4 30 | 7 3 | | | | | .2 | 6.5 | 0. | | 0.4 | 0. | | 0.9 | 1.1 |
| 5 0 5 30 | | $0 1.4 \\ 0 1.4$ | | | | .6 | 6.8 | 0. | | 0.5 | 0. | | 0.9 | 1.1 |
| 6 0 | 1 0 | 0 1.4 | 2.8 | _ | | .6 | 7.0 | 0. | 2 | 0.5 | 0. | .7 | 0.9 | 1.2 |
| 1 5 | То | find the | e Latit | | ABLE the A | | | | Pole | Star : | for 1 | 824. | | 100 |
| | | | 1st | An | | 1, | • 1. | 14 61 | | | 1s | | An. | |
| Merid | ian Dis | tance. | Correction. | - vari | 0 4 | | eridia | ın D | ıstar | ice. | Corre | - 1 | varia- tion. | Log. of A'' |
| | + + | I | •2011 | _ | | - | - - | - | + | = | | | | OI A. |
| h m h | m h n 2 0 12 | nh m | 1 37 4 | | 15 | h 3 | m h 0 9 | m h 0 13 | m h | | | " | // | 1 0000 |
| 0 0 1 | 50 12 | | | 8 19.4 | 19.200 | | | 50 | 10 | 50 | 1 9 | | | 1.6205 1.6569 |
| 20 | | | | | 9.80 | - | | 40 30 | 20 | 401 | | 52 | 12.51 | 1.6899 |
| 40 | | | | | 28 0.159 15 0.400 | _ | | 20 | 40 | 300 | | | | 1.7205 |
| 50 | | - | 1 35 3 | 30 18.9 | 97 0.59 | 119 | 50 | 10 | 50 | 100 | 0 52 | 33 | 10.45 | 1.7735 |
| 1 0 | | 0 23 0 | | | $ \begin{array}{c c} 60 & 0.74 \\ 54 & 0.87 \end{array} $ | _ | 08 | 50 | 6 0 | 20 0 50 | 0 48 0 45 | 54 | | 1.7965 1.8173 |
| 20 | 40 9 | 20 40 | 1 41 . | 54 18. | 30 0.98 | 97 | 20 | 40 | 20 | 40 | 0 41 | 19 | 8.22 | 1.8361 |
| 30 40 | | 30 30 40 20 | | | 99 1.08 $62 1.17$ | | 30 40 | 30 | 30 40 | | 0 37 | | | 1.8527 1.8675 |
| 50 | 10 | 50 10 | 1 26 | 45 17. | 26 1.25 | 03 | 50 | 10 | 50 | 10 | 0 29 | 25 | 5.85 | 1.8803 |
| 2 0 | 10 0 14 50 | | | | 83 1.31 41 1.38 | | 07 | 50 | 7 0 | 19 0 50 | $0 25 \\ 0 21$ | | | 1.8715 1.9007 |
| 20 | 40 | 20 40 | 1 20 | 7 15. | 92 1.43 | 87 | 20 | 40 | 20 | 40 | 0 16 | 59 | 3.38 | 1.9081 |
| 30 40 | | 30 30 40 20 | | | 42 1.49 90 1.53 | | 30 40 | 30 20 | 30 | 30 20 | | 46 32 | | 1.9139 1.9181 |
| 50 | | | 1 12 | | 36 2.58 | 09 | 50 | 10 | 50 | 10 | 0 4 | 16 | 0.85 | 1.9207 |
| - | | | | to de | 000 | [6 | 0 6 | 0 1 | 8 0 | 18 0 | 0 0 | 0 | 0.00 | 1.9215 |









26355

University of Toronto Library

DO NOT REMOVE THE

CARD

FROM

THIS POCKET

Acme Library Card Pocket Under Pat. "Ref. Index File Made by LIBRARY BUREAU

Galbraith, William Mathematical and Astronomical Tables.

Mat.Ta

